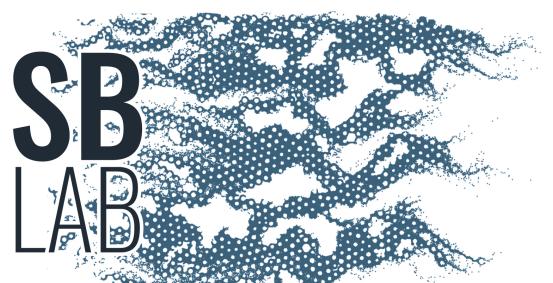

Introduction to machine learning in Hydrology

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Outline

- Getting into Matlab
- Why use Matlab
- Matlab desktop environment
- Variables and assignments
- Vector and matrices

The big picture

MATLAB → MAT(rix)LAB(oratory) → Written in C & Fortran



MATLAB is a very powerful software package that has many built-in tools for solving problems and developing graphical illustrations

MATLAB has built-in functions to perform many operations, and there are toolboxes that can be added to augment these functions (e.g., for signal processing)

Why use MATLAB

Easy to code: Develop the computational codes and debug easily

```
variablename = expression
```

```
>> mynum = 6
```

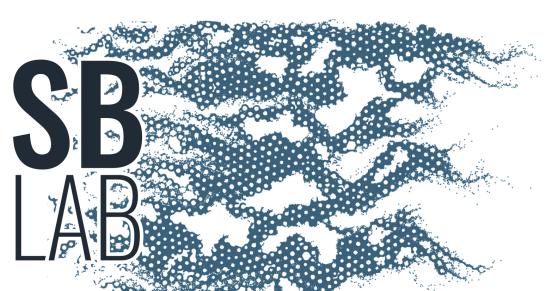
Supports GPU: Accelerate your code using basic GPU computing

Standalone compiler: No need to call libraries or compile codes/functions

Graphical User Interface: Inexperienced programmers can design/refine data-analysis programs

Toolboxes: Machine learning, image analysis, robotics, communications, etc.

Work with external code: C, C++, Python, Fortran



File types MATLAB

Algorithm, scripts, and functions

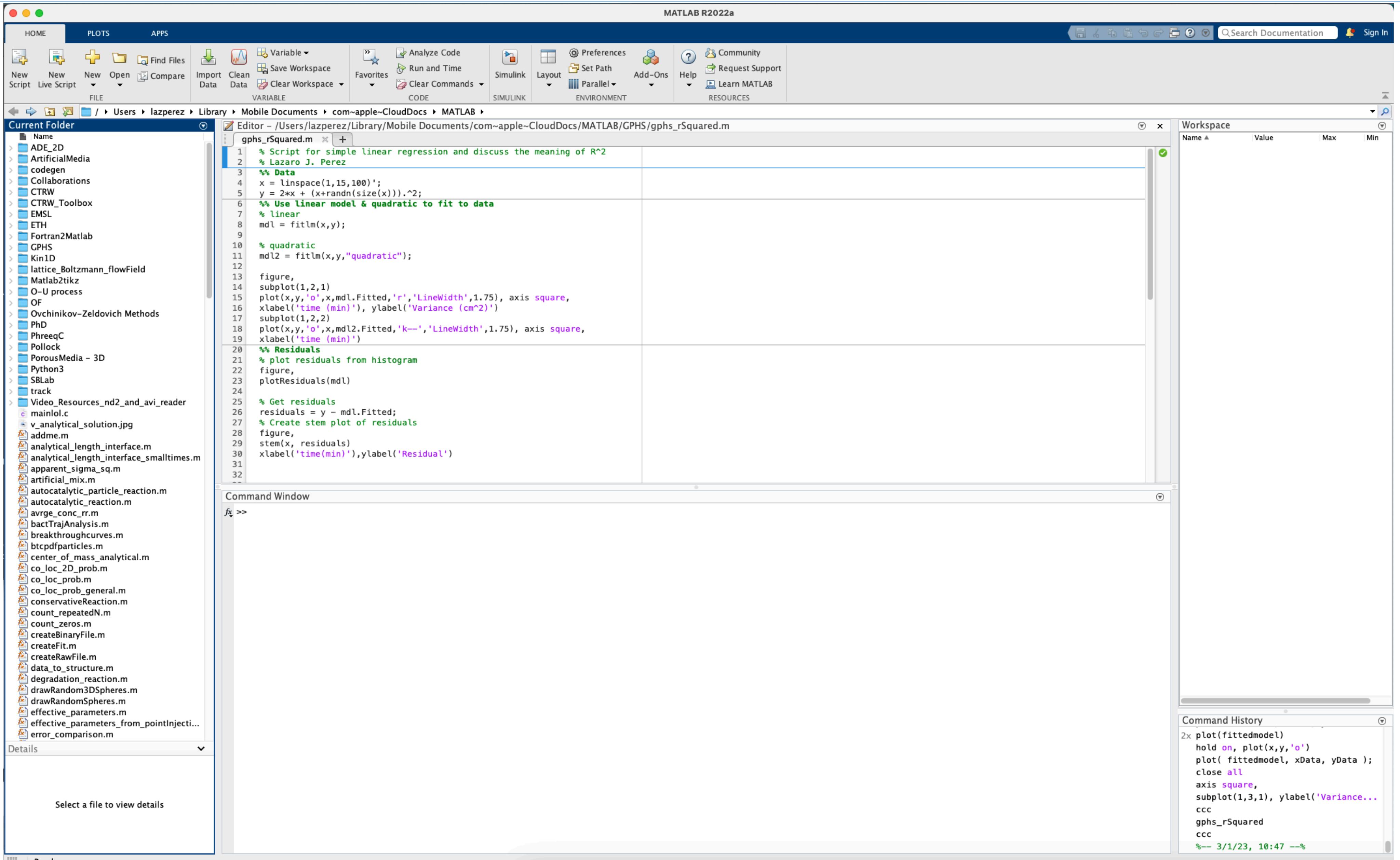
An algorithm is the sequence of steps needed to solve a problem

- Get the input: the radius
- Calculate the result: the area
- Display the output

A script is a sequence of MATLAB instructions that are stored in an M-file and saved

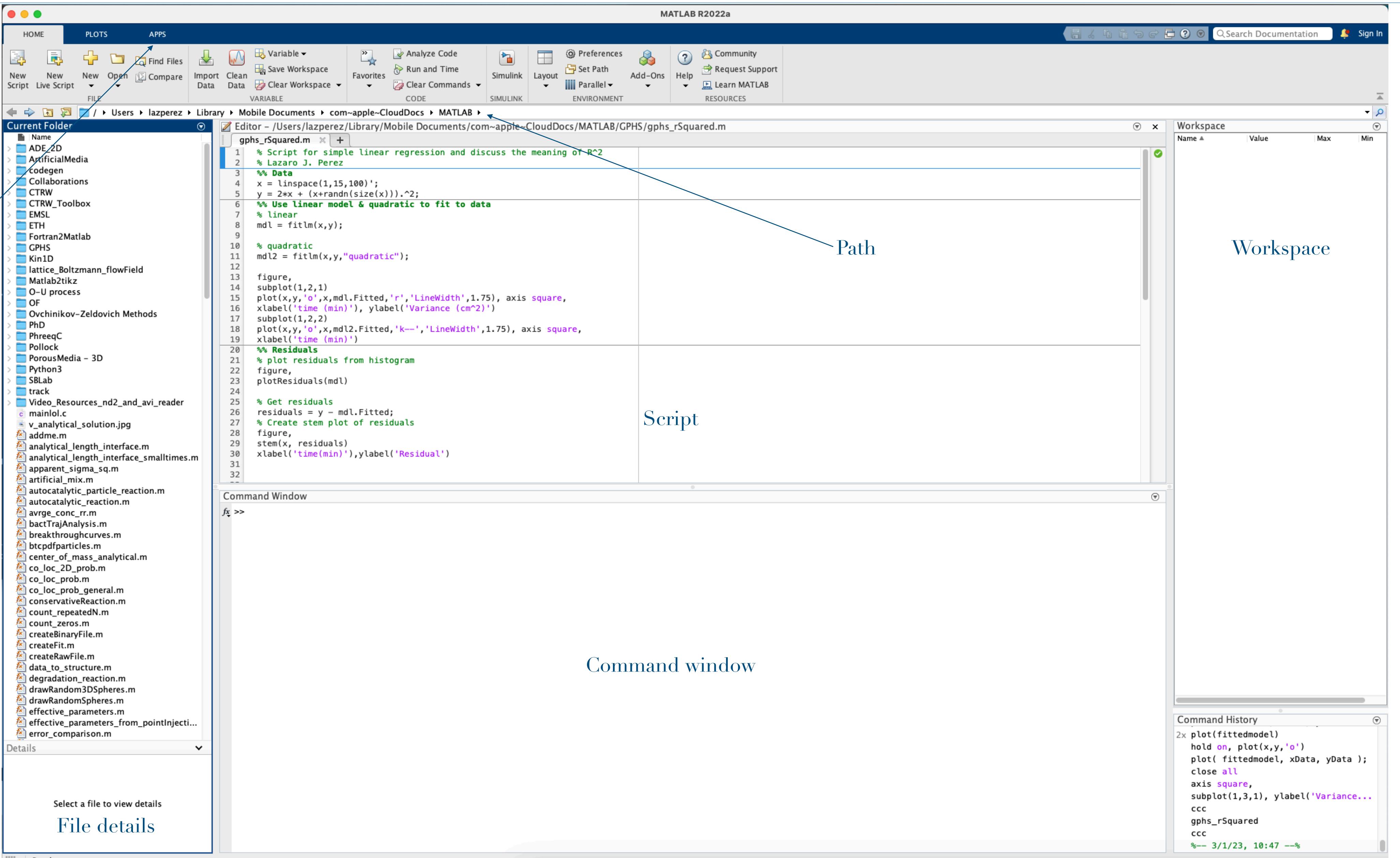
Functions provide more flexibility than a script, primarily because you can pass input values and return output values. In addition, functions avoid storing temporary variables in the base workspace and can run faster than scripts

MATLAB: Desktop Environment



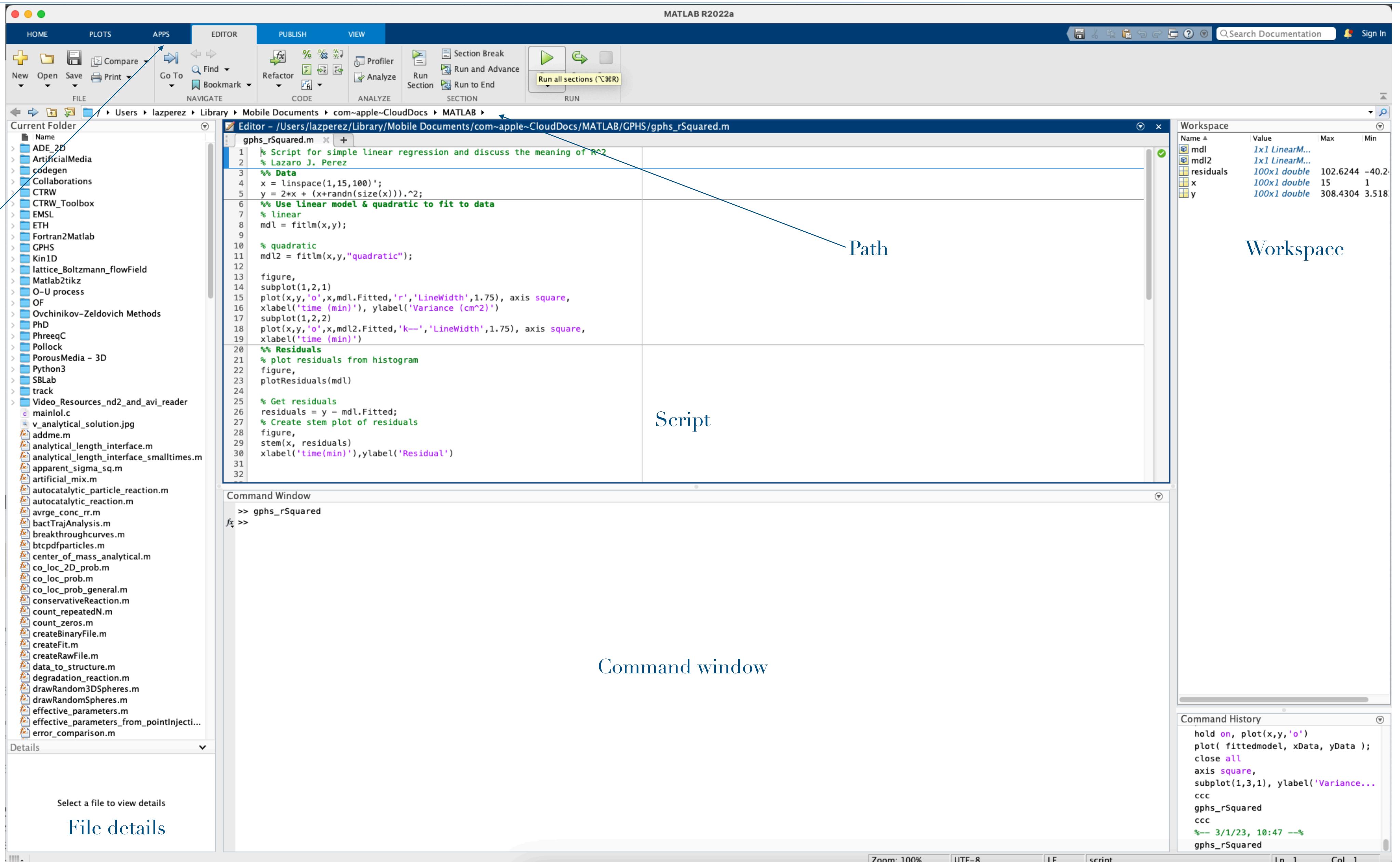
MATLAB: Desktop Environment

Toolboxes



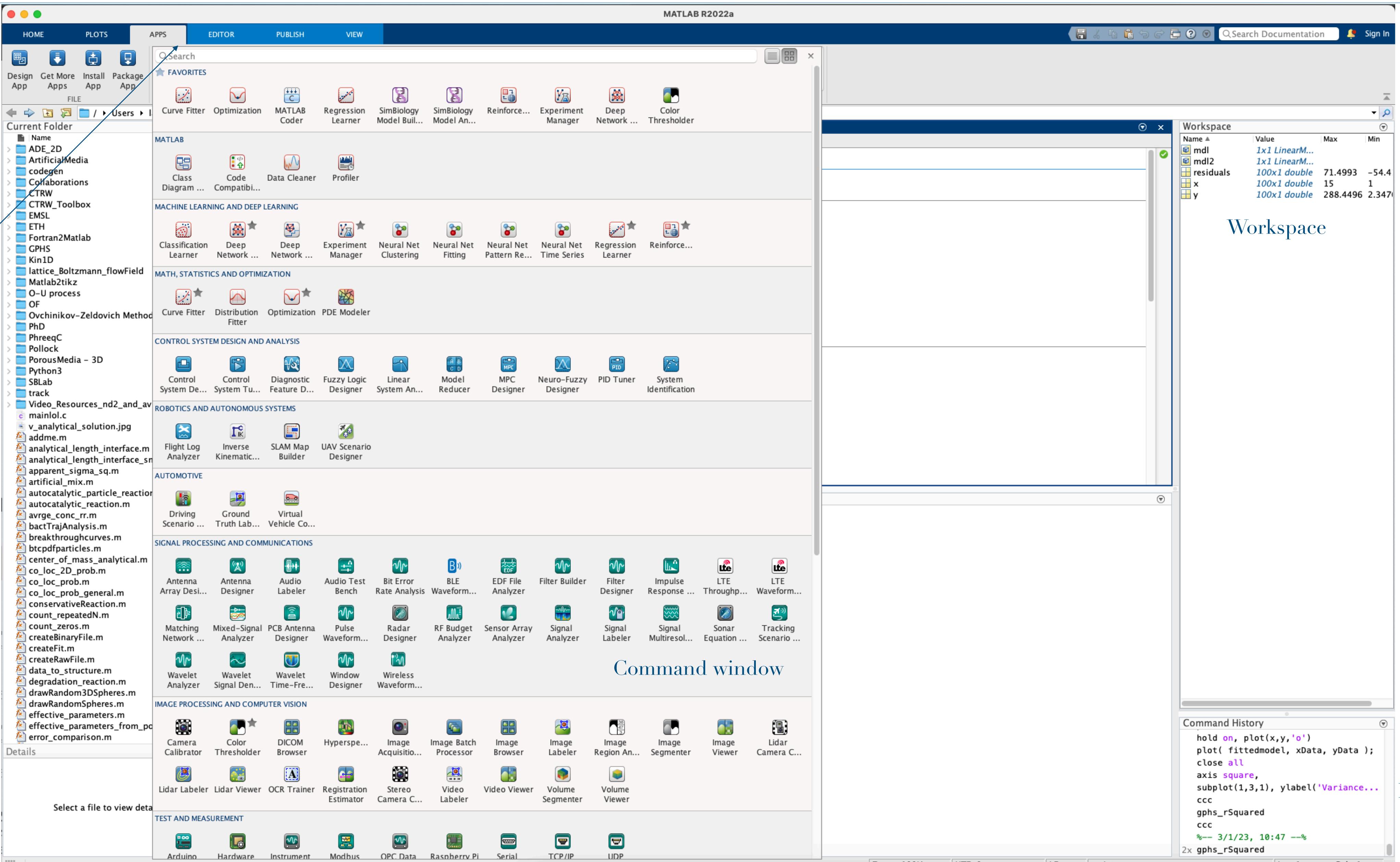
MATLAB: Desktop Environment

Toolboxes

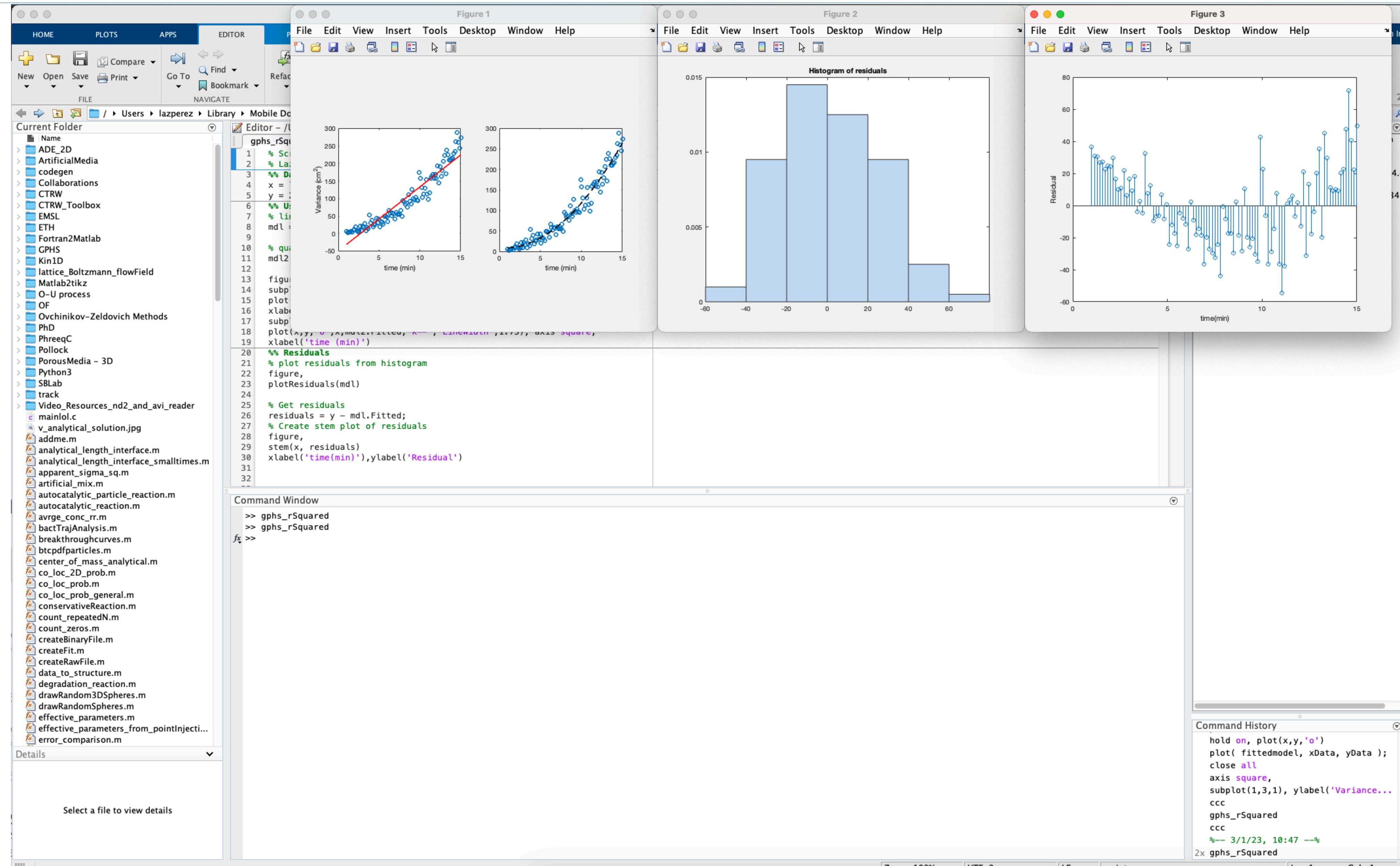


MATLAB: Desktop Environment

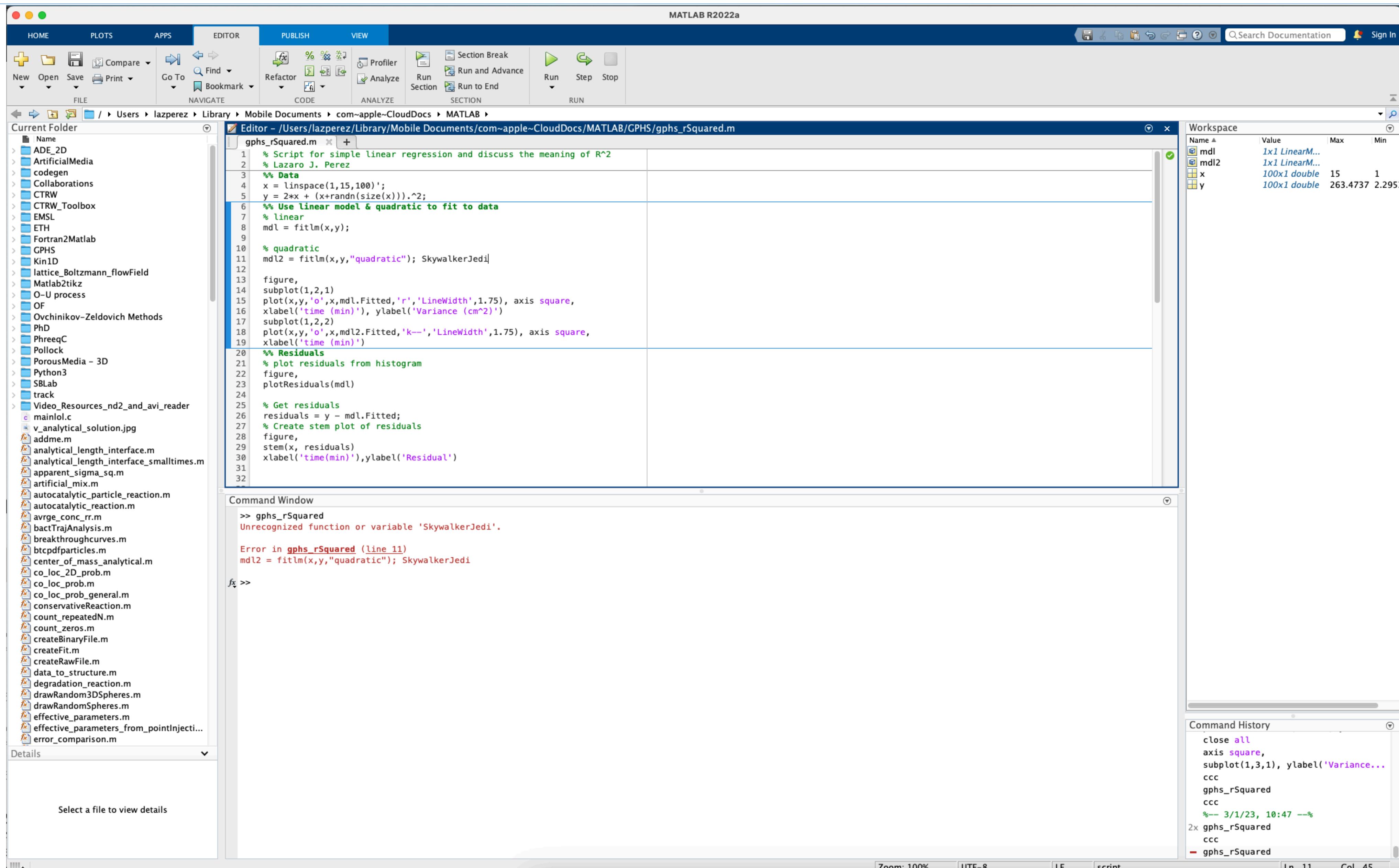
Toolboxes



MATLAB: Desktop Environment



MATLAB: Desktop Environment



Variables and assignments

Variable names are an example of identifier names

The name must begin with a letter of the alphabet

After that, the name can contain letters, digits, and the underscore character (e.g., value_1), but it cannot have a space

There is a limit to the length of the name; the built-in function namelengthmax tells what this maximum length is

MATLAB is case-sensitive

Putting a semicolon at the end of a statement suppresses the output

```
>> res = 9 - 2;  
>>
```

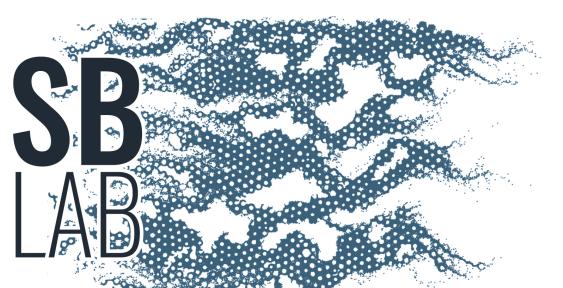
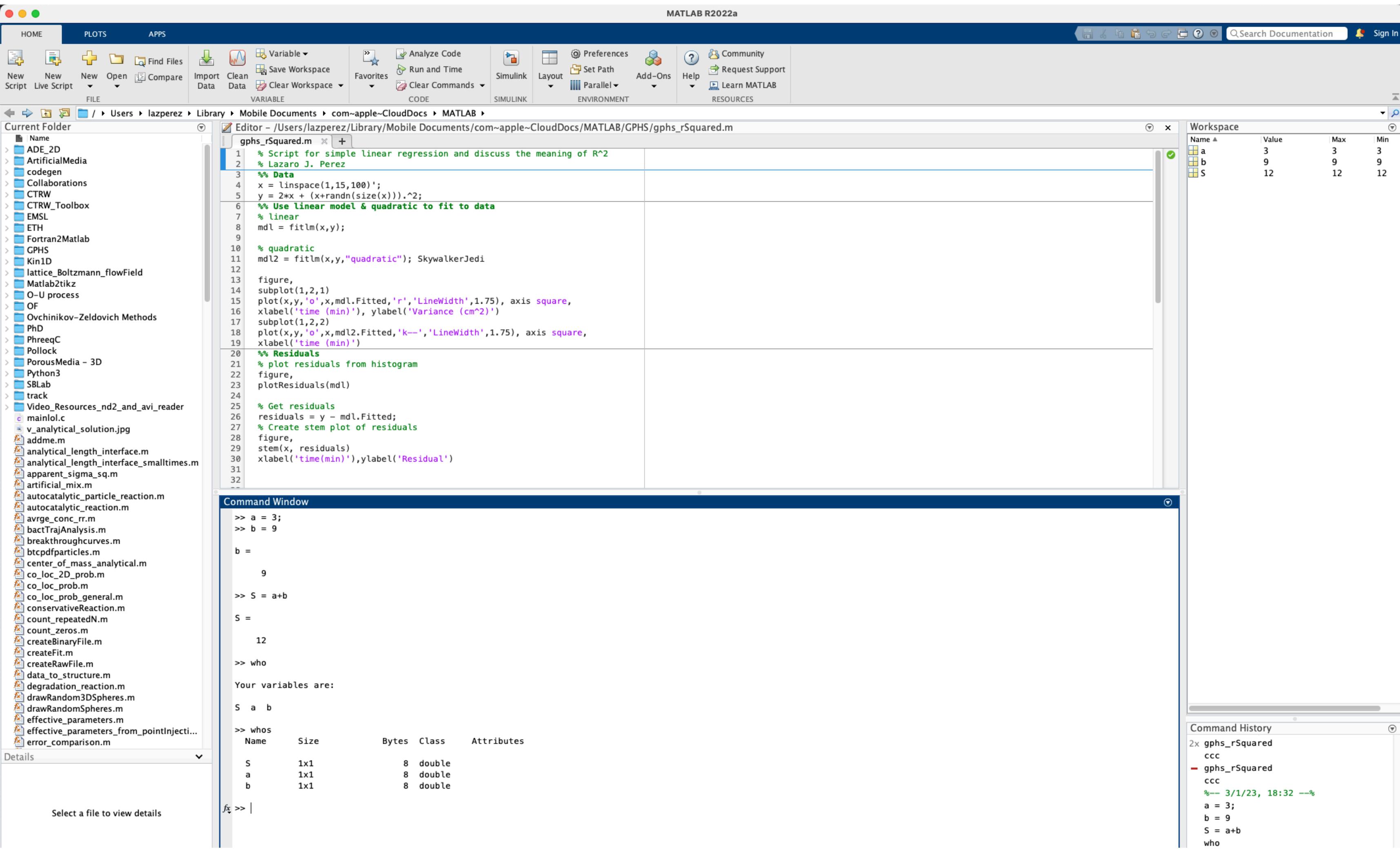
MATLAB uses a default variable named *ans* if an expression is typed at the prompt and it is not assigned to a variable

```
>> 6 + 3  
ans =  
9
```

```
>> result = 6 + 3  
result =  
9
```

Variables and assignments

The Workspace Window shows the variables that have been created in the current Command Window and their values



Variables and assignments

Operators

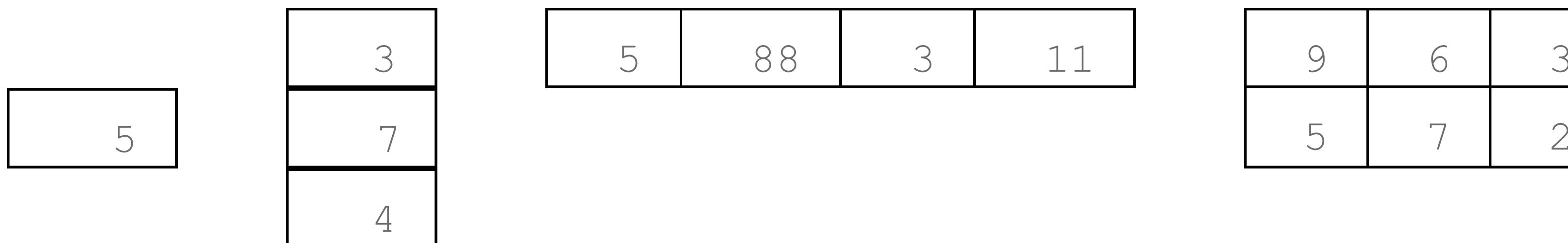
- + Addition
- Negation, subtraction
- * Multiplication
- / Division (divided by, e.g., $10/5$ is 2)
- \ Division (divided into, e.g., $10\backslash 5$ is 0.5)
- \wedge Exponentiation

Matrices

Vectors and matrices store sets of values, all of which are the same type

```
>> num = 6 + 3;  
>> numi = int32 (num) ;  
>> whos  
Name      Size      Bytes  Class       Attributes  
num       1 x 1        8  double  
numi      1 x 1        4  int32
```

A vector can be either a row vector or a column vector



Vectors and scalars are just special cases of matrices

Matrices

Vectors and matrices store sets of values, all of which are the same type

```
>> v = [1     2     3     4]  
v =  
    1     2     3     4
```

```
>> v = [1,2,3,4]  
v =  
    1     2     3     4
```

```
>> vec = 1:5  
vec =  
    1     2     3     4     5
```

Colon operator, linspace, and concatenating

```
>> nv = 1:2:9  
nv =  
    1     3     5     7     9
```

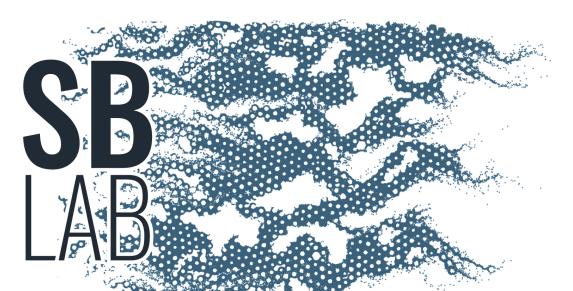
```
>> ls = linspace(3,15,5)  
ls =  
    3     6     9    12    15
```

```
>> newvec = [nv ls]  
newvec =  
    1     3     5     7     9     3     6     9    12    15
```

Indexing: starts at (1,1)

newvec

1	2	3	4	5	6	7	8	9	10
1	3	5	7	9	3	6	9	12	15



Matrices

Colon operator, linspace, and concatenating

```
>> nv = 1:2:9
```

nv =

1 3 5 7 9

```
>> ls = linspace(3,15,5)
```

ls =

3 6 9 12 15

```
>> newvec = [nv ls]
```

newvec =

1 3 5 7 9 3 6 9 12 15

Indexing: starts at (1,1)

newvec

1	2	3	4	5	6	7	8	9	10
1	3	5	7	9	3	6	9	12	15

Specific index

```
>> newvec(5)
```

ans =

9

Index sequence

```
>> b = newvec(4:6)
```

b =

7 9 3

Specific index vector

```
>> newvec([1 5 10])
```

ans =

1 9 15

Matrices

Column vectors

```
>> c = [1; 2; 3; 4]
```

```
c =
```

```
1  
2  
3  
4
```

One way to create a column vector is to explicitly put the values in square brackets, separated by semicolons (rather than commas or spaces)

Any row vector created using any method can be transposed to result in a column vector

```
>> r = 1:3;
```

```
>> c = r'
```

```
c =
```

```
1  
2  
3
```

For vectors, transposing a row vector results in a column vector, and transposing a column vector results in a row vector

A built-in operator, the apostrophe, in MATLAB will transpose

Matrices

Creating matrix variables

```
>> mat = [4 3 1; 2 5 6]
mat =
4     3     1
2     5     6
```

Creating a matrix variable is simply a generalization of creating row and column vector variables

That is, the values within a row are separated by either spaces or commas, and the different rows are separated by semicolons

There must always be the same number of values in each row.

If you attempt to create a matrix in which there are different numbers of values in the rows, the result will be an error message, such as in the following:

```
>> mat = [3 5 7; 1 2]
??? Error using ==> vertcat
CAT arguments dimensions are not consistent.
```

Matrix variables

```
>> rand(2)
ans =
0.2311    0.4860
0.6068    0.8913
```

```
>> rand(1,3)
ans =
0.7621    0.4565    0.0185
```

```
>> zeros(3)
ans =
0     0     0
0     0     0
0     0     0
```

```
>> ones(2,4)
ans =
1     1     1     1
1     1     1     1
```



Matrices

Referring to matrix elements

	Indexing	Subscript indexing	Row indexing	Column indexing																
<pre>>> mat = [2:4; 3:5]</pre> <pre>mat =</pre> <table><tr><td>2</td><td>3</td><td>4</td></tr><tr><td>3</td><td>4</td><td>5</td></tr></table>	2	3	4	3	4	5	<pre>>> mat(2,3)</pre> <pre>ans =</pre> <table><tr><td>5</td></tr></table>	5	<pre>>> mat(1:2,2:3)</pre> <pre>ans =</pre> <table><tr><td>3</td><td>4</td></tr><tr><td>4</td><td>5</td></tr></table>	3	4	4	5	<pre>>> mat(1,:)</pre> <pre>ans =</pre> <table><tr><td>2</td><td>3</td><td>4</td></tr></table>	2	3	4	<pre>>> mat(:,2)</pre> <pre>ans =</pre> <table><tr><td>3</td></tr><tr><td>4</td></tr></table>	3	4
2	3	4																		
3	4	5																		
5																				
3	4																			
4	5																			
2	3	4																		
3																				
4																				

Single index: If a single index is used with a matrix, MATLAB unwinds the matrix column by column

<pre>>> intmat = [100 77; 28 14]</pre> <pre>intmat =</pre> <table><tr><td>100</td><td>77</td></tr><tr><td>28</td><td>14</td></tr></table>	100	77	28	14	<pre>>> intmat(1)</pre> <pre>ans =</pre> <table><tr><td>100</td></tr></table>	100	<pre>>> intmat(2)</pre> <pre>ans =</pre> <table><tr><td>28</td></tr></table>	28	<pre>>> intmat(4)</pre> <pre>ans =</pre> <table><tr><td>14</td></tr></table>	14
100	77									
28	14									
100										
28										
14										

Matrices

Deleting elements in vectors

```
>> vec = 1:5  
vec =  
1 2 3 4 5
```

```
>> vec(3) = []  
vec =  
1 2 4 5
```

```
>> vec = 1:8  
vec =  
1 2 3 4 5 6 7 8
```

```
>> vec(2:4) = []  
vec =  
1 5 6 7 8
```

Deleting elements in matrices

```
>> mat = [7 9 8; 4 6 5]  
mat =  
7 9 8  
4 6 5
```

```
>> mat(1,2) = [];  
??? Indexed empty matrix assignment is not allowed.
```

```
>> mat(:,2) = []  
mat =  
7 8  
4 5
```

Matrices

Deleting elements in matrices

```
>> mat = [7 9 8; 4 6 5]  
mat =  
7 9 8  
4 6 5
```

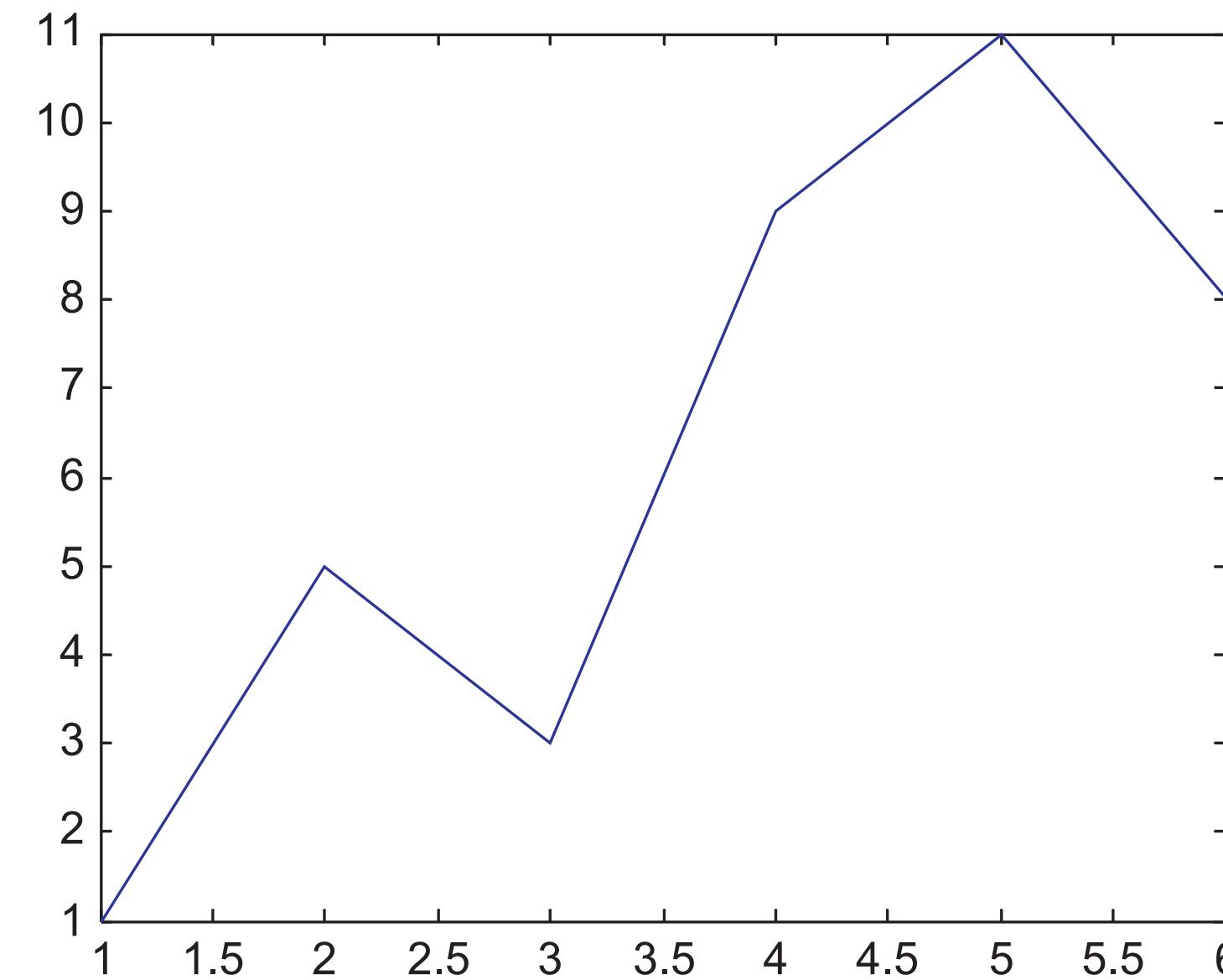
```
>> mat(1,2) = [];  
??? Indexed empty matrix assignment is not allowed.
```

```
>> mat = [7 9 8; 4 6 5]  
mat =  
7 9 8  
4 6 5
```

```
>> mat(3) = []  
mat =  
7 4 6 8 5
```

Plotting

```
>> x = 1:6;  
>> y = [1 5 3 9 11 8];  
>> plot(x,y)
```



Simple related plot functions

clf clears the Figure Window by removing everything from it.

figure creates a new, empty Figure Window when called without any arguments. Calling it as *figure(n)* where n is an integer is a way of creating and maintaining multiple Figure Windows, and of referring to each individually.

hold is a toggle that freezes the current graph in the Figure Window, so that new plots will be superimposed on the current one. Just *hold* by itself is a toggle, so calling this function once turns the *hold* on, and then the next time turns it off. Alternatively, the commands *hold on* and *hold off* can be used.

legend displays strings passed to it in a legend box in the Figure Window, in order of the plots in the Figure Window.

Tables

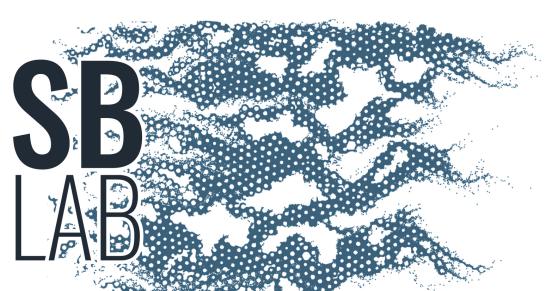
Tables are a data type suitable for column-oriented or tabular data that is often stored as columns in a text file or in a spreadsheet

Tables consist of rows and column-oriented variables

Each variable in a table can have a different data type and a different size, with the one restriction that each variable must have the same number of rows

Key Matlab functions to work with tables

Function	Description
<code>table</code>	Table array with named variables that can contain different types
<code>array2table</code>	Convert homogeneous array to table
<code>table2array</code>	Convert table to homogeneous array



Tables

The screenshot shows the MATLAB interface with the Classification Learner app open. The app window is titled "Classification Learner" and displays a "New Session from Workspace" dialog.

Data set section:

- Data Set Variable:** SW (87x10 table)
- Response:** gender (cell, 5 unique)
- Predictors:** A table listing variables: name, height, mass, hair_color, skin_color, eye_color. All variables are checked and selected as predictors.
- Add All** and **Remove All** buttons.
- [How to prepare data](#) link.

Validation section:

- Validation Scheme:** Cross-Validation (selected)
- Cross-validation folds:** 5
- [Read about validation](#) link.

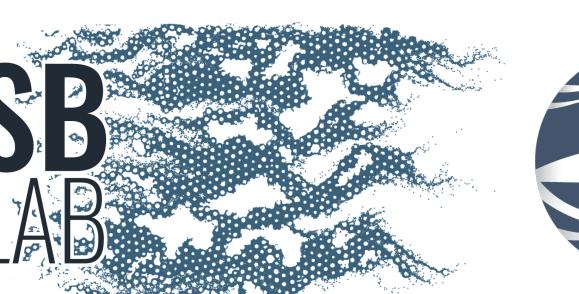
Test section:

- Set aside a test data set:** Unchecked checkbox.
- Percent set aside:** 0
- Description:** Use a test set to evaluate model performance after tuning and training models. To import a separate test set instead of partitioning the current data set, use the Test Data button after starting an app session.
- [Read about test data](#) link.

Buttons: Start Session and Cancel.

The workspace on the right side of the interface lists variables:

Name	Type	Max	Min
Age	[38;43;38;40;...]	49	38
BloodPress...	[124,93;109,...]	125	75
Height	[176;175;180...]	180	153
LastName	5x1 cell		
Smoker	5x1 logical		
SW	87x10 table		
T	5x6 table		
Weight	[71;79;80;52;...]	84	52



Tables

The screenshot shows the MATLAB IDE interface with the following components:

- Editor:** Displays the file `gphs_tableCreation.m` containing MATLAB code for creating a table from various data arrays.
- Command Window:** Shows the execution of the script and displays the resulting table `T` in the workspace.
- Workspace:** Lists all variables in the current workspace, including their names, data types, and dimensions.
- Command History:** Shows a history of commands entered in the MATLAB session.

Code in Editor:

```
% Let's create and store data in a table in Matlab
% Lazaro J. Perez
%% Table
% Data in matrix form
LastName = {'Calrissian';'Maul';'Solo';'Amidala';'Fett'};
Age = [38;43;38;40;49];
Smoker = logical([1;0;1;0;1]);
Weight = [71;79;80;52;84];
Height = [176;175;180;153;179];
BloodPressure = [124 93; 109 77; 125 83; 117 75; 122 80];
% Create table
T = table LastName, Age, Smoker, Height, Weight, BloodPressure;
```

Command Window Output:

```
>> gphs_tableCreation
T =
      LastName    Age    Smoker    Height    Weight    BloodPressure
      _____    ____    ____    _____    ____    _____
{'Calrissian'}    38    true    176     71    124     93
{'Maul'}        43   false    175     79    109     77
{'Solo'}         38    true    180     80    125     83
{'Amidala'}      40   false    153     52    117     75
{'Fett'}         49    true    179     84    122     80

>> A = table2array(T(:,2:4))
A =
    38    1    176
    43    0    175
    38    1    180
    40    0    153
    49    1    179
```

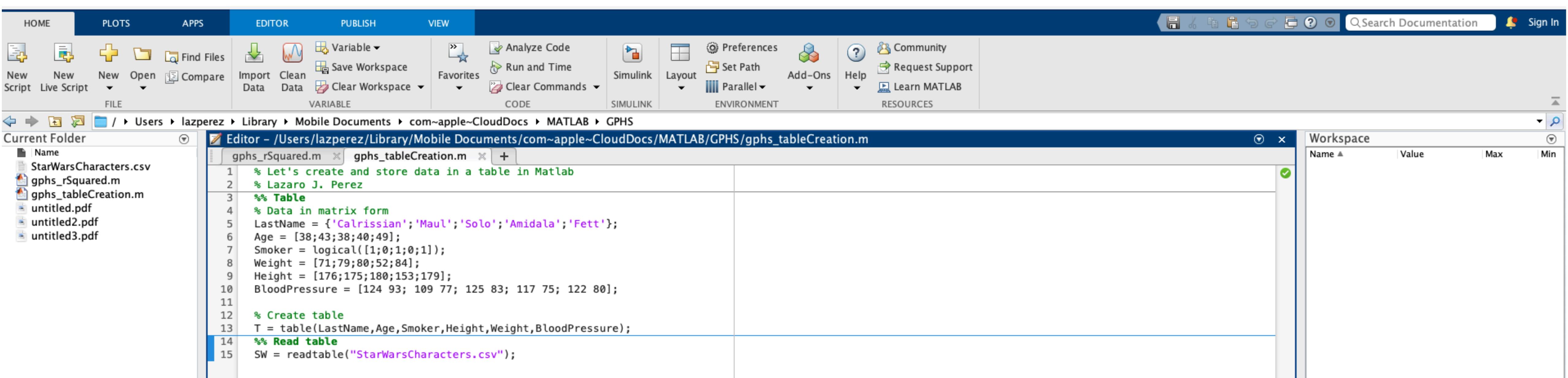
Workspace Variables:

Name	Type	Value	Max	Min
A	5x3 double	180	0	
Age	[38;43;38;40;...]	49	38	
BloodPressure	[124,93;109,...]	125	75	
Height	[176;175;180...]	180	153	
LastName	5x1 cell			
Smoker	5x1 logical			
T	5x6 table			
Weight	[71;79;80;52;...]	84	52	

Command History:

```
S = a+b
who
whos
clear a
clear
```

Tables



Machine learning

Coding:

The screenshot shows the MATLAB IDE interface with the following components:

- Toolbar:** HOME, PLOTS, APPS, EDITOR, PUBLISH, VIEW.
- File Explorer (Current Folder):** Shows files: StarWarsCharacters.csv, train_SW_Classifier.m, gphs_rSquared.m, gphs_tableCreation.m.
- Editor:** Displays the code for `train_SW_Classifier.m`. The code uses the Classification Learner R2022a API to train a classification tree on Star Wars character data. It includes sections for extracting predictors and response, training a classifier, creating a result struct with a predict function, and performing cross-validation.
- Workspace:** Shows a variable `SW` as an `87x10 table`.
- Command History:** Shows the command `gphs_tableCreation` run on 3/6/23 at 16:52.
- Details:** A dropdown menu indicating "Select a file to view details".
- Page Footer:** Zoom: 100%, UTF-8, LF, trainClassifier, Ln 49, Col 34.

```
% Extract predictors and response
% This code processes the data into the right shape for training the
% model.
inputTable = trainingData;
predictorNames = {'height', 'mass', 'skin_color', 'eye_color', 'birth_year', 'gender', 'homeworld', 'species'};
predictors = inputTable(:, predictorNames);
response = inputTable.hair_color;
isCategoricalPredictor = [false, false, true, true, true, true, true, true];
% Train a classifier
% This code specifies all the classifier options and trains the classifier.
classificationTree = fitctree(... predictors, ...
    response, ...
    'SplitCriterion', 'gdi', ...
    'MaxNumSplits', 100, ...
    'Surrogate', 'off', ...
    'ClassNames', {'NA'; 'auburn'; 'auburn, grey'; 'auburn, white'; 'black'; 'blond'; 'blonde'; 'brown'; 'brown, grey'; 'grey'; 'none'; 'white'});
% Create the result struct with predict function
predictorExtractionFcn = @(t) t(:, predictorNames);
treePredictFcn = @(x) predict(classificationTree, x);
trainedClassifier.predictFcn = @(x) treePredictFcn(predictorExtractionFcn(x));
% Add additional fields to the result struct
trainedClassifier.RequiredVariables = {'birth_year', 'eye_color', 'gender', 'height', 'homeworld', 'mass', 'skin_color', 'species'};
trainedClassifier.ClassificationTree = classificationTree;
trainedClassifier.About = 'This struct is a trained model exported from Classification Learner R2022a.';
trainedClassifier.HowToPredict = sprintf('To make predictions on a new table, T, use: \n yfit = c.predictFcn(T) \nreplacing ''c'' with the name of the variable');
% Extract predictors and response
% This code processes the data into the right shape for training the
% model.
inputTable = trainingData;
predictorNames = {'height', 'mass', 'skin_color', 'eye_color', 'birth_year', 'gender', 'homeworld', 'species'};
predictors = inputTable(:, predictorNames);
response = inputTable.hair_color;
isCategoricalPredictor = [false, false, true, true, true, true, true, true];
% Perform cross-validation
partitionedModel = crossval(trainedClassifier.ClassificationTree, 'KFold', 5);
% Compute validation predictions
[validationPredictions, validationScores] = kfoldPredict(partitionedModel);
% Compute validation accuracy
validationAccuracy = 1 - kfoldLoss(partitionedModel, 'LossFun', 'ClassifError');
```

Machine learning

Toolbox:

