Tahmini Ders İçeriği
(Tentative Couse Schedule – Syllabus)

1. Hafta: Sayı sistemleri, onluk/ikilik taban sayı gösterimleri, mantıksal kapılar, computer system overview, başarım (performance)

2. Hafta: 2'lik tabanda işaretli sayılar, mikroişlemci tarihi, benchmarking, başarım,

3. Hafta: Başarım, Amdahl yasası, RISC-V development Environment, Verilog HDL ile Birleşik (Combinational) devreler

4. Hafta:, Verilog HDL ile sıralı (sequential) mantıksal devre ve sonlu durum makinası tasarımı, timing analysis

5. Hafta: Aritmetik devre tasarımları: Toplama, çıkarma, çarpma, bölme, trigonometri, square-root, hyperbolic, exponential, logarithm

6. Hafta: Fixed ve Floating-Point sayı gösterimleri

7. Hafta: RISC-V buyruk kümesi mimarisi (ISA) ve buyrukların tanıtımı

8. Hafta: RISC-V buyruk kümesi mimarisi (ISA) ve buyrukların tanıtımı

9. Hafta: Tek-çevrim işlemci tasarımı (single-cycle CPU)

10. Hafta: Çok-çevrim işlemci tasarımı (multi-cycle CPU)

11. Hafta: Boruhatlı işlemci tasarımı (pipelined CPU)

12. Hafta: Bellek sistemi ve hiyerarşisi

13. Hafta: İleri mimari konuları: Branch prediction, superscalar cpu, out-of-order execution, multi-core systems

14. Hafta: Gömülü sistemler, mikrodenetleyiciler, SoCs

Sabit Noktalı x Kayan Noktalı (Fixed-Point vs Floating Point)

Doğal sayılar: Unsigned Tam Sayılar: Signed (2's complement for negative numbers)

Reel (real) sayılar: ???

$3.14159265\ldots_{ten}$ (pi)

$2.71828\ldots_{ten}$ (e)

0.000000001_{ten} or $1.0_{ten} \times 10^{-9}$ (seconds in a nanosecond)

$3{,}155{,}760{,}000_{ten}$ or $3.15576_{ten} \times 10^{9}$ (seconds in a typical century)

Taban Dönüşümü (Ondalıklı Sayılar)

$$(11010.11)_2 = (?)_{10}$$

$$1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} = 26.75$$

$$(0.6875)_{10} = (?)_2$$

Sayı	Çarpım	Elde	Bit Değer	Bit Sıra
0.6875	0.375	1	1	-1
0.375	0.75	0	0	-2
0.75	0.5	1	1	-3
0.5	0	1	1	-4

Ondalıklı kısım için sürekli 2 ile çarp, elde değeri bit değerini ifade eder. Bit sırası -1,-2,… şeklindedir. Çarpım ‘0’ olana kadar devam et.

$$(0.6875)_{10} = (0.1011)_2$$

Taban Dönüşümü (Base Conversion)

$(0.6875)_{10} = (?)_2$

Sayı	Çarpım	Elde	Bit Değer	Bit Sıra
0.6875	0.375	1	1	-1
0.375	0.75	0	0	-2
0.75	0.5	1	1	-3
0.5	0	0	1	-4

Ondalıklı kısım için sürekli 2 ile çarp, elde değeri bit değerini ifade eder. Bit sırası -1,-2,… şeklindedir. Çarpım '0' olana kadar devam et.

$(0.6875)_{10} = (0.1011)_2$

0.1011 → 2 ile çarp: 1.011

1.011 → 2 ile çarp: 10.11

10.11 → 2 ile çarp: 101.1

101.1 → 2 ile çarp: 1011

İkilik tabanda

Sola kaydırma → 2 ile çarpma

Sağa kaydırma → 2'ye bölme

Onluk tabanda

Sola kaydırma → 10 ile çarpma

Sağa kaydırma → 10'a bölme

Taban Dönüşümü (Ondalıklı Sayılar)

$(0.513)_{10} = (?)_2$

Sayı	Çarpım	Elde	Bit Değer	Bit Sıra
0.513	0.026	1	1	-1
0.026	0.052	0	0	-2
0.052	0.104	0	0	-3
0.104	0.208	0	0	-4
0.208	0.416	0	0	-5
0.416	0.832	0	0	-6
0.832	0.664	1	1	-7
0.664	0.328	1	1	-8

Eğer ondalıklı kısım için 8-bit ayrıldıysa 8 kere iterasyon devam ettirilir.

$(0.513)_{10} = (0.10000011)_2$

$(0.10000011)_2 = (0.51171875)_{10}$

Bilgi kaybı yaşandı!

Eğer ondalıklı kısım için sadece 4-bit ayrılmış olsaydı 0.513 sayısı ancak 0.5 olarak ifade edilebilecekti!

Sabit Noktalı x Kayan Noktalı (Fixed-Point vs Floating Point)

$(326.513)_{10} = (?)_2$

Sabit-Noktalı Gösterim: Tamsayı ve ondalıklı sayılar için sabit uzunlukta yer (bit) ayrılmıştır. Sayının tamsayı ya da ondalıklı sayı kısmının büyüklüğü, bu sabit uzunluğu değiştirmez. Örnek olarak tamsayı 10, ondalıklı 8 bit olursa:

$(326.513)_{10} = (0101000110.10000011)_2$

Kayan-Noktalı Gösterim: Tamsayı ve ondalıklı sayılar için sabit uzunlukta yer (bit) ayrıl**ma**mıştır. Sayının tamsayı ve ondalıklı kısımlarına göre noktanın yeri değişir, kayar. Bilgisayarlarda ondalıklı sayıları ifade edebilmek için IEEE-754 Single Precision ve Double Precision standartları oluşturulmuştur.

Single Precision : 32-bit
Double Precision : 32-bit

IEEE-754 standard ve fixed-point hakkında detaylı bilgi ileriki haftalarda anlatılacak

Signed Fixed-Point

$(s\ i_2\ i_1\ i_0\ .f_1\ f_2\ f_3\ f_4)_2$ Q4.4 : 4 integer bits (sign included), 4 fraction bits

Sign Bit (İşaret Biti): if s = 0 positive, if s = 1 negative

$$i_2 * 2^2 + i_1 * 2^1 + i_0 * 2^0 + f_1 * 2^{-1} + f_2 * 2^{-2} + f_3 * 2^{-3} + f_4 * 2^{-4}$$

2's complement:

$$-s * 2^3 + i_2 * 2^2 + i_1 * 2^1 + i_0 * 2^0 + f_1 * 2^{-1} + f_2 * 2^{-2} + f_3 * 2^{-3} + f_4 * 2^{-4}$$

Ex: -2.375

Sign Bit:

Önce 2.375 hesapla → 0010.0110

Sonra işaret bitini 1 yap → 1010.0110

Ex: -2.375

2's complement:

Önce 2.375 hesapla → 0010.0110

Sonra 1'e tümleyen al (tersle) → 1101.1001

1 ekle (en sağa) → 1101.1010

1101 = -8+4+1 = -3 .1010 = +0.5 + 0.125 = 0.625

-3+0.625 = -2.375

Signed Fixed-Point

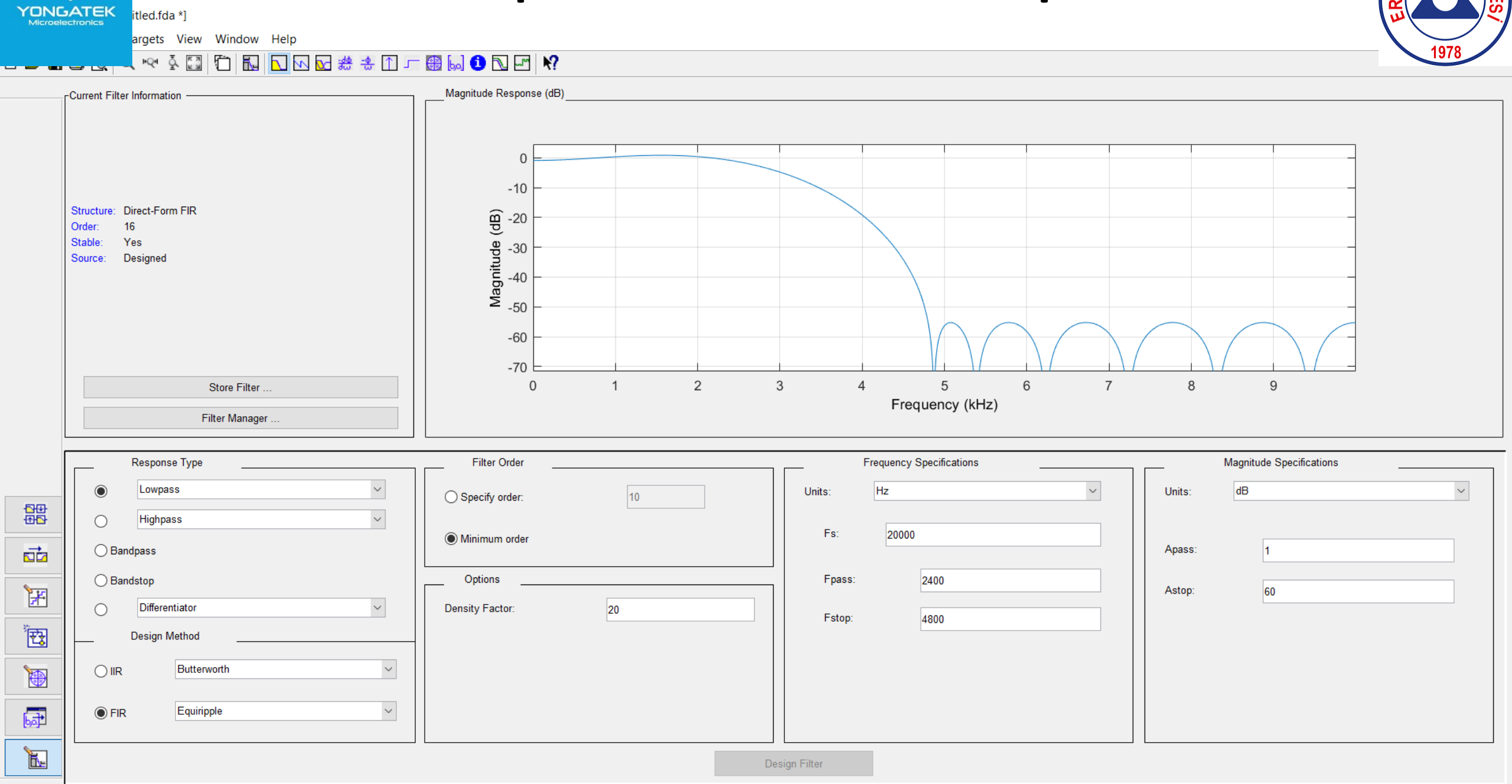
Ex: 0.75 + (-0.625) in Q4.4 form

0.750 → 0000.1100
-0.625 → 0.625 = 0000.1010 → 1's complement = 1111.0101 → +1 rightmost = 1111.0110

$$\begin{array}{r} 0000.1100 \\ +\ 1111.0110 \\ \hline 0000.0010 \end{array}$$

Fixed-point number systems are commonly used in digital signal processing (DSP), graphics, and machine learning applications because the computations are faster and consume less power than they would in floating-point systems. Q1.15 (also known as Q15) is the most common format, storing signed numbers in the range (−1, 1) with 15 bits of precision. Q1.31 (also called just Q31) is sometimes used for higher precision intermediate results, such as in a Fast Fourier Transform. U8.8 is sometimes used for sensor readings sampled by analog/digital converters (ADCs). Note that all of these formats pack into 16- or 32-bit words for efficient storage in computer memories, which are typically a power of 2 in width. (Harris & Harris)

DSP | Low-Pass Filter Example



DSP | Low-Pass Filter | Fixed-Point

Current Filter Information

Structure: Direct-Form FIR
Order: 16
Stable: Yes
Source: Designed (quantized)

Store Filter ...

Filter Manager ...

Filter Coefficients

```
Quantized Numerator:
 0.002197265625
-0.002471923828125
-0.0216064453125
-0.048553466796875
-0.050537109375
 0.0103759765625
 0.134796142578125
 0.265380859375
 0.321563720703125
 0.265380859375
 0.134796142578125
 0.0103759765625
-0.050537109375
-0.048553466796875
-0.0216064453125
-0.002471923828125
 0.002197265625

Reference Numerator:
```

Filter arithmetic: Fixed-point

Filter precision: Full

Coefficients | Input/Output | Filter Internals

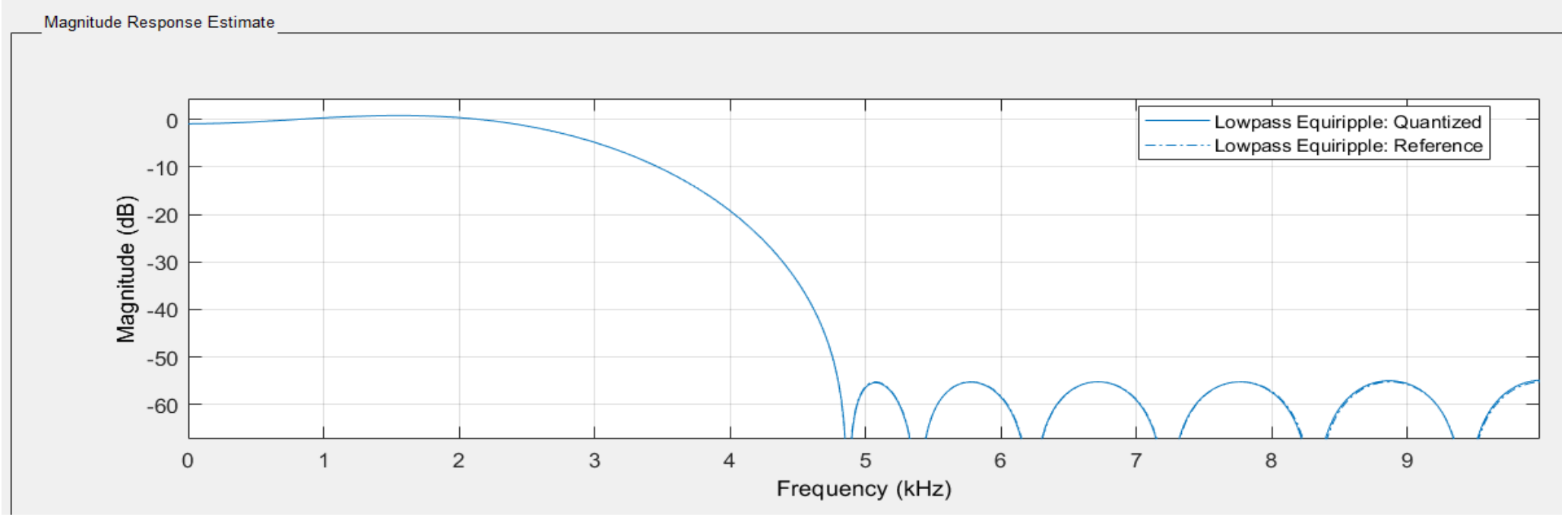
Numerator word length: 16 ☐ Best-precision fraction lengths

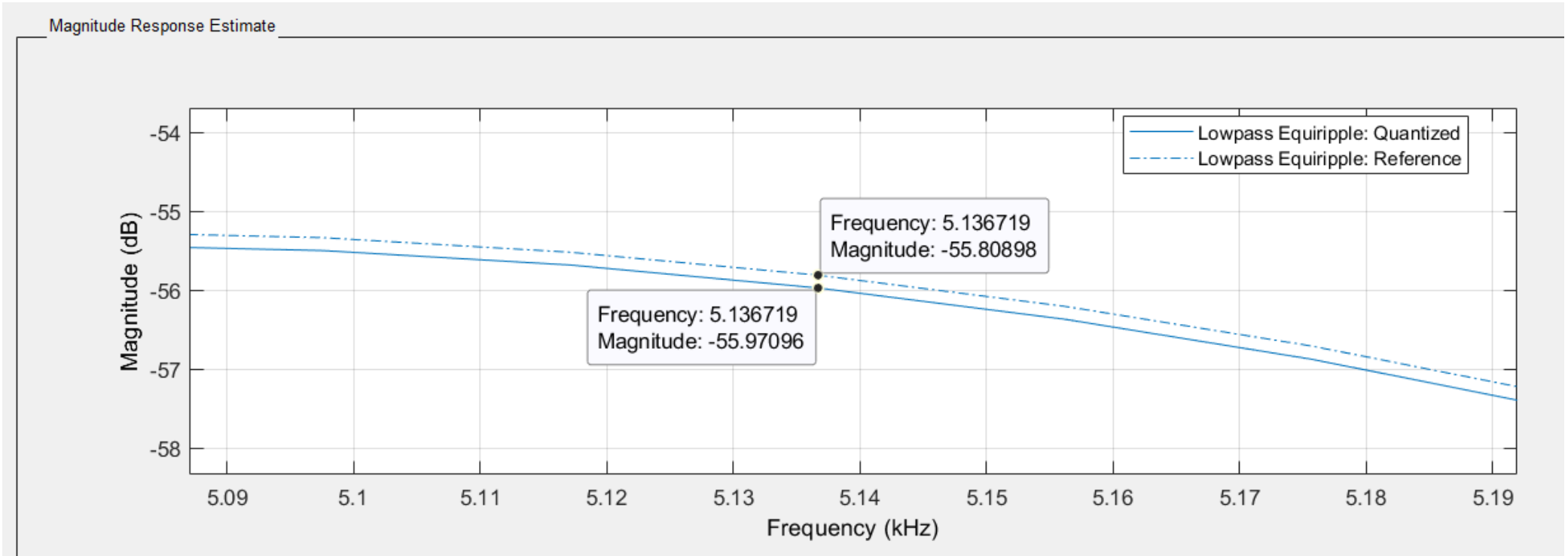
◉ Numerator frac. length: 15

○ Numerator range (+/-): 1

☐ Use unsigned representation

☐ Scale the numerator coefficients to fully utilize the entire dynamic range


Magnitude Response Estimate
Lowpass Equiripple: Quantized
Lowpass Equiripple: Reference
Magnitude (dB)
Frequency (kHz)
0
-10
-20
-30
-40
-50
-60
0
1
2
3
4
5
6
7
8
9


Magnitude Response Estimate
Lowpass Equiripple: Quantized
Lowpass Equiripple: Reference
Frequency: 5.136719
Magnitude: -55.80898
Frequency: 5.136719
Magnitude: -55.97096
Magnitude (dB)
Frequency (kHz)
-54
-55
-56
-57
-58
5.09
5.1
5.11
5.12
5.13
5.14
5.15
5.16
5.17
5.18
5.19

Generate HDL (Direct-Form FIR, order = 16)

Set Basic Options

Language: Verilog

Name: filter_fixed

Folder: hdlsrc Browse... Generate MATLAB code

Filter Architecture | Global Settings | Test Bench | EDA Tool Scripts

Architecture: Fully parallel

Folding factor: 1
Multiplier: 17

Coefficient source: Internal

Coefficient multipliers: Multiplier

Multiplier input pipeline: 0

Multiplier output pipeline: 0

Add pipeline registers

FIR adder style: Linear

Optimize for HDL

Resource	Estimation	Available	Utilization...
LUT	16	63400	0.03
FF	273	126800	0.22
DSP	19	240	7.92
IO	51	210	24.29
BUFG	1	32	3.13

Generate Close Help

Generate HDL (Direct-Form FIR, order = 16)

Set Basic Options

Language: Verilog

Name: filter_da

Folder: hdlsrc_da Browse... Generate MATLAB code

Filter Architecture | Global Settings | Test Bench | EDA Tool Scripts

Architecture: Distributed arithmetic (DA)

Specify folding: Folding factor 16

Specify LUT: Address width 6

Folding factor: 16
Address width: 6
Total LUT size(bits): 2336

View details

Coefficient multipliers: Multiplier

Multiplier input pipeline: 0

Multiplier output pipeline: 0

Resource	Estimation	Available	Utilization...
LUT	166	63400	0.26
LUTRAM	16	19000	0.08
FF	164	126800	0.13
IO	51	210	24.29
BUFG	1	32	3.13

Add pipeline registers

FIR adder style: Tree

Optimize for HDL

Generate Close Help

Verilog Fixed-Point

Özel bir şey yapmaya gerek yok

Addition: +

Subtraction: -

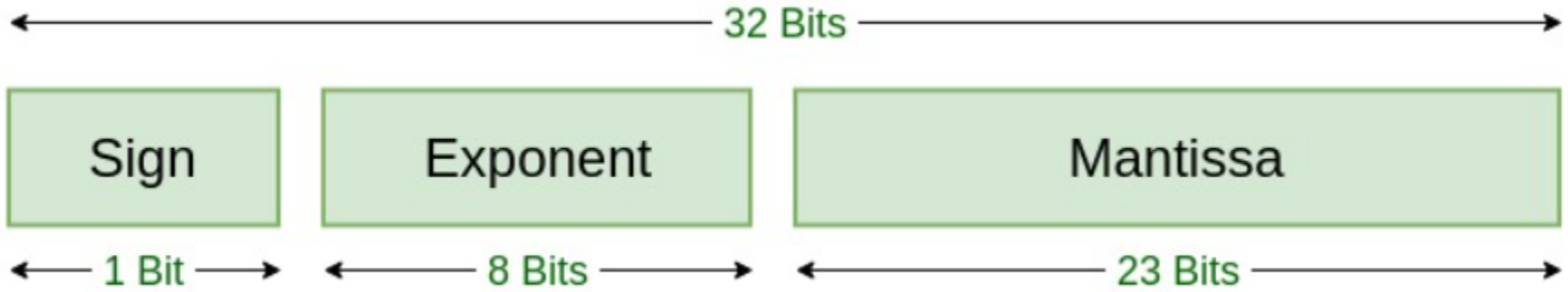
Multiplication: *

Çarpma yaparken input ve output'u "signed" olarak tanımlamayı unutmamak lazım

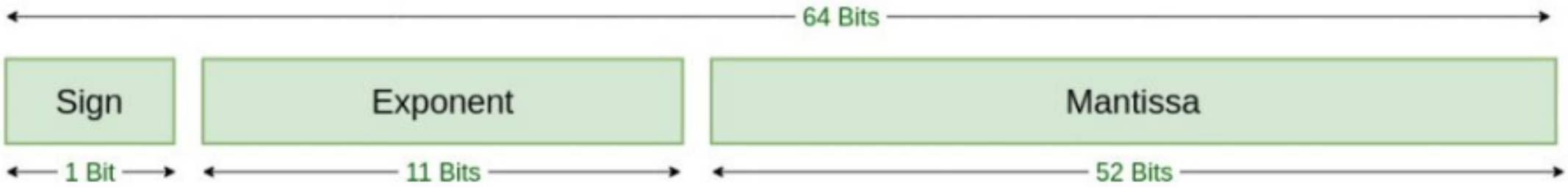
Floating-Point | IEEE-754

IEEE-754 floating-point standard (first in 1985, current version 2019)

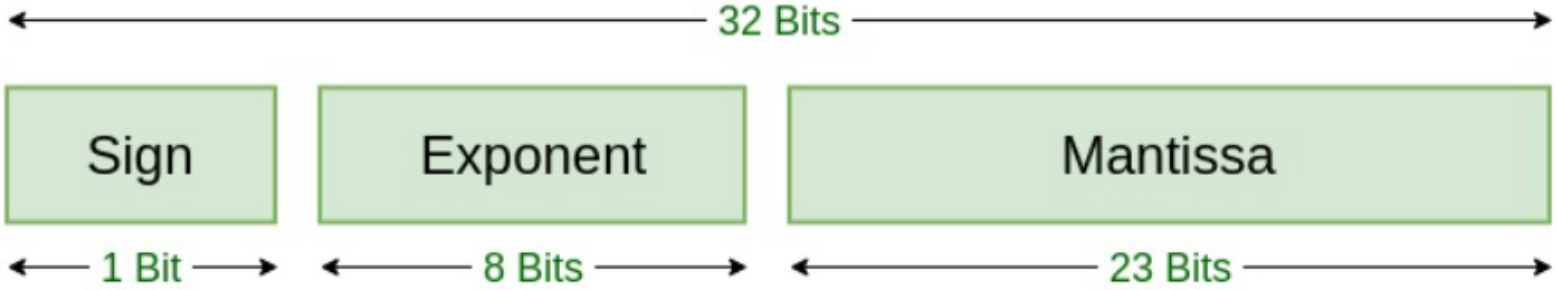
Single precision (32-bit)



Double precision (64-bit)



Floating-Point | IEEE-754



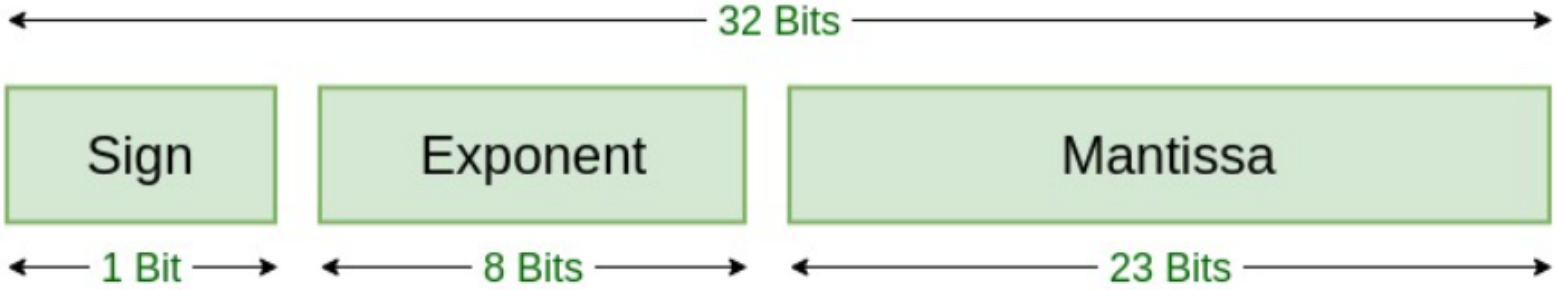
Sign : İşaret biti, ‘0’ pozitif, ‘1’ negatif
Exponent (Üs) : Biased (127) exponent.
Mantissa : Ondalıklı kısım

Ex: 85.125

85 = 1010101 0.125 = 001 85.125 = 1010101.001
Scientific Notation → 1.010101001 x 2^6

Sign : 0
Biased Exponent : 127+6 (2^6’nın altısı) = 133 = 10000101
Mantissa : 010101001 (23 bite tamamlarsak) = 01010100100000000000
: [0][10000101][01010100100000000000] → 0x42AA4000

Floating-Point | IEEE-754



Sign : İşaret biti, ‘0’ pozitif, ‘1’ negatif
Exponent (Üs) : Biased (127) exponent.
Mantissa : Ondalıklı kısım

Ex: - 0.75

0 = 0 0.75 = 110 0.75 = 0.110
Scientific Notation → 1.10 x 2^-1

Sign : 1
Biased Exponent : 127-1 (2^-1’in -1) = 126 = 01111110
Mantissa : 100000000 (23 bite tamamlarsak) = 10000000000000000000000
: [1][01111110][10000000000000000000000] → 0xBF400000

Floating-Point | IEEE-754

Number	Sign	Exponent	Fraction
0	X	00000000	00000000000000000000000
∞	0	11111111	00000000000000000000000
−∞	1	11111111	00000000000000000000000
NaN	X	11111111	Non-zero

Format	Total Bits	Sign Bits	Exponent Bits	Fraction Bits	Bias
Single	32	1	8	23	127
Double	64	1	11	52	1023
Quad	128	1	15	112	16363

IEEE 754 Converter (JavaScript), V0.22

	Sign	Exponent	Mantissa
Value:	+1	2^{127}	1.9999998807907104
Encoded as:	0	254	8388607
Binary:	☐	☑☑☑☑☑☑☑☐	☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑☑

Decimal representation: 3.40282346639e+38

Value actually stored in float: 340282346638528859811704183484516925440

Error due to conversion:

Binary Representation: 01111111011111111111111111111111

Hexadecimal Representation: 0x7f7fffff

+1

-1

Floating-Point | IEEE-754 | Rounding

IEEE 754 Converter (JavaScript), V0.22

	Sign	Exponent	Mantissa
Value:	+1	2^{0}	1.434213399887085
Encoded as:	0	127	3642446
Binary:	☐	☐ ☑ ☑ ☑ ☑ ☑ ☑ ☑	☐ ☑ ☑ ☐ ☑ ☑ ☑ ☑ ☐ ☐ ☑ ☐ ☑ ☐ ☐ ☐ ☑ ☐ ☐ ☑ ☑ ☑ ☐

You entered	1.434213423
Value actually stored in float:	1.434213399887085 09375
Error due to conversion:	-2.31129150390625E-8
Binary Representation	00111111101101111001010001001110
Hexadecimal Representation	0x3fb7944e

+1 -1

IEEE 754 Converter (JavaScript), V0.22

	Sign	Exponent	Mantissa
Value:	+1	2^{51}	1.38720703125
Encoded as:	0	178	3248128
Binary:	☐	☑ ☐ ☑ ☑ ☐ ☐ ☑ ☐	☐ ☑ ☑ ☐ ☐ ☐ ☑ ☑ ☐ ☐ ☑ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐

You entered	3123712467129421.123412412412
Value actually stored in float:	3123712534511616
Error due to conversion:	67382194.876587587588
Binary Representation	01011001001100011001000000000000
Hexadecimal Representation	0x59319000

+1 -1

Floating-Point | IEEE-754 | Addition

	Sign	Exponent	Mantissa
Value:	+1	2^{2}	1.96875
Encoded as:	0	129	8126464
Binary:	☐	☑ ☐ ☐ ☐ ☐ ☐ ☐ ☑	☑ ☑ ☑ ☑ ☑ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐

Decimal representation	7.875
Value actually stored in float:	7.875
Error due to conversion:	
Binary Representation	01000000111111000000000000000000
Hexadecimal Representation	0x40fc0000

+1

-1

	Sign	Exponent	Mantissa
Value:	+1	2^{-3}	1.5
Encoded as:	0	124	4194304
Binary:	☐	☐ ☑ ☑ ☑ ☑ ☑ ☐ ☐	☑ ☐

Decimal representation	0.1875
Value actually stored in float:	0.1875
Error due to conversion:	
Binary Representation	00111110010000000000000000000000
Hexadecimal Representation	0x3e400000

+1

-1

Floating-Point | IEEE-754 | Addition

7.875 + 0.1875 = ???

7.875 : 7 = 111, 0.875 = 0.111 → 111.111 = 1.11111 x 2^2

0.1875 : 0 = 0, 0.1875 = 0.0011 → 0.0011 = 1.1 x 2^-3

Floating-point numbers

0	10000001	111 1100 0000 0000 0000 0000
0	01111100	100 0000 0000 0000 0000 0000

	Exponent	Fraction
Step 1	10000001	111 1100 0000 0000 0000 0000
	01111100	100 0000 0000 0000 0000 0000
Step 2	10000001	1.111 1100 0000 0000 0000 0000
	01111100	1.100 0000 0000 0000 0000 0000
Step 3	10000001	1.111 1100 0000 0000 0000 0000
	− 01111100	1.100 0000 0000 0000 0000 0000
	101 (shift amount)	
Step 4	10000001	1.111 1100 0000 0000 0000 0000
	10000001	0.000 0110 0000 0000 0000 0000 00000

Step 5

10000001		1.111 1100 0000 0000 0000 0000
10000001	+	0.000 0110 0000 0000 0000 0000
		10.000 0010 0000 0000 0000 0000

Step 6

10000001		10.000 0010 0000 0000 0000 0000 >> 1
	+ 1	
10000010		1.000 0001 0000 0000 0000 0000

Step 7 (No rounding necessary)

Step 8

0	10000010	000 0001 0000 0000 0000 0000

Floating-Point | IEEE-754 | Multiplication

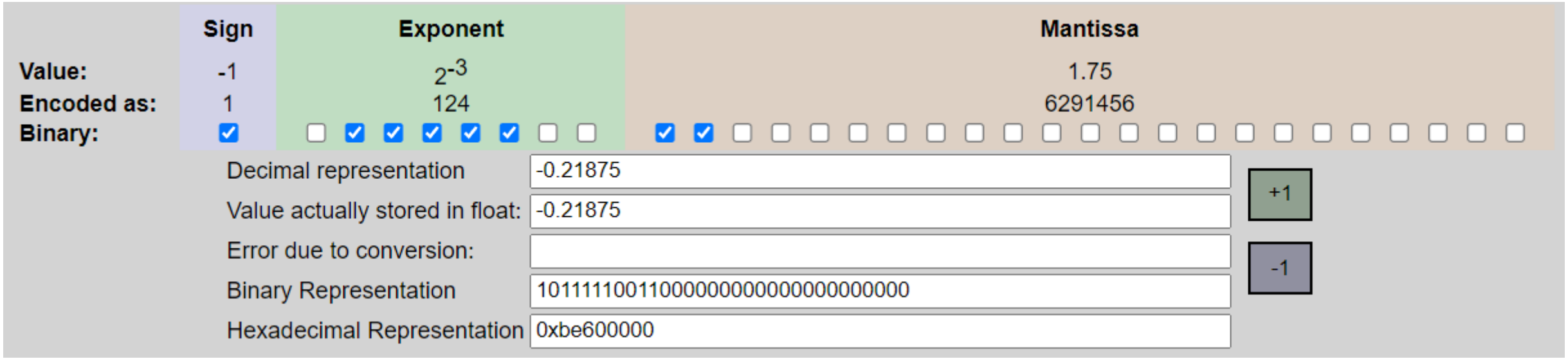
0.5 * (-0.4375) = ???

0.5	: 0 = 0, 0.5 = 0.1	→ 0.1	= 1.0 x 2^-1
0.4375	: 0 = 0, 0.4375 = 0.0111	→ 0.0111	= -1.11 x 2^-2

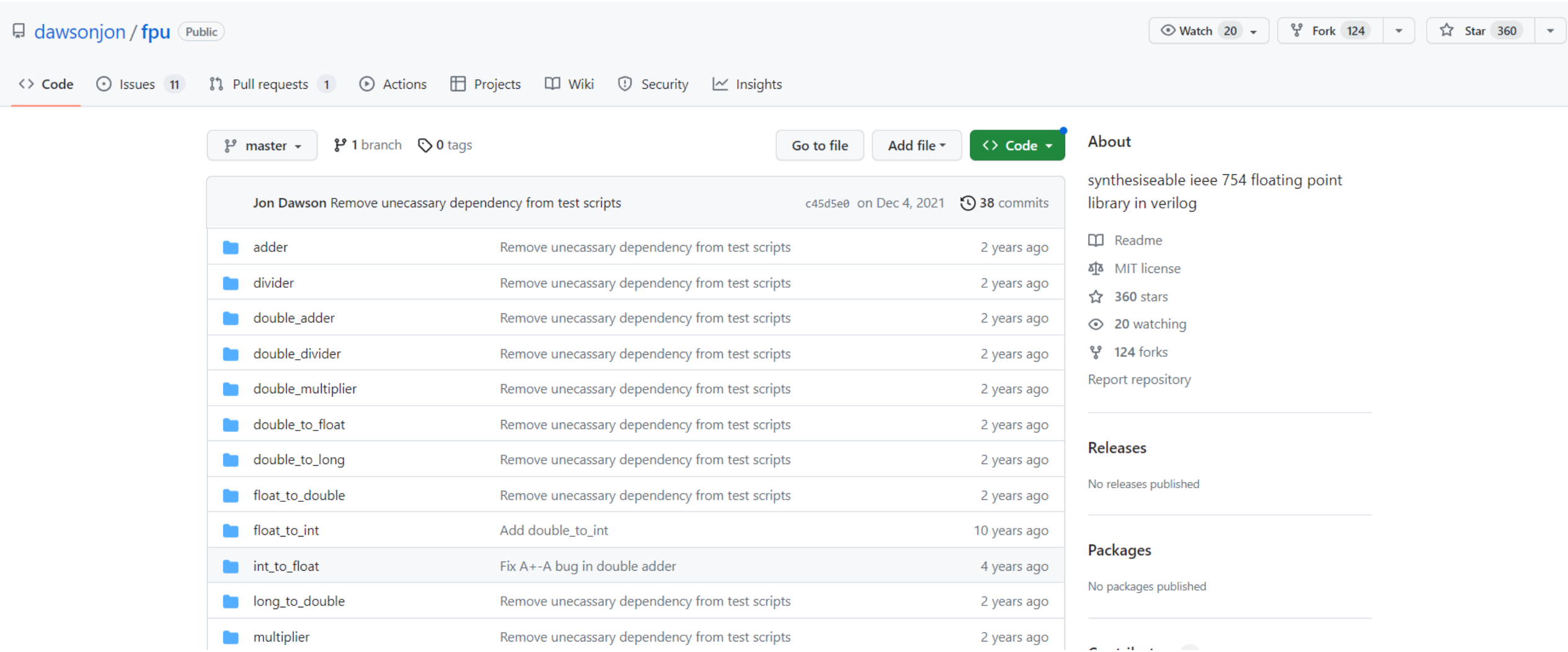
Add exponents: -1-2 = -3
Multiply fractions: 1.0 * 1.11 = 1.11

→ -1.11 * 2^-3 = -0.21875

[1][01111100][11000000000000000000000] → 0xBE600000



Floating-Point Arithmetic IP Cores



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master | 1 branch | 0 tags | Go to file | Add file | Code

Jon Dawson Remove unecassary dependency from test scripts c45d5e0 on Dec 4, 2021 38 commits

adder	Remove unecassary dependency from test scripts	2 years ago
divider	Remove unecassary dependency from test scripts	2 years ago
double_adder	Remove unecassary dependency from test scripts	2 years ago
double_divider	Remove unecassary dependency from test scripts	2 years ago
double_multiplier	Remove unecassary dependency from test scripts	2 years ago
double_to_float	Remove unecassary dependency from test scripts	2 years ago
double_to_long	Remove unecassary dependency from test scripts	2 years ago
float_to_double	Remove unecassary dependency from test scripts	2 years ago
float_to_int	Add double_to_int	10 years ago
int_to_float	Fix A+-A bug in double adder	4 years ago
long_to_double	Remove unecassary dependency from test scripts	2 years ago
multiplier	Remove unecassary dependency from test scripts	2 years ago

About

synthesiseable ieee 754 floating point library in verilog

Readme

MIT license

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20 watching

124 forks

Report repository

Releases

No releases published

Packages

No packages published

https://github.com/dawsonjon/fpu

Floating-Point Arithmetic IP Cores

Floating Point Unit

Overview | News | Downloads | Bugtracker

Details

Name: fpu
Created: Sep 25, 2001
Updated: Dec 16, 2018
SVN Updated: Mar 10, 2009
SVN: Browse
Latest version: download (might take a bit to start...)
Statistics: View
Bugs: 2 reported / 0 solved

★ Star | 15 you like it: star it!

Other project properties

Category:Coprocessor
Language:Verilog
Development status:Stable
Additional info:
WishBone compliant: No
WishBone version: n/a
License:

Project maintainers

- Usselmann, Rudolf

https://opencores.org/projects/fpu

Floating-Point Arithmetic IP Cores

Summary | IP Catalog

Cores | Interfaces

Search: flo (2 matches)

Name	AXI4	Status
Vivado Repository		
Math Functions		
Floating Point		
Floating-point	AXI4-Stream	Production

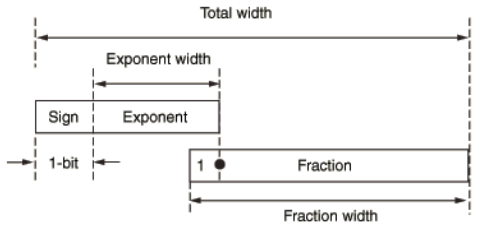
Component Name: floating_point_0

Operation Selection | Precision of Inputs | Optimizations | Interface Options

A Precision Type

Please select floating-point precision

Half | Single | Double | Custom



Exponent Width: 8 [0 - 64]

Fraction Width: 24 [0 - 64]

Total Width : 32

Component Name: floating_point_0

Operation Selection | Precision of Inputs | Optimizations | Interface Options

Please select from the following functions:

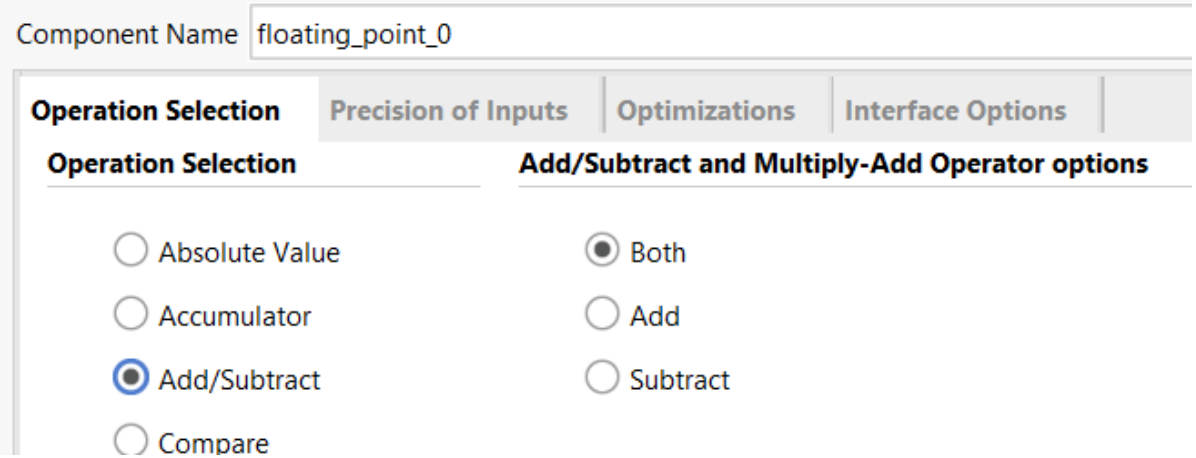
Operation Selection

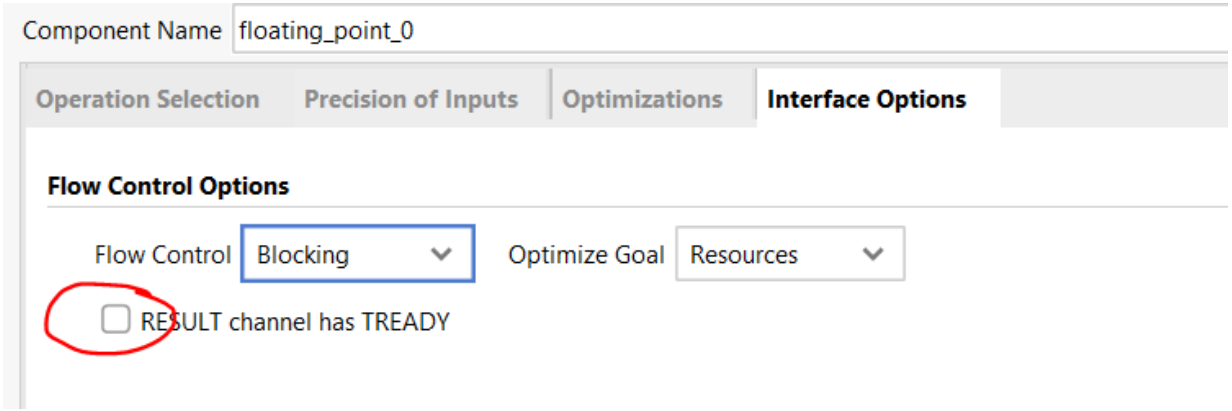
- Absolute Value
- Accumulator
- Add/Subtract
- Compare
- Divide
- Exponential
- Fixed-to-float
- Float-to-fixed
- Float-to-float
- Fused Multiply-Add
- Logarithm
- Multiply
- Reciprocal
- Reciprocal Square Root
- Square-root

Add/Subtract and Multiply-Add Operator options

- Both
- Add
- Subtract

Floating-Point Arithmetic IP Cores





FP Operation		s_axis_operation_tdata(5:0)
Add		000000
Subtract		000001
Compare (Programmable)	Unordered(1)	000100
	Less Than	001100
	Equal	010100
	Less Than or Equal	011100
	Greater Than	100100
	Not Equal	101100
	Greater Than or Equal	110100

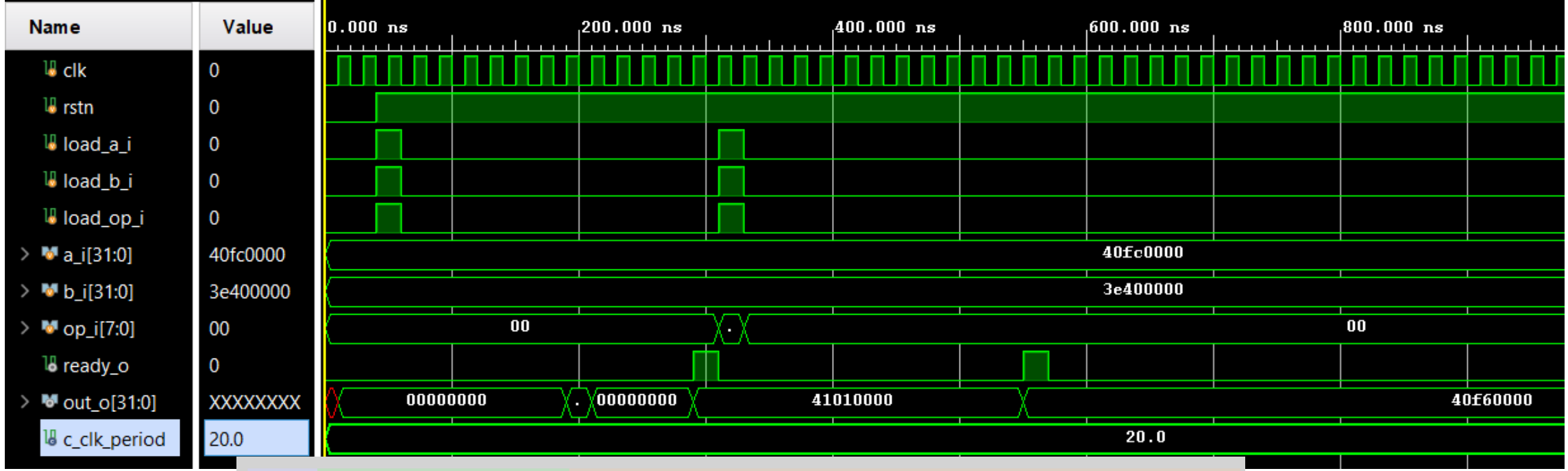
Floating-Point Arithmetic IP Cores

```
module fpu
(
input clk,
input rstn,
input load_a_i,
input load_b_i,
input load_op_i,
input [31:0] a_i,
input [31:0] b_i,
input [7:0] op_i,
output ready_o,
output [31:0] out_o
);

reg [31:0] a;
reg [31:0] b;
reg [7:0] op;
reg a_valid;
reg b_valid;
reg op_valid;
```

```
fp_addsub fp_addsub_i
(
.aclk                       (clk),
.s_axis_a_tvalid            (a_valid),
.s_axis_a_tready            (),
.s_axis_a_tdata             (a),
.s_axis_b_tvalid            (b_valid),
.s_axis_b_tready            (),
.s_axis_b_tdata             (b),
.s_axis_operation_tvalid    (op_valid),
.s_axis_operation_tready    (),
.s_axis_operation_tdata     (op),
.m_axis_result_tvalid       (ready_o),
.m_axis_result_tdata        (out_o)
);
```

Resource	Estimation	Available	Utilization...
LUT	204	63400	0.32
LUTRAM	13	19000	0.07
FF	455	126800	0.36
DSP	2	240	0.83
IO	103	210	49.05
BUFG	1	32	3.13

```
always @(posedge clk) begin
    if (!rstn) begin
        a           <= 0;
        b           <= 0;
        op          <= 0;
        a_valid     <= 0;
        b_valid     <= 0;
        op_valid    <= 0;
    end
    else begin
        a_valid     <= 0;
        b_valid     <= 0;
        op_valid    <= 0;
        if (load_a_i) begin
            a           <= a_i;
            a_valid     <= 1;
        end
        if (load_b_i) begin
            b           <= b_i;
            b_valid     <= 1;
        end
        if (load_op_i) begin
            op          <= op_i;
            op_valid    <= 1;
        end
    end
end

endmodule
```



Sign	Exponent	Mantissa
+1	2^3	1.0078125
0	130	65536

Decimal representation: 8.0625
Value actually stored in float: 8.0625
Error due to conversion:
Binary Representation: 01000001000000010000000000000000
Hexadecimal Representation: 0x41010000

+1 -1

Sign	Exponent	Mantissa
+1	2^2	1.921875
0	129	7733248

Decimal representation: 7.6875
Value actually stored in float: 7.6875
Error due to conversion:
Binary Representation: 01000000111101100000000000000000
Hexadecimal Representation: 0x40f60000

+1 -1

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