Introduction to machine learning in Hydrology

Lazaro J. Perez & Marc Berghouse

contact: lazaro.perez@dri.edu

Outline

- Decision Trees
- Decision Trees in Matlab
- Classification and Regression Learner App

Decision trees

Definition

A decision tree is a non-parametric supervised learning algorithm that is utilized for both classification and regression tasks

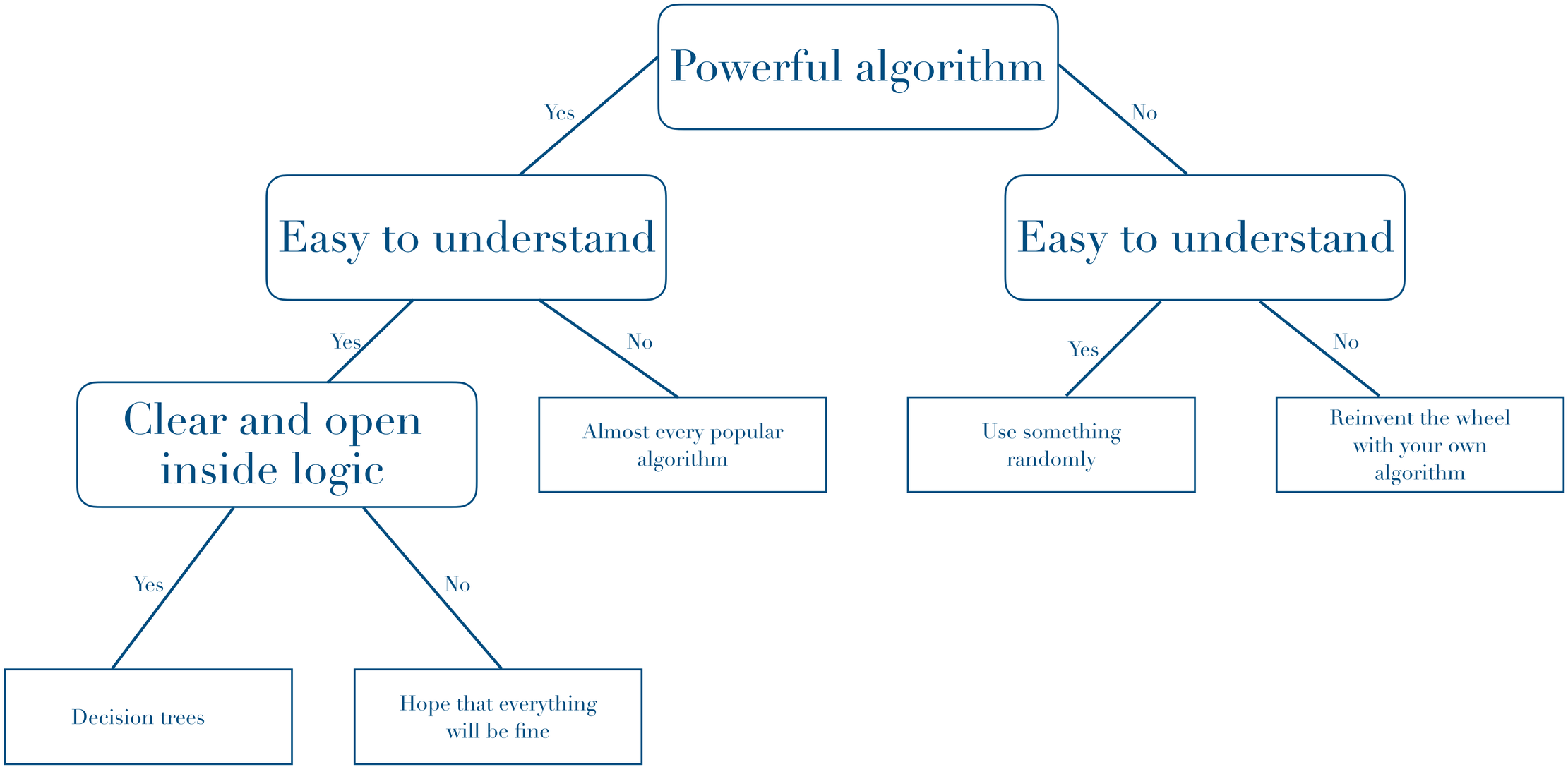
It has a hierarchical tree structure, which consists of a root node, branches, internal nodes, and leaf nodes

General consensus

It’s a binary tree that recursively splits the dataset until we’re left with pure leaf nodes

A decision tree analysis is a divide-and-conquer approach to classification and regression

Decision trees: Graphical representation

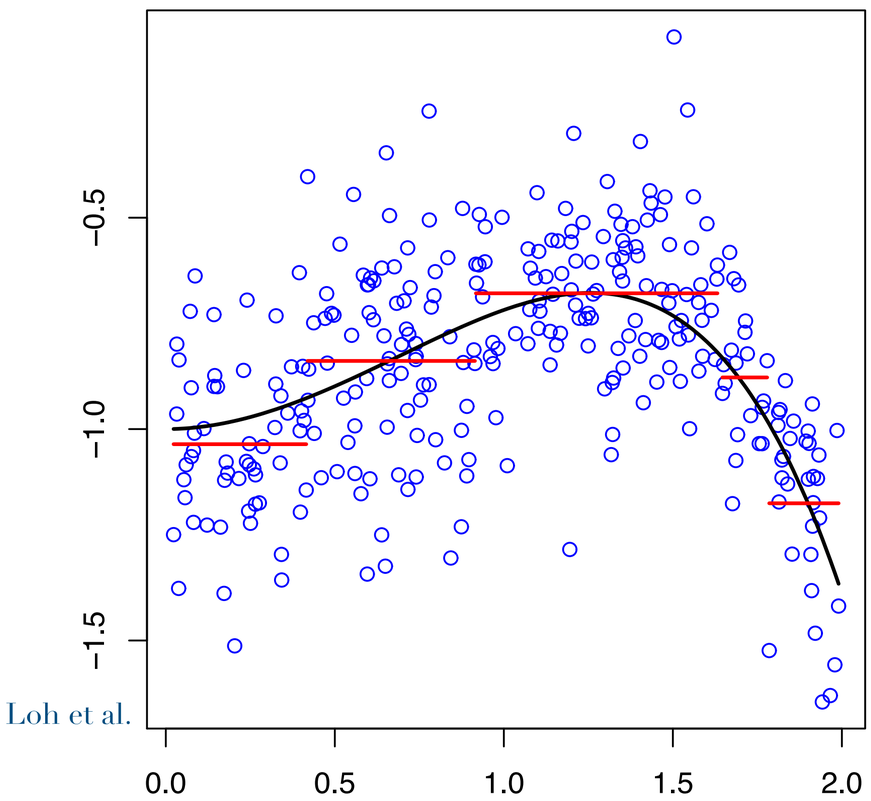


Decision trees

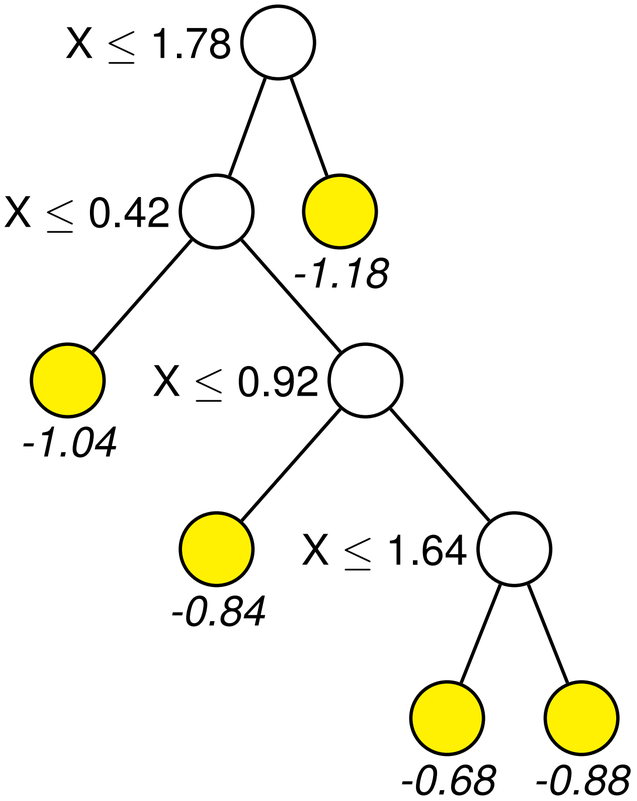
Development

First generation

Automatic interaction detection (AID): Morgan and Sonquist, 1963



Loh et al.

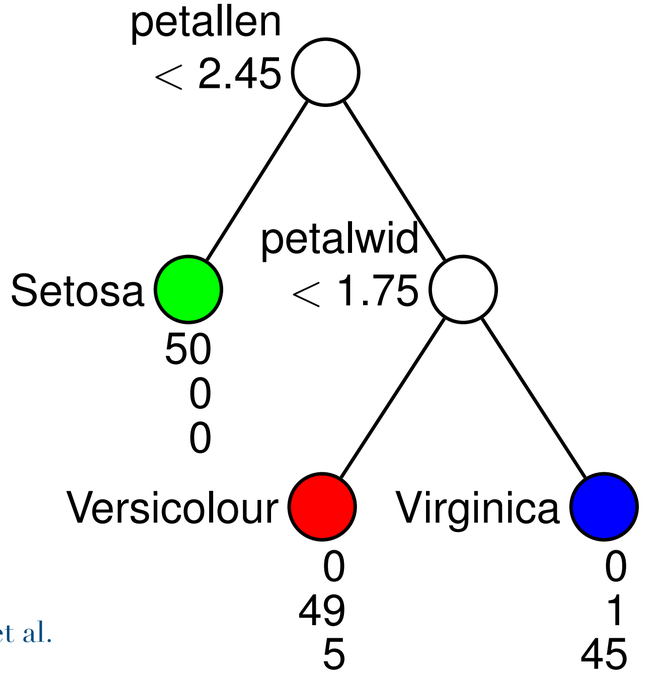


Decision trees

Development

First generation

Theta automatic interaction detection (THAID): Messenger and Mandell, 1972



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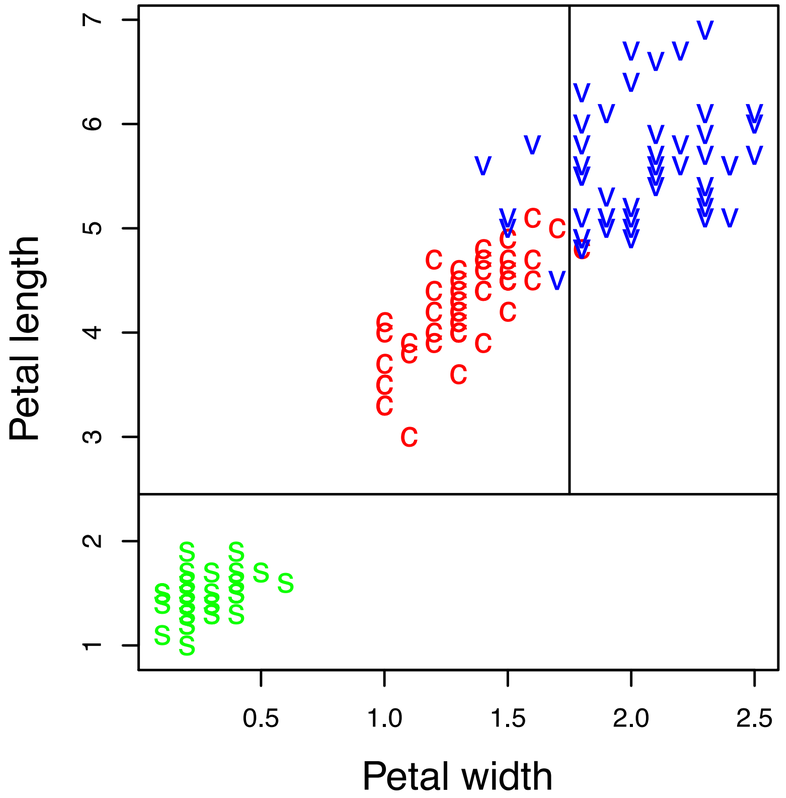


Decision trees

Development

Second generation

Classification and regression tree (CART): Breiman et al., 1984

- Adds cross-validation
- Adds pruning

Third generation

Quick unbiased efficient statistical tree (QUEST): Loh and Shih, 1997

- Merge classes to get binary splits

Fourth generation

Random forest: Breiman et al., 2001

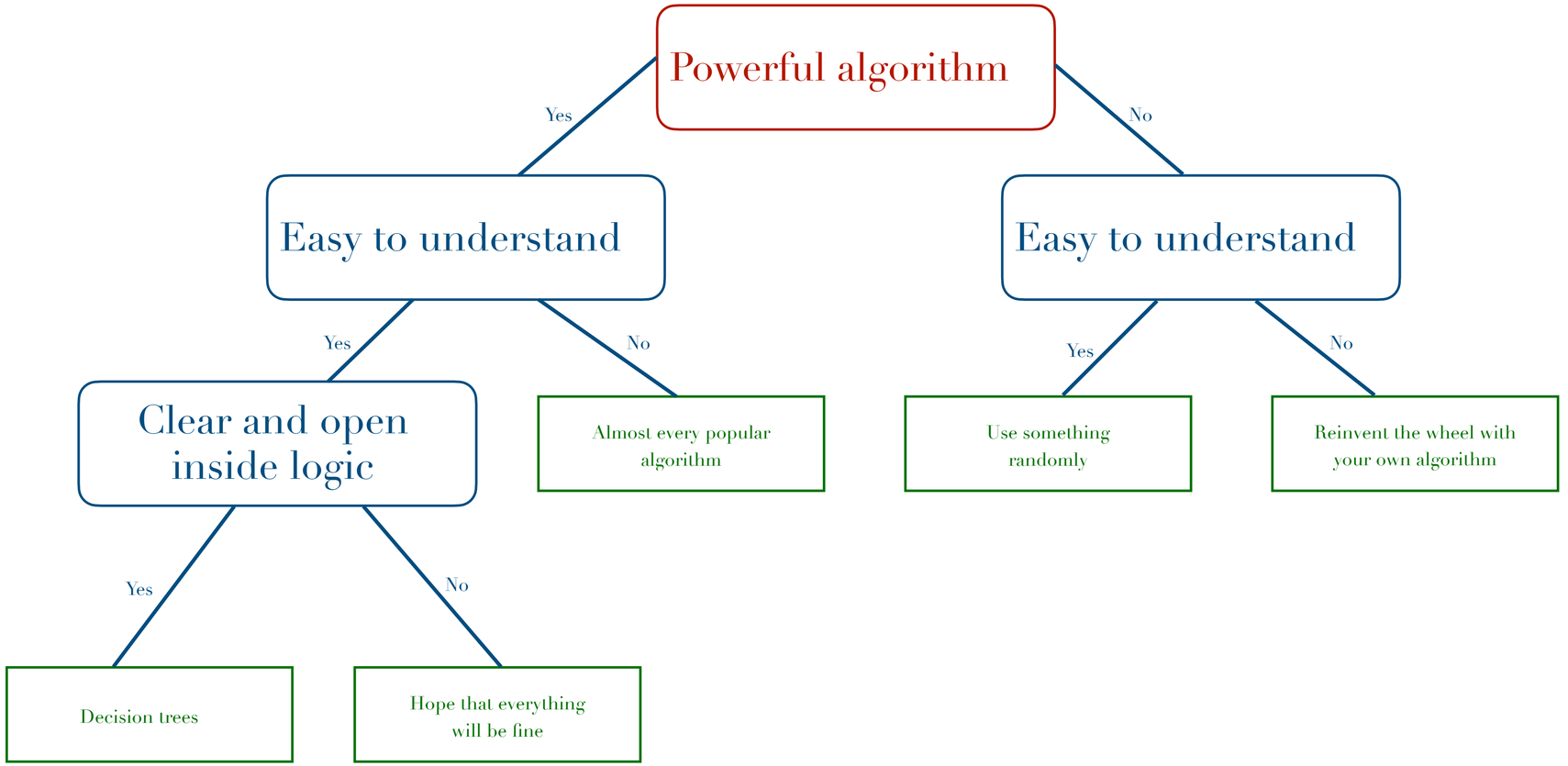
- Final predicted value is average of values from the trees

Decision trees: Key concepts

Root: Top node

Node: Each object in a tree

Leaf node: Final node



Decision trees: Splitting criterion

Entropy

$$S = -\sum_{k \in K} p(k) \log_2 p(k)$$

Entropy values fall between 0 and 1

Pure leaf nodes (only one class) has S=0

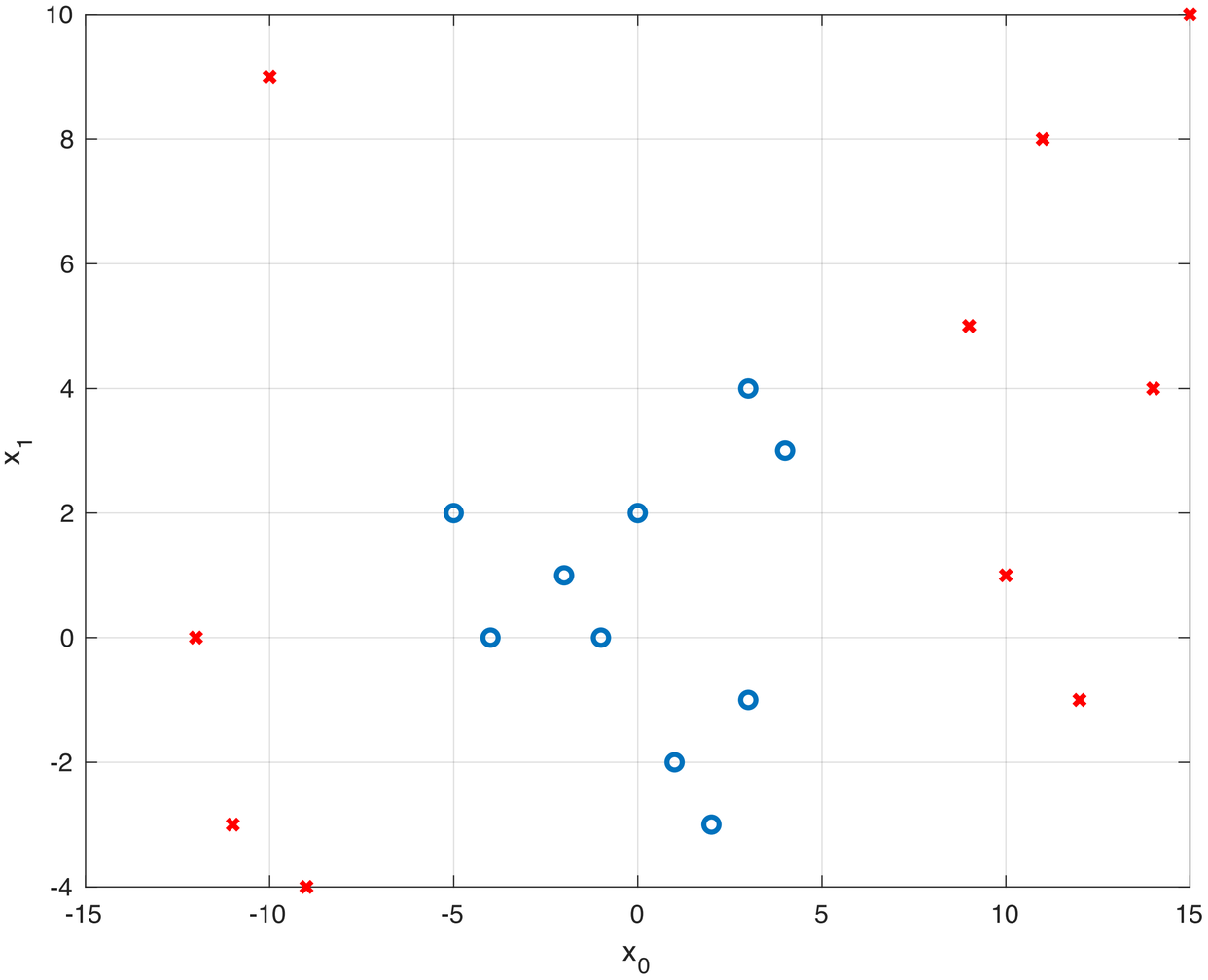
Information gain

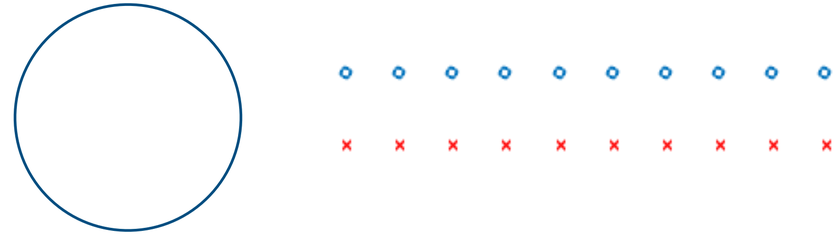
$$\Theta = S(p) - \sum w_i S(c_i)$$

Information contained in a state

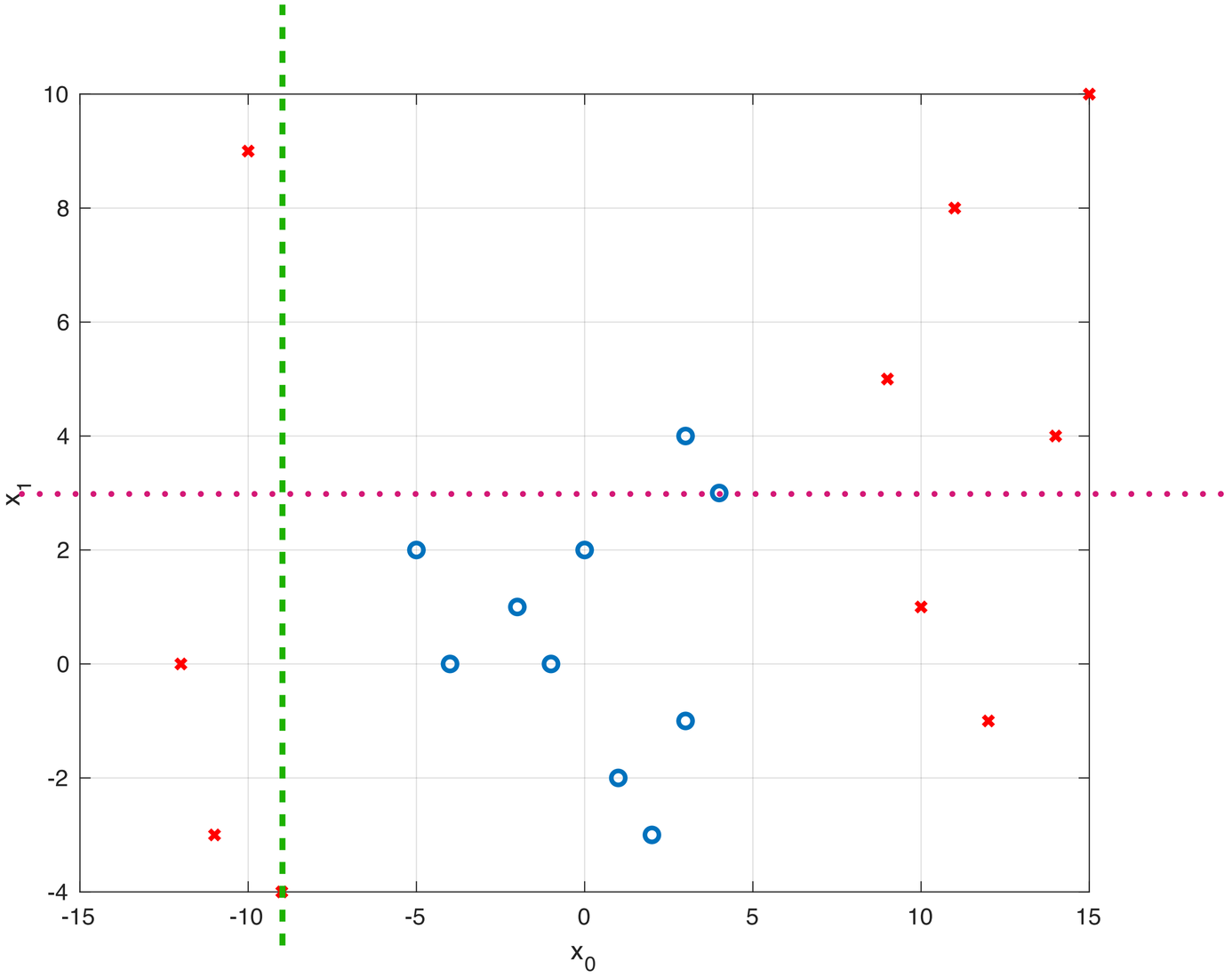
The attribute with the highest information gain will produce the best split

Decision trees: Example



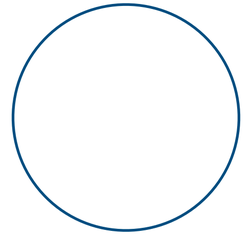


Decision trees: Example



$x_1 \leq 3$

$x_0 \leq -9$



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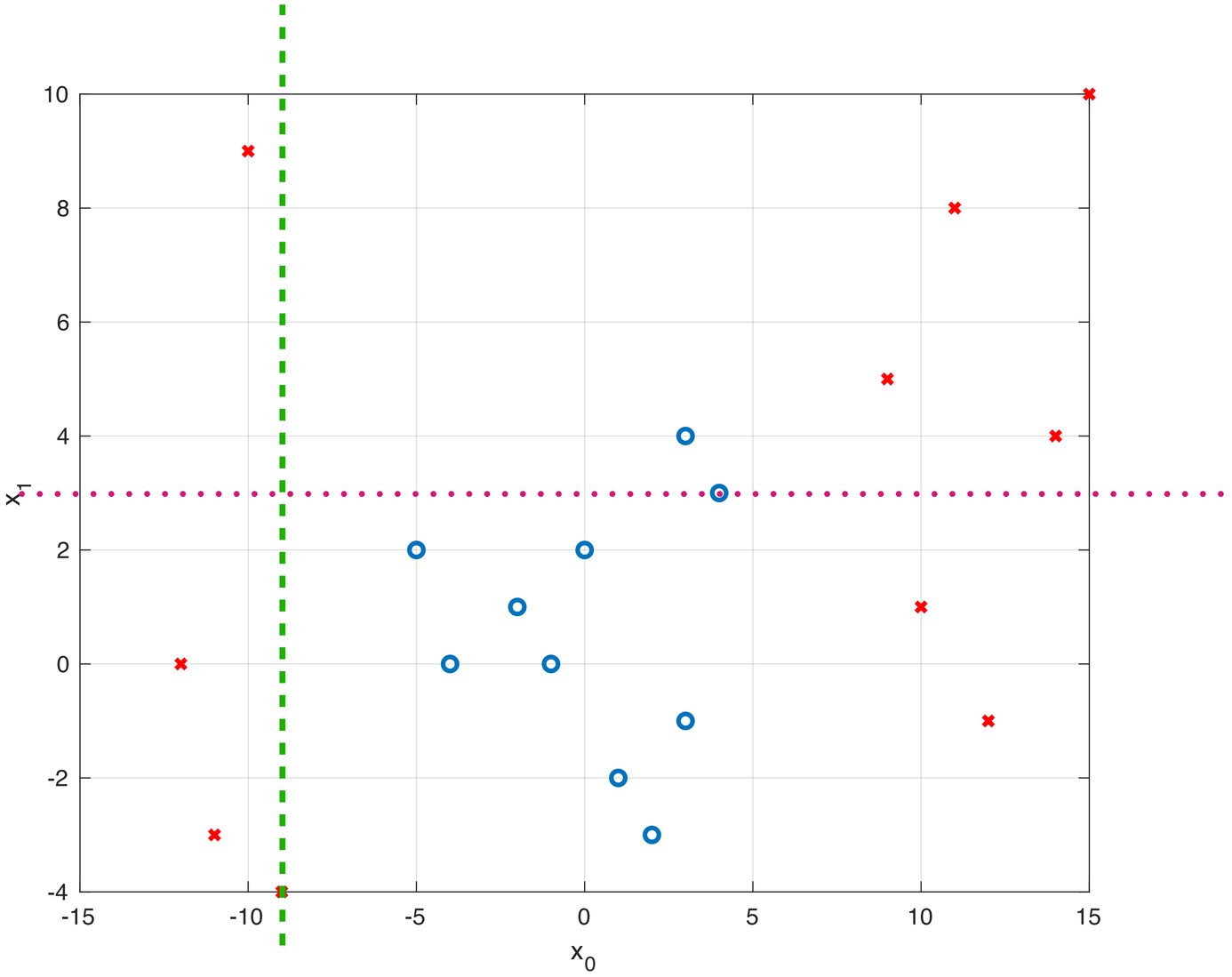

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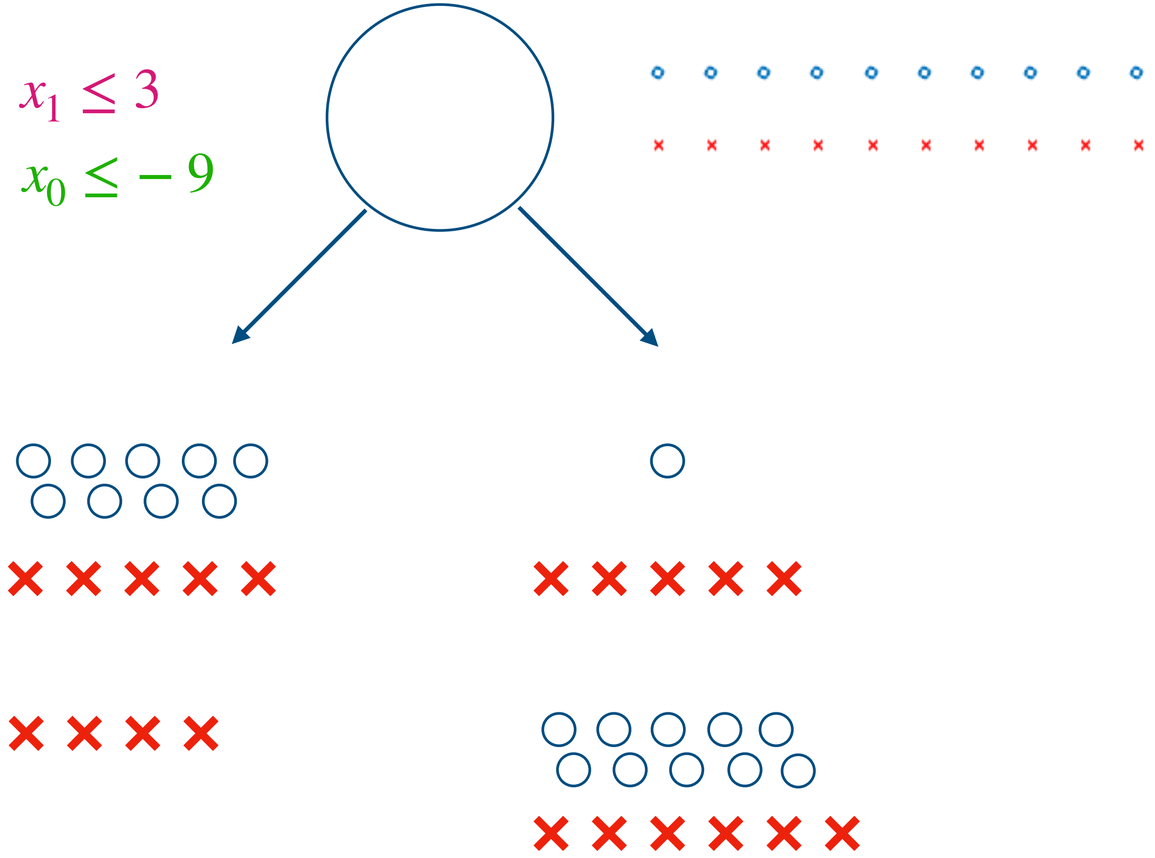

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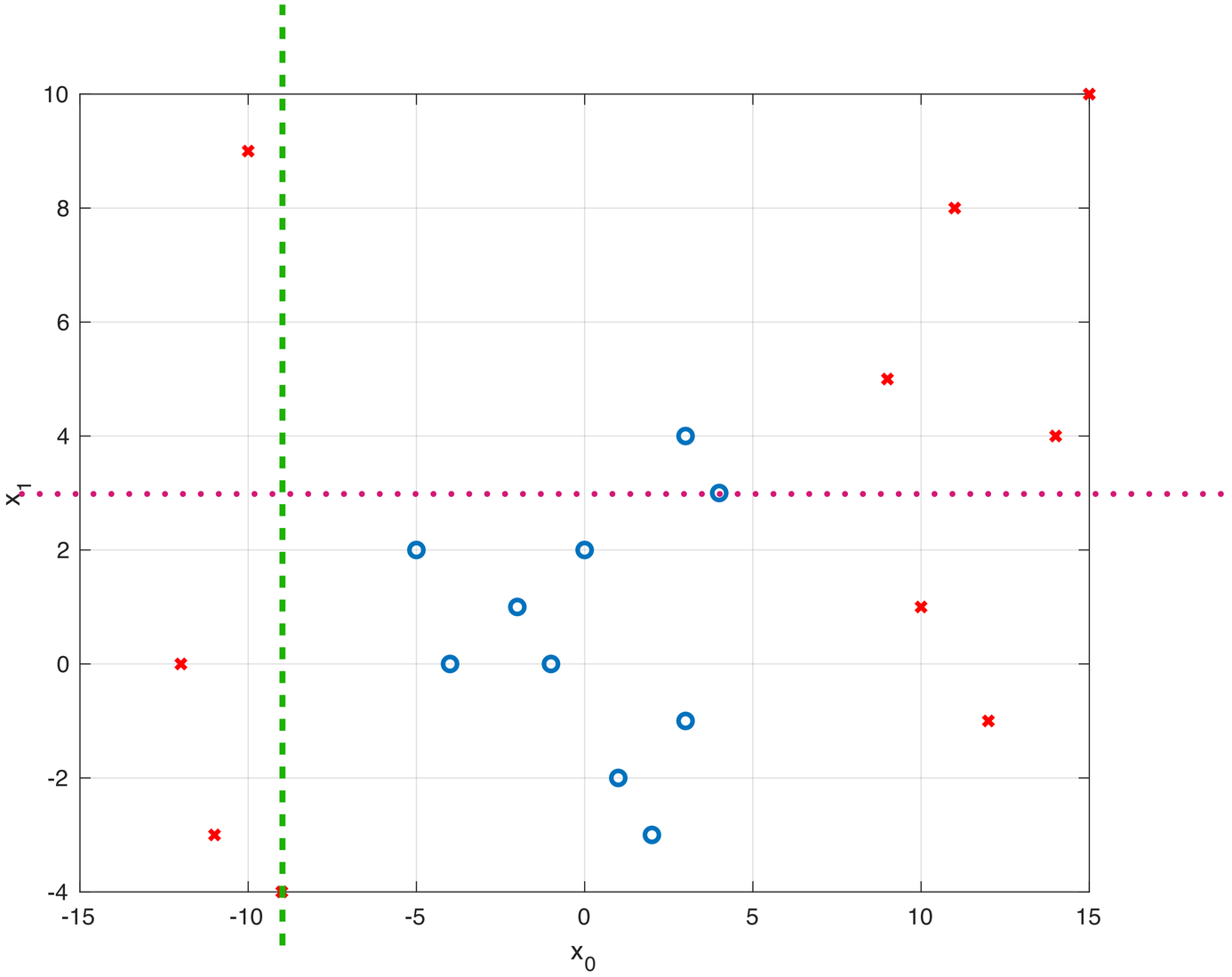

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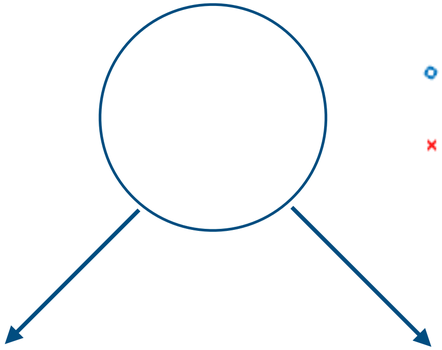

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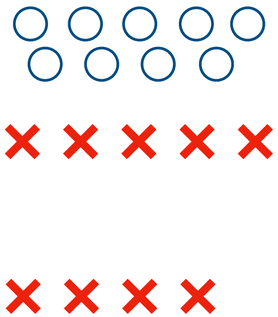
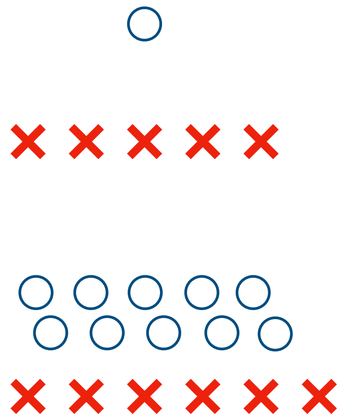
$$S = -0.5\log(0.5) - 0.5\log(0.5) = 1$$





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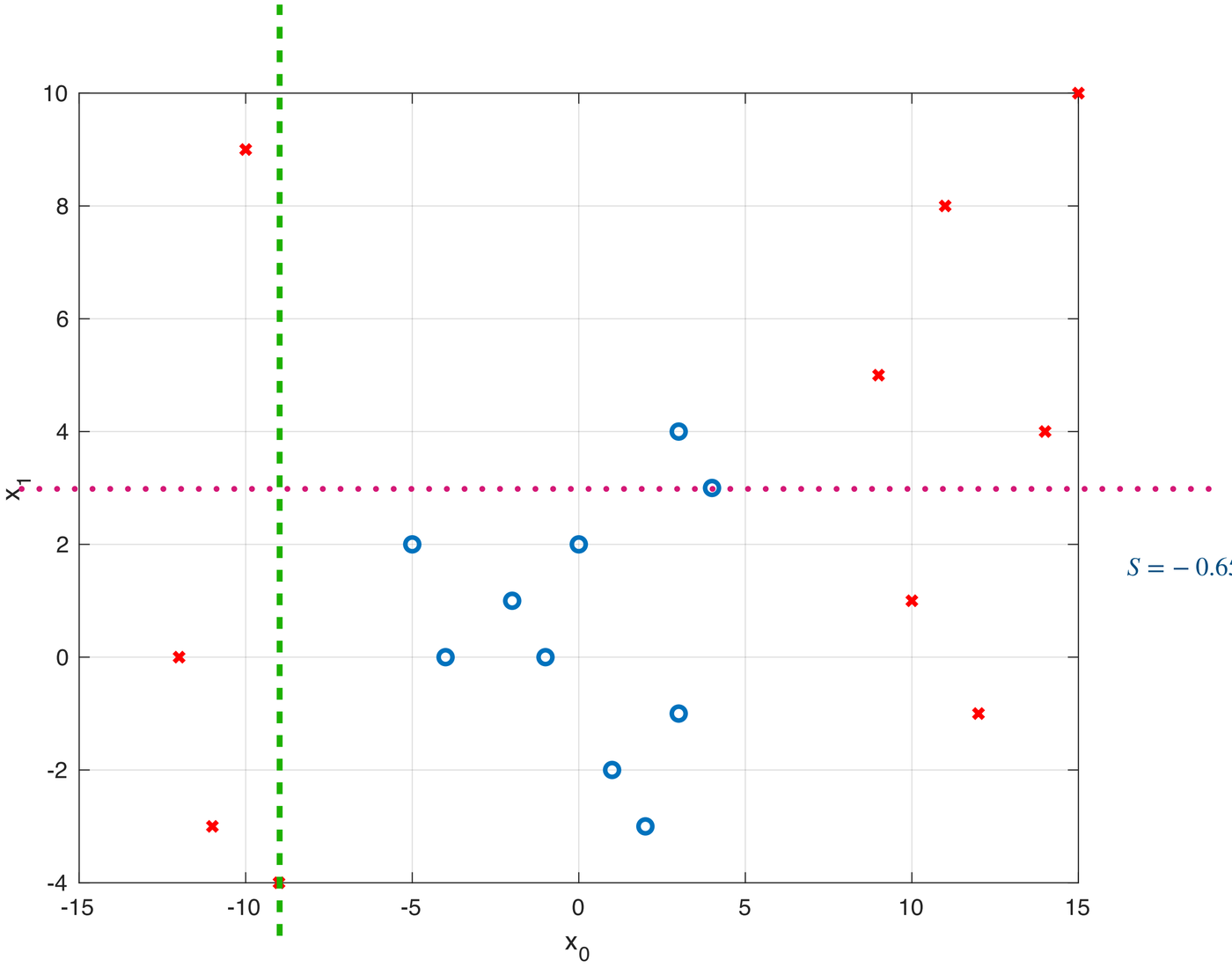

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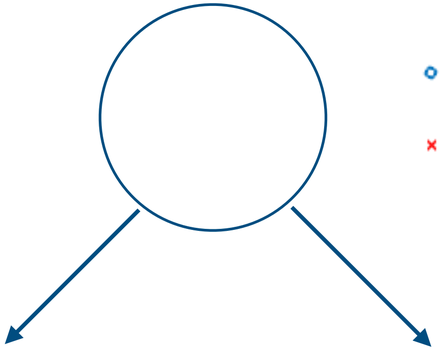

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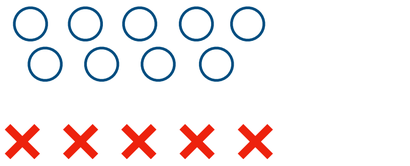
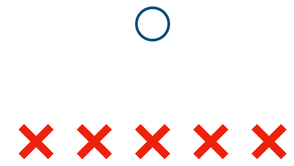
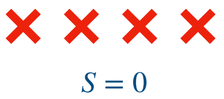


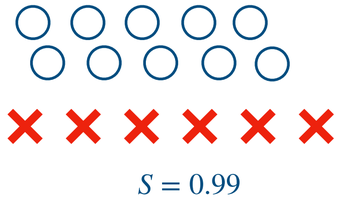
$S = -0.65\log(0.65) - 0.35\log(0.35) = 0.94$



$S = -0.17\log(0.17) - 0.83\log(0.83) = 0.65$



$S = 0$



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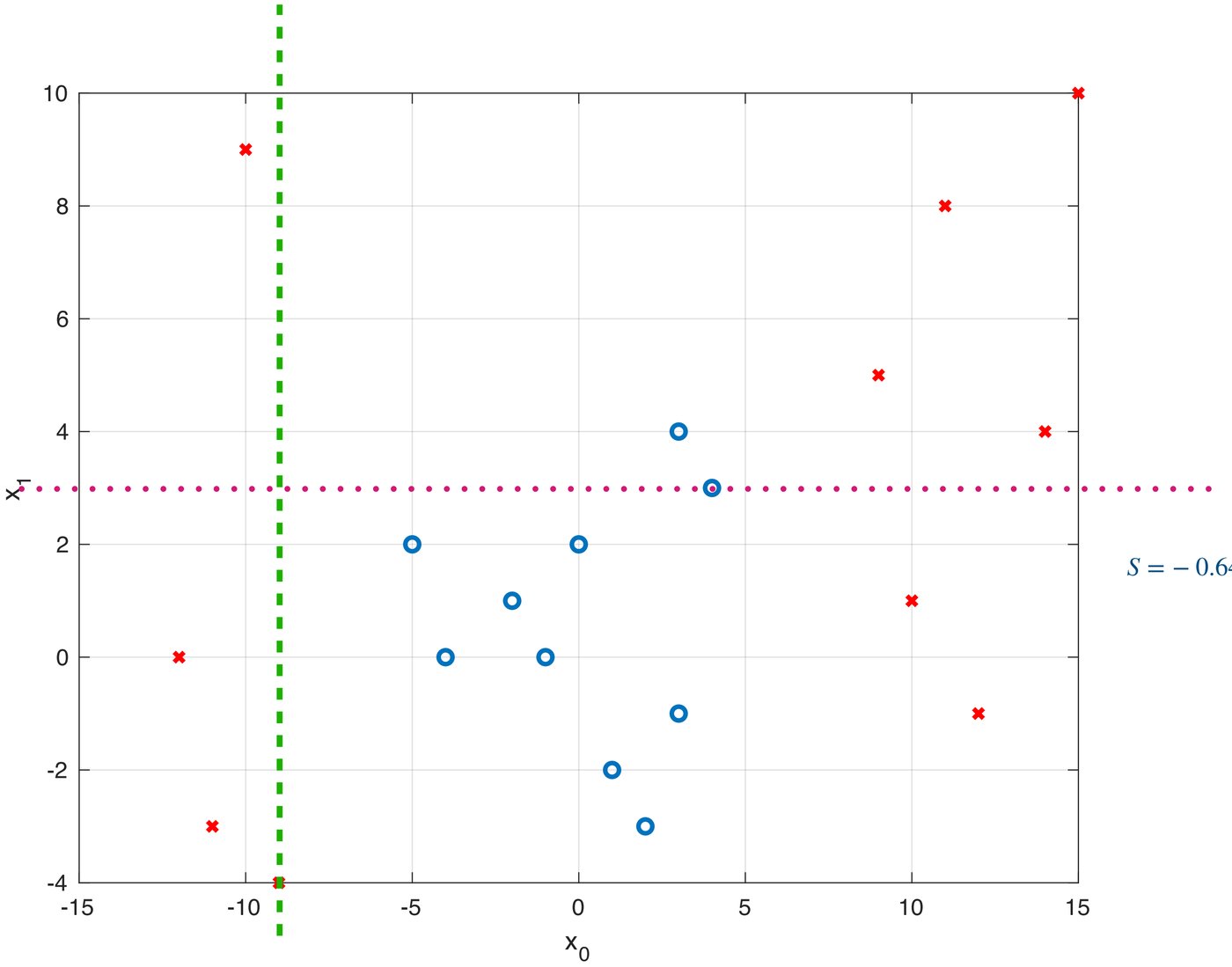
Decision trees: Example



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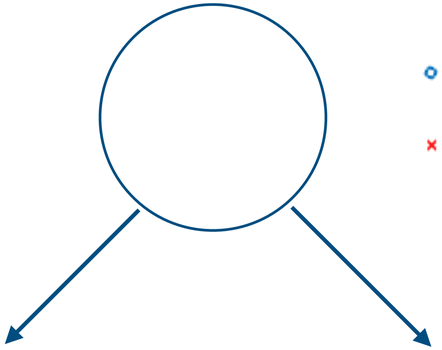

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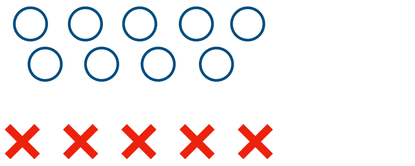
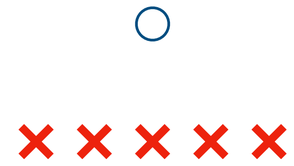


$S = -0.64\log(0.64) - 0.35\log(0.35) = 0.94$



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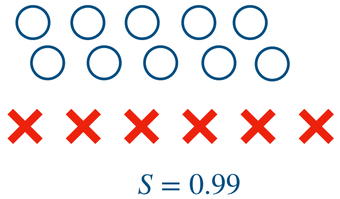


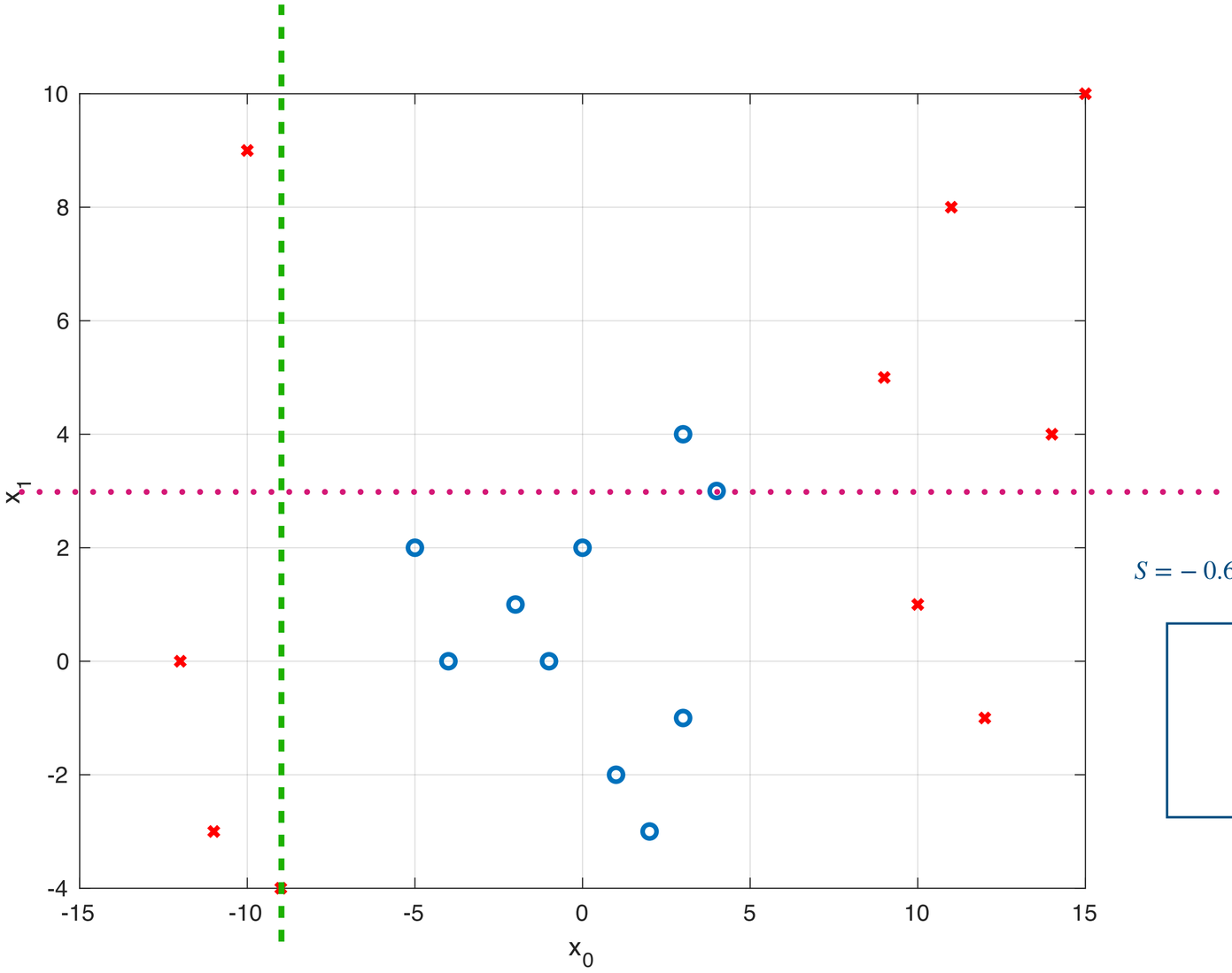
$S = 0.99$

$$\Theta = S(p) - \sum w_i S(c_i)$$

$$\Theta_1 = 1 - \frac{14}{20} * 0.94 - \frac{6}{20} * 0.65 = 0.14$$

$$\Theta_2 = 1 - \frac{4}{20} * 0 - \frac{16}{20} * 0.99 = 0.2$$

Decision trees: Example



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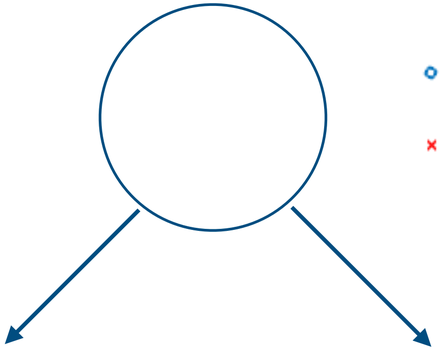

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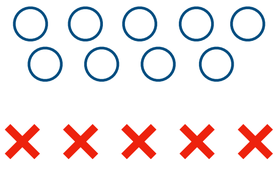

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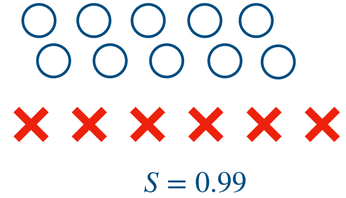

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$$\Theta_2 > \Theta_1$$

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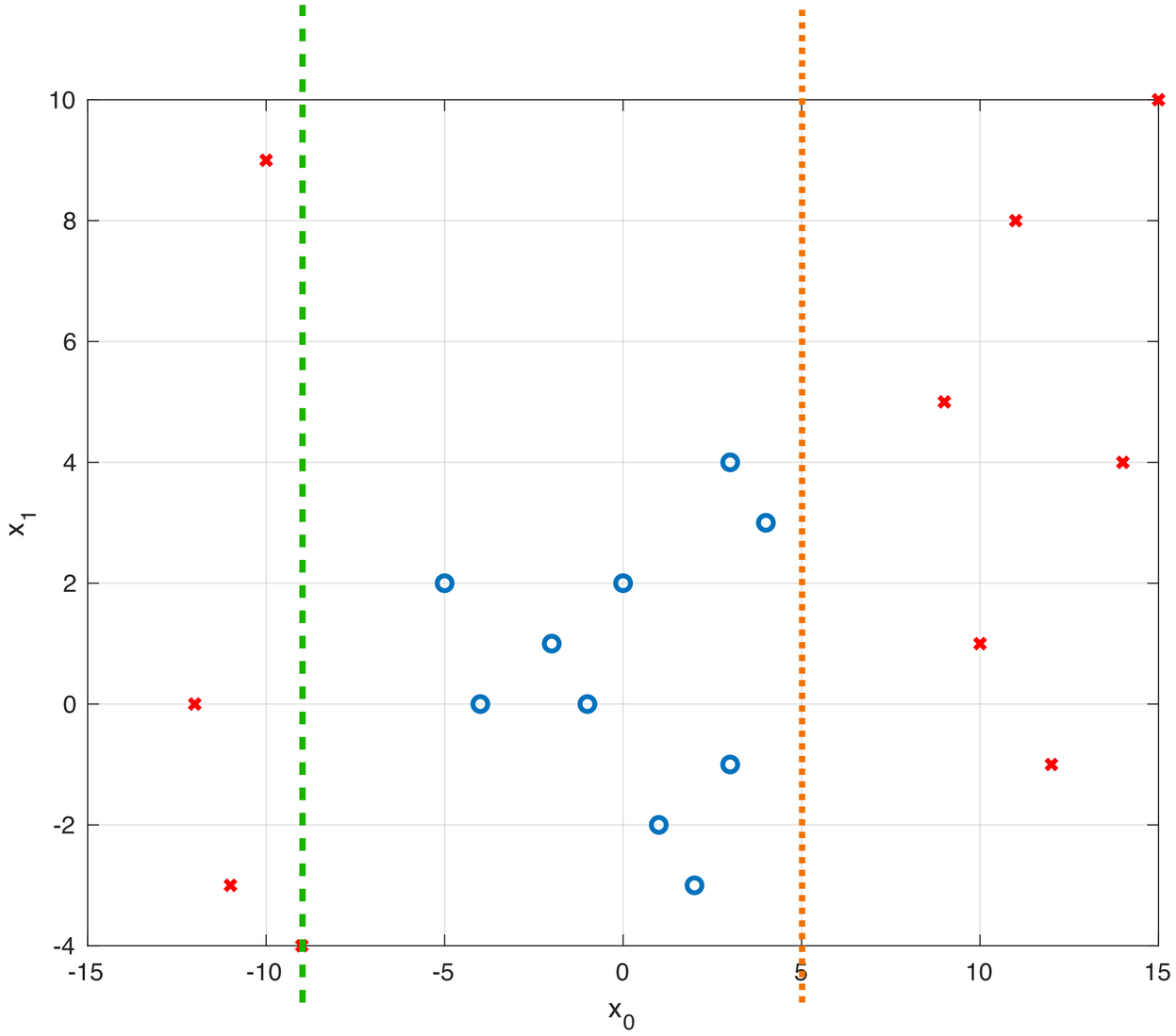
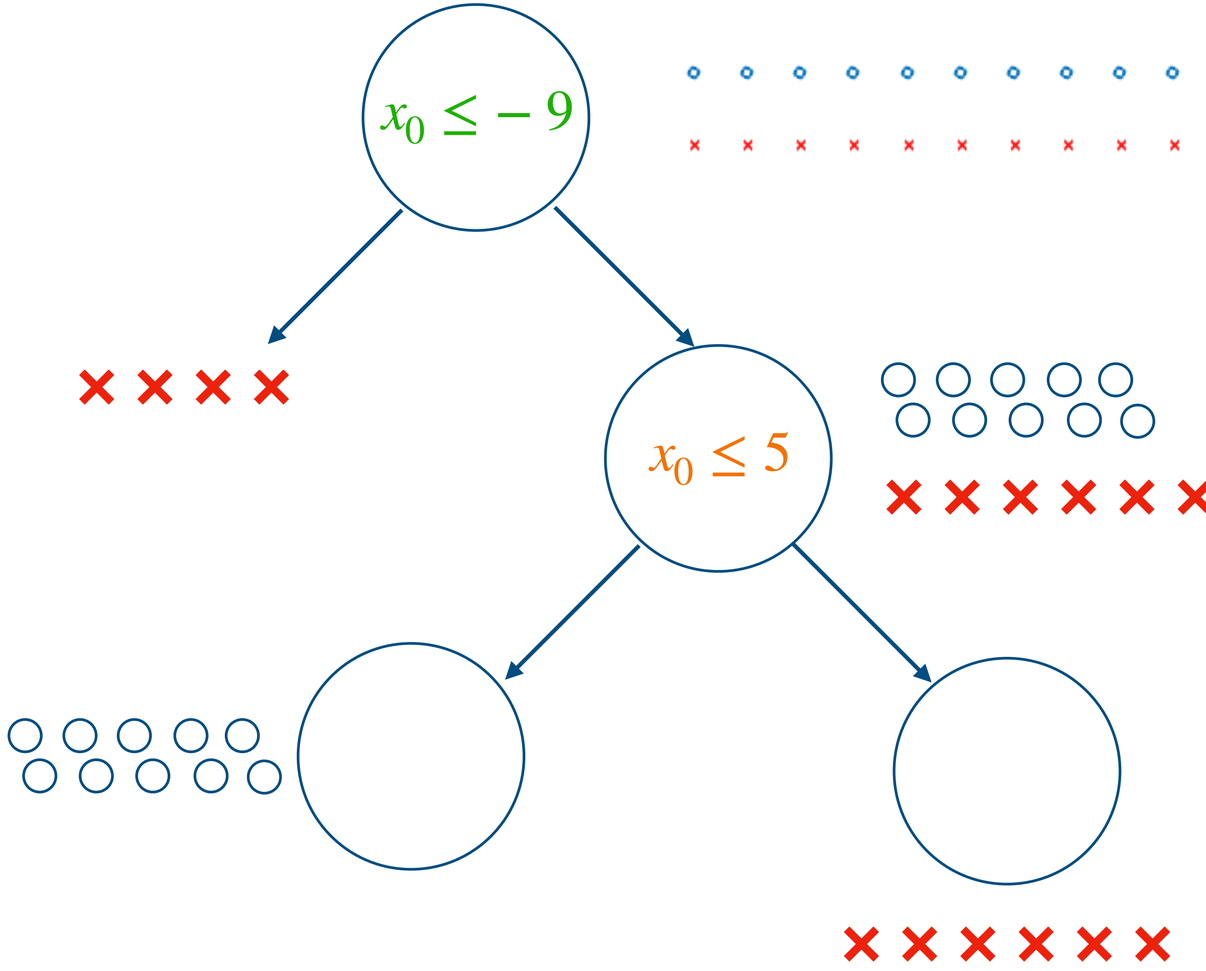




Decision trees

Advantages

Simple to understand: visual representations of decision trees make them easier to understand

Little to no data preparation

Flexible: can be leveraged for both classification and regression tasks

Disadvantages

Prone to overfitting: Complex decision trees tend to overfit

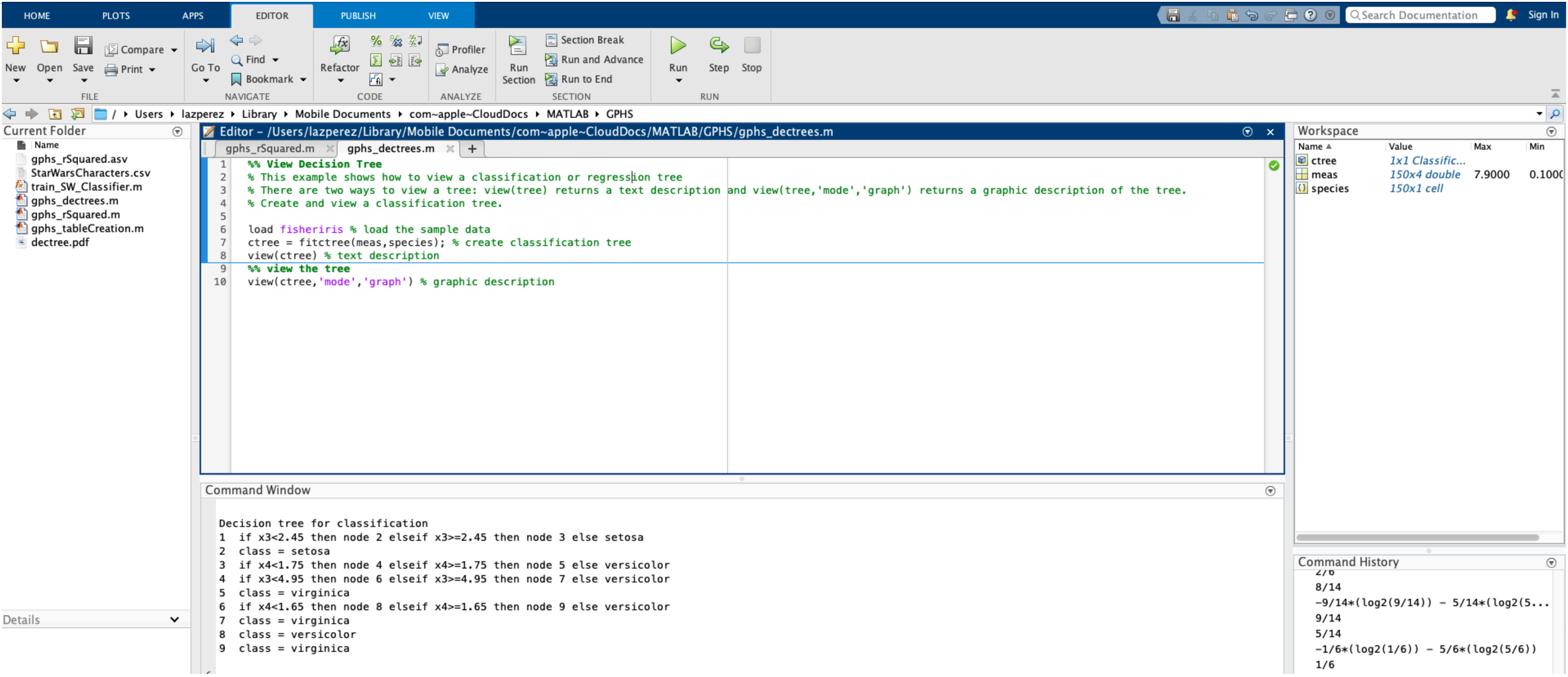
High variance estimator: Small variations within data can produce a very different decision tree

Decision trees in Matlab

Classification and regression tree (CART): Breiman et al., 1984

- Decision trees, or classification trees and regression trees, predict responses to data in Matlab
- Allows you to predict a response following the decisions in the tree from the root (beginning) node down to a leaf node
- The leaf node contains the response
- Classification trees give nominal responses, such as `'true'` or `'false'`
- Regression trees give numeric responses.

Decision trees in Matlab



Decision trees in Matlab