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Speech & Music

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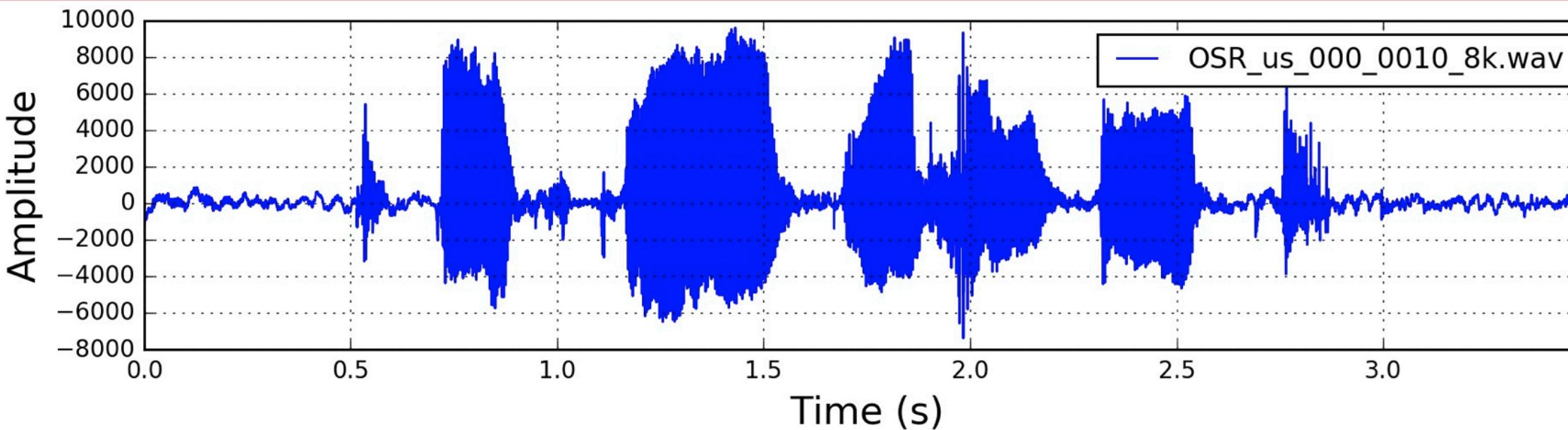


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Mel-Spectrogram and Mel-Frequency Cepstral Coefficients (MFCCs)

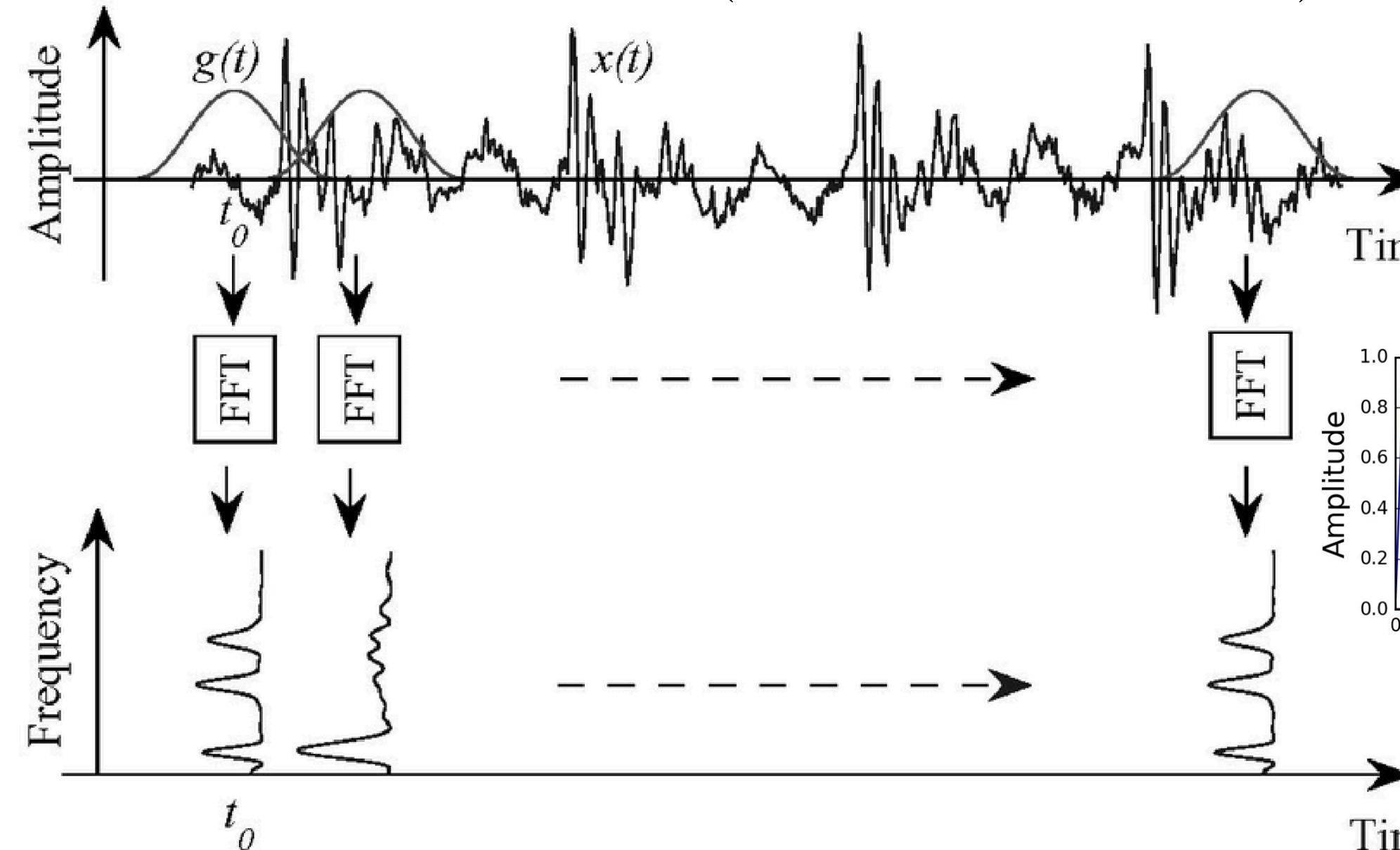


<https://haythamfayek.com/2016/04/21/speech-processing-for-machine-learning.html>

Short-Time Fourier-Transform (STFT)

$x \rightarrow$ signal in the time domain (e.g., $x \in \mathbb{R}^{28,200 = 3.525 \text{ seconds} \times 8,000 \text{ Hz}}$)
sampling frequency (number of samples per seconds)

$g \rightarrow$ sliding window function (e.g., Hamming function)



Gao, Robert X., and Ruqiang Yan. "Non-stationary signal processing for bearing health monitoring." *International journal of manufacturing research* 1.1 (2006): 18-40.

$$X_i \in \mathbb{R}^{200} \rightarrow i\text{-th frame of signal } x \text{ (25ms frames)}$$

$$80 \rightarrow \text{frame step (10ms)} \implies X \in \mathbb{R}^{200 \times 350} \quad (350 = (28,200 - 200)/80)$$

$$\tilde{X}_i \in \mathbb{C}^K \rightarrow \text{discrete Fourier transform of } X_i \implies \tilde{X} \in \mathbb{C}^{K \times 350}$$

$$\tilde{X}_i(k) = \sum_{n=1}^N X_i(n)g(n)e^{-j2\pi kn/N}, k = 1, \dots, K \quad N = 200$$

$K = 257 \rightarrow$ number of discrete Fourier transform coefficients

$$P_i(k) = \frac{1}{N} |\tilde{X}_i(k)|^2 \rightarrow \text{Periodogram estimate of the power spectrum}$$

$$\implies P \in \mathbb{R}^{257 \times 350}$$

<http://practicalcryptography.com/miscellaneous/machine-learning/guide-mel-frequency-cepstral-coefficients-mfccs/>

<https://www.youtube.com/watch?v=WJI-17MNpdE>

$$f(k) = 300 + \frac{k-1}{K-1}(4,000 - 300)$$

Mel-spaced Filterbank

300 Hz \rightarrow lower frequency

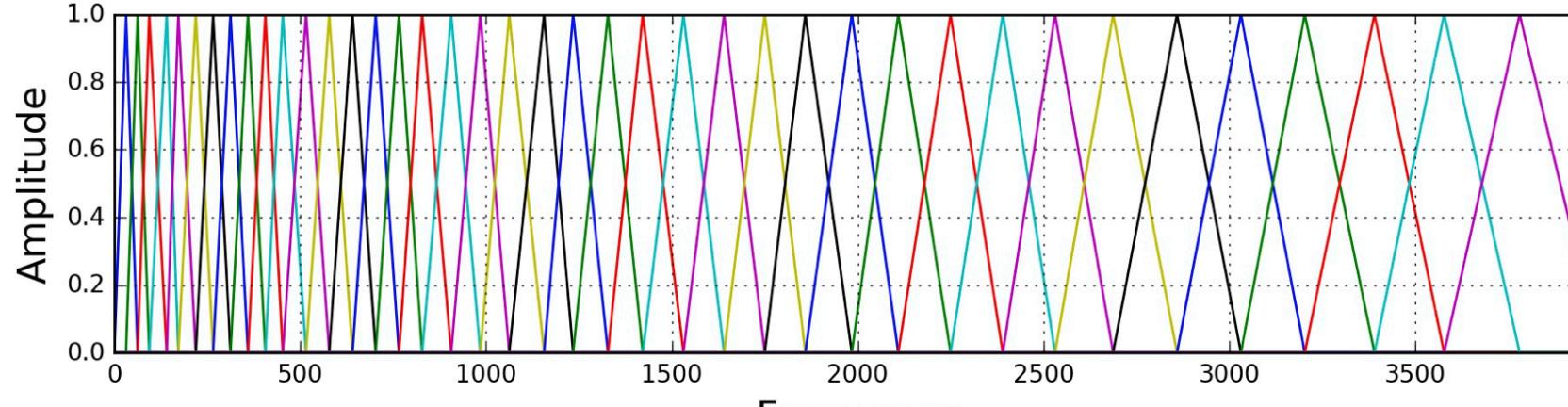
4,000 Hz \rightarrow upper frequency

$M(f) = 1,125 \ln(1 + f/700) \rightarrow$ convert frequency to Mel scale

$M^{-1}(m) = 700(\exp(m/1,125) - 1) \rightarrow$ convert Mel scale to Hz

$M^{-1}(\text{linspace}(M(300), M(4,000), 26 + 2))$

26 \rightarrow number of triangular filters

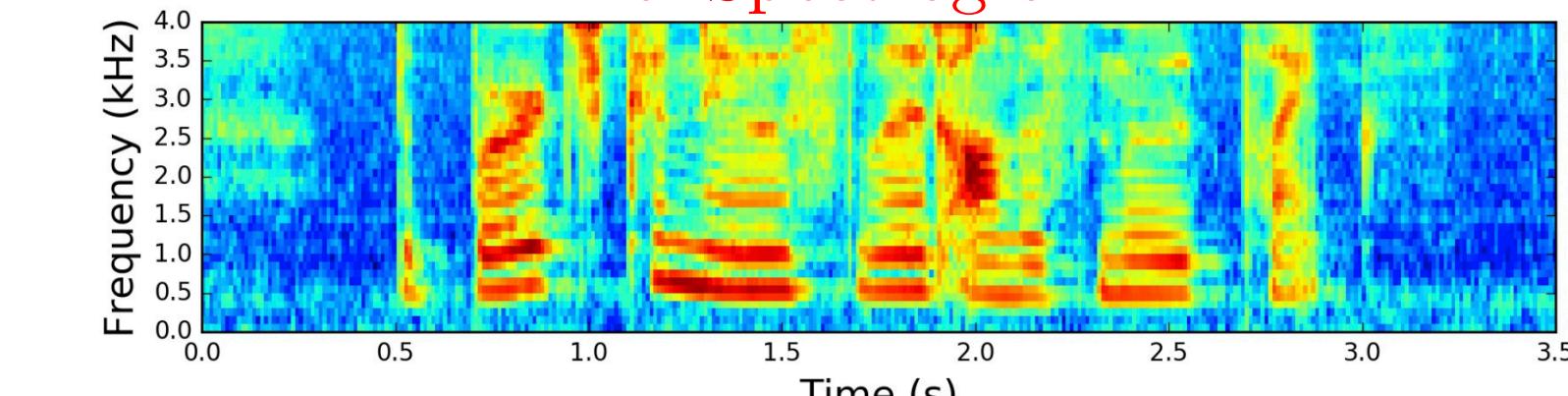
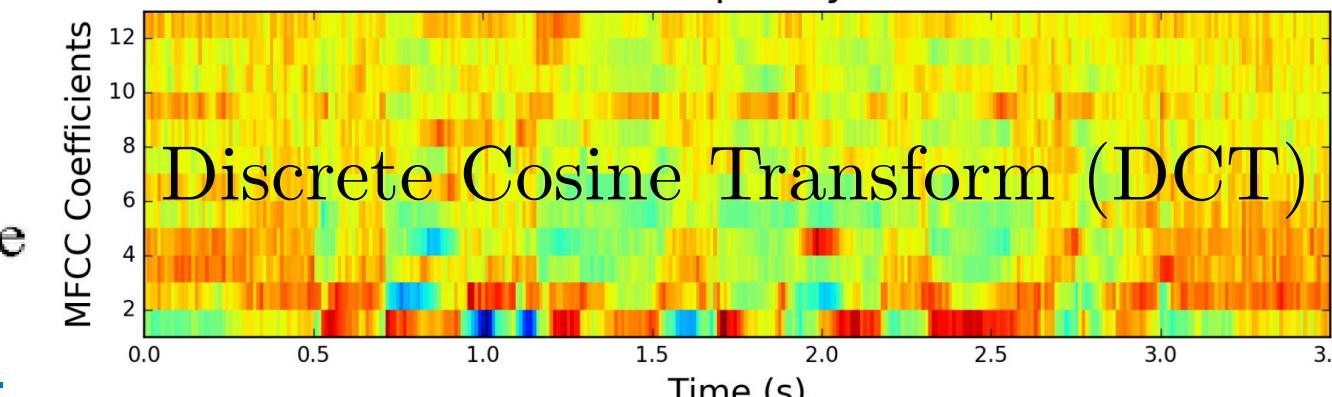


$T \in \mathbb{R}^{26 \times 257} \implies E = TP \in \mathbb{R}^{26 \times 350}$

$E_i(l) \rightarrow$ amount of energy in filter bank l at frame i

$\log(E) \in \mathbb{R}^{26 \times 350} \rightarrow$ log filter bank energy

Mel Spectrogram



Connectionist Temporal Classification: Labelling Unsegmented Sequence Data with Recurrent Neural Networks


[YouTube Video](#)

speech recognition: transcribe an acoustic signal into words and subwords units
noisy, real-valued input streams are annotated with strings of discrete labels (e.g., letters or words)

– handwriting recognition – speech recognition – gesture recognition

temporal classification: the task of labelling unsegmented data sequences

connectionist temporal classification: use of RNNs

framewise classification: independent labelling of each time-step or frame of the input sequence

Temporal Classification

$S \rightarrow$ set of training examples drawn from a fixed distribution $\mathcal{D}_{\mathcal{X} \times \mathcal{Z}}$

$\mathcal{X} = (\mathbb{R}^m)^* \rightarrow$ input space (set of all sequences of m dimensional real-valued vectors)

$\mathcal{Z} = L^* \rightarrow$ target space (set of all sequences over the finite alphabet L of labels)

$l \in L^* \rightarrow$ label sequence or labelling

$(x, z) \in S \rightarrow$ an example pair of sequences

$x = (x_1, \dots, x_T) \rightarrow$ input sequence

$z = (z_1, \dots, z_U) \rightarrow$ target sequence

$U \leq T \rightarrow$ the target sequence is at most as long as the input sequence

Problem: No a priori way of aligning x & z !

Label Error Rate

$h : \mathcal{X} \rightarrow \mathcal{Z}$

temporal classifier (to be trained using S)

$S' \subset \mathcal{D}_{\mathcal{X} \times \mathcal{Z}} \rightarrow$ test set disjoint from S

$$\text{LER}(h, S') = \frac{1}{|S'|} \sum_{(x, z) \in S'} \frac{\text{ED}(h(x), z)}{|z|}$$

$\text{ED}(h(x), z) \rightarrow$ edit distance

minimum number of insertions, substitutions,
and deletions required to change $h(x)$ to z

Connectionist Temporal Classification

$$\mathcal{N}_w : (\mathbb{R}^m)^T \rightarrow (\mathbb{R}^n)^T$$

↳ RNN with weight vector w

$y = \mathcal{N}_w(x) \rightarrow$ sequence of the network outputs

$$y_k^t \rightarrow$$
 activation of output unit k at time t

$y_k^t \rightarrow$ probability of observing label k at time t

$$p(\pi|x) = \prod_{t=1}^T y_{\pi_t}^t, \forall \pi \in \underbrace{(L \cup \{\text{blank}\})^T}_{\text{path } =: \Lambda}$$

defines a distribution over the set Λ^T of length T sequences over the alphabet Λ

$\mathcal{B} : \Lambda^T \rightarrow L^{\leq T}$ $L^{\leq T} \rightarrow$ set of all possible labelings (set of sequences of length $\leq T$ over the original label alphabet L)
↳ many-to-one map $\mathcal{B}(a - ab -) = aab = \mathcal{B}(-aa - -abb) \rightarrow$ remove of all blanks and repeated labels

$$p(l|x) = \sum_{\pi \in \mathcal{B}^{-1}(l)} p(\pi|x)$$

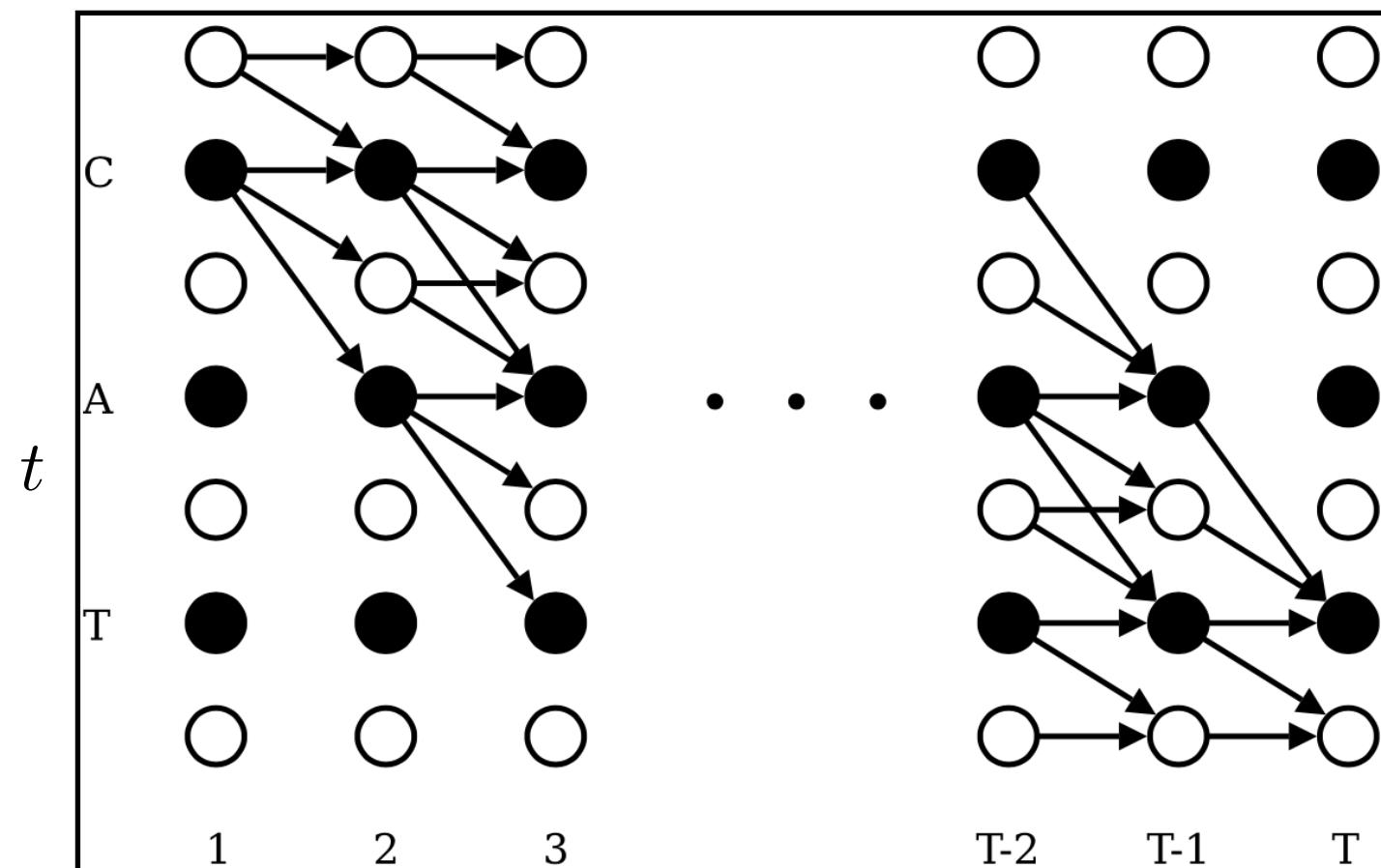
$l \in L^{\leq T} \rightarrow$ labeling

↳ the input sequence

Best path decoding

$$h(x) \approx \mathcal{B}(\pi^*)$$

$$\pi^* = \arg \max_{\pi \in \Lambda^T} p(\pi|x)$$



Training the Network (Dynamic Programming)

$$\alpha_t(s) := \sum_{\substack{\pi \in \Lambda^T: \\ \mathcal{B}(\pi_{1:t}) = l_{1:s}}} \prod_{\tau=1}^t y_{\pi_\tau}^\tau \rightarrow \text{total probability of } l_{1:s} \text{ at time } t$$

$$\bar{\alpha}_t(s) \stackrel{\text{def}}{=} \alpha_{t-1}(s) + \alpha_{t-1}(s-1)$$

$$\alpha_t(s) = \begin{cases} \bar{\alpha}_t(s)y_{l'_s}^t & \text{if } l'_s = b \text{ or } l'_{s-2} = l'_s \\ (\bar{\alpha}_t(s) + \alpha_{t-1}(s-2))y_{l'_s}^t & \text{otherwise} \end{cases}$$

$$\alpha_1(1) = y_b^1$$

$$\alpha_1(2) = y_{l_1}^1$$

$$\alpha_1(s) = 0, \forall s > 2$$

$$p(l|x) = \alpha_T(|l'|) + \alpha_T(|l'| - 1)$$

$l' \rightarrow$ blanks added to the beginning and the end
and inserted between every pair of labels

Illustration of the forward algorithm applied to the labelling 'CAT'. For the backward algorithm please refer to the paper.



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Speech Recognition with Deep Recurrent Neural Networks



[YouTube Video](#)

$x = (x_1, \dots, x_T) \rightarrow$ input sequence

$h = (h_1, \dots, h_T) \rightarrow$ hidden vector sequence

$y = (y_1, \dots, y_T) \rightarrow$ output vector sequence

RNN

$$h_t = \mathcal{H}(W_{xh}x_t + W_{hh}h_{t-1} + b_h)$$

$$y_t = W_{hy}h_t + b_y \quad t = 1, \dots, T$$

LSTM

$$i_t = \sigma(W_{xi}x_t + W_{hi}h_{t-1} + W_{ci}c_{t-1} + b_i)$$

$$f_t = \sigma(W_{xf}x_t + W_{hf}h_{t-1} + W_{cf}c_{t-1} + b_f)$$

$$c_t = f_t c_{t-1} + i_t \tanh(W_{xc}x_t + W_{hc}h_{t-1} + b_c)$$

$$o_t = \sigma(W_{xo}x_t + W_{ho}h_{t-1} + W_{co}c_t + b_o)$$

$$h_t = o_t \tanh(c_t)$$

$W_{ci}, W_{cf}, W_{co} \rightarrow$ diagonal

Bidirectional RNN

$$\vec{h}_t = \mathcal{H}\left(W_x \vec{h} x_t + W_{\vec{h}} \vec{h}_{t-1} + b_{\vec{h}}\right)$$

$$\overleftarrow{h}_t = \mathcal{H}\left(W_x \overleftarrow{h} x_t + W_{\overleftarrow{h}} \overleftarrow{h}_{t+1} + b_{\overleftarrow{h}}\right)$$

$$y_t = W_{\vec{h} y} \vec{h}_t + W_{\overleftarrow{h} y} \overleftarrow{h}_t + b_y$$

Deep RNN

$$h_t^n = \mathcal{H}(W_{h^{n-1} h^n} h_{t-1}^{n-1} + W_{h^n h^n} h_{t-1}^n + b_h^n)$$

$$y_t = W_{h^N y} h_t^N + b_y$$

$$h^0 = x \text{ and } n = 1, \dots, N$$

$\Pr(y|x) \rightarrow$ differentiable distribution parametrized by the network

$x \rightarrow$ acoustic input sequence

$y \rightarrow$ phonetic output sequence

$z \rightarrow$ target output sequence

$\log \Pr(z|x) \rightarrow$ objective function

$T \rightarrow$ length of x & y

$U \rightarrow$ length of z

Connectionist Temporal Classification

$$y_t = W_{\vec{h}^N y} \vec{h}_t^N + W_{\overleftarrow{h}^N y} \overleftarrow{h}_t^N + b_y$$

$$\Pr(k|t) = \frac{\exp(y_t[k])}{\sum_{k'=1}^K \exp(y_t[k'])}$$

$k = 1, \dots, K, \underbrace{K+1}_{\text{blank symbol } \emptyset \text{ (non-output)}}$

RNN Transducer

Combine a CTC-like network with a separate RNN that predicts each phoneme given the previous ones, thereby yielding a jointly trained acoustic and language model.

$t \rightarrow$ input timestep

$u \rightarrow$ output timestep

$$\Pr(k|t, u) = \frac{\exp(y_{t,u}[k])}{\sum_{k'=1}^K \exp(y_{t,u}[k'])}$$

$$y_{t,u} = W_{hy}h_{t,u} + b_y$$

$$h_{t,u} = \tanh(W_{lh}l_t + W_{ph}p_u + b_h)$$

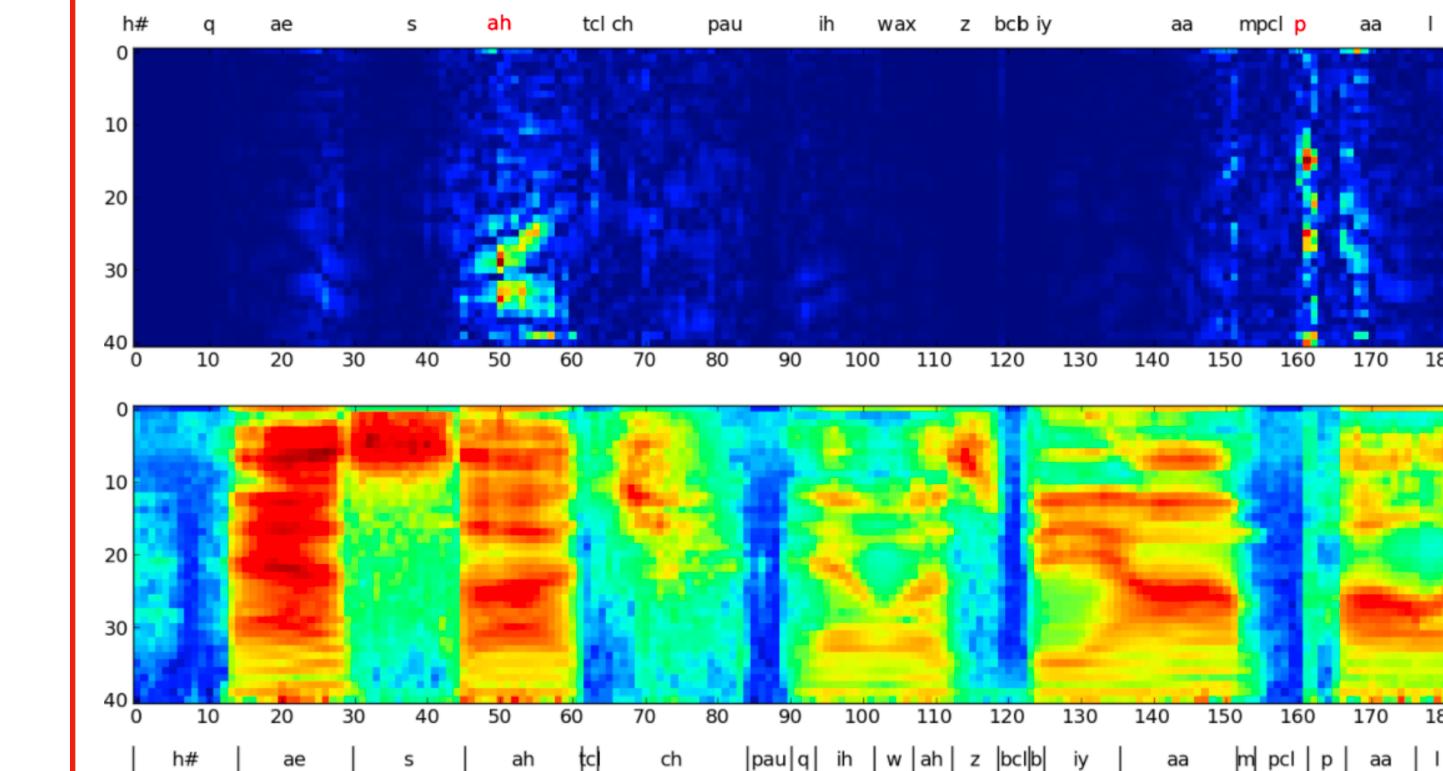
$p \rightarrow$ hidden state of the prediction network

$$l_t = W_{\vec{h}^N l} \vec{h}_t^N + W_{\overleftarrow{h}^N l} \overleftarrow{h}_t^N + b_l$$

\vec{h}^N and \overleftarrow{h}^N \rightarrow hidden sequences of the CTC network

Decoding: beam search

NETWORK	WEIGHTS	EPOCHS	PER → phoneme error rate
CTC-3L-500H-TANH	3.7M	107	37.6% → RNN
CTC-1L-250H	0.8M	82	23.9%
CTC-1L-622H	3.8M	87	23.0%
CTC-2L-250H	2.3M	55	21.0%
CTC-3L-421H-UNI	3.8M	115	19.6% → unidirectional
CTC-3L-250H	3.8M	124	18.6%
CTC-5L-250H	6.8M	150	18.4%
TRANS-3L-250H	4.3M	112	18.3%
PRETRANS-3L-250H	4.3M	144	17.7%



Input Sensitivity of a deep CTC RNN. The heatmap (top) shows the derivatives of the 'ah' and 'p' outputs printed in red with respect to the filterbank inputs (bottom). The TIMIT ground truth segmentation is shown below.



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Empirical Evaluation of Gated Recurrent Neural Networks on Sequence Modeling



[YouTube Video](#)

- Polyphonic music modeling
- speech signal modeling

RNN

$$x = (x_1, x_2, \dots, x_T)$$

$$h_0 = 0$$

$$h_t = \phi(h_{t-1}, x_t), t = 1, \dots, T$$

$$y = (y_1, y_2, \dots, y_T)$$

$$h_t = g(Wx_t + Uh_{t-1})$$

Generative RNN

$$p(x_1, \dots, x_T) = p(x_1)p(x_2 | x_1)p(x_3 | x_1, x_2) \cdots p(x_T | x_1, \dots, x_{T-1})$$

$$p(x_t | x_1, \dots, x_{t-1}) = g(h_t)$$

LSTM

$$h_t = o_t \tanh(c_t)$$

c_t → memory cell

o_t → output gate

$$o_t = \sigma(W_o x_t + U_o h_{t-1} + V_o c_t)$$

V_o → diagonal

$$c_t = f_t c_{t-1} + i_t \tilde{c}_t$$

f_t → forget gate

i_t → input gate

\tilde{c}_t → new memory

$$\tilde{c}_t = \tanh(W_c x_t + U_c h_{t-1})$$

$$f_t = \sigma(W_f x_t + U_f h_{t-1} + V_f c_{t-1})$$

$$i_t = \sigma(W_i x_t + U_i h_{t-1} + V_i c_{t-1})$$

V_f, V_i → diagonal

Gated Recurrent Unit (GRU)

$$h_t = (1 - z_t)h_{t-1} + z_t \tilde{h}_t$$

$$z_t = \sigma(W_z x_t + U_z h_{t-1}) \rightarrow \text{update gate}$$

$$\tilde{h}_t = \tanh(Wx_t + U(r_t \odot h_{t-1}))$$

$$r_t = \sigma(W_r x_t + U_r h_{t-1}) \rightarrow \text{reset gate}$$

$$\text{or } \tilde{h}_t = \tanh(Wx_t + r_t \odot (Uh_{t-1}))$$

$$\text{If } z_t = r_t = 1 \text{ then } h_t = \tilde{h}_t = \tanh(Wx_t + Uh_{t-1}).$$

$$\text{If } z_t = 0 \text{ then } h_t = h_{t-1}.$$

$$\text{If } z_t = 1 \text{ and } r_t = 0 \text{ then } h_t = \tilde{h}_t = \tanh(Wx_t).$$

Sequence modeling

$$\max_{\theta} \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} \log p(x_t^n | x_1^n, \dots, x_{t-1}^n; \theta)$$

Polyphonic music modeling datasets

Nottingham, JSB Chorales, MuseData and Piano-midi.

Each symbol in these datasets is respectively a 93-, 96-, 105-, and 108-dimensional binary vector.

Logistic sigmoid function as output units

Speech signal modeling

Look at 20 consecutive samples to predict the following 10 consecutive samples in a one-dimensional raw audio signal.

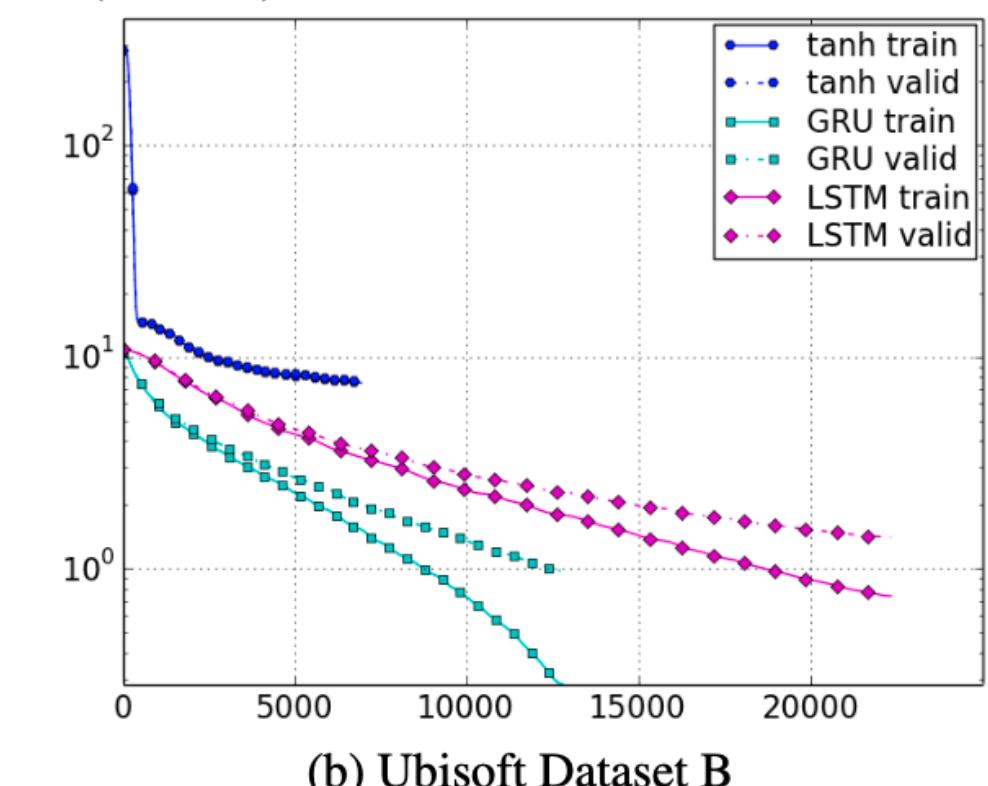
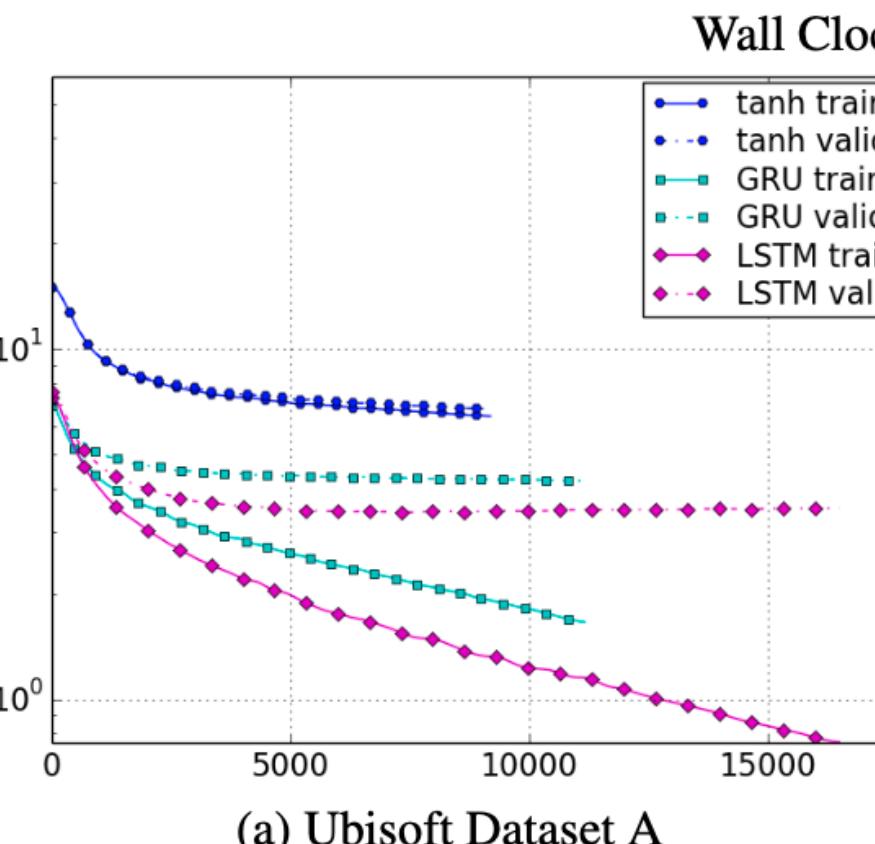
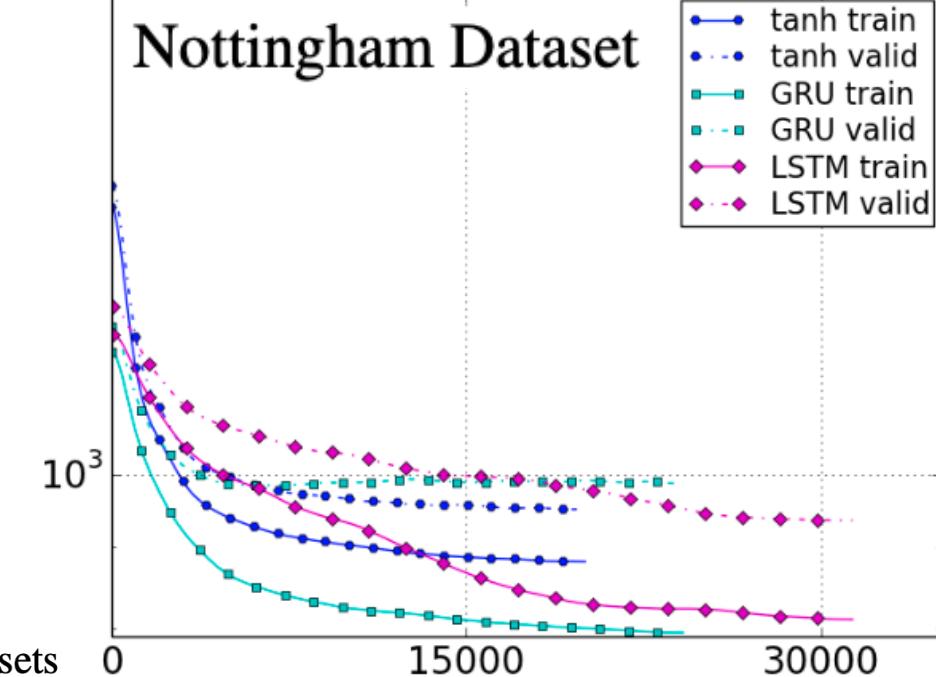
Mixture of Gaussians with 20 components as output layer

Unit	# of Units	# of Parameters
Polyphonic music modeling		
LSTM	36	$\approx 19.8 \times 10^3$
GRU	46	$\approx 20.2 \times 10^3$
tanh	100	$\approx 20.1 \times 10^3$
Speech signal modeling		
LSTM	195	$\approx 169.1 \times 10^3$
GRU	227	$\approx 168.9 \times 10^3$
tanh	400	$\approx 168.4 \times 10^3$

The average negative log-probabilities of the training and test sets

		tanh	GRU	LSTM
Music Datasets	Nottingham	train	3.22	2.79
	Nottingham	test	3.13	3.23
	JSB Chorales	train	8.82	6.94
	JSB Chorales	test	9.10	8.54
MuseData	MuseData	train	5.64	5.06
	MuseData	test	6.23	5.99
	Piano-midi	train	5.64	4.93
	Piano-midi	test	9.03	8.82
Ubisoft Datasets	Ubisoft dataset A	train	6.29	2.31
	Ubisoft dataset A	test	6.44	3.59
	Ubisoft dataset B	train	7.61	0.38
	Ubisoft dataset B	test	7.62	0.88

Results are not conclusive in comparing LSTM and GRU!





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Towards End-to-End Speech Recognition with Recurrent Neural Networks

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Automatic Speech Recognition (ASR): Transcribe Audio Data with Text
 $x = (x_1, \dots, x_T) \rightarrow$ input sequence (spectrogram)

$y = (y_1, \dots, y_T) \rightarrow$ output sequence (Deep Bidirectional LSTM)

Connectionist Temporal Classification

Sayre's Paradox for automated handwriting recognition systems: A cursively written word cannot be recognized without being segmented and cannot be segmented without being recognized!

$$p(k, t|x) = \frac{\exp(y_t^k)}{\sum_{k'} \exp(y_t^{k'})} \rightarrow \text{probability of emitting the label}$$

The output layer contains a single unit for each of the transcription labels (characters, phonemes, musical notes etc.), plus an extra “blank” unit.

$a = (a_1, \dots, a_T) \rightarrow$ CTC alignment (sequence of blank & label indices)

$\mathcal{B} \rightarrow$ operator that first removes the repeated labels & then the blanks

$$\mathcal{B}(a - bc --) = abc = \mathcal{B}(-- a - bc)$$

$$\mathcal{B}(abbbcc) = abc = \mathcal{B}(a - b - cc)$$

$$\Pr(z|x) = \sum_{a \in \mathcal{B}^{-1}(z)} \Pr(a|x) \rightarrow \text{can be efficiently evaluated \& differentiated using dynamic programming}$$

$z = (z_1, \dots, z_U) \rightarrow$ target sequence

$$\text{CTC}(x) = -\log \Pr(z^*|x) \rightarrow \text{objective function}$$

Expected Transcription Loss

$$\mathcal{L}(x) = \sum_z \Pr(z|x) \underbrace{\mathcal{L}(x, z)}_{\text{real-valued transcription loss (e.g., word error rate)}}$$

$$\mathcal{L}(x) = \sum_z \sum_{a \in \mathcal{B}^{-1}(z)} \Pr(a|x) \mathcal{L}(x, z) = \sum_a \Pr(a|x) \mathcal{L}(x, \mathcal{B}(a))$$

Graves, Alex, and Navdeep Jaitly. "Towards end-to-end speech recognition with recurrent neural networks." *International conference on machine learning*. 2014.

$$\mathcal{L}(x) \approx \frac{1}{N} \sum_{i=1}^N \mathcal{L}(x, \mathcal{B}(a^i)), a^i \sim \Pr(a|x)$$

$$\frac{\partial \log \Pr(\mathbf{a}|\mathbf{x})}{\partial \Pr(k, t|\mathbf{x})} = \frac{\delta_{\mathbf{a}_t k}}{\Pr(k, t|\mathbf{x})}$$

$$\nabla_x f(x) = f(x) \nabla_x \log f(x)$$

$$\begin{aligned} \frac{\partial \mathcal{L}(\mathbf{x})}{\partial \Pr(k, t|\mathbf{x})} &= \sum_{\mathbf{a}} \frac{\partial \Pr(\mathbf{a}|\mathbf{x})}{\partial \Pr(k, t|\mathbf{x})} \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a})) \\ &= \sum_{\mathbf{a}} \Pr(\mathbf{a}|\mathbf{x}) \frac{\partial \log \Pr(\mathbf{a}|\mathbf{x})}{\partial \Pr(k, t|\mathbf{x})} \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a})) \\ &= \sum_{\mathbf{a}: \mathbf{a}_t = k} \Pr(\mathbf{a}|\mathbf{x}, \mathbf{a}_t = k) \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a})) \end{aligned}$$

Decoding

$$\arg \max_z \Pr(z|x) \approx \mathcal{B}(\arg \max_a \Pr(a|x))$$

$\Pr^-(y, t) \rightarrow$ blank probability assigned to some (partial) output transcription y , at time t by the beam search

$\Pr^+(y, t) \rightarrow$ non-blank probability ...

$\Pr(y, t) = \Pr^-(y, t) + \Pr^+(y, t) \rightarrow$ total probability ...

$$\Pr(k, y, t) = \Pr(k, t|\mathbf{x}) \Pr(k|y) \begin{cases} \Pr^-(y, t-1) \text{ if } y^e = k \\ \Pr(y, t-1) \text{ otherwise} \end{cases}$$

extension probability of y by label k at time t

$\Pr(k|y)$ is the transition probability from y to $y+k$ and y^e is the final label in y . Define \hat{y} as the prefix of y with the last label removed, and \emptyset as the empty sequence, noting that $\Pr^+(\emptyset, t) = 0, \forall t$.

$\Pr(k|y) \rightarrow$ prior linguistic information

$$\frac{\partial \mathcal{L}(\mathbf{x})}{\partial \Pr(k, t|\mathbf{x})} \approx \frac{1}{N} \sum_{i=1}^N \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a}^{i,t,k}))$$

$$\mathbf{a}^i \sim \Pr(\mathbf{a}|\mathbf{x})$$

$$\mathbf{a}_{t'}^{i,t,k} = \mathbf{a}_t^i, \forall t' \neq t, \mathbf{a}_t^{i,t,k} = k$$

$$\frac{\partial \mathcal{L}(\mathbf{x})}{\partial y_t^k} \approx \frac{\Pr(k, t|\mathbf{x})}{N} \sum_{i=1}^N \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a}^i)) - \mathcal{Z}(\mathbf{a}^i, t)$$

$$\mathcal{Z}(\mathbf{a}^i, t) = \sum_{k'} \Pr(k', t|\mathbf{x}) \mathcal{L}(\mathbf{x}, \mathcal{B}(\mathbf{a}^{i,t,k'}))$$

With CTC, label activations are the probability of making transitions into different states, and the blank activation is the probability of remaining in the current state.

Algorithm 1 CTC Beam Search

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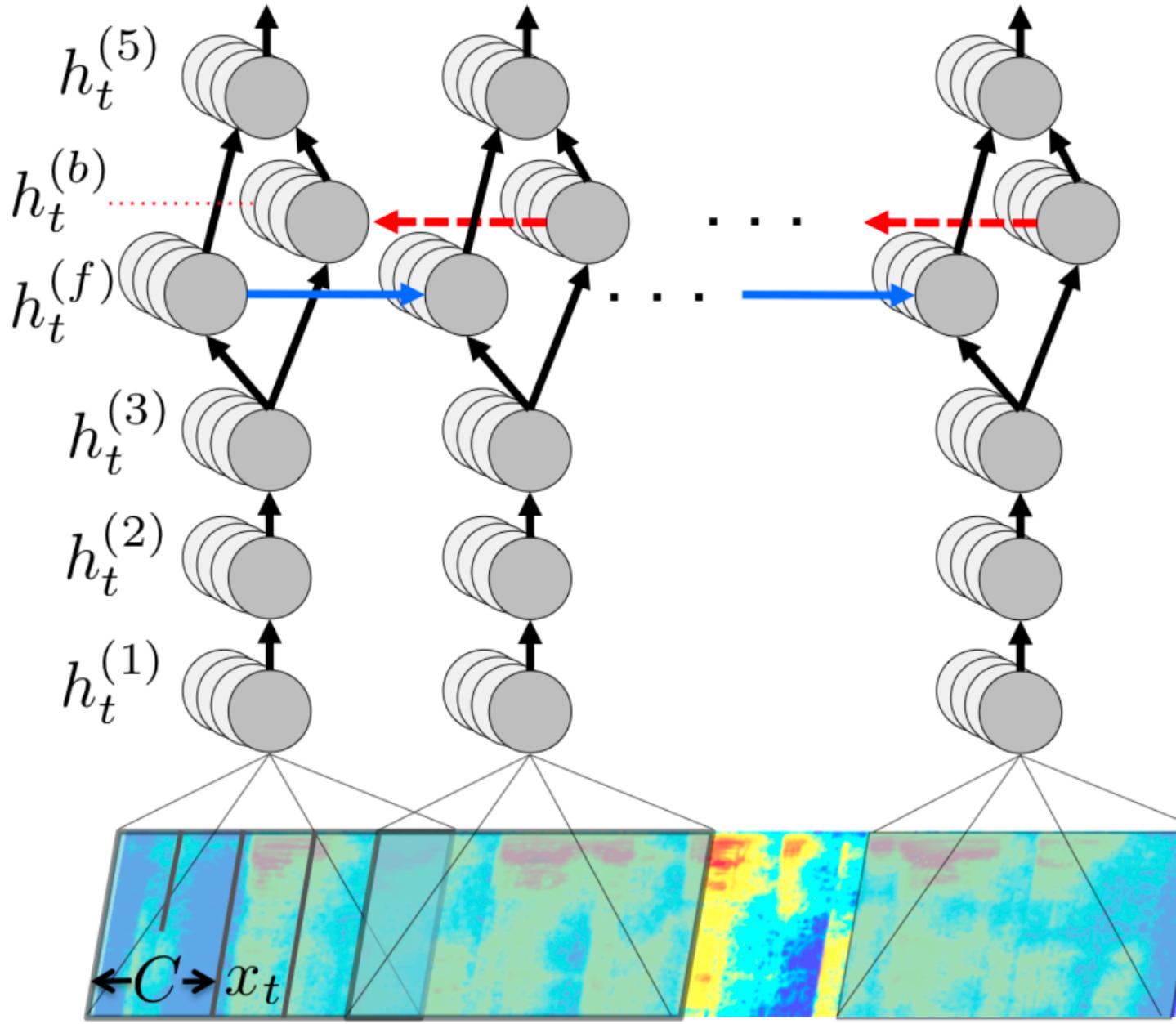
Initialise:  $B \leftarrow \{\emptyset\}; \Pr^-(\emptyset, 0) \leftarrow 1$ 
for  $t = 1 \dots T$  do
     $\hat{B} \leftarrow$  the  $W$  most probable sequences in  $B$ 
     $B \leftarrow \{\}$ 
    for  $y \in \hat{B}$  do
        if  $y \neq \emptyset$  then
             $\Pr^+(y, t) \leftarrow \Pr^+(y, t-1) \Pr(y^e, t|\mathbf{x})$ 
        if  $\hat{y} \in \hat{B}$  then
             $\Pr^+(\hat{y}, t) \leftarrow \Pr^+(\hat{y}, t-1) + \Pr(y^e, \hat{y}, t)$ 
         $\Pr^-(y, t) \leftarrow \Pr(y, t-1) \Pr(-, t|\mathbf{x})$ 
        Add  $y$  to  $B$ 
    for  $k = 1 \dots K$  do
         $\Pr^-(y+k, t) \leftarrow 0$ 
         $\Pr^+(y+k, t) \leftarrow \Pr(k, y, t)$ 
        Add  $(y+k)$  to  $B$ 
    Return:  $\max_{y \in B} \Pr^{\frac{1}{|y|}}(y, T)$ 

```



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Deep Speech: Scaling up end-to-end speech recognition

[YouTube Video](#)

$x \rightarrow$ a single utterance (speech spectrogram)

$y \rightarrow$ label (text transcription)

$\mathcal{X} = \{(x^1, y^1), (x^2, y^2), \dots\} \rightarrow$ training set

$x^i \rightarrow$ utterance (time series of length T^i)

$x_t^i, t = 1, \dots, T^i \rightarrow$ vector of audio features

$x_{t,p}^i \rightarrow$ power of the p -th frequency bin
in the audio frame at time t

$\hat{y}_t = p(c_t|x)$

$c_t \in \{a, b, \dots, z, space, apostrophe, blank\}$

$h^{(l)} \rightarrow$ hidden units at layers $l = 1, 2, \dots, 5$

$h^{(0)} \rightarrow$ input

First layer: the output at each time t depends on the spectrogram frame x_t along with a context of C frames on each side.

$$h_t^{(l)} = g(W^{(l)} h_t^{(l-1)} + b^{(l)}) \quad l = 1, 2, 3$$

$$g(z) = \min\{\max\{0, z\}, 20\}$$

The first three layers are not recurrent!

$$h_t^{(f)} = g(W^{(4)} h_t^{(3)} + W_r^{(f)} h_{t-1}^{(f)} + b^{(4)})$$

$$h_t^{(b)} = g(W^{(4)} h_t^{(3)} + W_r^{(b)} h_{t+1}^{(b)} + b^{(4)})$$

$$h_t^{(4)} = h_t^{(f)} + h_t^{(b)}$$

$$h_t^{(5)} = g(W^{(5)} h_t^{(4)} + b^{(5)})$$

$$h_{t,k}^{(6)} = \hat{y}_{t,k} \equiv \mathbb{P}(c_t = k|x) = \frac{\exp(W_k^{(6)} h_t^{(5)} + b_k^{(6)})}{\sum_j \exp(W_j^{(6)} h_t^{(5)} + b_j^{(6)})}$$

k -th column of the weight matrix

$\mathcal{L}(\hat{y}, y) \rightarrow$ CTC Loss

Decoding

$\arg \max_c Q(c) \rightarrow$ beam search

$$Q(c) = \log(\mathbb{P}(c|x)) + \alpha \log(\mathbb{P}_{lm}(c)) + \beta \text{word_count}(c)$$

N -gram Language Model

Dataset	Type	Hours	Speakers
WSJ	read	80	280
Switchboard	conversational	300	4000
Fisher	conversational	2000	23000
Baidu	read	5000	9600

RNN output

what is the weather like in boston right now
prime minister narendra modi
are there any tickets for the game

Decoded Transcription (Language Model)

what is the weather like in boston right now
prime minister narendra modi
are there any tickets for the game

Model

Model	SWB	CH	Full
Vesely et al. (GMM-HMM BMMI) [44]	18.6	33.0	25.8
Vesely et al. (DNN-HMM sMBR) [44]	12.6	24.1	18.4
Maas et al. (DNN-HMM SWB) [28]	14.6	26.3	20.5
Maas et al. (DNN-HMM FSH) [28]	16.0	23.7	19.9
Seide et al. (CD-DNN) [39]	16.1	n/a	n/a
Kingsbury et al. (DNN-HMM sMBR HF) [22]	13.3	n/a	n/a
Sainath et al. (CNN-HMM) [36]	11.5	n/a	n/a
Soltan et al. (MLP/CNN+I-Vector) [40]	10.4	n/a	n/a
Deep Speech SWB	20.0	31.8	25.9
Deep Speech SWB + FSH	12.6	19.3	16.0

System	Clean (94)	Noisy (82)	Combined (176)
Apple Dictation	14.24	43.76	26.73
Bing Speech	11.73	36.12	22.05
Google API	6.64	30.47	16.72
wit.ai	7.94	35.06	19.41
Deep Speech	6.56	19.06	11.85



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LSTM: A Search Space Odyssey

- handwriting recognition & generation
- language modeling & translation
- acoustic modeling of speech
- speech synthesis
- protein secondary structure prediction
- analysis of audio
- video data

Large-scale analysis of eight LSTM variants on three representative tasks: speech recognition, handwriting recognition, and polyphonic music modeling.

Vanilla LSTM

$x^t \rightarrow$ input vector at time t

$N \rightarrow$ number of LSTM blocks

$M \rightarrow$ number of inputs

$W_z, W_i, W_f, W_o \in \mathbb{R}^{N \times M} \rightarrow$ input weights

$R_z, R_i, R_f, R_o \in \mathbb{R}^{N \times N} \rightarrow$ recurrent weights

$p_i, p_f, p_o \in \mathbb{R}^N \rightarrow$ peephole weights
not very critical

$b_z, b_i, b_f, b_o \in \mathbb{R}^N \rightarrow$ bias weights

$g(x) = h(x) = \tanh(x)$

$\sigma(x) = \frac{1}{1 + \exp(-x)}$

$\bar{z}^t = W_z x^t + R_z y^{t-1} + b_z$

$z^t = g(\bar{z}^t) \rightarrow$ block input

$$\bar{i}^t = W_i x^t + R_i y^{t-1} + p_i \odot c^{t-1} + b_i$$

$i^t = \sigma(\bar{i}^t) \rightarrow$ input gate

$$\bar{f}^t = W_f x^t + R_f y^{t-1} + p_f \odot c^{t-1} + b_f$$

$f^t = \sigma(\bar{f}^t) \rightarrow$ forget gate

$$c^t = z^t \odot i^t + c^{t-1} \odot f^t \rightarrow \text{critical}$$

cell

$$\bar{o}^t = W_o x^t + R_o y^{t-1} + p_o \odot c^t + b_o$$

$o^t = \sigma(\bar{o}^t) \rightarrow$ output gate

$$y^t = h(c^t) \odot o^t \rightarrow$$
 block output

NIG: No input gate: $i^t = 1$

NFG: No forget gate: $f^t = 1$

NOG: No output gate: $o^t = 1$

NIAF: No input activation function: $g(x) = x$

NOAF: No output activation function: $h(x) = x$

CIFG: Coupled input and forget gate: $f^t = 1 - i^t$

NP: No peepholes:

$$\bar{i}^t = W_i x^t + R_i y^{t-1} + b_i$$

$$\bar{f}^t = W_f x^t + R_f y^{t-1} + b_f$$

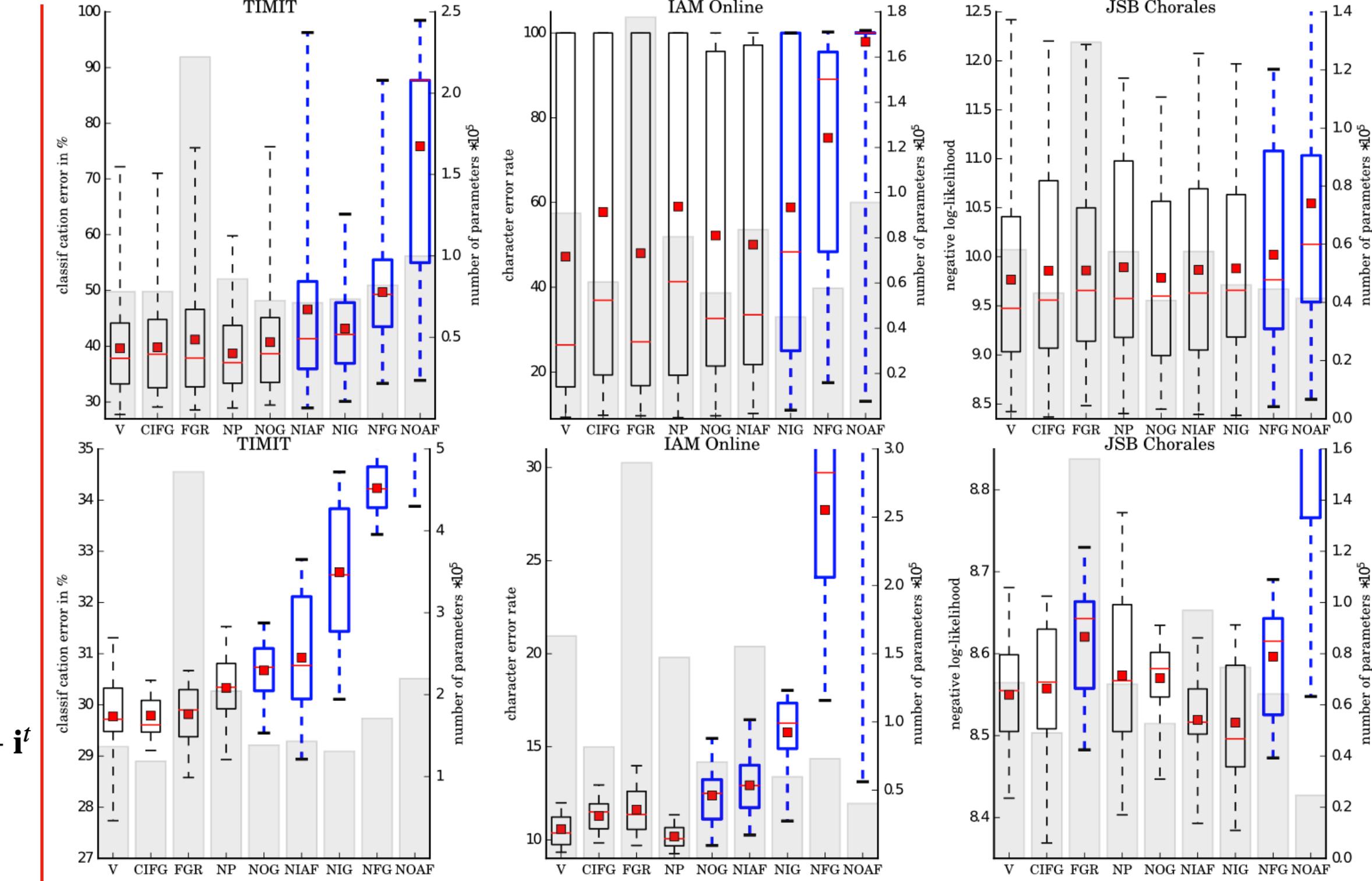
$$\bar{o}^t = W_o x^t + R_o y^{t-1} + b_o$$

FGR: Full gate recurrence

$$\bar{i}^t = W_i x^t + R_i y^{t-1} + p_i \odot c^{t-1} + b_i \\ + R_{ii} i^{t-1} + R_{fi} f^{t-1} + R_{oi} o^{t-1}$$

$$\bar{f}^t = W_f x^t + R_f y^{t-1} + p_f \odot c^{t-1} + b_f \\ + R_{if} i^{t-1} + R_{ff} f^{t-1} + R_{of} o^{t-1}$$

$$\bar{o}^t = W_o x^t + R_o y^{t-1} + p_o \odot c^{t-1} + b_o \\ + R_{io} i^{t-1} + R_{fo} f^{t-1} + R_{oo} o^{t-1}$$



Test set performance for all 200 trials (top) and for the best 10% (bottom) trials (according to the validation set) for each data set and variant. Boxes: range between the 25th and 75th percentiles of the data. Whiskers: whole range. Red dot: mean. Red line: median of the data. Thick blue lines: boxes of variants that differ significantly from the vanilla LSTM. Gray histogram in the background: average number of parameters for the top 10% performers of every variant.

TIMIT: framewise classification task (classify each audio as one of 61 phones)

IAM Online: handwriting database

Each frame of the sequence is a 4-D vector containing \bar{x} , \bar{y} (the change in pen position), t (time since the beginning of the stroke), and a fourth dimension that contains value of one at the time of the pen lifting (a transition to the next stroke) and zeroes at all other time steps.

JSB Chorales: a collection of 382 four-part harmonized chorales by Bach

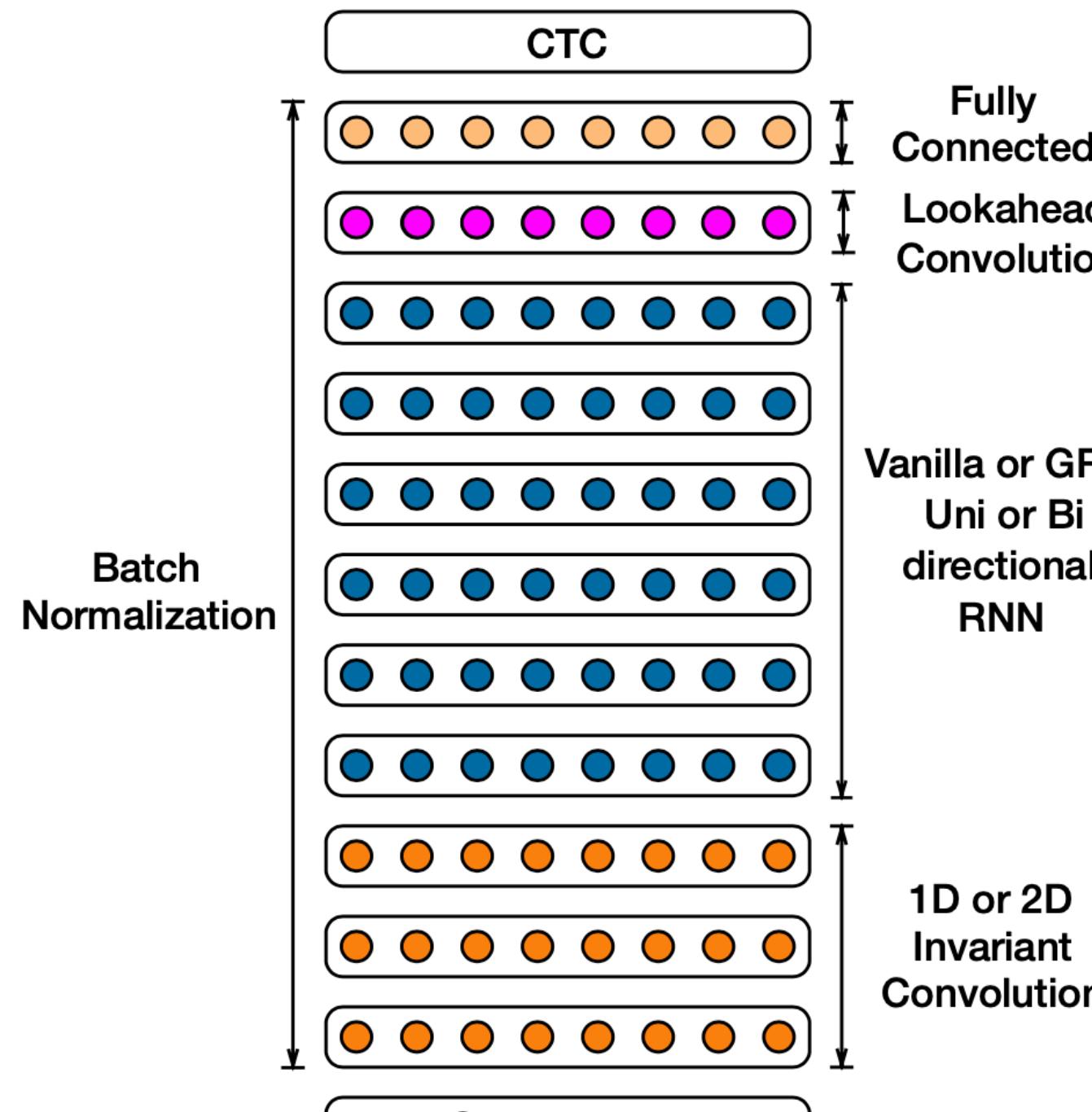


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Deep Speech 2 : End-to-End Speech Recognition in English and Mandarin



[YouTube Video](#)



The outputs are the alphabet of each language.

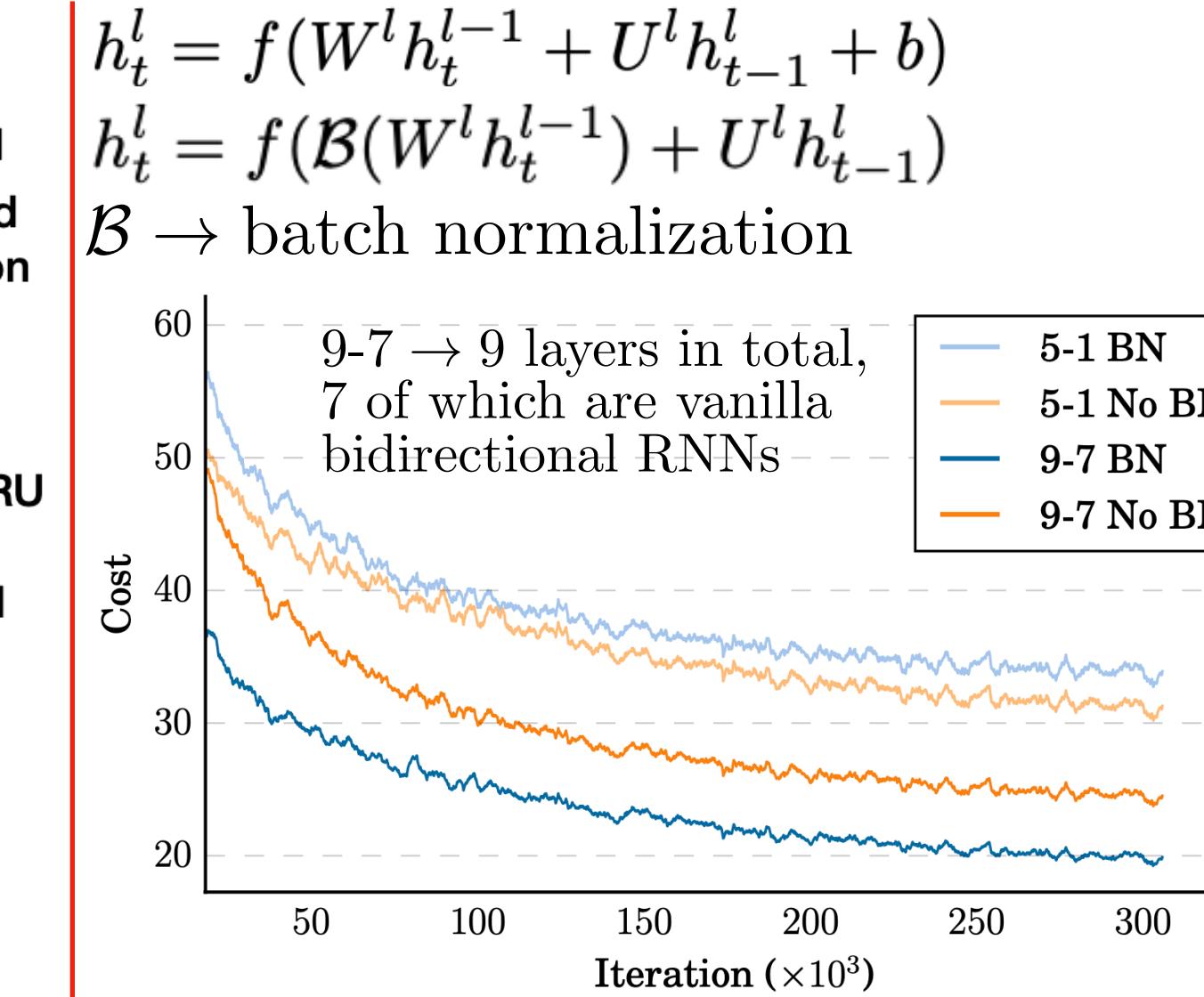
$$p(\ell_t|x) \rightarrow \text{RNN prediction}$$

ℓ_t → either a character in the alphabet or the blank symbol

$$\ell_t \in \{a, b, \dots, z, \text{space}, \text{apostrophe}, \text{blank}\}$$

inference → $\arg \max_y Q(y)$

$$Q(y) = \log(p_{\text{RNN}}(y|x)) + \alpha \log(p_{\text{LM}}(y)) + \beta \text{wc}(y)$$



SortaGrad (curriculum learning): use the length of the utterance as a heuristic for difficulty and train on the shorter (easier) utterances first.

Convolution in the time-and-frequency domain (2D) and in the time-only domain (1D).

Lookahead Convolution

$$r_{t,i} = \sum_{j=1}^{\tau+1} W_{i,j} h_{t+j-1,i}, \text{ for } 1 \leq i \leq d.$$

$$W \in \mathbb{R}^{d \times \tau}$$

Dataset Construction

Given an audio-transcript pair (x, y) , the most likely alignment is calculated as:

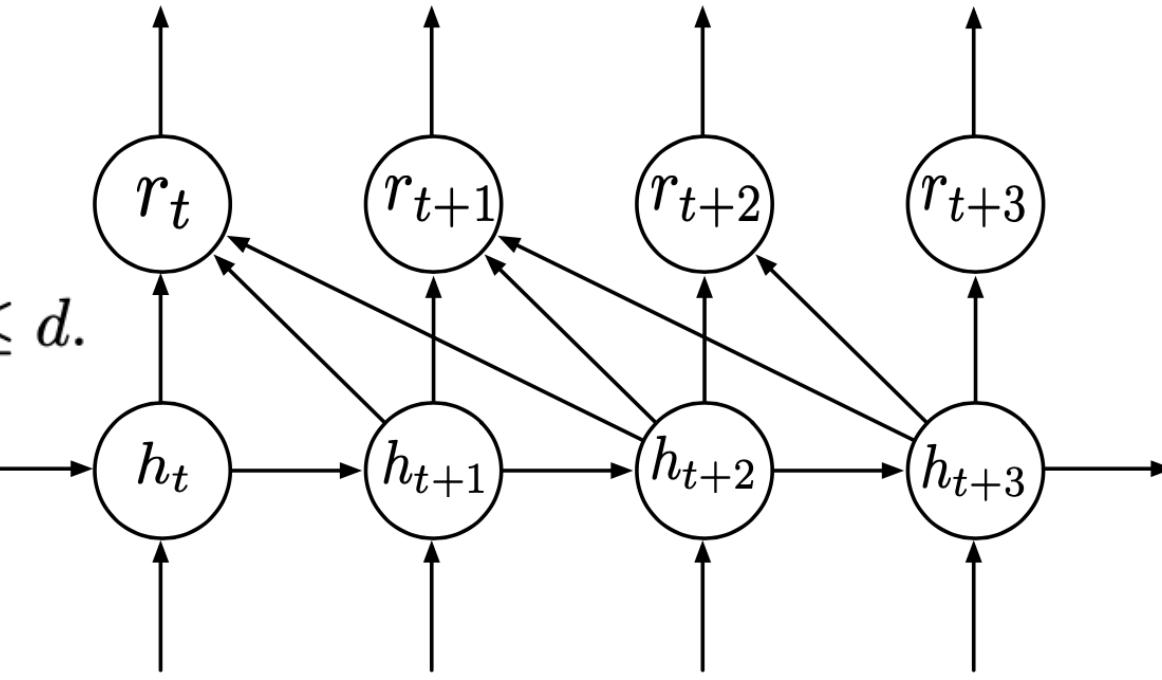
$$\ell^* = \arg \max_{\ell \in \text{Align}(x,y)} \prod_t p_{\text{ctc}}(\ell_t|x; \theta)$$

Fraction of Data	Hours	Regular Dev	Noisy Dev
1%	120	29.23	WER 50.97
10%	1200	13.80	22.99
20%	2400	11.65	20.41
50%	6000	9.51	15.90
100%	12000	8.46	13.59

Test set	Ours	Human
WSJ eval'92	3.10	5.03
WSJ eval'93	4.42	8.08
LibriSpeech test-clean	5.15	5.83
LibriSpeech test-other	12.73	12.69

Read	Ours	Human
VoxForge American-Canadian	7.94	4.85
VoxForge Commonwealth	14.85	8.15
VoxForge European	18.44	12.76
VoxForge Indian	22.89	22.15

Noisy	Ours	Human
CHiME eval real	21.59	11.84
CHiME eval sim	42.55	31.33



The best English model has 2 layers of 2D convolution, followed by 3 layers of unidirectional recurrent layers with 2560 GRU cells each, followed by a lookahead convolution layer with $\tau = 80$, trained with BatchNorm and SortaGrad.

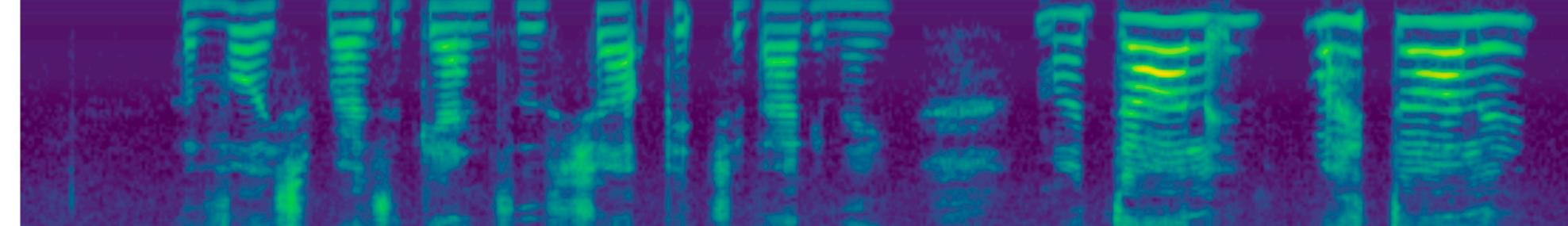
Test	Mandarin	Human	RNN
100 utterances / committee		4.0	3.7
250 utterances / individual		9.7	5.7

Architecture	Dev	Test
5-layer, 1 RNN	7.13	15.41
5-layer, 3 RNN	6.49	11.85
5-layer, 3 RNN + BatchNorm	6.22	9.39
9-layer, 7 RNN + BatchNorm + frequency Convolution	5.81	7.93

SpecAugment: A Simple Data Augmentation Method for Automatic Speech Recognition


[YouTube Playlist](#)

log mel spectrogram of the base input with no augmentation

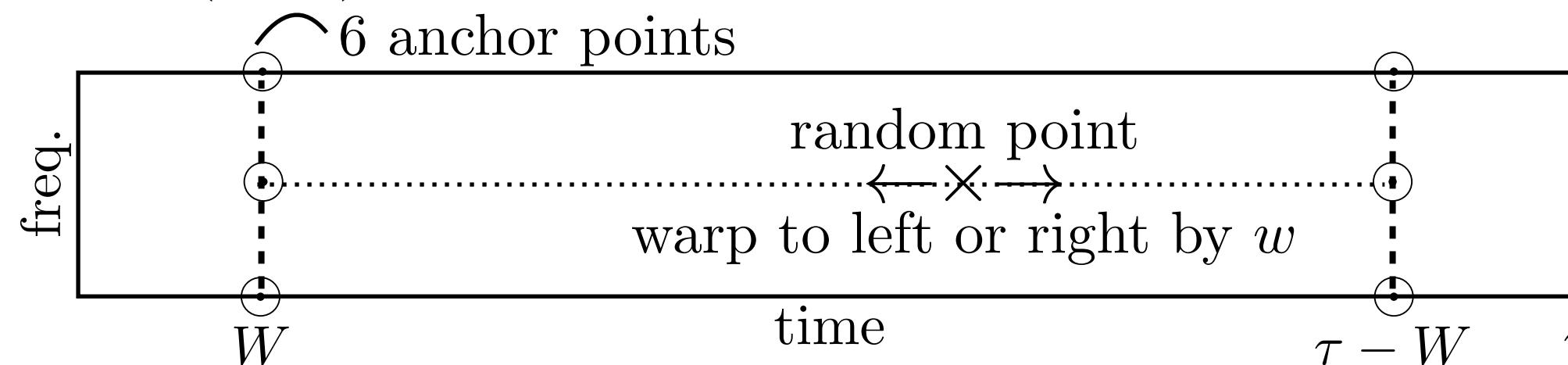


Time Warping

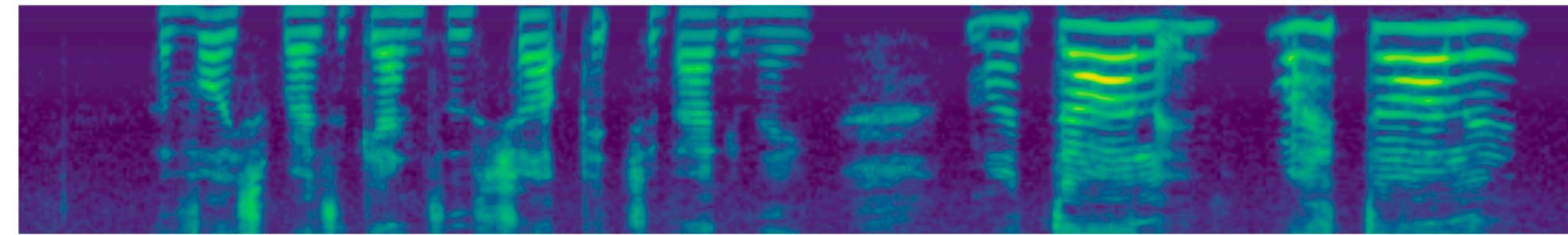
$\tau \rightarrow$ number of time steps in the log mel spectrogram

$W \rightarrow$ time warp parameter

$w \sim U(0, W)$



function `sparse_image_warp` of TensorFlow



Frequency Masking

$[f_0, f_0 + f] \rightarrow f$ consecutive mel frequency channels to be masked

$f \sim U(0, F) \quad F \rightarrow$ frequency mask parameter

$f_0 \rightarrow$ chosen from $[0, \nu - f]$

$\nu \rightarrow$ number of mel frequency channels

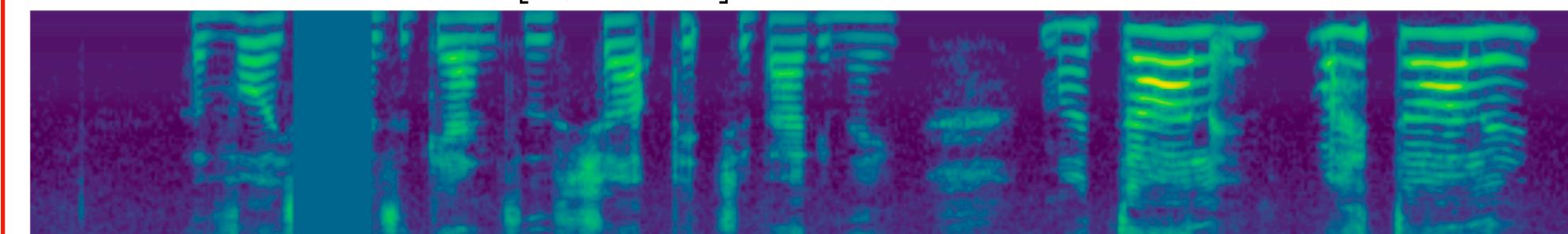


Time Masking

$[t_0, t_0 + t] \rightarrow t$ consecutive time steps to be masked

$t \sim U(0, T) \quad T \rightarrow$ time mask parameter

$t_0 \rightarrow$ chosen from $[0, \tau - t]$

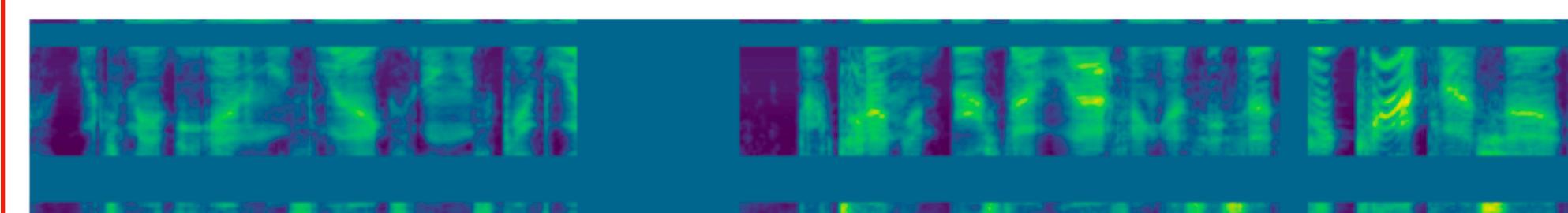
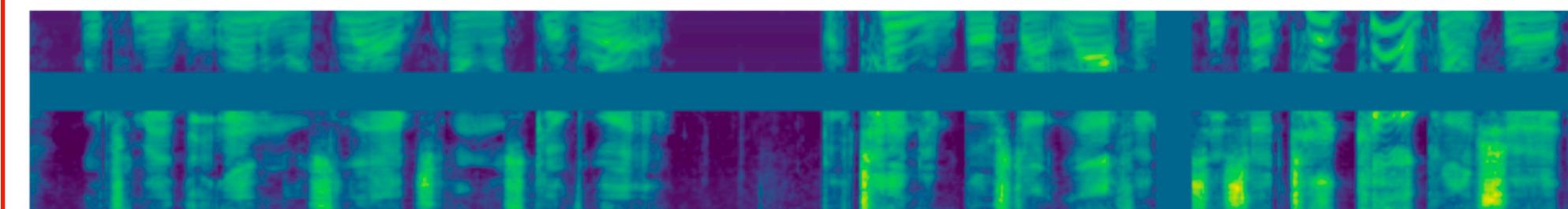
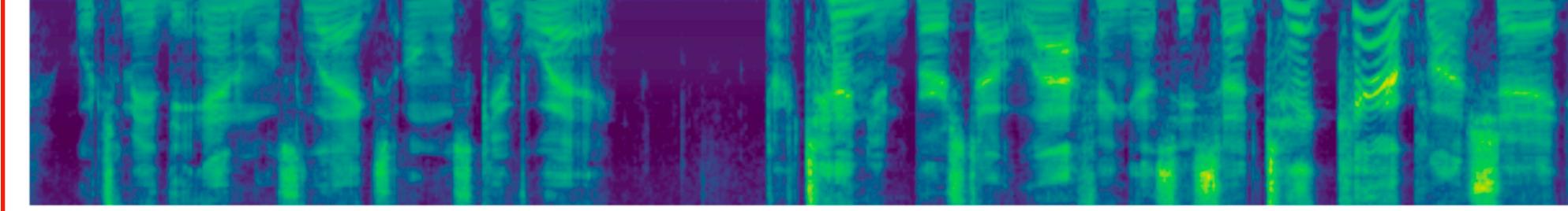


Augmentation Policies

Policy	W	F	m_F	T	p	m_T
None	0	0	-	0	-	-
LibriSpeech Basic \leftarrow LB	80	27	1	100	1.0	1
LibriSpeech Double \leftarrow LD	80	27	2	100	1.0	2
Switchboard Mild \leftarrow SM	40	15	2	70	0.2	2
Switchboard Strong \leftarrow SS	40	27	2	70	0.2	2

$m_F \rightarrow$ number of frequency masks applied

$m_T \rightarrow$ number of time masks applied



Listen, Attend and Spell (LAS)

log mel spectrogram \triangleright

2-layer CNN with max-pooling & stride 2 \triangleright

encoder (d stacked bidirectional LSTMS with cell size w)

\rightarrow attention vectors

attention vectors \triangleright

2-layer RNN decoder of cell dimension w

\rightarrow tokens for transcription

Text is tokenized using a Word Piece Model (WPM)

Language Model

$$\mathbf{y}^* = \underset{\mathbf{y}}{\operatorname{argmax}} (\log P(\mathbf{y}|\mathbf{x}) + \lambda \log P_{LM}(\mathbf{y}))$$

Results

Three training results for which time warping, time masking and frequency masking have been turned off, respectively.

test-other	test	
10.0	3.7	\rightarrow Test set WER (%)
10.1	3.8	\rightarrow Time Warping
11.0	4.0	\rightarrow Time Masking
10.9	4.1	\rightarrow Freq. Masking

Datasets

- LibriSpeech960h

- Switchboard300h

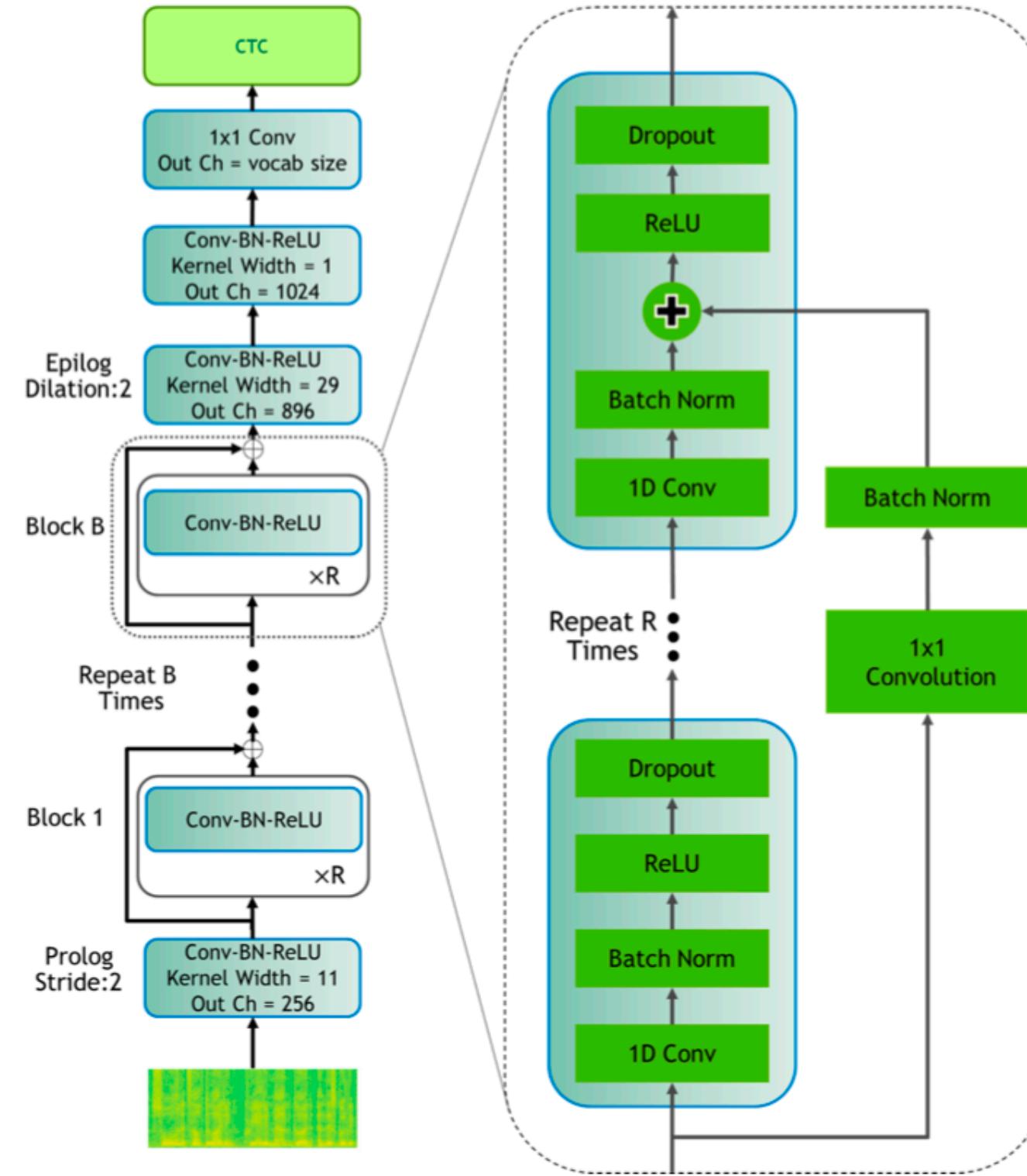


Boulder

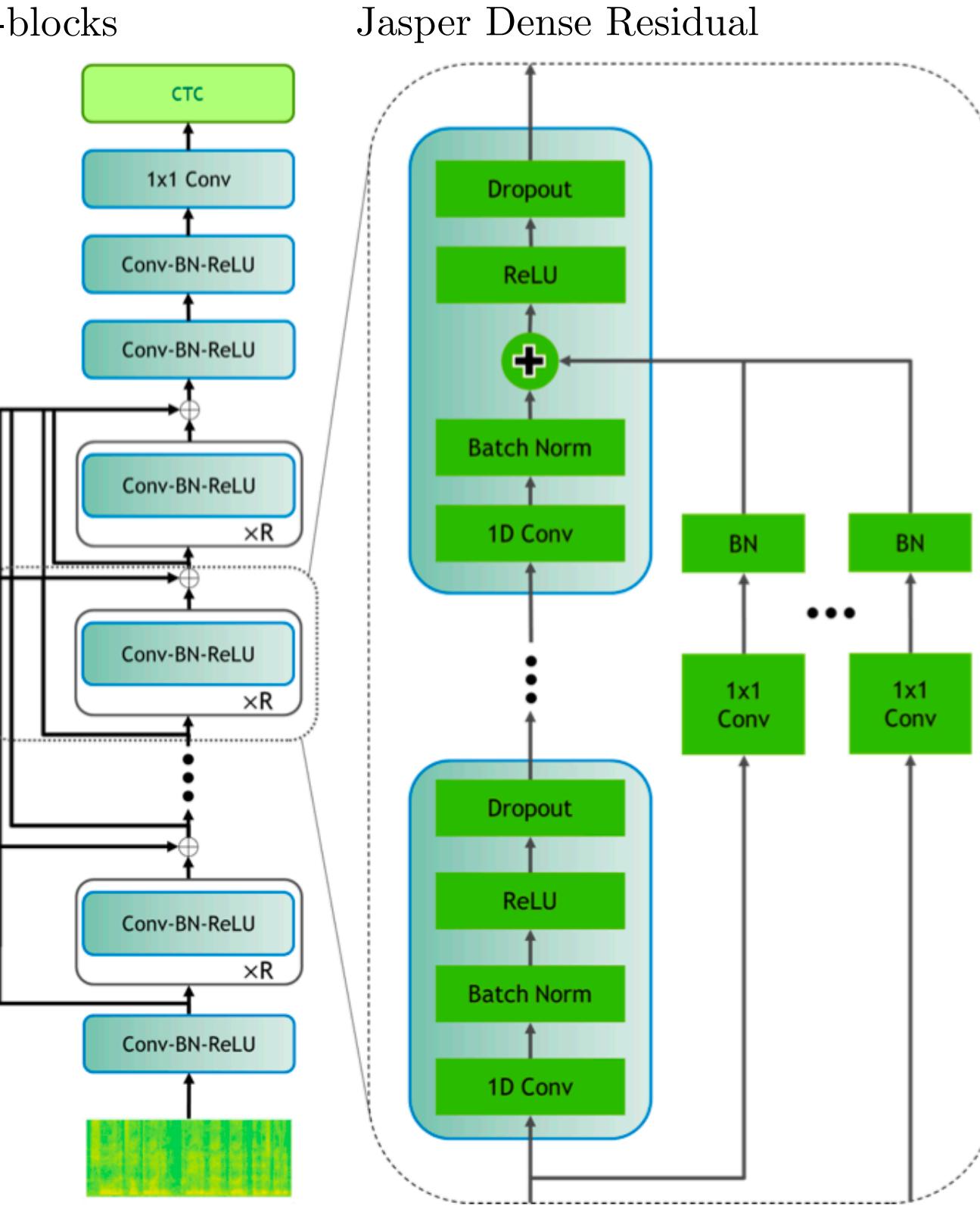
Jasper: An End-to-End Convolutional Neural Acoustic Model



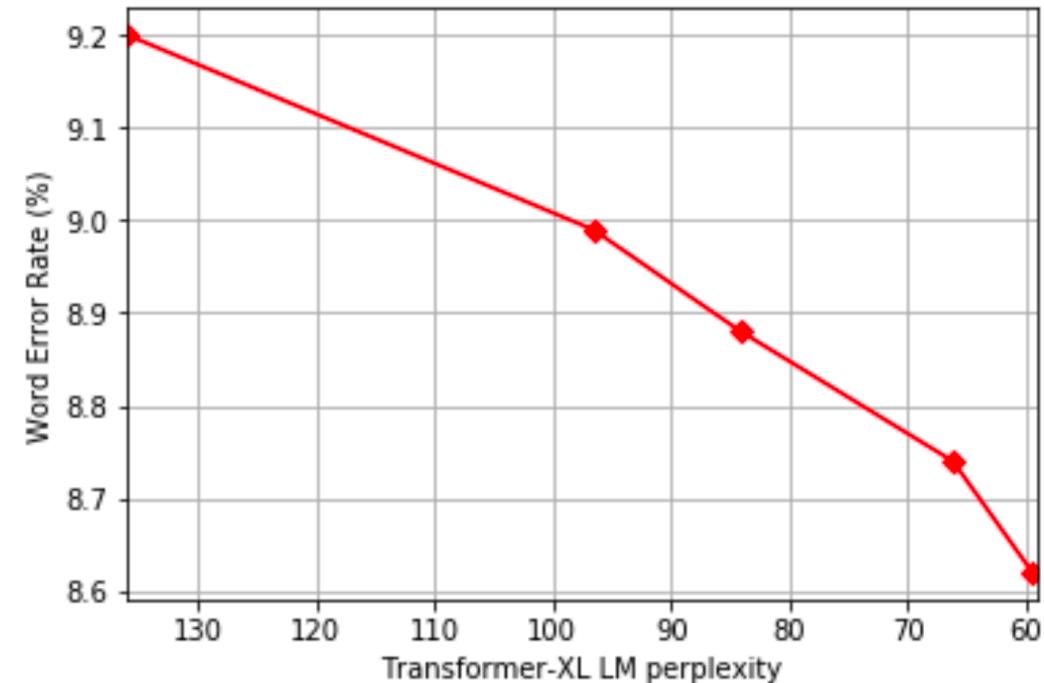
YouTube Video

Jasper $B \times R$ model: B - number of blocks, R - number of sub-blocks

Jasper Dense Residual



# Blocks	Block	Kernel	# Output Channels	Dropout	# Sub Blocks
1	Conv1	11 stride=2	256	0.2	1
2	B1	11	256	0.2	5
2	B2	13	384	0.2	5
2	B3	17	512	0.2	5
2	B4	21	640	0.3	5
2	B5	25	768	0.3	5
1	Conv2	29 dilation=2	896	0.4	1
1	Conv3	1	1024	0.4	1
1	Conv4	1	# graphemes	0	1



NovoGrad

NovoGrad is similar to Adam, except that its second moments are computed per layer instead of per weight.

$$v_t^l = \beta_2 \cdot v_{t-1}^l + (1 - \beta_2) \cdot \|g_t^l\|^2$$

$$m_t^l = \beta_1 \cdot m_{t-1}^l + \frac{g_t^l}{\sqrt{v_t^l + \epsilon}}$$

$$m_t^l = \beta_1 \cdot m_{t-1}^l + \frac{g_t^l}{\sqrt{v_t^l + \epsilon}} + d \cdot w_t$$

weight decay

$$w_{t+1} = w_t - \alpha_t \cdot m_t$$

Model	#params, M	Dev	Clean	Other
Residual	201	4.65	14.36	
Dense Residual	211	4.51	14.15	
DenseNet	205	4.77	14.55	
DenseRNet	211	4.32	14.21	

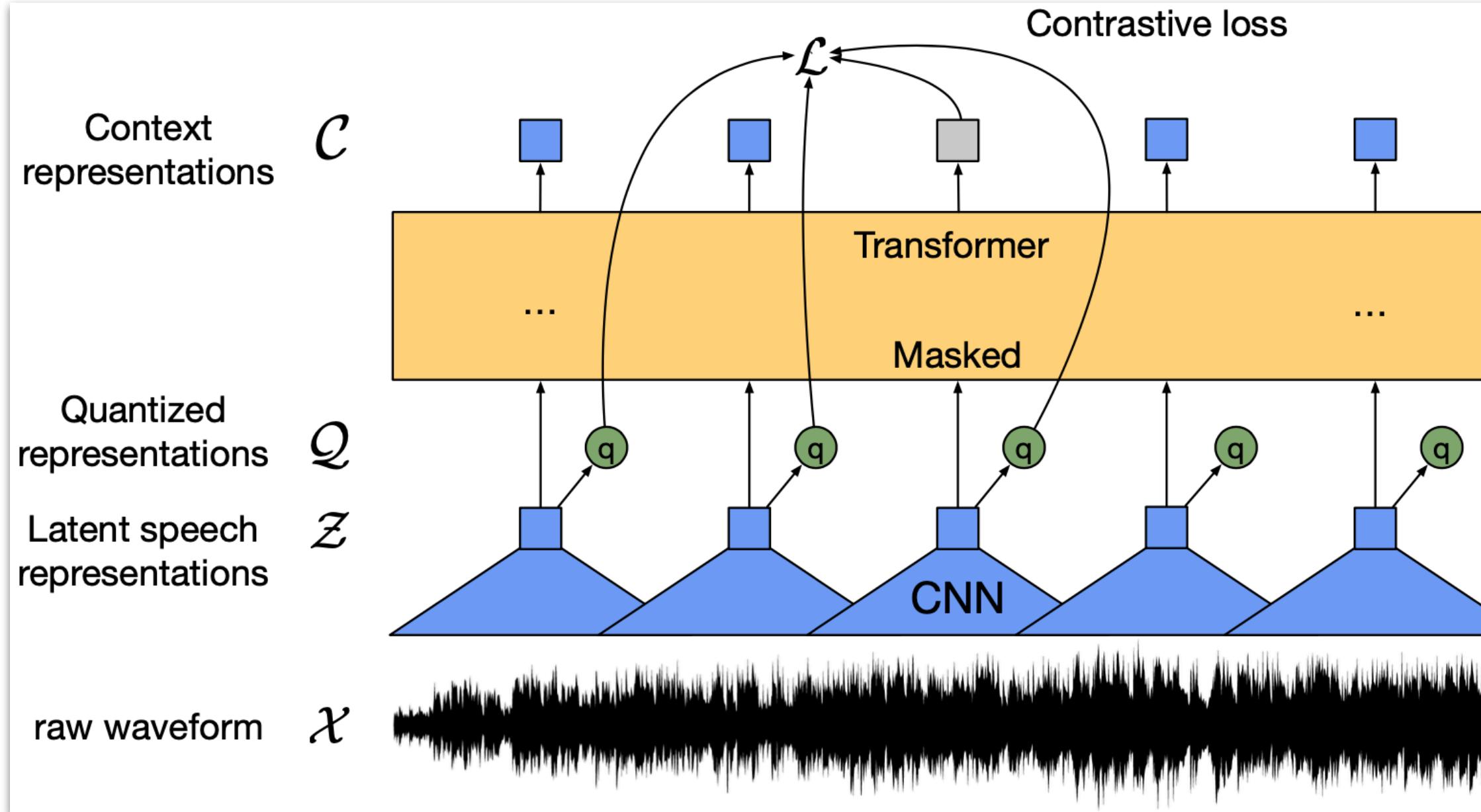
Model	E2E	LM	dev-clean	dev-other	test-clean	test-other
CAPIO (single) [23]	N	RNN	3.02	8.28	3.56	8.58
pFSMN-Chain [25]	N	RNN	2.56	7.47	2.97	7.5
DeepSpeech2 [26]	Y	5-gram	-	-	5.33	13.25
Deep bLSTM w/ attention [21]	Y	LSTM	3.54	11.52	3.82	12.76
wav2letter++ [27]	Y	ConvLM	3.16	10.05	3.44	11.24
LAS + SpecAugment ⁴ [28]	Y	RNN	-	-	2.5	5.8
Jasper DR 10x5	Y	-	3.64	11.89	3.86	11.95
Jasper DR 10x5	Y	6-gram	2.89	9.53	3.34	9.62
Jasper DR 10x5	Y	Transformer-XL	2.68	8.62	2.95	8.79
Jasper DR 10x5 + Time/Freq Masks ⁴	Y	Transformer-XL	2.62	7.61	2.84	7.84

LibriSpeech, WER (%)

WSJ End-to-End Models, WER (%)			
Model	LM	nov93	nov92
seq2seq + deep conv [35]	-	-	10.5
wav2letter++ [27]	4-gram	9.5	5.6
wav2letter++ [27]	ConvLM	7.5	4.1
E2E LF-MMI [14]	3-gram	-	4.1
Jasper 10x3	-	16.1	13.3
Jasper 10x3	4-gram	9.9	7.1
Jasper 10x3	Transformer-XL	9.3	6.9

Model	E2E	LM	SWB	CHM
LF-MMI [14]	N	RNN	7.3	14.2
Attention Seq2Seq [36]	Y	-	8.3	15.5
RNN-T [37]	Y	4-gram	8.1	17.5
Char E2E LF-MMI [14]	Y	RNN	8.0	17.6
Phone E2E LF-MMI [14]	Y	RNN	7.5	14.6
CTC + Gram-CTC	Y	N-gram	7.3	14.7
Jasper DR 10x5	Y	4-gram	8.3	19.3
Jasper DR 10x5	Y	Transformer-XL	7.8	16.2

wav2vec 2.0: A Framework for Self-Supervised Learning of Speech Representations


[YouTube Video](#)


$$f : \mathcal{X} \mapsto \mathcal{Z}$$

└ multi-layer convolutional feature encoder

$\mathcal{X} \rightarrow$ input raw audio

$\mathcal{Z} = (z_1, z_2, \dots, z_T) \rightarrow$ latent speech representations

$$g : \mathcal{Z} \mapsto \mathcal{C}$$

└ transformer

$\mathcal{C} = (c_1, c_2, \dots, c_T) \rightarrow$ representations capturing information from the entire sequence

Instead of fixed positional embeddings which encode absolute positional information, use a convolutional layer which acts as relative positional embedding.

$$\mathcal{Z} \xrightarrow{Q} \mathcal{Q}$$

quantization module
 $\mathcal{Q} = (q_1, q_2, \dots, q_T)$

diversity loss: encourage the model to use the codebook entries equally often

Quantization Module

$G \rightarrow$ number of codebooks/groups

$V \rightarrow$ number of entries

$$e \in \mathbb{R}^{V \times d/G}$$

Choose one entry/row from each codebook e and concatenate the resulting vectors e_1, \dots, e_G and apply a linear transformation $\mathbb{R}^d \rightarrow \mathbb{R}^f$ to obtain $q \in \mathbb{R}^f$. The Gumbel softmax enables choosing discrete codebook entries in a fully differentiable way!

$$z \mapsto l$$

$z \rightarrow$ feature encoder output

$$l \in \mathbb{R}^{G \times V} \rightarrow \text{logits}$$

$$p_{g,v} = \frac{\exp(l_{g,v} + n_v)/\tau}{\sum_{k=1}^V \exp(l_{g,k} + n_k)/\tau}$$

probability of choosing the v -th codebook entry for group g

$\tau \rightarrow$ non-negative temperature

$$n = -\log(-\log(u)) \rightarrow \text{Gumbel noise} \quad u \sim U(0, 1)$$

Forward pass: $i = \arg \max_j p_{g,j} \rightarrow$ codeword i

Backward pass: true gradient of the Gumbel softmax outputs

$$\text{Pre-training} \quad \mathcal{L}_m = -\log \frac{\exp(\text{sim}(\mathbf{c}_t, \mathbf{q}_t)/\kappa)}{\sum_{\tilde{\mathbf{q}} \sim \mathbf{Q}_t} \exp(\text{sim}(\mathbf{c}_t, \tilde{\mathbf{q}})/\kappa)} \quad \text{sim}(\mathbf{a}, \mathbf{b}) = \mathbf{a}^T \mathbf{b} / \|\mathbf{a}\| \|\mathbf{b}\|$$

contrastive loss: identify the true quantized latent speech representation for a masked time step within a set of distractors.

$$\mathcal{L}_d = \frac{1}{GV} \sum_{g=1}^G -H(\bar{p}_g) = \frac{1}{GV} \sum_{g=1}^G \sum_{v=1}^V \bar{p}_{g,v} \log \bar{p}_{g,v} \quad \mathcal{L} = \mathcal{L}_m + \alpha \mathcal{L}_d$$



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Questions?

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