

3.) Given a 2-class classification problem:

Assume  
 $\log = \ln$

$= -\infty$ , so  
assume just  
a bit  
bigger  
0

$\hat{p}_{m1}$	Gini Index = $G_m = \sum_{k=1}^K \hat{p}_{mk}(1-\hat{p}_{mk})$	Classification Error = $E_m = 1 - \max_k(\hat{p}_{mk})$	Entropy = $D_m =$ $-\sum_{k=1}^K \hat{p}_{mk} \log(\hat{p}_{mk})$
0	$(0)(1-0) + (1)(1-1) = 0$	$E = 1 - \max(0,1) = 0$	$-(0) \cdot \log(0) - (1)(0) = 0$
0.1	$(0.1)(1-0.1) + (0.9)(1-0.9) = 0.18$	$E = 1 - \max(0.1,0.9) = 0.1$	$-(0.1)\log(0.1) - 0.9\log(0.9) = 0.325$
0.2	$(0.2)(1-0.2) + (0.8)(1-0.8) = 0.32$	$E = 1 - \max(0.2,0.8) = 0.2$	$-(0.2)\log(0.2) - 0.8\log(0.8) = 0.50$
0.3	$(0.3)(1-0.3) + (0.7)(1-0.7) = 0.42$	$E = 1 - \max(0.3,0.7) = 0.3$	$-(0.3)\log(0.3) - 0.7\log(0.7) = 0.61$
0.4	$(0.4)(1-0.4) + (0.6)(1-0.6) = 0.48$	$E = 1 - \max(0.4,0.6) = 0.4$	$-(0.4)\log(0.4) - 0.6\log(0.6) = 0.673$
0.5	$(0.5)(1-0.5) + (0.5)(1-0.5) = 0.50$	$E = 1 - \max(0.5,0.5) = 0.5$	$-(0.5)\log(0.5) - 0.5\log(0.5) = 0.693$
0.6	$(0.6)(1-0.6) + (0.4)(1-0.4) = 0.48$	$E = 1 - \max(0.6,0.4) = 0.4$	$-(0.6)\log(0.6) - 0.4\log(0.4) = 0.673$
0.7	$(0.7)(1-0.7) + (0.3)(1-0.3) = 0.42$	$E = 1 - \max(0.7,0.3) = 0.3$	$-(0.7)\log(0.7) - 0.3\log(0.3) = 0.61$
0.8	$(0.8)(1-0.8) + (0.2)(1-0.2) = 0.32$	$E = 1 - \max(0.8,0.2) = 0.2$	$-(0.8)\log(0.8) - 0.2\log(0.2) = 0.50$
0.9	$(0.9)(1-0.9) + (0.1)(1-0.1) = 0.18$	$E = 1 - \max(0.9,0.1) = 0.1$	$-(0.9)\log(0.9) - 0.1\log(0.1) = 0.325$
1.0	$(1.0)(1-1) + (0)(1-0) = 0$	$E = 1 - \max(1,0) = 0$	$-(1)\log(1) - 0\log(0) = 0$

Values  
of  
Metrics

