

# Adjustments Made Easy:

A Look at Clustering Time Series from the US Census Bureau Manufacturers' Shipments, Inventories, and Orders



## **Problem Statement**

- Taking data released from the Domestic Manufacturing Sector of the Economic Directorate
- Clustering data together based on certain correlations
- Use clusters to adjust data in a multivariate manner instead of univariately

Disclaimer: This report is released to inform interested parties of research and to encourage discussion. The views expressed on statistical issues are those of the authors and not those of the U.S. Census Bureau.

# Results 0.0e+00 5.0e+07 UDXTTI UMNMTI UMNMNO UMNMNO UDXDNO UDXDNO UDXDNO UDXDWS UMDMNO UMDMVS UMDMVS 2005 2010 2015 Dynamic Time Warping Matching **Euclidean Matching**

# **Approach**

- Gathered economic data
  - Converted the data into time series objects
- Clustered related data using Dynamic Time Warping
- Outputted data from DTW into a dendrogram
  - Showcase similarities between time series objects
- R programming language
- GitHub collaborative coding environment



# **Approach**

$$DTW(x, x') = \min_{\pi \in \mathcal{A}(x, x')} \sqrt{\sum_{(i,j) \in \pi} d(x_i, x'_j)^2}$$

where  $\mathcal{A}(x,x')$  is the set of all admissible paths ,i.e., the set of paths  $\pi$  such that:  $\pi = [\pi_0, \dots, \pi_K]$  is a path that satisfies the following properties:

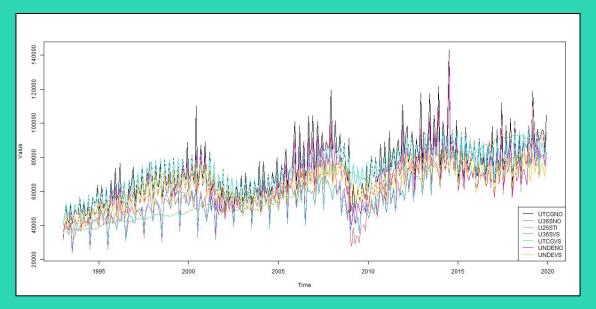
- $\pi$  is a sequence  $[\pi_0, \dots, \pi_{K-1}]$  of index pairs  $\pi_k = (i_k, j_k)$  with  $0 \le i_k < n$  and  $0 \le j_k < m$
- $\pi_0 = (0,0)$  and  $\pi_{K-1} = (n-1, m-1)$
- for all  $k > 0, \pi_k = (i_k, j_k)$  is related to  $\pi_{k-1} = (i_{k-1}, j_{k-1})$  as follows

$$i_{k-1} \le i_k \le i_{k-1} + 1$$

$$iotall j_{k-1} \le j_k \le j_{k-1} + 1$$

# Results

## **Unadjusted Domestic Manufacturing Sector Clusters from the US Census Bureau Economic Directorate**



Cluster 4



## **Review of Problem and Results**

#### Problem:

Clustering Economic
 Directorate data using a
 multivariate approach
 rather than univariate.

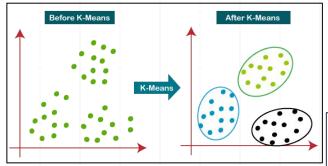


#### Results:

- Dynamic Time Warping methods clearly and effectively cluster time series in a multivariate manner
- Hierarchical clustering graphics show the relations between industries

## **Suggested Future Work**

## Clustering Using Other Methods



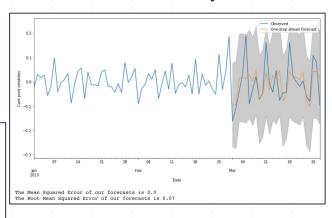
Compiling More Data from Different Directorates

#### **List of Business Surveys**

The U.S. Census Bureau conducts more than 100 surveys each year. These surveys include the business surveys listed below, and many more. To find more information on a specific survey you received please select it from the list of business surveys below.

- · Small Business Pulse Survey
- · Economic Census
- Annual Retail Trade Survey (ARTS)
- · Service Annual Survey (SAS)
- · Annual Wholesale Trade Survey (AWTS)
- Export Statistics
- Annual Survey of Entrepreneurs

## Creating Models for the Data for Analysts



## **Acknowledgements**

PIC Math is a program of the Mathematical Association of America (MAA) and the Society for Industrial and Applied Mathematics (SIAM). Support is provided by the National Science Foundation (NSF grant DMS-1722275).

Special thanks to our industrial liaison Dr. James Livsey and advisor Dr. Lan Cheng for their continued support with the project. Also, thank you to Dr. H. Joseph Straight for his mentorship.





