

ORNSTEIN-UHLENBECK DYNAMICS IN TRANSFORMERS

STOCHASTIC EQUATION:

$$dq = \theta(\mu - q)dt + \sigma dW$$

↑
Restoring Force

FITTED PARAMETERS:

- Mean-reversion rate: $\theta = 0.083$
- Saturation variance: $\sigma^2_\infty = 0.078$
- Relaxation time: $\tau = 6$ tokens

KEY FINDINGS:

VARIANCE GROWTH

$H = 0.04$
(vs 0.5 theory)

12x SLOWER

ALIGNMENT DECAY

$\beta = 0.17$
(vs 0.5 theory)

3x SLOWER

MEMORY RETRIEVAL

Rate = 100%
(no degradation)

PRESERVED

IMPLICATIONS:

- Transformer attention is MORE STABLE than Brownian theory predicts
- "Lost in the Middle" effect is WEAK or ABSENT
- Attention mechanisms act as implicit RESTORING FORCES
- Context can be longer before significant degradation