

## ORNSTEIN-UHLENBECK DYNAMICS IN TRANSFORMERS

STOCHASTIC EQUATION:  $dq = \theta(\mu - q)dt + \sigma dW$

↑  
Restoring Force

### FITTED PARAMETERS:

- Mean-reversion rate:  $\theta = 0.083$
- Saturation variance:  $\sigma^2_{\infty} = 0.078$
- Relaxation time:  $\tau = 6$  tokens

### KEY FINDINGS:

#### VARIANCE GROWTH

$H = 0.04$   
(vs 0.5 theory)

12× SLOWER

#### ALIGNMENT DECAY

$\beta = 0.17$   
(vs 0.5 theory)

3× SLOWER

#### MEMORY RETRIEVAL

Rate = 100%  
(no degradation)

PRESERVED

### IMPLICATIONS:

- Transformer attention is MORE STABLE than Brownian theory predicts
- "Lost in the Middle" effect is WEAK or ABSENT
- Attention mechanisms act as implicit RESTORING FORCES
- Context can be longer before significant degradation