Data Mining [02_Data]



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Data Mining: Data

Lecture Notes for Chapter 2

Introduction to Data Mining by Tan, Steinbach, Kumar



Collection of data objects and their attributes

An attribute is a property or characteristic of an object

- Examples: eye color of a person, temperature, etc.
- Attribute is also known as variable, field, characteristic, or feature

A collection of attributes describe an object

 Object is also known as record, point, case, sample, entity, or instance

Attributes

	()		
_	Tid	Refund	Marital Status	Taxable Income	Cheat		
	1	Yes	Single	125K	No		
	2	No	Married	100K	No		
	3	No	Single	70K	No		
	4	Yes	Married	120K	No		
	5	No	Divorced	95K	Yes		
	6	No	Married	60K	No		
	7	Yes	Divorced	220K	No		
	8	No	Single	85K	Yes		
	9	No	Married	75K	No		
_	10	No	Single	90K	Yes		

Objects



Attribute values are numbers or symbols assigned to an attribute

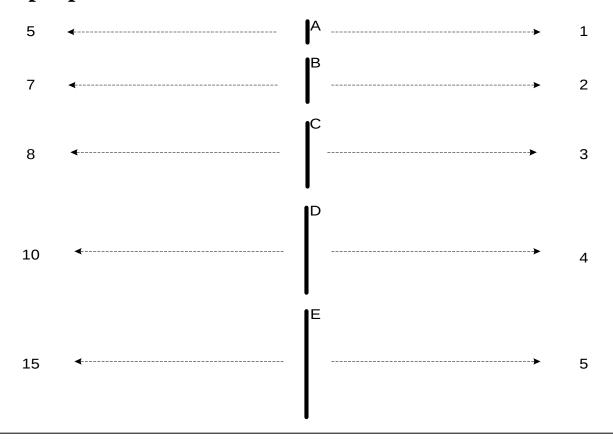
Distinction between attributes and attribute values

- Same attribute can be mapped to different attribute values
 - Example: height can be measured in feet or meters
- Different attributes can be mapped to the same set of values
 - Example: Attribute values for ID and age are integers
 - But properties of attribute values can be different
 - ID has no limit but age has a maximum and minimum value



Measurement of Length

 The way you measure an attribute is somewhat may not match the attributes properties.





Types of Attributes

There are different types of attributes

- Nominal
 - Examples: ID numbers, eye color, zip codes
- Ordinal
 - Examples: rankings (e.g., taste of potato chips on a scale from 1-10), grades, height in {tall, medium, short}
- Interval
 - Examples: calendar dates, temperatures in Celsius or Fahrenheit.
- Ratio
 - Examples: temperature in Kelvin, length, time, counts



Properties of Attribute Values

The type of an attribute depends on which of the following properties it possesses:

- Distinctness: $= \neq$
- Order: < >
- Addition: + -
- Multiplication: * /
- Nominal attribute: distinctness
- Ordinal attribute: distinctness & order
- Interval attribute: distinctness, order & addition
- Ratio attribute: all 4 properties



Properties of Attribute Values

Attribute Type	Description	Examples	Operations		
Nominal	The values of a nominal attribute are just different names, i.e., nominal attributes provide only enough information to distinguish one object from another. $(=, \neq)$	zip codes, employee ID numbers, eye color, sex: {male, female}	mode, entropy, contingency correlation, χ^2 test		
Ordinal	The values of an ordinal attribute provide enough information to order objects. (<, >)	hardness of minerals, {good, better, best}, grades, street numbers	median, percentiles, rank correlation, run tests, sign tests		



Properties of Attribute Values

Attribute Type	Description	Examples	Operations		
Interval	For interval attributes, the differences between values are meaningful, i.e., a unit of measurement exists. (+, -)	calendar dates, temperature in Celsius or Fahrenheit	mean, standard deviation, Pearson's correlation, <i>t</i> and <i>F</i> tests		
Ratio	For ratio variables, both differences and ratios are meaningful. (*, /)	temperature in Kelvin, monetary quantities, counts, age, mass, length, electrical current	geometric mean, harmonic mean, percent variation		



Discrete and Continuous Attributes

Discrete Attribute

- Has only a finite or countably infinite set of values
- Examples: zip codes, counts, or the set of words in a collection of documents
- Often represented as integer variables.
- Note: binary attributes are a special case of discrete attributes

Continuous Attribute

- Has real numbers as attribute values
- Examples: temperature, height, or weight.
- Practically, real values can only be measured and represented using a finite number of digits.
- Continuous attributes are typically represented as floating-point variables.



Types of data sets

Record

- Data Matrix
- Document Data
- Transaction Data

Graph

- World Wide Web
- Molecular Structures

Ordered

- Spatial Data
- Temporal Data
- Sequential Data
- Genetic Sequence Data



Important Characteristics of Structured Data

- Dimensionality
 - Curse of Dimensionality

- Sparsity
 - Only presence counts

- Resolution
 - Patterns depend on the scale



Data that consists of a collection of records, each of which consists of a fixed set of attributes

Tid	Refund	Marital Status	Taxable Income	Cheat	
1	Yes	Single	125K	No	
2	No	Married	100K	No	
3	No	Single	70K	No	
4	Yes	Married	120K	No	
5	No	Divorced	95K	Yes	
6	No	Married	60K	No	
7	Yes	Divorced	220K	No	
8	No	Single	85K	Yes	
9	No	Married	75K	No	
10	No	Single	90K	Yes	



If data objects have the same fixed set of numeric attributes, then the data objects can be thought of as points in a multidimensional space, where each dimension represents a distinct attribute

Such data set can be represented by an m by n matrix, where there are m rows, one for each object, and n columns, one for each attribute

Projection of the ad	Projection of y load	Distance	L o a d	Thickness
1 0 . 2 3	5 . 2 7	1 5 . 2 2	2 . 7	1 . 2
1 2 . 6 5	6 . 2 5	1 6 . 2 2	2 . 2	1 . 1



Document Data

Each document becomes a `term' vector,

each term is a component (attribute) of the vector,

 the value of each component is the number of times the corresponding term occurs in the

document.

e difficile.		team	coach	play	ball	score	game	win	lost	timeout	season
	Document 1	3	0	5	0	2	6	0	2	0	2
	Document 2	0	7	0	2	1	0	0	3	0	0
	Document 3	0	1	0	0	1	2	2	0	3	0



Transaction Data

A special type of record data, where

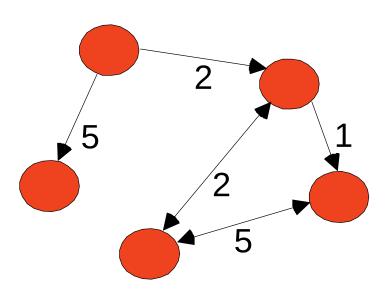
- each record (transaction) involves a set of items.
- For example, consider a grocery store. The set of products purchased by a customer during one shopping trip constitute a transaction, while the individual products that were purchased are the

item	TID	Items
10011	1	Bread, Coke, Milk
2 Beer, Bre		Beer, Bread
	3	Beer, Coke, Diaper, Milk
4 Beer, Bre		Beer, Bread, Diaper, Milk
	5	Coke, Diaper, Milk



Graph Data

Examples: Generic graph and HTML Links



Data Mining

Graph Partitioning

<a href="papers/papers.html

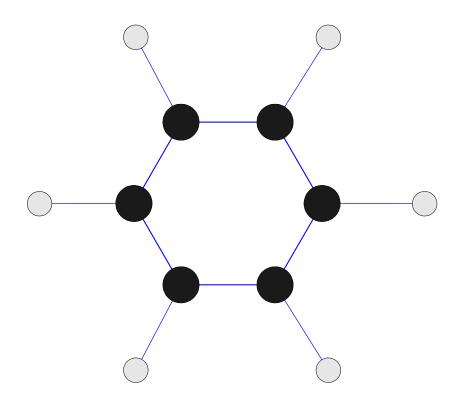
Parallel Solution of Sparse Linear System of Equations

N-Body Computation and Dense Linear System Solvers



Chemical Data

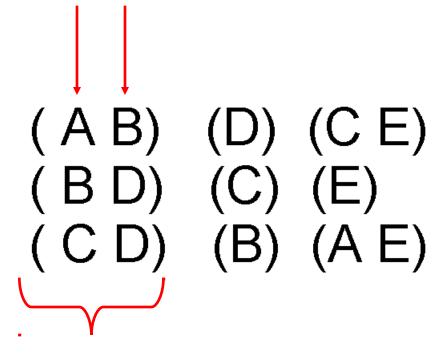
Benzene Molecule: C₆H₆





Ordered Data

Sequences of transactions Items/Events



An element of the sequence



Ordered Data

Genomic sequence data

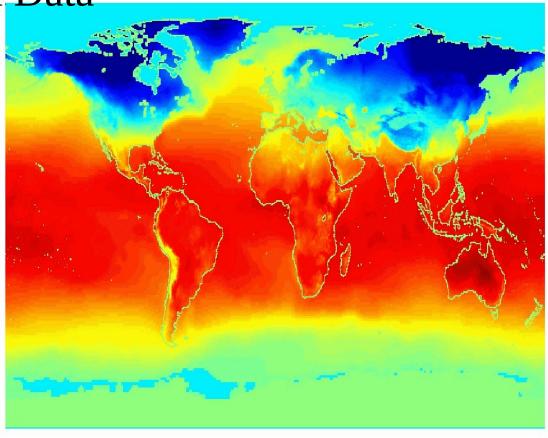


Ordered Data

Spatio-Temporal Data

Jan

Average Monthly Temperature of land and ocean





What kinds of data quality problems?
How can we detect problems with the data?
What can we do about these problems?

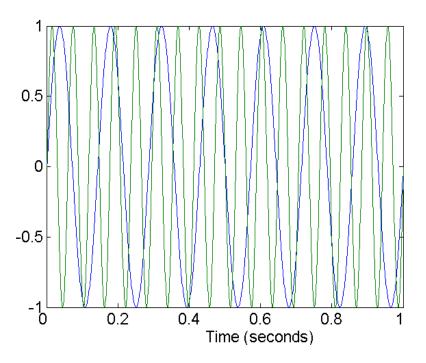
Examples of data quality problems:

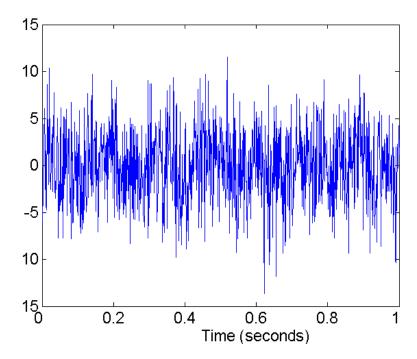
- Noise and outliers
- missing values
- duplicate data



Noise refers to modification of original values

 Examples: distortion of a person's voice when talking on a poor phone and "snow" on television screen



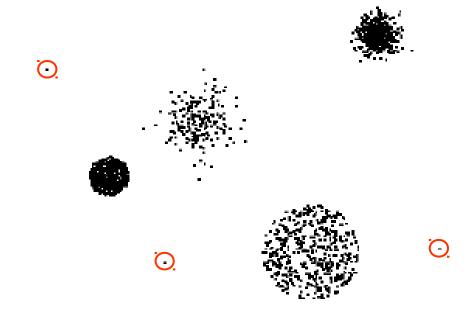


Two Sine Waves

Two Sine Waves + Noise



Outliers are data objects with characteristics that are considerably different than most of the other data objects in the data set





Missing Values

Reasons for missing values

- Information is not collected
 (e.g., people decline to give their age and weight)
- Attributes may not be applicable to all cases
 (e.g., annual income is not applicable to children)

Handling missing values

- Eliminate Data Objects
- Estimate Missing Values
- Ignore the Missing Value During Analysis
- Replace with all possible values (weighted by their probabilities)



Duplicate Data

Data set may include data objects that are duplicates, or almost duplicates of one another

Major issue when merging data from heterogeous sources

Examples:

Same person with multiple email addresses

Data cleaning

Process of dealing with duplicate data issues



Data Preprocessing

Aggregation

Sampling

Dimensionality Reduction

Feature subset selection

Feature creation

Discretization and Binarization

Attribute Transformation



Aggregation

Combining two or more attributes (or objects) into a single attribute (or object)

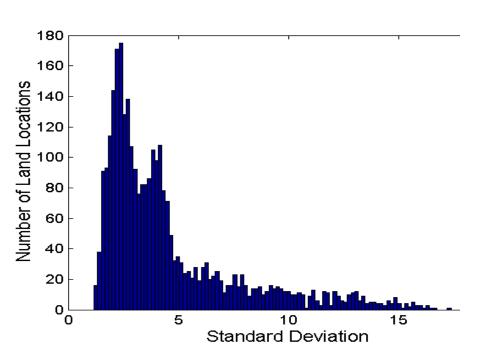
Purpose

- Data reduction
 - Reduce the number of attributes or objects
- Change of scale
 - Cities aggregated into regions, states, countries, etc
- More "stable" data
 - Aggregated data tends to have less variability

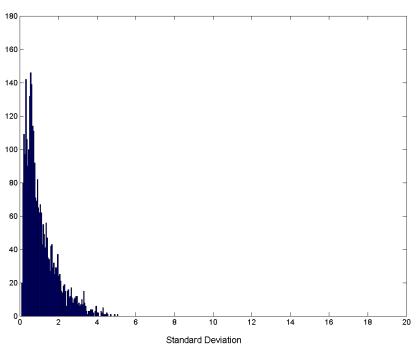


Aggregation

Variation of Precipitation in Australia



Standard Deviation of Average Monthly Precipitation



Standard Deviation of Average Yearly Precipitation



- Sampling is the main technique employed for data selection.
 - It is often used for both the preliminary investigation of the data and the final data analysis.
- Statisticians sample because obtaining the entire set of data of interest is too expensive or time consuming.
- Sampling is used in data mining because processing the entire set of data of interest is too expensive or time consuming.



The key principle for effective sampling is the following:

- using a sample will work almost as well as using the entire data sets, if the sample is representative
- A sample is representative if it has approximately the same property (of interest) as the original set of data



Types of Sampling

Simple Random Sampling

There is an equal probability of selecting any particular item

Sampling without replacement

As each item is selected, it is removed from the population

Sampling with replacement

- Objects are not removed from the population as they are selected for the sample.
 - In sampling with replacement, the same object can be picked up more than once

Stratified sampling

Split the data into several partitions; then draw random samples from each partition



Sample Size



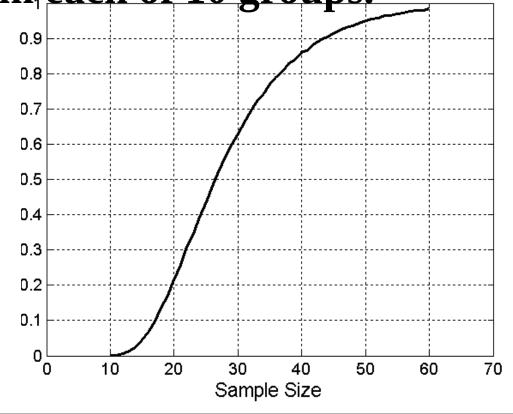
8000 points 2000 Points 500 Points



Sample Size

What sample size is necessary to get at least one object from each of 10 groups.



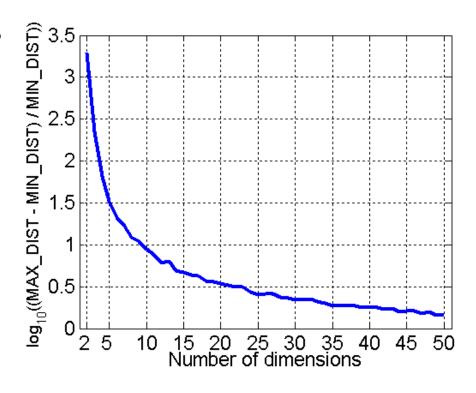




Curse of Dimensionality

When dimensionality increases, data becomes increasingly sparse in the space that it occupies

Definitions of density and distance between points, which is critical for clustering and outlier detection, become less meaningful



- Randomly generate 500 points
- Compute difference between max and min distance between any pair of points



Dimensionality Reduction

Purpose:

- Avoid curse of dimensionality
- Reduce amount of time and memory required by data mining algorithms
- Allow data to be more easily visualized
- May help to eliminate irrelevant features or reduce noise

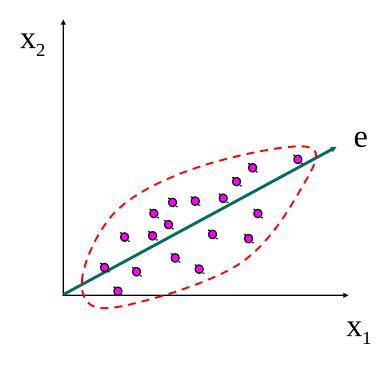
Techniques

- Principle Component Analysis
- Singular Value Decomposition
- Others: supervised and non-linear techniques



Dimensionality Reduction: PCA

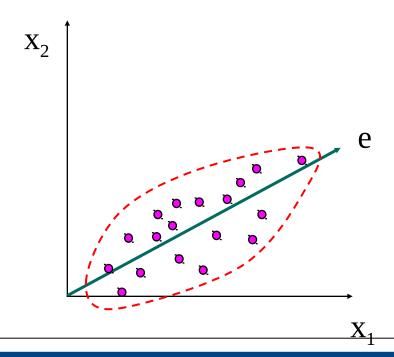
Goal is to find a projection that captures the largest amount of variation in data





Dimensionality Reduction: PCA

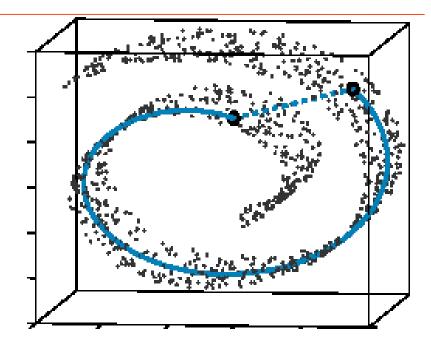
Find the eigenvectors of the covariance matrix The eigenvectors define the new space





Dimensionality Reduction: ISOMAP

By: Tenenbaum, de Silva, Langford (2000)



Construct a neighbourhood graph

For each pair of points in the graph, compute the shortest path distances – geodesic distances



Feature Subset Selection

Another way to reduce dimensionality of data

Redundant features

- duplicate much or all of the information contained in one or more other attributes
- Example: purchase price of a product and the amount of sales tax paid

Irrelevant features

- contain no information that is useful for the data mining task at hand
- Example: students' ID is often irrelevant to the task of predicting students' GPA



Feature Subset Selection

Techniques:

- Brute-force approch:
 - Try all possible feature subsets as input to data mining algorithm
- Embedded approaches:
 - Feature selection occurs naturally as part of the data mining algorithm
- Filter approaches:
 - Features are selected before data mining algorithm is run
- Wrapper approaches:
 - Use the data mining algorithm as a black box to find best subset of attributes



Feature Creation

Create new attributes that can capture the important information in a data set much more efficiently than the original attributes

Three general methodologies:

- Feature Extraction
 - domain-specific
- Mapping Data to New Space
- Feature Construction
 - combining features



Feature Creation

Create new attributes that can capture the important information in a data set much more efficiently than the original attributes

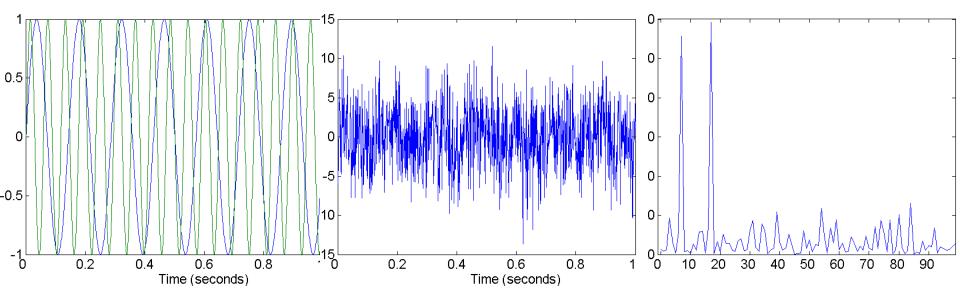
Three general methodologies:

- Feature Extraction
 - domain-specific
- Mapping Data to New Space
- Feature Construction
 - combining features



Mapping Data to a New Space

- Fourier transform
- Wavelet transform



Two Sine Waves

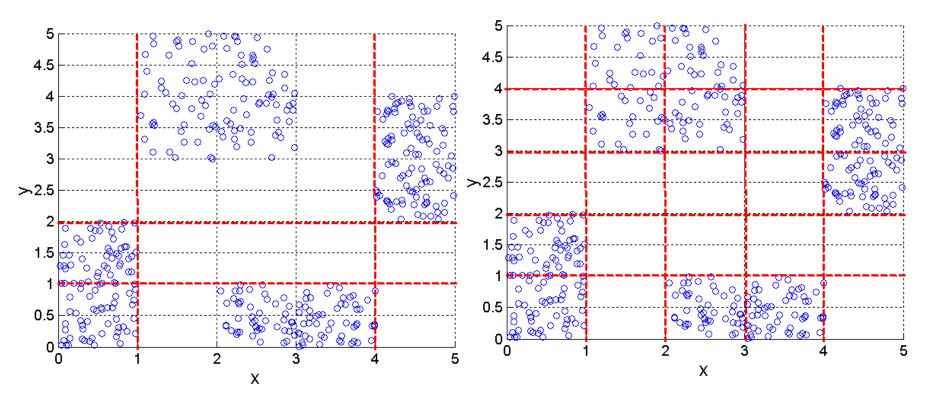
Two Sine Waves + Noise

Frequency



Discretization Using Class Labels

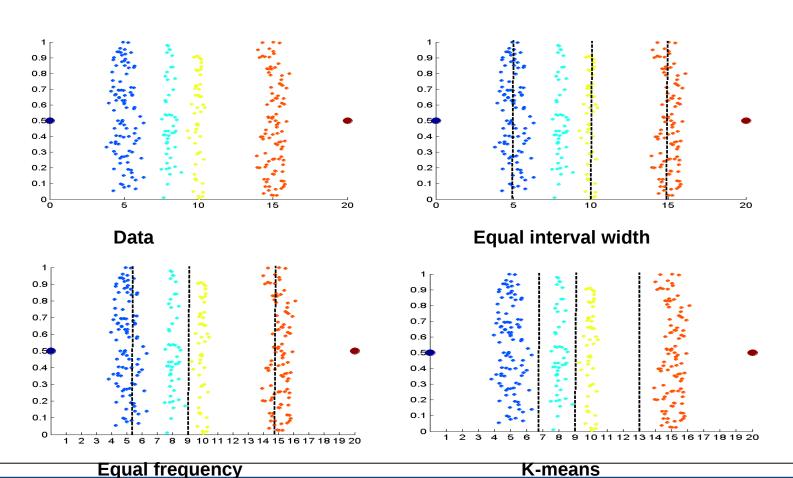
Entropy based approach



3 categories for both x and y

5 categories for both x and y

Discretization Without Using Class Labels



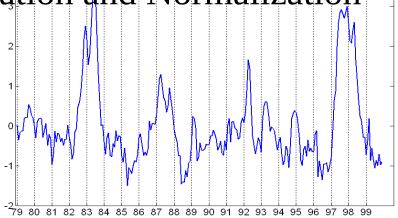
STT-NF



Attribute Transformation

A function that maps the entire set of values of a given attribute to a new set of replacement values such that each old value can be identified with one of the new values

- Simple functions: x^k , log(x), e^x , |x|
- Standardization and Normalization





Similarity and Dissimilarity

Similarity

- Numerical measure of how alike two data objects are.
- Is higher when objects are more alike.
- Often falls in the range [0,1]

Dissimilarity

- Numerical measure of how different are two data objects
- Lower when objects are more alike
- Minimum dissimilarity is often 0
- Upper limit varies

Proximity refers to a similarity or dissimilarity



Similarity/Dissimilarity for Simple Attributes

p and q are the attribute values for two data objects.

Attribute	Dissimilarity	Similarity
Type		
Nominal	$d = \begin{cases} 0 & \text{if } p = q \\ 1 & \text{if } p \neq q \end{cases}$	$s = \begin{cases} 1 & \text{if } p = q \\ 0 & \text{if } p \neq q \end{cases}$
Ordinal	$d = \frac{ p-q }{n-1}$ (values mapped to integers 0 to $n-1$, where n is the number of values)	$s = 1 - \frac{ p-q }{n-1}$
Interval or Ratio	d = p - q	$s = -d, \ s = \frac{1}{1+d}$ or
		$s = -d$, $s = \frac{1}{1+d}$ or $s = 1 - \frac{d - min_d}{max_d - min_d}$

Table 5.1. Similarity and dissimilarity for simple attributes



Euclidean Distance

Euclidean Distance

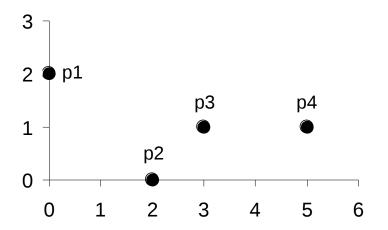
$$dist = \sqrt{\sum_{k=1}^{n} (p_k - q_k)^2}$$

Where n is the number of dimensions (attributes) and p_k and q_k are, respectively, the k^{th} attributes (components) or data objects p and q.

Standardization is necessary, if scales differ.



Euclidean Distance



point	X	y
p1	0	2
p 2	2	0
р3	3	1
p4	5	1

	p1	p 2	р3	p4
p1	0	2.828	3.162	5.099
p 2	2.828	0	1.414	3.162
р3	3.162	1.414	0	2
p4	5.099	3.162	2	0

Distance Matrix



Minkowski Distance

Minkowski Distance is a generalization of Euclidean Distance

$$dist = \left(\sum_{k=1}^{n} |p_k - q_k|^r\right)^{\frac{1}{r}}$$

Where r is a parameter, n is the number of dimensions (attributes) and p_k and q_k are, respectively, the kth attributes (components) or data objects p and q.



Minkowski Distance: Examples

- r = 1. City block (Manhattan, taxicab, L₁ norm) distance.
 - A common example of this is the Hamming distance, which is just the number of bits that are different between two binary vectors
- r = 2. Euclidean distance
- $r \to \infty$. "supremum" (L_{max} norm, L_{∞} norm) distance.
 - This is the maximum difference between any component of the vectors
- Do not confuse *r* with *n*, i.e., all these distances are defined for all numbers of dimensions.



Minkowski Distance

point	X	y
p1	0	2
p 2	2	0
р3	3	1
p4	5	1

L1	p1	p 2	р3	p4
p1	0	4	4	6
p 2	4	0	2	4
р3	4	2	0	2
p4	6	4	2	0

L2	p1	p 2	р3	p4
p1	0	2.828	3.162	5.099
p 2	2.828	0	1.414	3.162
р3	3.162	1.414	0	2
p4	5.099	3.162	2	0

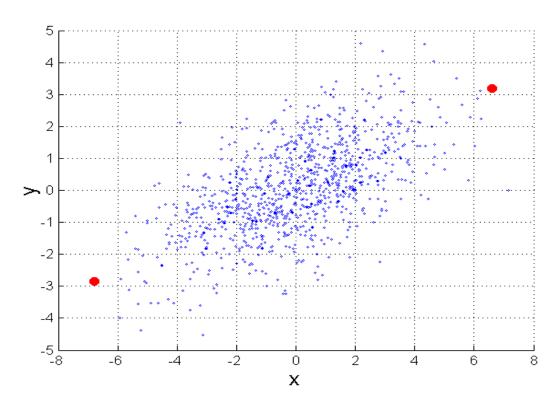
L_{∞}	p1	p 2	р3	p4
p1	0	2	3	5
p 2	2	0	1	3
р3	3	1	0	2
p4	5	3	2	0

Distance Matrix



Mahalanobis Distance

mahalanobis
$$(p,q)=(p-q)\sum^{-1}(p-q)^{T}$$



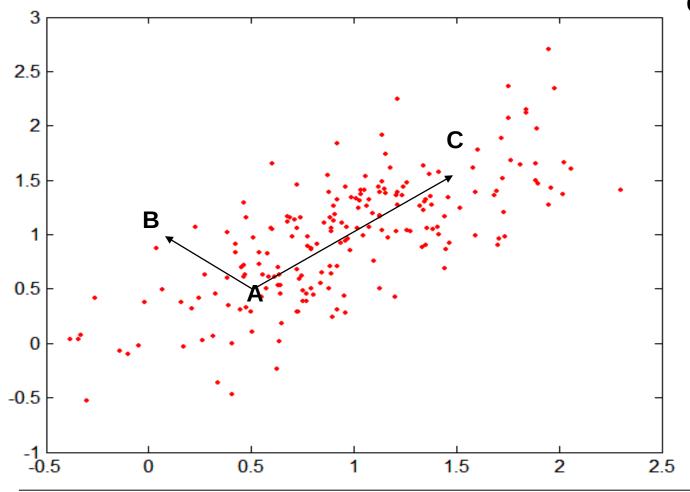
Σ is the covariance matrix of the input data X

$$\Sigma_{j,k} = \frac{1}{n-1} \sum_{i=1}^{n} (X_{ij} - \overline{X}_{j}) (X_{ik} - \overline{X}_{k})$$

For red points, the Euclidean distance is 14.7, Mahalanobis distance is 6.



Mahalanobis Distance



Covariance Matrix:

$$\Sigma = \begin{bmatrix} 0.3 & 0.2 \\ 0.2 & 0.3 \end{bmatrix}$$

A: (0.5, 0.5)

B: (0, 1)

C: (1.5, 1.5)

Mahal(A,B) = 5

Mahal(A,C) = 4



Common Properties of a Distance

- Distances, such as the Euclidean distance, have some well known properties.
 - 1. $d(p, q) \ge 0$ for all p and q and d(p, q) = 0 only if p = q. (Positive definiteness)
 - 2. d(p, q) = d(q, p) for all p and q. (Symmetry)
 - 3. $d(p, r) \le d(p, q) + d(q, r)$ for all points p, q, and r. (Triangle Inequality)
 - where d(p, q) is the distance (dissimilarity) between points (data objects), p and q.
- A distance that satisfies these properties is a metric



Common Properties of a Similarity

- Similarities, also have some well known properties.
 - 1. s(p, q) = 1 (or maximum similarity) only if p = q.
 - 2. s(p, q) = s(q, p) for all p and q. (Symmetry)

where s(p, q) is the similarity between points (data objects), p and q.



Similarity Between Binary Vectors

- Common situation is that objects, p and q, have only binary attributes
- Compute similarities using the following quantities M_{01} = the number of attributes where p was 0 and q was 1 M_{10} = the number of attributes where p was 1 and q was 0 M_{00} = the number of attributes where p was 0 and q was 0 M_{11} = the number of attributes where p was 1 and q was 1
- Simple Matching and Jaccard Coefficients

```
SMC = number of matches / number of attributes
= (M_{11} + M_{00}) / (M_{01} + M_{10} + M_{11} + M_{00})
```

J = number of 11 matches / number of not-both-zero attributes values = $(M_{11}) / (M_{01} + M_{10} + M_{11})$



SMC versus Jaccard: Example

$$p = 1000000000$$

$$q = 0000001001$$

 $M_{01} = 2$ (the number of attributes where p was 0 and q was 1)

 $M_{10} = 1$ (the number of attributes where p was 1 and q was 0)

 $M_{00} = 7$ (the number of attributes where p was 0 and q was 0)

 $M_{11} = 0$ (the number of attributes where p was 1 and q was 1)

SMC =
$$(M_{11} + M_{00})/(M_{01} + M_{10} + M_{11} + M_{00}) = (0+7)/(2+1+0+7) = 0.7$$

$$J = (M_{11}) / (M_{01} + M_{10} + M_{11}) = 0 / (2 + 1 + 0) = 0$$



Cosine Similarity

• If d_1 and d_2 are two document vectors, then

$$\cos(d_1, d_2) = (d_1 \bullet d_2) / ||d_1|| ||d_2||,$$

where \bullet indicates vector dot product and ||d|| is the length of vector d.

• Example:

$$d_1 = 3205000200$$

$$d_2 = 100000102$$

$$d_1 \bullet d_2 = 3*1 + 2*0 + 0*0 + 5*0 + 0*0 + 0*0 + 0*0 + 2*1 + 0*0 + 0*2 = 5$$

$$||d_1|| = (3*3+2*2+0*0+5*5+0*0+0*0+0*0+2*2+0*0+0*0)$$
_{0.5} = (42) _{0.5} = 6.481

$$||d_2|| = (1*1+0*0+0*0+0*0+0*0+0*0+0*0+1*1+0*0+2*2)$$
 0.5 = (6) 0.5 = 2.245

$$\cos(d_1, d_2) = .3150$$



Extended Jaccard Coefficient (Tanimoto)

Variation of Jaccard for continuous or count attributes

Reduces to Jaccard for binary attributes

$$T(p,q) = rac{p ullet q}{\|p\|^2 + \|q\|^2 - p ullet q}$$



Correlation

Correlation measures the linear relationship between objects

To compute correlation, we standardize data objects, p and q, and then take their dot product

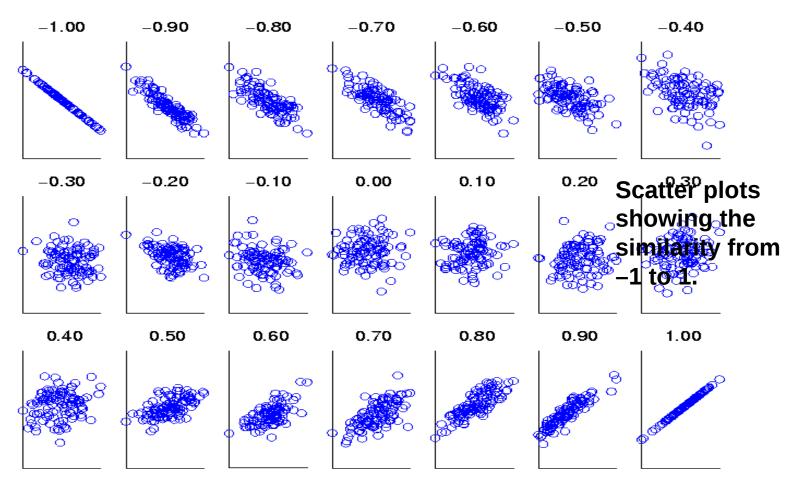
$$p'_{k} = (p_{k} - mean(p))/std(p)$$

$$q_{k}^{'}=(q_{k}-mean(q))/std(q)$$

$$correlation(p,q) = p' \cdot q'$$



Visually Evaluating Correlation





General Approach for Combining Similarities

- Sometimes attributes are of many different types, but an overall similarity is needed.
- 1. For the k^{th} attribute, compute a similarity, s_k , in the range [0,1].
- 2. Define an indicator variable, δ_k , for the k_{th} attribute as follows:
 - $\delta_k = \left\{ \begin{array}{ll} 0 & \text{if the k^{th} attribute is a binary asymmetric attribute and both objects have} \\ & \text{a value of 0, or if one of the objects has a missing values for the k^{th} attribute} \\ & 1 & \text{otherwise} \end{array} \right.$
- 3. Compute the overall similarity between the two objects using the following formula:

$$similarity(p,q) = rac{\sum_{k=1}^{n} \delta_k s_k}{\sum_{k=1}^{n} \delta_k}$$



Using Weights to Combine Similarities

May not want to treat all attributes the same.

– Use weights w_k which are between 0 and 1 and sum to 1.

$$similarity(p,q) = \frac{\sum_{k=1}^{n} w_k \delta_k s_k}{\sum_{k=1}^{n} \delta_k}$$

$$distance(p,q) = \left(\sum_{k=1}^n w_k |p_k - q_k|^r
ight)^{1/r}.$$



Density-based clustering require a notion of density

Examples:

- Euclidean density
 - Euclidean density = number of points per unit volume
- Probability density
- Graph-based density



Euclidean Density – Cell-based

Simplest approach is to divide region into a number of rectangular cells of equal volume and define density as # of points the cell contains

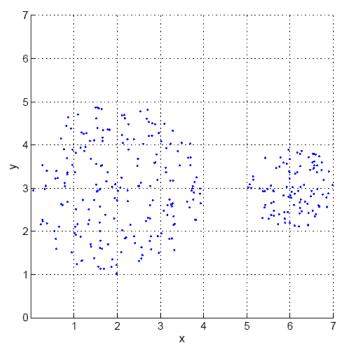


Figure 7.13. Cell-based density.

0	0	0	0	0	0	0
0	0	0	0	0	0	0
4	17	18	6	0	0	0
14	14	13	13	0	18	27
11	18	10	21	0	24	31
3	20	14	4	0	0	0
0	0	0	0	0	0	0

Table 7.6. Point counts for each grid cell.



Euclidean Density - Center-based

Euclidean density is the number of points within a specified radius of the point

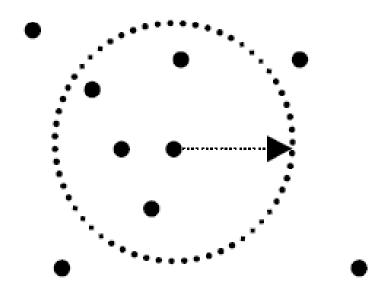


Figure 7.14. Illustration of center-based density.