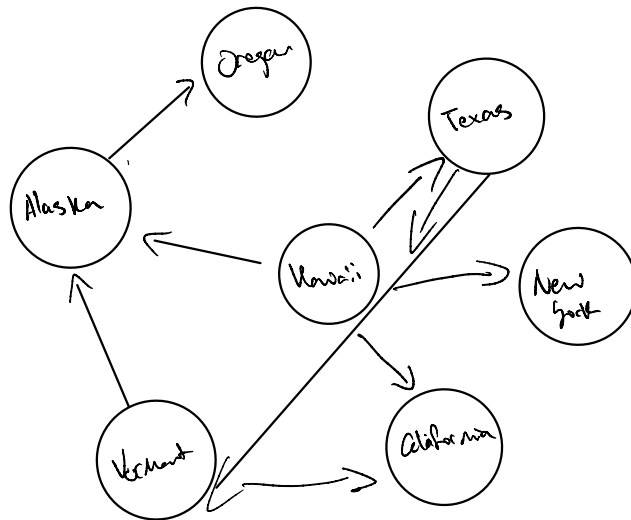


$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$

$E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

1. Draw the StateGraph



1. Describe the graph pictured above, using the formal graph notation.

$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$

$E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

2. a. Is there a path from Oregon to any other state in the graph?

No

b. Is there a path from Hawaii to every other state in the graph?

Yes

c. From which state(s) in the graph is there a path to Hawaii?

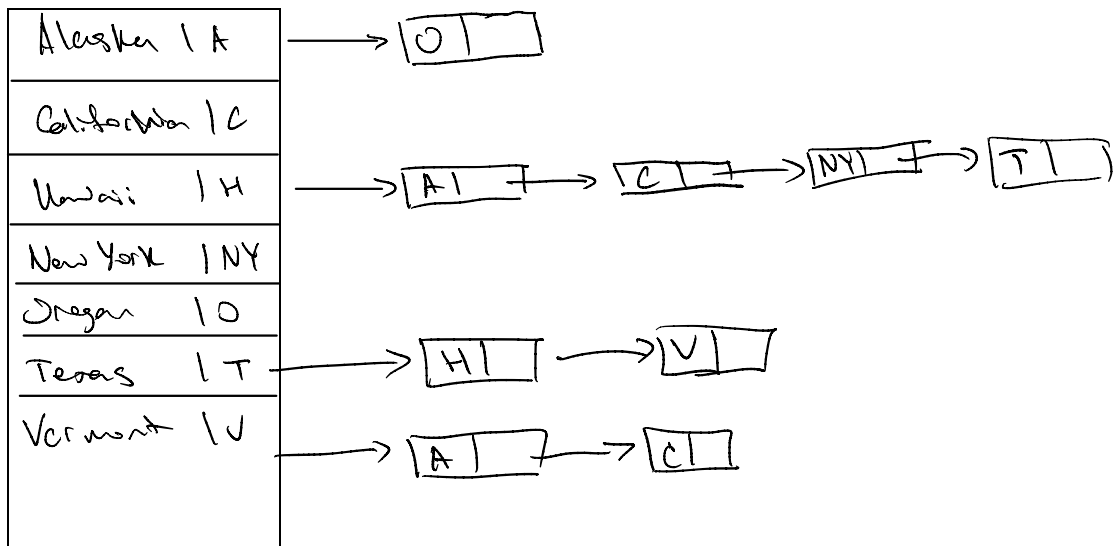
Texas

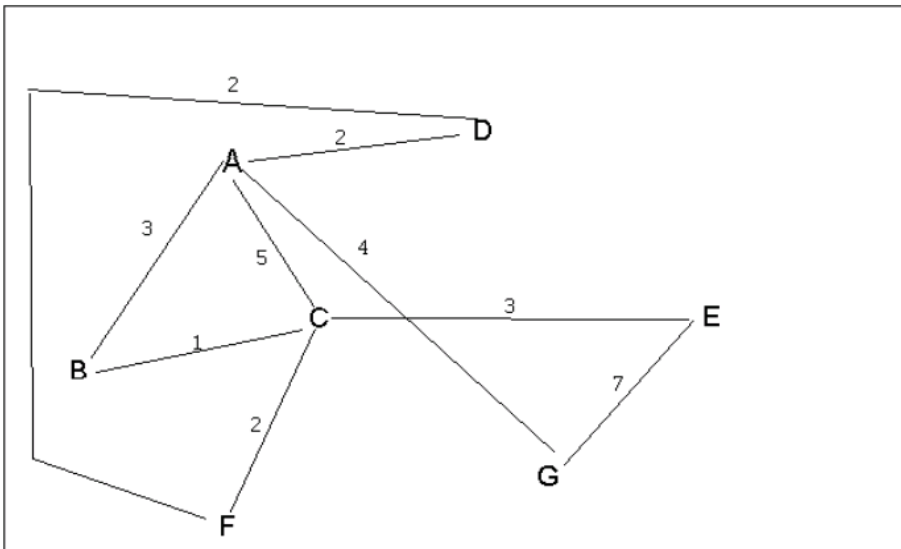
3. a. Show the adjacency matrix that would describe the edges in the graph.
Store the vertices in alphabetical order

States									
Alaska	0								
California	1								
Hawaii	2								
New York	3								
Oregon	4								
Texas	5								
Vermont	6								

	0	1	2	3	4	5	6
0	0	0	0	0	1	0	0
1	0	0	0	0	0	0	0
2	1	1	0	1	0	1	0
3	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0
5	0	0	1	0	0	0	1
6	1	1	0	0	0	0	0

3. b. Show the adjacency lists
that would describe the edges in the graph



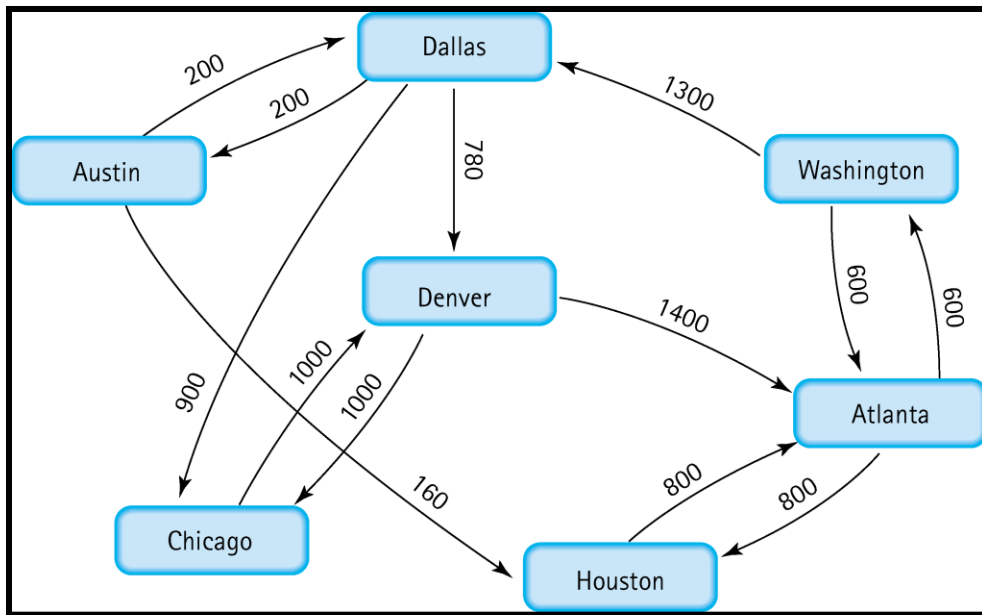


4 a. Which of the following lists the graph nodes in depth first order beginning with E?

- A) E, G, F, C, D, B, A
- B) G, A, E, C, B, F, D
- ☒ C) E, G, A, D, F, C, B
- D) E, C, F, B, A, D, G

4 b. Which of the following lists the graph nodes in breadth first order beginning at F?

- ☒ A) F, C, D, A, B, E, G
- B) F, D, C, A, B, C, G
- C) F, C, D, B, G, A, E
- D) a, b, and c are all breadth first traversals



5. Find the shortest distance from Atlanta to every other city

Washington → 600

Houston → 800

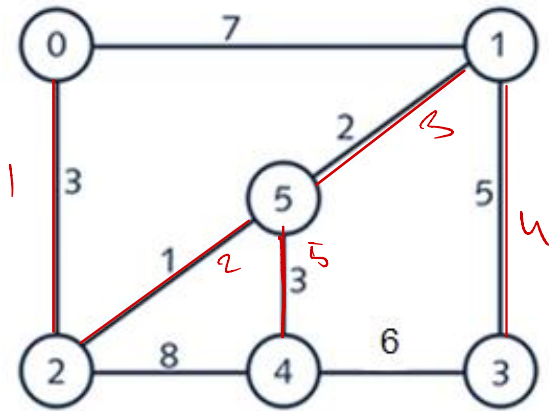
Dallas → 1900

Austin → 2100

Denver → 2680

Chicago → 2800

6. Find the minimal spanning tree using Prim's algorithm. Use 0 as the source vertex . Show the steps.



$$V(T) = \{0\}$$

compare 3, 7

$$1. V(T) = \{0, 2\}$$

compare 1, 6

$$2. V(T) = \{0, 2, 5\}$$

compare 2, 3

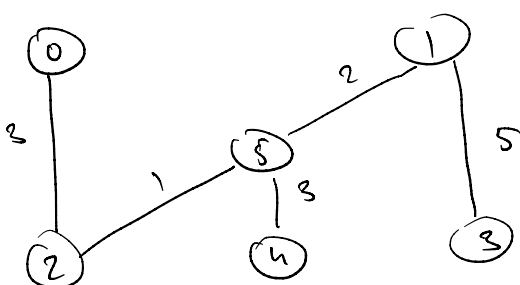
$$3. V(T) = \{0, 2, 5, 1\}$$

compare 3, 6

$$4. V(T) = \{0, 2, 5, 1, 3\}$$

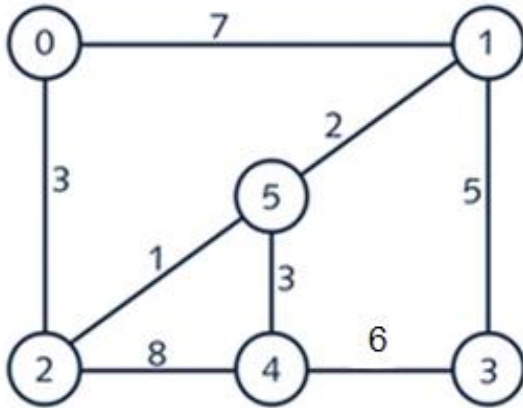
compare 6, 3

$$5. V(T) = \{0, 2, 5, 1, 3, 4\}$$



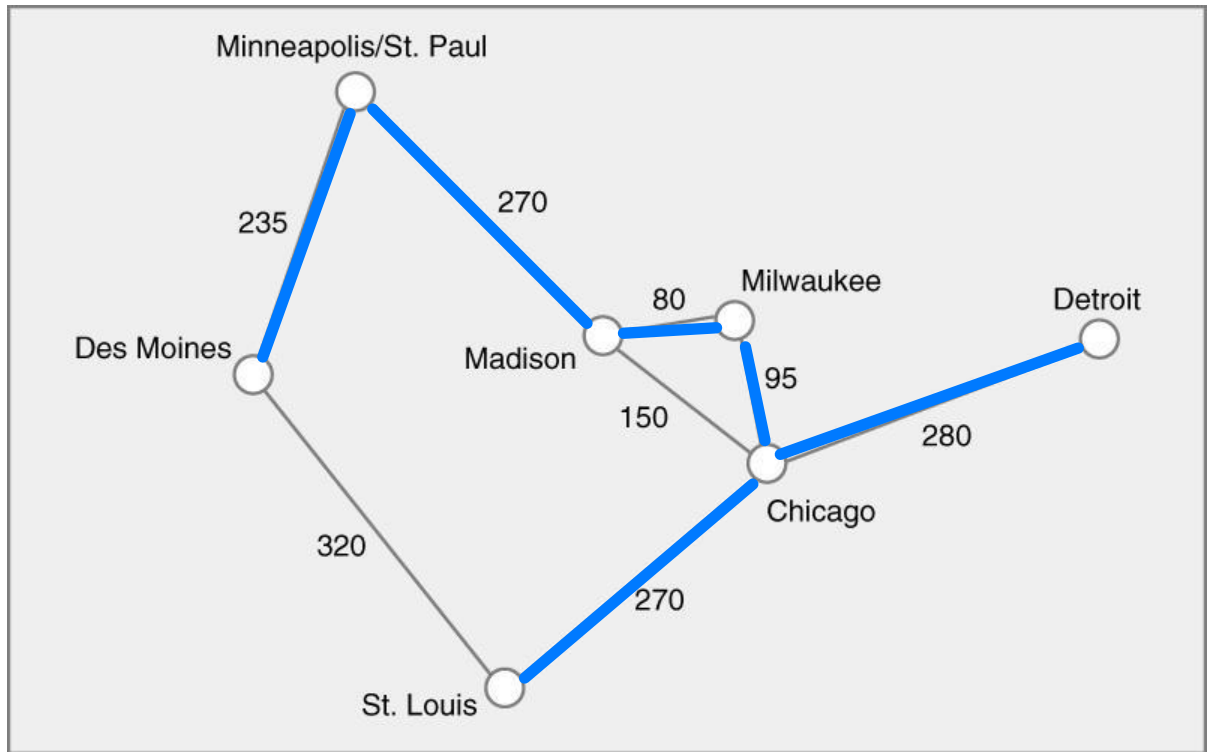
MST

7. Find the minimal spanning tree using Kruskal's algorithm. Show the weights in order and the steps.

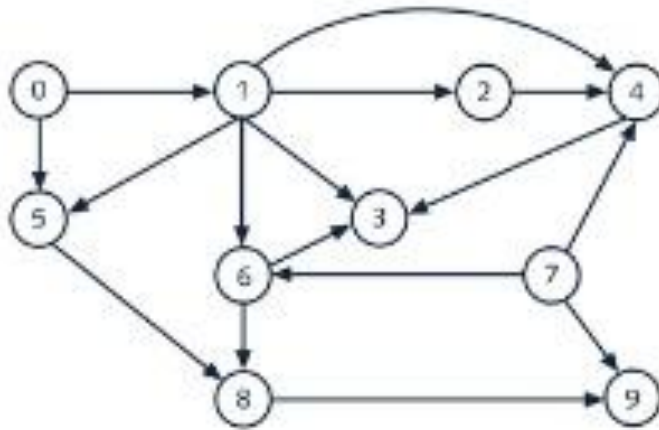


1. $2 \rightarrow 5$ (1) ✓
2. $1 \rightarrow 5$ (2) ✓
3. $0 \rightarrow 2$ (3) ✓
4. $4 \rightarrow 5$ (3) ✓
5. $1 \rightarrow 3$ (5) ✓
6. $3 \rightarrow 4$ (6) ✗
7. $0 \rightarrow 1$ (7) ✗
8. $2 \rightarrow 4$ (8) ✗

8. Find the minimal spanning tree using the algorithm you prefer. Use Minneapolis/St. Paul as the source vertex



9. List the nodes of the graph in a breadth first topological ordering. Show the steps using arrays predCount, topologicalOrder and a queue



0 1 2 3 4 5 6 7 8 9

pred count

0 0 0 0 0 0 0 0 0 0

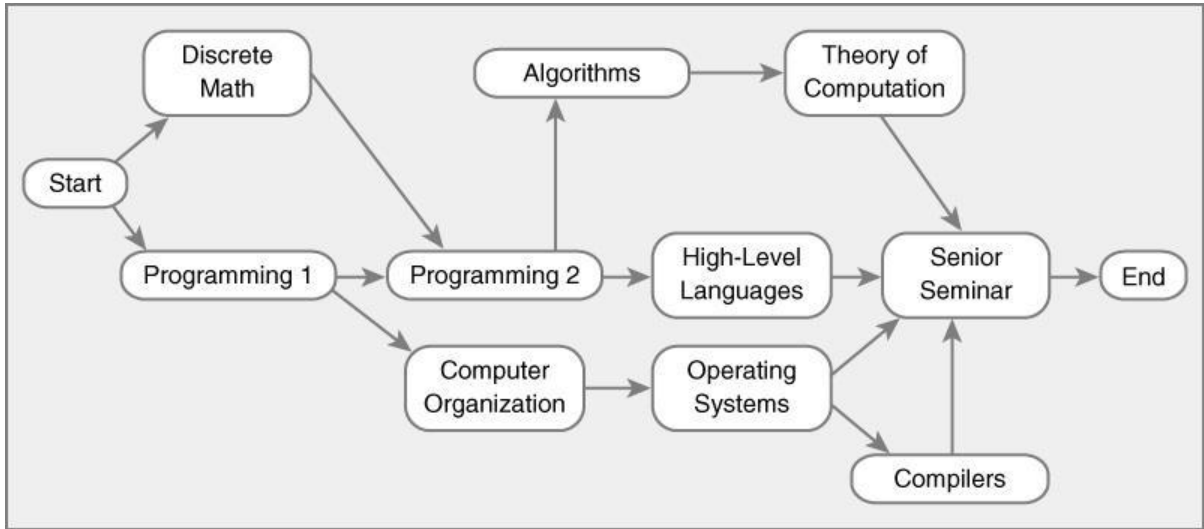
topological order

0 7 1 2 5 6 4 8 3 9

queue

0 7 1 2 5 6 4 8 3 9

10. List the nodes of the graph in a breadth first topological ordering.



Start → Discrete Math → Programming 1 → Programming 2 → Computer
→ Algorithms → High-level language → Operating Systems → Theory of Computation →
→ Compilers → Senior Seminar → End.