## CSE 330 Summer 2024 Assignment 5

**Total Marks: 25** 

1. A linear system is described by the following equations:

$$-3x + 7y + 2z = 15$$

$$4x + 3y + \frac{3}{2}z = 11$$

$$x - 9y - 3z = -25$$

Based on these equations, answer the questions below.

- (a) [1 mark] From the given linear equations, identify the matrices **A**, **x** and **b** such that the linear system can be expressed as a matrix equation.
- (b) [5 marks] Construct the Frobenius matrices  $\mathbf{F}^{(1)}$  and  $\mathbf{F}^{(2)}$  from this system.
- (c) [5 + 2 = 7 marks] Compute the **upper triangular matrix U** and the **lower triangular matrix L** and prove that **LU = A**.
- (d) [5 marks] Now find the solution of the linear system using the LU decomposition method.
- 2. A function is given by  $f(x) = e^{-3x} + \cos x x^4$  which is to be integrated on the interval [1, 3].
- a. (2 marks) Evaluate the exact integral I(f).
- b. (3 marks) Compute the numerical integral by using the Trapezoid Rule
- c. (2 marks) Find the relative percentage error