

**BRAC UNIVERSITY**  
**CSE331 : Automata and Computability**  
**Assignment 4**

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**1. Draw the state diagram of a PDA for the following CFL:**

- A.  $L(M) \rightarrow \{0^n 1^m \mid n, m \geq 0 \text{ and } 2n = 3m\}$ , where  $\Sigma = \{0, 1\}$
- B.  $L(M) \rightarrow \{0^n 1^m 2^m 3^n \mid n, m > 0\}$ , where  $\Sigma = \{0, 1, 2, 3\}$
- C.  $L(M) \rightarrow \{w = 0^i 1^j 2^k \mid i, j, k \geq 0 \text{ and } j < i + k\}$ , where  $\Sigma = \{0, 1, 2\}$
- D.  $L(M) \rightarrow \{w_1 \# w_2 \mid \text{the number of } 00 \text{ in } w_1 \text{ is equal to the number of } 11 \text{ in } w_2\}$ , where  $\Sigma = \{0, 1\}$
- E.  $L(M) \rightarrow \{w \# x \mid w^R \text{ is a substring of } x\}$ , where  $\Sigma = \{0, 1\}$

**2. Draw the state diagram of a TM that decides the following languages:**

- A.  $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains equal numbers of } 0\text{s and } 1\text{s}\}$ , where  $\Sigma = \{0, 1\}$
- B.  $L(M) \rightarrow \{0^n 1^n 2^n \mid n, m \geq 0\}$ , where  $\Sigma = \{0, 1, 2\}$
- C.  $L(M) \rightarrow \{0^i 1^j 2^k \mid i, j, k > 0 \text{ and } k = i * j\}$ , where  $\Sigma = \{0, 1, 2\}$
- D.  $L(M) \rightarrow \{0^{2^n} \mid n \geq 0\}$ , where  $\Sigma = \{0\}$
- E.  $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ is a palindrome}\}$ , where  $\Sigma = \{0, 1\}$

**3. Prove that the following languages are decidable.**

- A.  $L = \{\langle M, w \rangle \mid \text{The Turing machine } M \text{ halts on input } w \text{ within } N \text{ steps}\}$
- B.  $L = \{\langle G \rangle \mid G \text{ is a connected undirected graph}\}$

**4. Show that the following statements are true:**

- A. The collection of decidable languages is closed under Union.
- B. The collection of decidable languages is closed under Complement.