

# Groups & Vector Spaces

## Mathematical Methods in the Physical Sciences

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# Introduction

# Definition

A group is a set of elements,  $G$ , together with a set operation,  $\cdot$ , that satisfies the following conditions.

## Group Conditions

Closure:  $\forall a, b \in G, a \cdot b \in G$

Association:  $\forall a, b, c \in G, (a \cdot b) \cdot c = a \cdot (b \cdot c)$

Identity:  $\exists$  exactly 1 element,  $i \in G \mid \forall a \in G, i \cdot a = a \cdot i = a$

Inversion:  $\forall a \in G \exists b \mid a \cdot b = b \cdot a = i$ , where  $i$  is the identity element.

# This is a test-a-roonie

Another test to see how Vim handles L<sup>A</sup>T<sub>E</sub>X.

## Block Test

$$\begin{aligned}x &= \sin(y) \\ &= -\cos(y)^2\end{aligned}$$

# Block Types

This is a Block

This is important information

This is an Alert block

This is an important alert

This is an Example block

This is an example