

1, 10, 2

$$\sum_{n=0}^{\infty} \frac{(2x)^n}{3^n}$$

$$\{x: 2|x| < 3\}$$

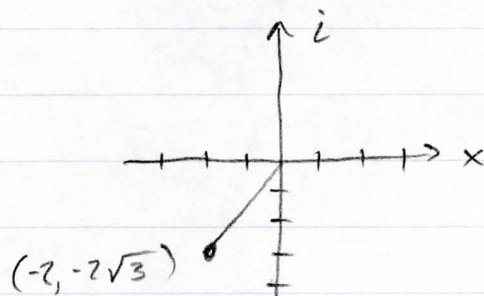
$$\{x: |x| < 3/2\}$$

$$(-1.5, 1.5)$$

2, 4, 12

$$\begin{aligned} 4 \left(\cos \frac{2\pi}{3} - i \sin \frac{2\pi}{3} \right) &= 4 \left(\frac{1}{2} + i \frac{\sqrt{3}}{2} \right) \\ &= -2(1 + i\sqrt{3}) \\ &= -2 - 2i\sqrt{3} \end{aligned}$$

polar: $r=4$, $\theta = -120^\circ$



$$-2 - 2i\sqrt{3} = 4 \left(\cos \frac{2\pi}{3} - i \sin \frac{2\pi}{3} \right) = 4e^{i2\pi/3}$$

$$x = r \cdot \cos \theta$$

$$y = r \cdot \sin \theta$$

$$x = -2$$

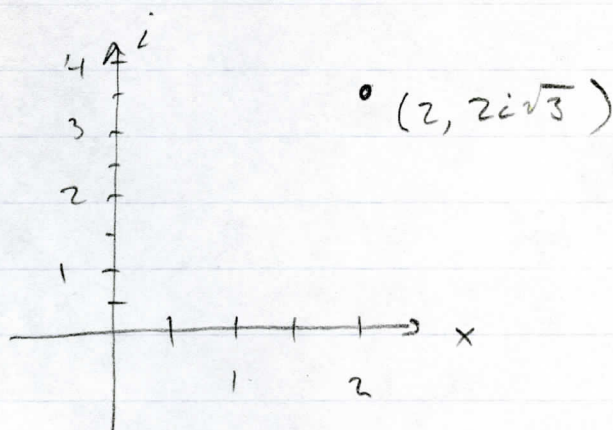
$$y = -2i\sqrt{3}$$

$$x = 4 \cos \frac{2\pi}{3}$$

$$y = 4 \sin \frac{2\pi}{3}$$

2.5.5

$$\begin{aligned}(i + \sqrt{3})^2 &= (i + \sqrt{3})(i + \sqrt{3}) \\&= i^2 + 2i\sqrt{3} + 3 \\&= 2 + 2i\sqrt{3}\end{aligned}$$



2.5.41

$$(2x - 3y - 5) + i(x + 2y + 1) = 0$$

$$2x - 3y - 5 + (0 + i)(x + 2y + 1) = 0$$

$$(2 + i)x + 5 + i + (-3 + 2i)y = 0$$

$$(2 + i)x = 5 - i + (3 - 2i)y$$

Solve for x:

$$x = \frac{5 - i + (3 - 2i)y}{(2 + i)} = \frac{(2 - i)((3 - 2i)y + 5 - i)}{5}$$

Solve for y:

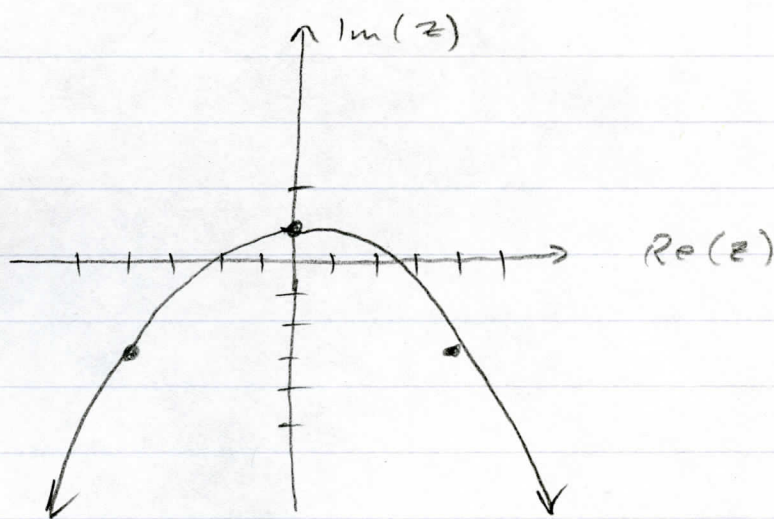
$$y = \frac{(2 + i)x - 5 + i}{(3 - 2i)} = \frac{(3 - 2i)((2 + i)x - 5 + i)}{13}$$

$$y = \left(\frac{4}{13} + \frac{7i}{13} \right) x + \left(-\frac{17}{13} - \frac{7i}{13} \right) = \frac{7i(x - 1) + 4x - 17}{13}$$

2.5.59 $|z + 3i| = 4$ has complex solutions

$$z = -4 - 3i \quad \text{and}$$

$$z = 4 - 3i$$



$$-\sqrt{16 - z^2} - 3 \rightarrow z = -4 - 3i$$

$$\sqrt{16 - z^2} - 3 \rightarrow z = 4 - 3i$$