

# Algebra 2 Workbook

Ratios and proportions



#### **RATIOS AND PROPORTIONS**

- 1. The class has 12 girls and 18 boys. What is the ratio of boys to the total number of students in the class?
- $\blacksquare$  2. The ratio of boys to girls in the class is 4:3. The total number of students in the class is 28. How many girls are in the class?
- $\blacksquare$  3. The ratio of boys to girls in the class is 5:3. The total number of students in the class is 32. How many boys are in the class?
- 4. Two numbers have a ratio of 1 to 4 and a sum of 40. What are the two numbers?
- 5. There are 11 quarters, 9 dimes, and 13 nickels. What is the ratio of dimes to the total number of coins?
- 6. The ratio of dimes to quarters is 3:2. The total value of the coins is \$2.40. How many quarters are there?

#### CHEMICAL COMPOUNDS

■ 1. Find the molar mass for one molecule of table salt in grams per mole. Table salt has the molecular formula NaCl.

Sodium (Na) has a molar mass of 22.989770 g/mol

Chlorine (CI) has a molar mass of 35.453 g/mol

■ 2. Find the molar mass for one molecule of isopropyl chloride in grams per mole. Isopropyl chloride has the molecular formula  $C_3H_7CI$ .

Carbon (C) has a molar mass of 12.0107 g/mol

Hydrogen (H) has a molar mass of 1.00794 g/mol

Chlorine (CI) has a molar mass of 35.453 g/mol

- 3. Glucose,  $C_6H_{12}O_6$ , has a molar mass of 180.156 g/mol. What is the mass of oxygen in a 100 g glucose sample given that the molar mass of carbon is 12.01 g/mol and the molar mass of hydrogen is 1.00794 g/mol.
- 4. Find the total mass of a sample of silver phosphate,  $Ag_3PO_4$ , in grams per mole given that it contains 25.55 g of silver with the molar mass 107.8682 g/mol. The molar mass of  $Ag_3PO_4$  is 418.58 g/mol.



■ 5. If vitamin C has the molecular formula  $C_6H_8O_6$  and the molar mass of vitamin C is 176.12 g/mol, find the mass of each element in a 325 g vitamin C sample.

Carbon (C) has a molar mass of 12.01 g/mol

Hydrogen (H) has a molar mass of 1.00794 g/mol

Oxygen (O) has a molar mass of 15.9994 g/mol

■ 6. Find the molar mass of calcium (Ca) in one mole of calcium carbonate.  $CaCO_3$  has a molar mass of 100.0869 g/mol.

Carbon (C) has a mass of 12.0107 g/mol

Oxygen (O) has a mass of 15.9994 g/mol



## FRACTIONS TO DECIMALS TO PERCENTS

- 1. Convert 60 % to a fraction in lowest terms.
- 2. Convert 33.5 % to a decimal.
- 3. Convert 2/3 to a percent.
- 4. Find 15 % of 48.
- $\blacksquare$  5. Find a mixed fraction that represents 8% of 120.
- $\blacksquare$  6. Convert 100/160 to a percent.



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#### PERCENT MARKUP

- 1. A book store purchases a book for \$6.00 and sells it for \$9.00. What percentage of the original price is the markup amount?
- 2. A bike shop buys a used bike for \$130 and marks up the price by 35%. What is the markup amount?
- 3. It costs a car manufacturer \$12,800 to produce a car. The percent markup is 48%. What is the selling price of the car.
- 4. A bakery purchases a dozen sugar cookies for \$2.25. The markup percent is 60%. What is the selling price of the dozen sugar cookies?
- 5. A store purchases dresses from a manufacturer, marks them up by 75%, and sells each dress for \$91. How much did the store pay the manufacturer for each dress?
- 6. If a furniture store purchases a chair from a manufacturer, marks it up by 24%, and sells the chair for \$84.94. How much did the furniture store pay the manufacturer for the chair?

#### PERCENT MARKDOWN

■ 1. A computer has an original price of \$375 and is now on sale for \$255. What is the percent markdown?

■ 2. A sweater has an original price of \$34 and is now on sale for \$25.50. What is the percent markdown?

■ 3. The regular price of an item is \$75, but the item is now on clearance for 40% off the regular price. What is the sale price of the item?

■ 4. The regular price of the latest smartphone is \$749. After two years, the smartphone is on sale for 25% off. What is the sale price of the item?

■ 5. The price of a house was marked down to \$250,000, and the sale price was 12% off of the original price. What was the original price of the house?

■ 6. The sale price of a shirt is \$68.00, and the shirt is on sale for 25% off the original price. What was the original price of the shirt?

#### CALCULATING COMMISSION

- 1. A makeup company advertises that we can make 15% commission on sales of their product. If we sell \$3,252 worth of product, how much money do we earn?
- 2. An employee at a clothing store earned \$1,450 in hourly pay for the month. She also sold \$4,250 worth of merchandise and will earn a commission of 6% on those sales. What is the employee's expected paycheck before tax deductions?
- 3. A local bakery sells croissants for \$5.00 each. A sales clerk makes a 6% commission on the selling price of each croissant he sells. How many croissants does he need to sell to earn \$60 in commission?
- 4. A car salesman earns \$48,000 per year plus a commission of 12% on all the cars he sells. If he wants a yearly salary of \$72,500, how much money in car sales does he need to make?
- 5. Brittany earns \$1,772.10 in commission of makeup products. If she earns 18% commission, how much money in makeup sales did she make?



■ 6. Anthony works at a clothing store and earned \$1,644.75 last month before tax deductions. If he earns 7.5% in commission and his hourly pay was \$975 for the month, how much clothing did he sell?



#### **CALCULATING SIMPLE INTEREST**

- 1. If we deposit \$300 into a savings account and it earns 2% in simple interest, how much interest will we earn on the account in 7 years?
- 2. If we invest \$500 that earns 13% in simple interest, how much interest will we earn in 12 years?
- $\blacksquare$  3. What is the simple interest rate if we invest \$7,000 and earn \$3,250 in interest in 15 years?
- 4. If we deposit \$275 into a savings account that earns 4% simple interest, how much is in the account after 2 years?
- 5. If we invest \$450 that earns 15% simple interest, how many years will it take to have \$1,800 in the account?
- 6. If we invest \$1,230 that earns 14% simple interest, how much is in the account after 10 years?

# **COMPLEX FRACTIONS**

■ 1. Simplify the expression.

■ 2. Simplify the expression.

$$\frac{y}{x}$$

■ 3. Simplify the expression.

$$\frac{x}{b}$$

■ 4. Simplify the expression.

$$\frac{\frac{a}{m}}{n+\frac{1}{h}}$$

■ 5. Simplify the expression.

$$\frac{\frac{1}{y} - \frac{1}{x}}{1 - \frac{1}{y}}$$

■ 6. Simplify the expression.

$$\frac{1}{a-5} - \frac{1}{a+5}$$

$$\frac{5}{a+5}$$



## RATIOS AND PROPORTIONS WITH COMPLEX FRACTIONS

■ 1. Solve for the variable.

$$\frac{x}{\frac{1}{2}} = \frac{\frac{3}{4}}{\frac{1}{4}}$$

■ 2. Solve for the variable.

$$\frac{\frac{4}{7}}{\frac{1}{6}} = \frac{y}{\frac{7}{2}}$$

■ 3. Solve for the variable.

$$\frac{\frac{x}{2}}{\frac{8}{3}} = \frac{\frac{3}{4}}{\frac{2}{5}}$$

■ 4. Solve for the variable.

$$\frac{\frac{3}{8}}{\frac{x}{2}} = \frac{\frac{1}{4}}{\frac{4}{5}}$$

■ 5. Solve for the variable.

$$\frac{\frac{4}{5} - \frac{1}{2}}{\frac{3}{2}} = \frac{\frac{6}{7} + \frac{1}{7}}{\frac{b}{8}}$$

■ 6. Solve for the variable.

$$\frac{\frac{2}{3}}{\frac{1}{c}} = \frac{\frac{4}{5}}{\frac{7}{6}}$$



## **IMAGINARY AND COMPLEX NUMBERS**

■ 1. Simplify the imaginary expression.

$$2 - 6i - 4 + 9i$$

■ 2. Simplify the imaginary expression.

$$-3 - 7i + 8 + 3i$$

■ 3. Simplify the imaginary expression.

$$\sqrt{-4} + ii + 5i - 2i^3$$

■ 4. Simplify the imaginary expression.

$$\sqrt{27} - 3ii + 2i - 7i^3 + \sqrt{-36}$$

■ 5. Simplify the imaginary expression.

$$\sqrt{-9} + 2i^3 + 6i - \sqrt{25}\sqrt{-25} - 2\sqrt{-16}$$

■ 6. Simplify the imaginary expression.

$$\sqrt{-4} + 2i^4 + 6i^5 - \sqrt{-49} - 2i^6$$



### RATIONALIZING COMPLEX DENOMINATORS

■ 1. Use the conjugate method to simplify the imaginary expression.

$$\frac{2+6i}{3-i}$$

■ 2. Use the conjugate method to simplify the imaginary expression.

$$\frac{2-2i}{4i-1}$$

■ 3. Use the conjugate method to simplify the imaginary expression.

$$\frac{3i + 2i^2}{5i^3 + 4i^4}$$

■ 4. Use the conjugate method to simplify the imaginary expression.

$$\frac{2i + 4i^2}{6 - 6i}$$

■ 5. Use the conjugate method to simplify the imaginary expression.

$$\frac{\sqrt{-5}\sqrt{-5} - 7i^3}{3+i}$$

■ 6. Use the conjugate method to simplify the imaginary expression.

$$\frac{\sqrt{-2}\sqrt{-2} + 3i^3}{i - 4}$$



