

**CSE 330 (Summer 2024)**  
**Assignment 2**  
**Total Marks: 40**

1. Consider the following table of data points/nodal points:

Time (sec) $t$	Velocity (m/s) $v(t)$
10	22
12	28
15	40

- (a) [3+1 marks] Find an interpolating polynomial of velocity that goes through the above data points by using **Vandermonde Matrix** method. Also compute an approximate value of acceleration at Time,  **$t=23$  sec**.
- (b) [4 marks] Find an interpolating polynomial of velocity that goes through the above data points by using **Lagrange** method.
- (c) [2 marks] If a **new data point** is added in the above scenario, which method should you use in finding a new interpolating polynomial? Also what will be the degree of that new polynomial? Explain your answers.

2. Read the following and answer accordingly:

- (a) [4 marks] Consider the nodes  **$[-\pi/4, 0, \pi/4]$** . Find an interpolating polynomial of appropriate degree by using **Newton's Divided-Difference** method for  **$f(x) = x \cos(x)$** .
- (b) [2 marks] Use the interpolating polynomial to find an approximate value at  **$\pi/6$** , and compute the percentage relative error at  **$\pi/6$** .
- (c) [4 marks] Add a new node  **$\pi$**  to the above nodes, and find the interpolating polynomial of appropriate degree.

3. An interpolating polynomial,  **$p_1(x) = 1.648(x - 1)$**  is derived for the function  **$f(x) = x \ln x$**  at the nodes ( **$x_0 = 1, x_1 = 3$** ) using the Lagrange method. Answer the following keeping up to 4 significant figures.

- (a) (1 mark) Explain what you need to do to obtain a **degree 3** interpolating polynomial for the same function  **$f(x)$**  and for the same nodal points ( **$x_0 = 1, x_1 = 3$** ).
- (b) (4 marks) Calculate the bases of the **degree 3** polynomial.

4. [5 marks] The function  **$f(x) = e^{3x} - e^{-3x}$**  has been interpolated at the nodes at  **$(-2, 0, 2)$**  using Lagrange method. Evaluate the upper bound of the interpolation error for the interval  **$[-3, 3]$**  using Cauchy's theorem. Keep up to 7 significant figures.

5. Consider the following **Runge Function**  **$f(x) = 1/(1+25x^2)$** , given interval  **$[-5/2, 5/2]$**  and  **$n = 2$** . Answer the following using the given data,

- (a) [5 marks] Calculate the corresponding **equal angled points**.
- (b) [5 marks] Calculate the **Chebyshev Nodes** up to 5 significant figures.