

12. (7 pts) To compare five different formulations of fuel, seven different armored vehicles drove the identical route once with each fuel type. For each vehicle/fuel-type combination a fuel cost-of-operation value was determined. These numbers were analyzed with a **standard Two-Factor ANOVA** model yielding the table which is partially filled in below.

$n = 35$
 $35 - (6 \times 4) = 11$

Source	D.F.	Sums of Squares	Mean Squares	Fs	F $\alpha = .05$
Armored Vehicle	6	82	13.667	3.417	0.0372
Fuel Types	4	48	12	3	0.0669
Exp. Error	11	44	4		
Total	34	174			

(total trials) - 1

$\frac{SS}{DF}$ $\frac{MS}{MS_E}$

A) Fill in the missing entries.

B) Making the normal assumptions, would you accept the hypothesis that there is no significant difference between the fuel cost of operations for each vehicle type, with $\alpha = .05$? Why?

Reject due to p-value 0.0372 for vehicle type.

13. (10) A reduced regression model for predicting Sonar Detection Range included Water Depth (w), Sensor Modification (s), and Water Depth/SensorMod (ws) Interactions in the form:

$$\hat{Y} = \beta_0 + \beta_1 w + \beta_2 s + \beta_{12} ws + e$$

grand mean $\approx 1/2$ factor effect for w

$\beta_2 = 1/2$ factor effect for s

The 2^k factor settings, calculated factor effects and the grand mean of the data are below:

Factor	Settings
Water Depth (w)	200 ft (-)
	900 ft (+)
Sensor Modifications (s)	Mod I (-)
	Mod II (+)

Factor Effects:	
Grand Mean of Data	41.0
Water Depth (w):	3.8
Sensor Modification (s):	-5.2
Water/Sensor Interaction (ws)	-2.4

1. (3) Determine the coefficients for the reduced Regression Equation:

$$\beta_0 = 41 \quad \beta_1 = 1.9 \quad \beta_2 = -2.6 \quad \beta_{12} = -1.2$$

2. (5) Predict the result for Run (5) (200 ft and Mod II):

$$\hat{Y} = 41 + 1.9(-1) - 2.6 - 1.2(-1) = 41 - 1.9 - 2.6 + 1.2 = 37.7$$

3. (2) The result for Run (5) was 35.5, what was the residual for Run (5)?

$$35.5 - 37.7 = -2.2$$