

# Algebra 2 Workbook

Rational functions



# SIMPLIFYING RATIONAL FUNCTIONS

■ 1. Simplify the rational function to lowest terms.

$$\frac{x^4 + x^3 - 6x^2}{x^3 + x^2 - 2x}$$

■ 2. Reduce the fraction to its lowest terms.

$$\frac{10x^2 - 5x + 20}{15x^2}$$

■ 3. Reduce the fraction to its lowest terms.

$$\frac{18y^2 + 6y}{8y}$$

■ 4. Simplify each expression in the difference.

$$\frac{3ab + 2a^2b^2}{5ab} - \frac{12a^3b^3 + 3a^2b^2}{6a^2b^2}$$

■ 5. Simplify each expression in the sum.

$$\frac{2ab^2 + 3a^2b^3}{a^3b^3} + \frac{2ab^3 + b^4}{ab^3}$$

■ 6. Simplify each expression in the difference.

$$\frac{21x^2y^2}{14x^3y} - \frac{24xy + 12y}{96y}$$



# ADDING AND SUBTRACTING RATIONAL FUNCTIONS

■ 1. Simplify the expression.

$$\frac{2}{3ab} + \frac{b}{4a} + \frac{ab}{6}$$

2. Simplify the expression.

$$\frac{x+1}{x-1} + \frac{2x}{x-5} + \frac{x+2}{x^2-6x+5}$$

■ 3. Simplify the expression.

$$\frac{a}{3xy} + \frac{b}{15y^2} + \frac{c}{5x^3y^2}$$

■ 4. Simplify the expression.

$$\frac{x}{2x^2y} + \frac{y}{3z} + \frac{z}{5yz^2}$$

■ 5. Simplify the expression.

$$\frac{3ab}{4c} + \frac{2bc}{6a^3} + \frac{5}{8ab^2c^3}$$

■ 6. Simplify the expression.

$$\frac{x}{x+6} + \frac{x-6}{x}$$



#### FACTORING TO FIND A COMMON DENOMINATOR

■ 1. Simplify the expression by combining the two fractions.

$$\frac{x+1}{2x^2+5x-3} + \frac{2}{x+3}$$

■ 2. What is the common denominator of the rational expressions?

$$\frac{x^2-1}{x^2-4}$$
 and  $\frac{x+1}{3x^2-3x-6}$ 

■ 3. Simplify the expression by combining the two fractions.

$$\frac{3}{x-2} - \frac{x-4}{x^2-5x+6}$$

■ 4. Fill in the blank with the correct term.

$$\frac{2}{x^2 - 9} = \frac{2(x - 3) - 4(x - 2)}{4(x - 3)(x + 3)}$$

■ 5. Simplify the expression by combining the two fractions.

$$\frac{4}{x^2 - 2x - 3} - \frac{1}{x^2 + 5x + 4}$$

■ 6. What went wrong in the following simplification?

$$\frac{3}{x^2 - 25} - \frac{1}{x + 5}$$

$$\frac{3-x-5}{(x-5)(x+5)}$$



# **MULTIPLYING RATIONAL FUNCTIONS**

■ 1. Simplify the expression.

$$\frac{25x^2 - 4}{x^2 - 36} \cdot \frac{x + 6}{5x - 2}$$

■ 2. Simplify the expression.

$$\frac{4x^2 - 49}{9x^2 - 16} \cdot \frac{3x + 4}{2x + 7}$$

■ 3. Simplify the expression.

$$\frac{x^2 + 8x + 16}{9x^2 + 36x + 36} \cdot \frac{3x + 6}{x + 4}$$

■ 4. Simplify the expression.

$$\frac{16x^2 + 16x + 4}{x^2 + 18x + 81} \cdot \frac{x^2 - 81}{16x^2 - 4}$$

■ 5. Simplify the expression.

$$\frac{x^2 + 5x - 14}{x^2 + 2x - 3} \cdot \frac{x^2 + 4x - 5}{x^2 + 9x + 14}$$

# ■ 6. Simplify the expression.

$$\frac{2x^2 - 13x - 24}{3x^2 - x - 4} \cdot \frac{3x^2 - 7x + 4}{x^2 - 6x - 16}$$



#### **DIVIDING RATIONAL FUNCTIONS**

■ 1. Simplify the expression.

$$\frac{2x+16}{9x^2+27x} \div \frac{3x+24}{x+3}$$

■ 2. Simplify the expression.

$$\frac{3x^3 - 3x^2 - 6x}{2x^2 - 14x + 24} \div \frac{3x^2 + 21x}{x^2 - 8x + 15}$$

■ 3. Simplify the expression.

$$\frac{2x^2 - 13x - 7}{12x + 6} \div \frac{3x - 2}{3x^2 - 17x + 10}$$

■ 4. Simplify the expression.

$$\frac{4x^2 + 13x + 10}{3x + 6} \div \frac{3x - 1}{3x^2 - 13x + 4}$$

■ 5. Simplify the expression.

$$\frac{4x^2 - 9}{x^2 + 12x + 36} \div \frac{4x^2 - 12x + 9}{x^2 + 7x + 6}$$

■ 6. Simplify the expression.

$$\frac{15x^2 + 75x + 90}{5x^2 + 50x + 125} \div \frac{x^2 - 3x + 2}{x^2 - 25}$$



