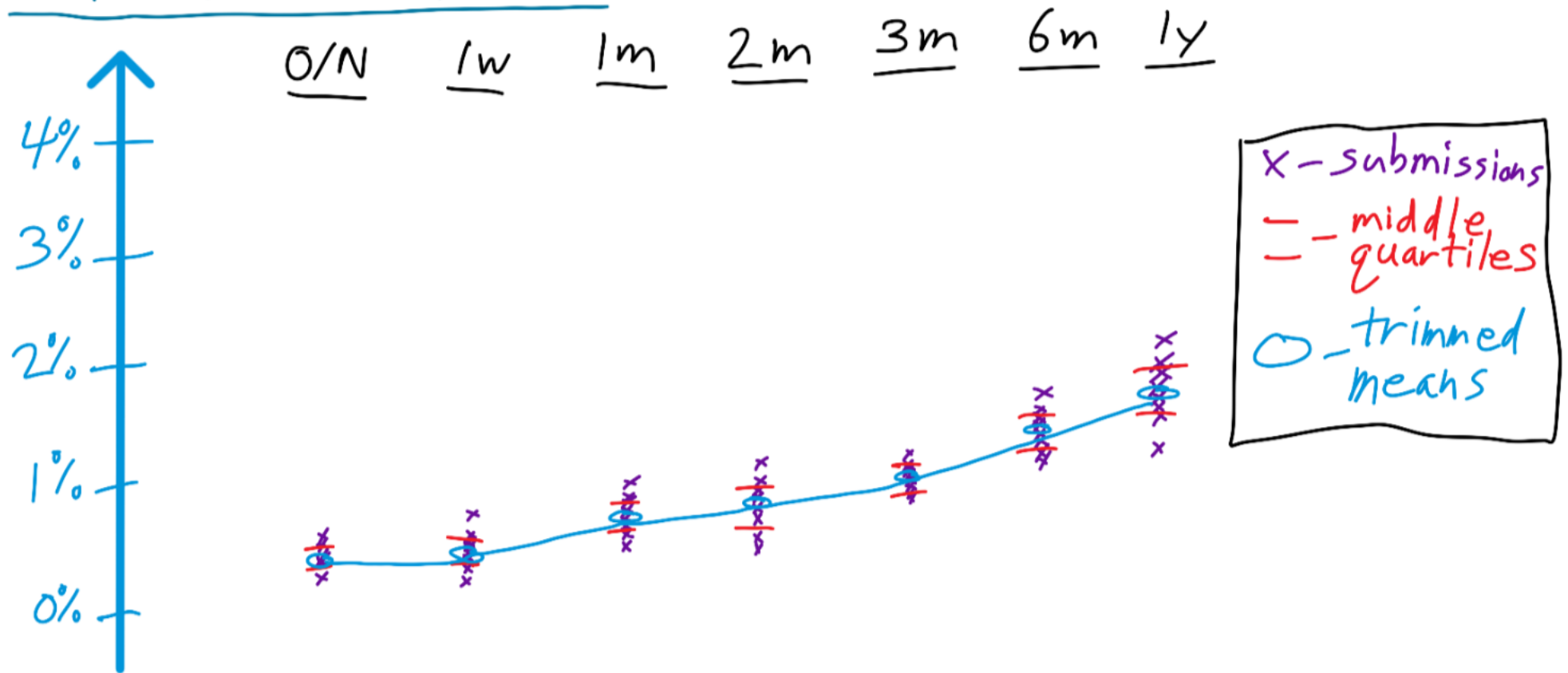


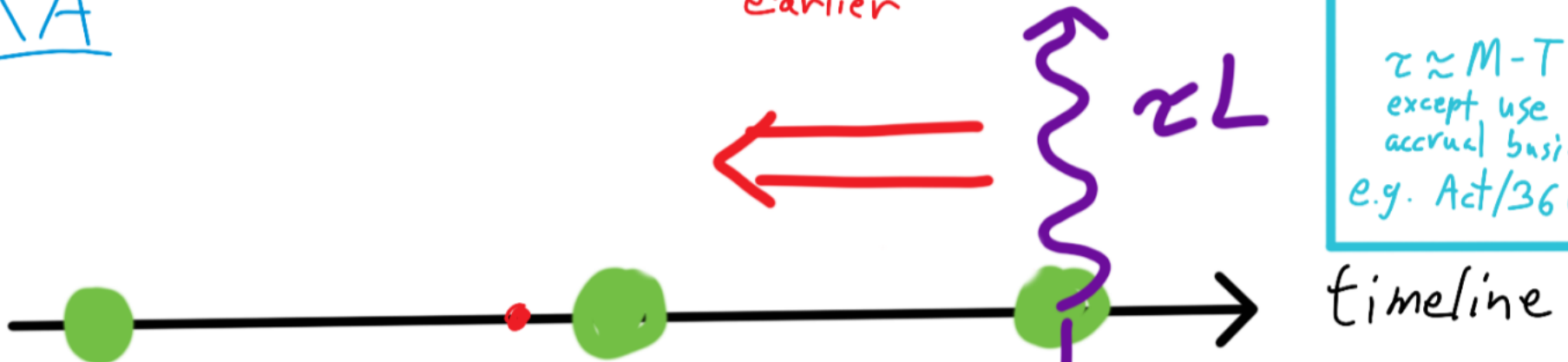
LIBOR Calculation



FRA

move payment exchange
earlier

$\tau \approx M - T$
except use
accrual basis
e.g. Act/360



$T-2$:
published

T - settlement
date

M - term
maturity

t - trade
date
negotiate strike
 $K = 5.5\%$

exchange payment
 $\tau(L - K)$

FRA

$\tau \approx M - T$
except use
accrual basis
e.g. Act/360



$T-2$:
published

t - trade
date

negotiate strike

$$K = 5.5\%$$

T - settlement
date

$$\frac{\tau(L - K)}{1 + \tau L}$$

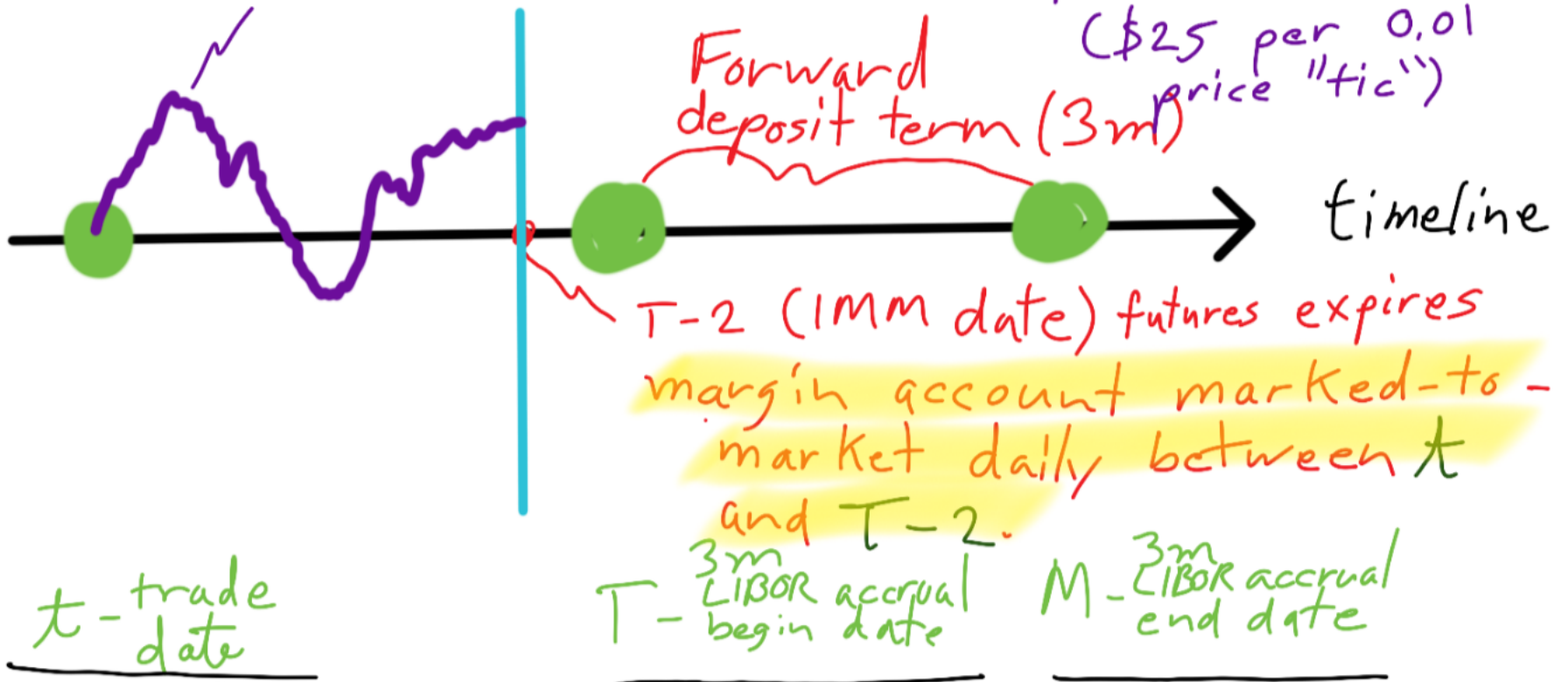
M - term
maturity

} prompt
payment
amount

(FRA
convention)

Eurodollar Futures

cumulative mark-to-market from futures price movement (\$25 per 0.01 price "tic")

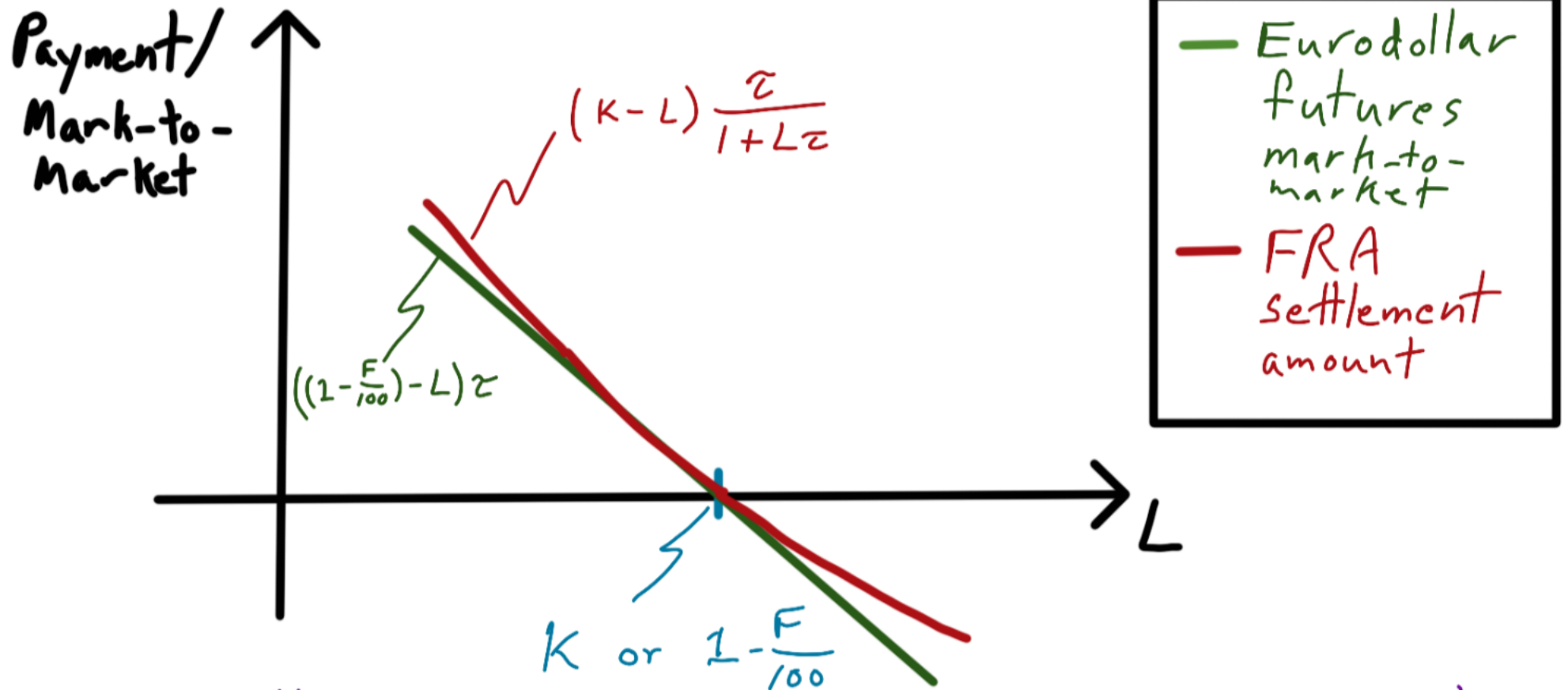


t - trade date

go long future contract at 93.50

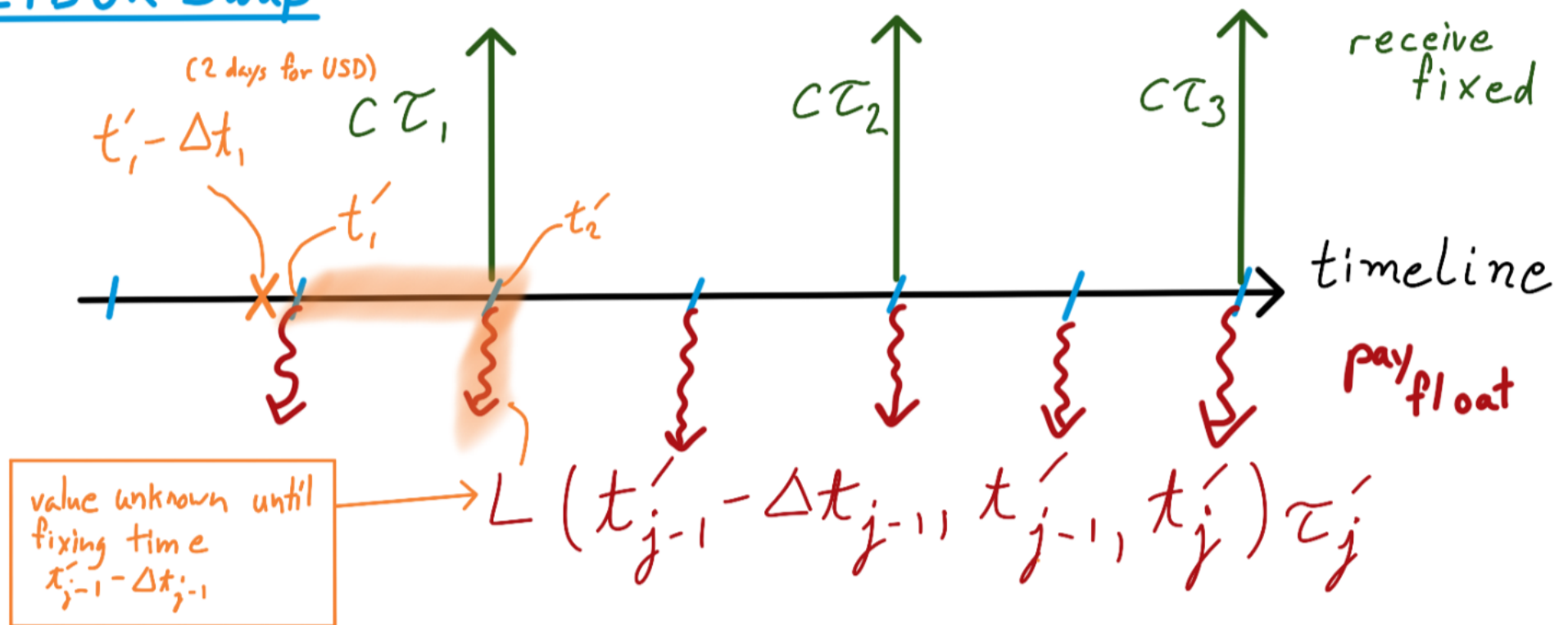
T-2 final futures price settlement is $100 \times (1 - L)$
where L is in percentage terms, e.g., 0.06.

Eurodollar Futures Convexity



Eurodollar futures has negative convexity versus an FRA.

LIBOR Swap



$$t'_0 = t_0 \leq t'_1 \leq t'_2 = t_1 \leq t'_3 \leq t'_4 = t_2 \leq \dots$$

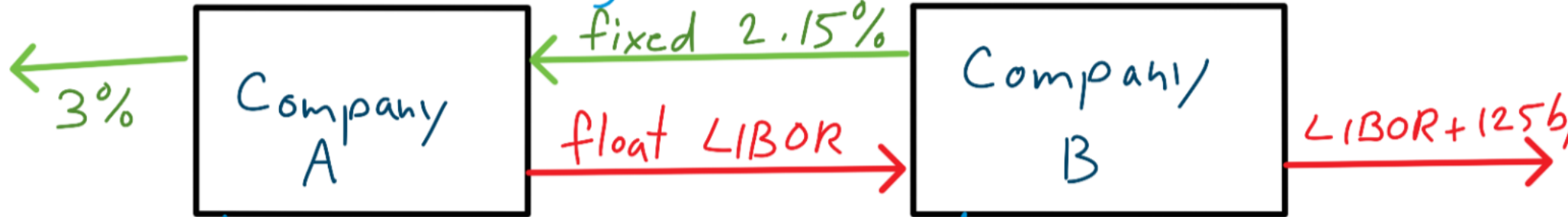
$$\tau'_j \approx t'_j - t'_{j-1} \quad \tau_i \approx t_i - t_{i-1}$$

Swap → Relative Funding Advantage

A issues
fixed

enter swap
agreement

B issues
float



nets $\text{LIBOR} + 85 \text{ bp}$

can issue fixed
note at 3%

can issue float
at $\text{LIBOR} + 100 \text{ bp}$

prefers to issue float

nets 3.40%

can issue fixed
at 3.50%

can issue float
at $\text{LIBOR} + 125 \text{ bp}$

prefers fixed

Swap Floating Payment Replication (Arbitrage-Free Pricing)

	(today) t	(LIBOR fixing) T_F	T_B	(LIBOR accrual period) T_E	Strategy timeline
			2d	e.g. 3m	
actions	<ul style="list-style-type: none"> ▷ buy T_B-maturity bond ▷ sell T_E-maturity bond ▷ agree to pay $L(T_F, T_B, T_E)$ at time T_E 	<ul style="list-style-type: none"> ▷ arrange Eurodollar deposit beginning on T_B and maturing on T_E 			
net payments	$-P(t, T_B)$ $+P(t, T_E)$ $+ \tau L(t, T_B, T_E) P(t, T_E)$	= ?	$+1$ -1	= 0	$= 0$ $-1 - \tau L(T_F, T_B, T_E)$ $+(1 + \tau L(T_F, T_B, T_E))$

Either

$$P(t, T_E) - P(t, T_B) + \tau L(t, T_B, T_E) P(t, T_E) = 0$$

or this strategy supplies an arbitrage.

Hence in the absence of arbitrage,

$$L(t, T_B, T_E) = \frac{P(t, T_B) / P(t, T_E) - 1}{\tau}$$