

Homework

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Midterm Project

Problem 1 (redux)

(a)

$$\begin{aligned}\lim_{s \rightarrow \infty} s \times \frac{1}{s} \times \frac{\frac{1}{s^2 + s + 2}}{1 + \frac{1}{s^2 + s + 2} \times \frac{1}{s + 1}} &= 0 \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^2} \times \frac{\frac{1}{s^2 + s + 2}}{1 + \frac{1}{s^2 + s + 2} \times \frac{1}{s + 1}} &= 1 \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^3} \times \frac{\frac{1}{s^2 + s + 2}}{1 + \frac{1}{s^2 + s + 2} \times \frac{1}{s + 1}} &= \infty\end{aligned}$$

(b)

$$\begin{aligned}\lim_{s \rightarrow \infty} s \times \frac{1}{s} \times \frac{\frac{1}{s(s+5)}}{1 + \frac{1}{s(s+5)} \times 5} &= 0.2 \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^2} \times \frac{\frac{1}{s(s+5)}}{1 + \frac{1}{s(s+5)} \times 5} &= \infty \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^3} \times \frac{\frac{1}{s(s+5)}}{1 + \frac{1}{s(s+5)} \times 5} &= \infty\end{aligned}$$

(c)

$$\begin{aligned}\lim_{s \rightarrow \infty} s \times \frac{1}{s} \times \frac{\frac{1}{s^2(s+10)}}{1 + \frac{1}{s^2(s+10)} \times \frac{s+1}{s+5}} &= 5 \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^2} \times \frac{\frac{1}{s^2(s+10)}}{1 + \frac{1}{s^2(s+10)} \times \frac{s+1}{s+5}} &= \infty \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^3} \times \frac{\frac{1}{s^2(s+10)}}{1 + \frac{1}{s^2(s+10)} \times \frac{s+1}{s+5}} &= \infty\end{aligned}$$

(d)

$$\begin{aligned}\lim_{s \rightarrow \infty} s \times \frac{1}{s} \times \frac{\frac{1}{s^2(s+12)}}{1 + \frac{1}{s^2(s+12)} \times 5(s+2)} &= 0.1 \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^2} \times \frac{\frac{1}{s^2(s+12)}}{1 + \frac{1}{s^2(s+12)} \times 5(s+2)} &= \infty \\ \lim_{s \rightarrow \infty} s \times \frac{1}{s^3} \times \frac{\frac{1}{s^2(s+12)}}{1 + \frac{1}{s^2(s+12)} \times 5(s+2)} &= \infty\end{aligned}$$