




# AI in Biomedical Data

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# یادگیری ماشین در زیست پزشکی

## Chapter 6. Decision Trees

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- ❑ Like SVMs, **Decision Trees** are versatile Machine Learning algorithms that can perform both classification and regression tasks, and even **multioutput tasks**.
- ❑ They are powerful algorithms, capable of fitting complex datasets. **For example, in Chapter 2 you trained a *DecisionTreeRegressor* model on the California housing dataset, fitting it perfectly (actually, overfitting it).**
- ❑ Decision Trees are also the fundamental components of *Random Forests*, which are among the most powerful Machine Learning algorithms available today.
- ❑ In this chapter we will start by discussing **how to train**, **visualize**, and **make predictions** with Decision Trees.
- ❑ Then we will go through the **CART training algorithm used by Scikit-Learn**, and we will discuss **how to regularize trees and use them for regression tasks**. Finally, we will discuss some of the limitations of Decision Trees.

# Model Interpretation: White Box Versus Black Box

- **Decision Trees** are intuitive, and their decisions are easy to interpret. Such models are often called *white box models*.
- In contrast, as we will see, **Random Forests or neural networks** are generally considered *black box models*. They make great predictions, and you can easily check the calculations that they performed to make these predictions; nevertheless, **it is usually hard to explain in simple terms why the predictions were made**.
- For example, if a neural network says that a particular person appears on a picture, it is hard to know what contributed to this prediction: did the model recognize that person's eyes? Their mouth? Their nose? Their shoes? Or even the couch that they were sitting on?
- Conversely, **Decision Trees** provide nice, simple classification rules that can even be applied manually if need be (e.g., for flower classification).

# Training and Visualizing a Decision Tree

To understand Decision Trees, let's build one and take a look at how it makes predictions. The following code trains a *DecisionTreeClassifier* on the iris dataset

```
from sklearn.datasets import load_iris
from sklearn.tree import DecisionTreeClassifier

iris = load_iris()
X = iris.data[:, 2:] # petal length and width
y = iris.target

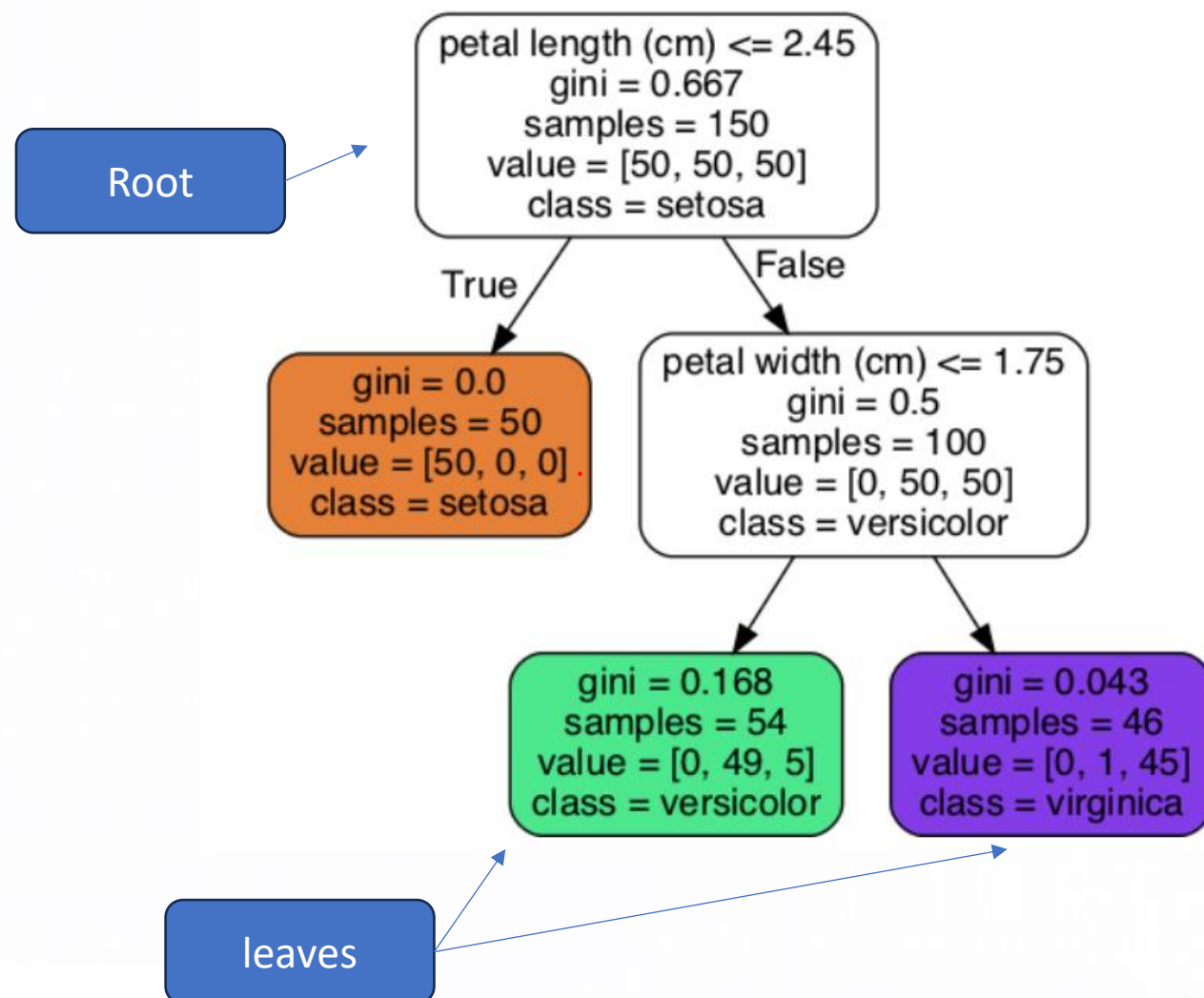
tree_clf = DecisionTreeClassifier(max_depth=2)
tree_clf.fit(X, y)
```

# Training and Visualizing a Decision Tree

You can visualize the trained Decision Tree by first using the `export_graphviz()` method to output a graph definition file called `iris_tree.dot`

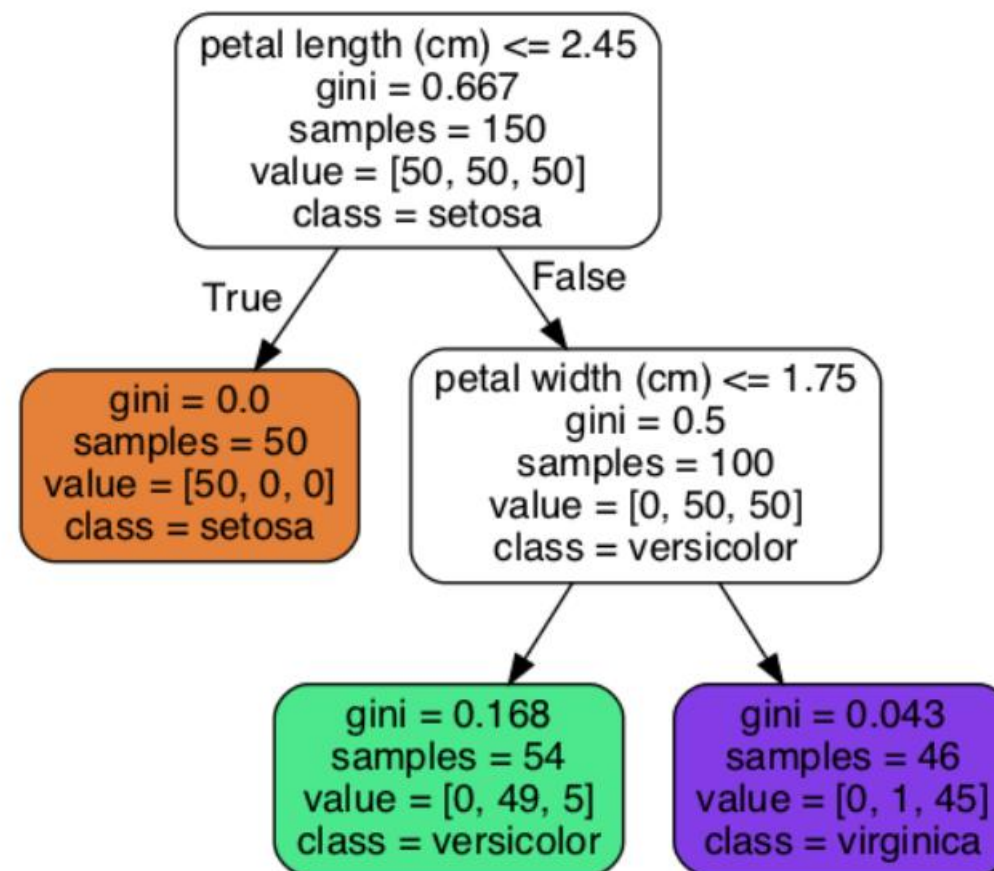
```
from sklearn.tree import export_graphviz

export_graphviz(
    tree_clf,
    out_file=image_path("iris_tree.dot"),
    feature_names=iris.feature_names[2:],
    class_names=iris.target_names,
    rounded=True,
    filled=True
)
```





- ❖ A node's **samples** attribute counts how many training instances it applies to.
- ❖ For example, 100 training instances have a petal length greater than 2.45 cm (depth 1, right), and of those 100, 54 have a petal width smaller than 1.75 cm (depth 2, left).
- ❖ A node's **value** attribute tells you how many training instances of each class this node applies to: for example, the bottom-right node applies to 0 *Iris setosa*, 1 *Iris versicolor*, and 45 *Iris virginica*.
- ❖ Finally, a node's **gini** attribute measures its **impurity**: a node is “pure” (gini=0) if all training instances it applies to belong to the same class.
- ❖ For example, since the *depth-1* left node applies only to *Iris setosa* training instances, it is pure and its gini score is 0. Equation 6-1 shows how the training algorithm computes the gini score  $G_i$  of the  $i^{\text{th}}$  node. The depth-2 left node has a gini score equal to  $1 - (0/54)^2 - (49/54)^2 - (5/54)^2 \approx 0.168$ .



### Equation 6-1. Gini impurity

$$G_i = 1 - \sum_{k=1}^n p_{i,k}^2$$

In this equation:

- $p_{i,k}$  is the ratio of class  $k$  instances among the training instances in the  $i^{\text{th}}$  node.



Scikit-Learn uses the CART algorithm, which produces only *binary trees*: nonleaf nodes always have two children (i.e., questions only have yes/no answers). However, other algorithms such as ID3 can produce Decision Trees with nodes that have more than two children.

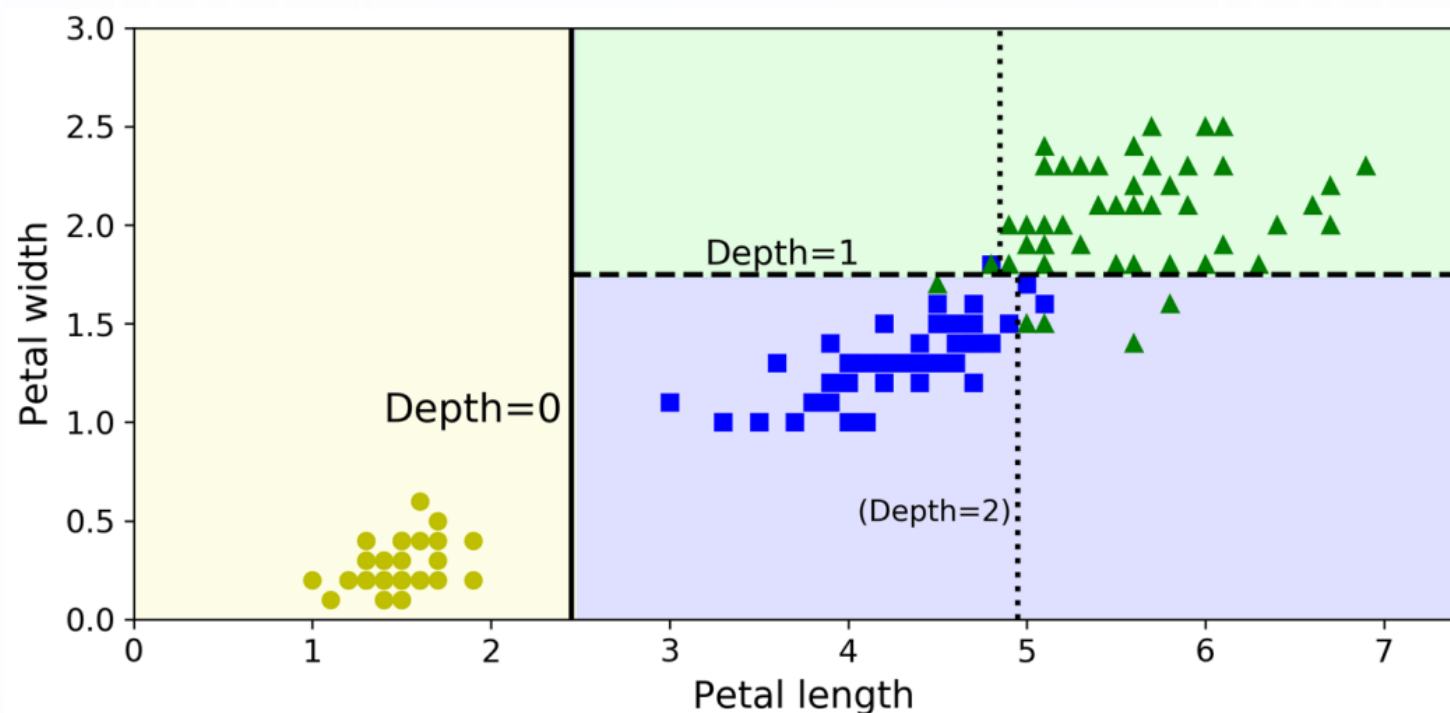


Figure 6-2 shows this Decision Tree's decision boundaries. The thick vertical line represents the decision boundary of the root node (depth 0): petal length = 2.45 cm.

Since the lefthand area is pure (only *Iris setosa*), it cannot be split any further. However, the righthand area is impure, so the depth-1 right node splits it at petal width = 1.75 cm (represented by the dashed line).

Since `max_depth` was set to 2, the Decision Tree stops right there.

If you set `max_depth` to 3, then the two depth-2 nodes would each add another decision boundary (represented by the dotted lines).



# Estimating Class Probabilities

- A Decision Tree can also estimate the probability that an instance belongs to a particular class  $k$ .
- First it traverses the tree to find the leaf node for this instance, and then it returns the ratio of training instances of class  $k$  in this node.
- For example, suppose you have found a flower whose petals are 5 cm long and 1.5 cm wide. The corresponding leaf node is the depth-2 left node, so the Decision Tree should output the following probabilities: 0% for *Iris setosa* (0/54), 90.7% for *Iris versicolor* (49/54), and 9.3% for *Iris virginica* (5/54).
- If you ask it to predict the class, it should output *Iris versicolor* (class 1) because it has the highest probability. Let's check this:

```
>>> tree_clf.predict_proba([[5, 1.5]])  
array([[0.          , 0.90740741, 0.09259259]])  
>>> tree_clf.predict([[5, 1.5]])  
array([1])
```

# The CART Training Algorithm

- Scikit-Learn uses the *Classification and Regression Tree (CART) algorithm* to train Decision Trees (also called “growing” trees).
- The algorithm works by first splitting the training set into two subsets using a single feature  $k$  and a threshold  $t_k$  (e.g., “petal length  $\leq 2.45$  cm”).
- How does it choose  $k$  and  $t_k$ ? It searches for the pair  $(k, t_k)$  that produces the purest subsets (weighted by their size). Equation 6-2 gives the cost function that the algorithm tries to minimize.

*Equation 6-2. CART cost function for classification*

$$J(k, t_k) = \frac{m_{\text{left}}}{m} G_{\text{left}} + \frac{m_{\text{right}}}{m} G_{\text{right}}$$

where  $\begin{cases} G_{\text{left/right}} & \text{measures the impurity of the left/right subset,} \\ m_{\text{left/right}} & \text{is the number of instances in the left/right subset.} \end{cases}$

- Once the CART algorithm has successfully split the training set in two, it splits the subsets using the same logic, then the sub-subsets, and so on, recursively.
- It stops recursing once it reaches the maximum depth (defined by the `max_depth` hyperparameter), or if it cannot find a split that will reduce impurity.
- A few other hyperparameters (described in a moment) control additional stopping conditions (`min_samples_split`, `min_samples_leaf`, `min_weight_fraction_leaf`, and `max_leaf_nodes`).

- As you can see, the CART algorithm is a *greedy algorithm*:
- It greedily searches for an optimum split at the top level, then repeats the process at each subsequent level.
- It does not check whether or not the split will lead to the lowest possible impurity several levels down.
- A greedy algorithm often produces a solution that's reasonably good but not guaranteed to be optimal.
- This is why we must settle for a “reasonably good” solution.

# Gini Impurity or Entropy?

- By default, the Gini impurity measure is used, but you can select the *entropy* impurity measure instead by setting the criterion hyperparameter to "entropy".
- The concept of entropy originated in thermodynamics as a measure of molecular disorder: entropy approaches zero when molecules are still and well ordered.
- Entropy later spread to a wide variety of domains, including Shannon's *information theory*, where it measures the average information content of a message: entropy is zero when all messages are identical.
- In Machine Learning, entropy is frequently used as an impurity measure: a set's entropy is zero when it contains instances of only one class.
- Equation 6-3 shows the definition of the entropy of the  $i^{\text{th}}$  node. For example, the depth-2 left node in Figure 6-1 has an entropy equal to  $-(49/54) \log_2(49/54) - (5/54) \log_2(5/54) \approx 0.445$ .

Equation 6-3. Entropy

$$H_i = - \sum_{\substack{k=1 \\ p_{i,k} \neq 0}}^n p_{i,k} \log_2(p_{i,k})$$



- ❑ So, should you use Gini impurity or entropy?
- ❑ The truth is, most of the time it does not make a big difference: they lead to similar trees.
- ❑ Gini impurity is slightly faster to compute, so it is a good default.
- ❑ However, when they differ, Gini impurity tends to isolate the most frequent class in its own branch of the tree, while entropy tends to produce slightly more balanced trees

# Regularization Hyperparameters

- ❖ Decision Trees make very few assumptions about the training data (as opposed to linear models, which assume that the data is linear, for example).
- ❖ The tree structure will adapt itself to the training data, fitting it very closely—indeed, most likely overfitting it.
- ❖ Such a model is often called a *nonparametric model*, not because it does not have any parameters (it often has a lot) but because the number of parameters is not determined prior to training, so the model structure is free to stick closely to the data.
- ❖ In contrast, a *parametric model*, such as a linear model, has a predetermined number of parameters, so its degree of freedom is limited, reducing the risk of overfitting (but increasing the risk of underfitting).

- To avoid overfitting the training data, you need to restrict the Decision Tree's freedom during training. As you know by now, this is called regularization.
- The regularization hyperparameters depend on the algorithm used, but generally you can at least restrict the maximum depth of the Decision Tree.
- In Scikit-Learn, this is controlled by the `max_depth` hyperparameter (the default value is `None`, which means unlimited). Reducing `max_depth` will regularize the model and thus reduce the risk of overfitting.

The `DecisionTreeClassifier` class has a few other parameters that similarly restrict the shape of the Decision Tree:

<code>min_samples_split</code>	the minimum number of samples a leaf node must have
<code>min_weight_fraction_leaf</code>	same as <code>min_samples_leaf</code> but expressed as a fraction of the total number of weighted instances
<code>max_leaf_nodes</code>	the maximum number of leaf nodes
<code>max_features</code>	the maximum number of features that are evaluated for splitting at each node
<code>min_samples_leaf</code>	the minimum number of samples required to be at a leaf node

Figure 6-3 shows two Decision Trees trained on the moons dataset (introduced in Chapter 5). On the left the Decision Tree is trained with the default hyperparameters (i.e., no restrictions), and on the right it's trained with `min_samples_leaf=4`. It is quite obvious that the model on the left is overfitting, and the model on the right will probably generalize better.

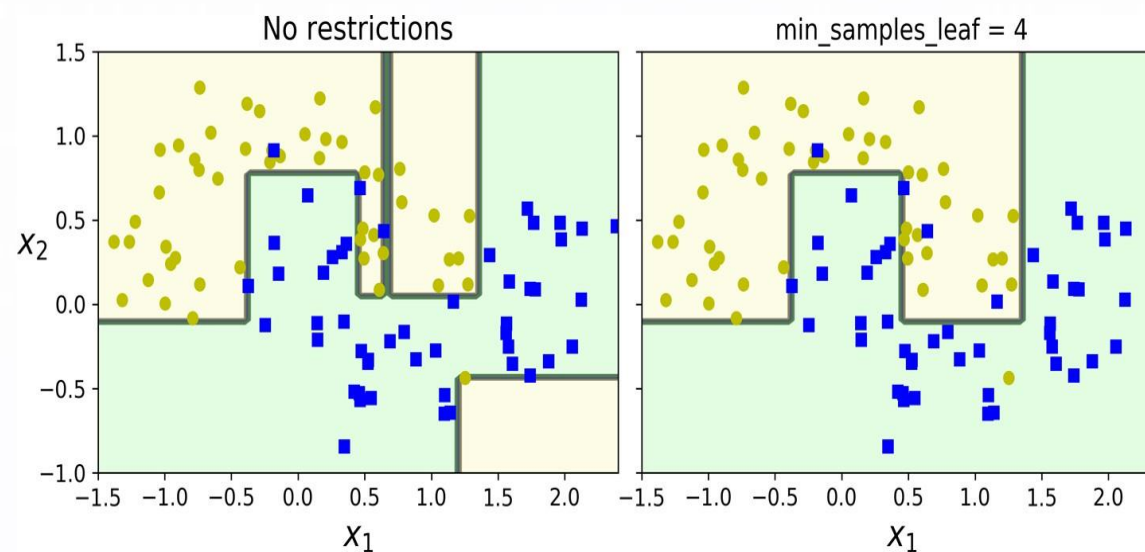


Figure 6-3. Regularization using `min_samples_leaf`

# DT for Regression

Decision Trees are also capable of performing regression tasks. Let's build a regression tree using Scikit-Learn's `DecisionTreeRegressor` class, training it on a noisy quadratic dataset with `max_depth=2`:

```
from sklearn.tree import DecisionTreeRegressor

tree_reg = DecisionTreeRegressor(max_depth=2)
tree_reg.fit(X, y)
```

The resulting tree is represented in Figure 6-4.

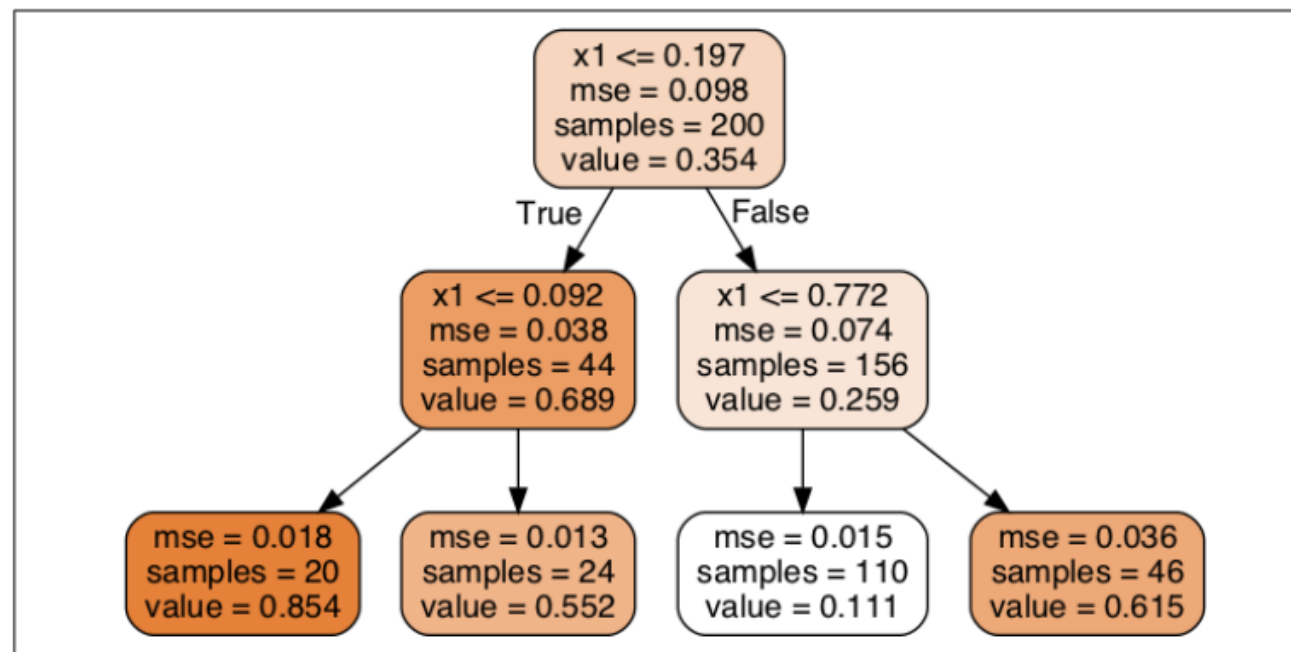


Figure 6-4. A Decision Tree for regression



- This tree looks very similar to the classification tree you built earlier. The main difference is that **instead of predicting a class in each node, it predicts a value**.
- For example, suppose you want to make a prediction for a new instance with  $x_1 = 0.6$ . You traverse the tree starting at the root, and you eventually reach the leaf node that predicts  $\text{value}=0.111$ .
- This prediction is **the average target value of the 110 training instances associated with this leaf node**, and it results in a mean squared error equal to 0.015 over these 110 instances.
- This model's predictions are represented on the left in **Figure 6-5**. If you set  $\text{max\_depth}=3$ , you get the predictions represented on the right.
- **Notice how the predicted value for each region is always the average target value of the instances in that region**. The algorithm splits each region in a way that makes most training instances as close as possible to that predicted value.

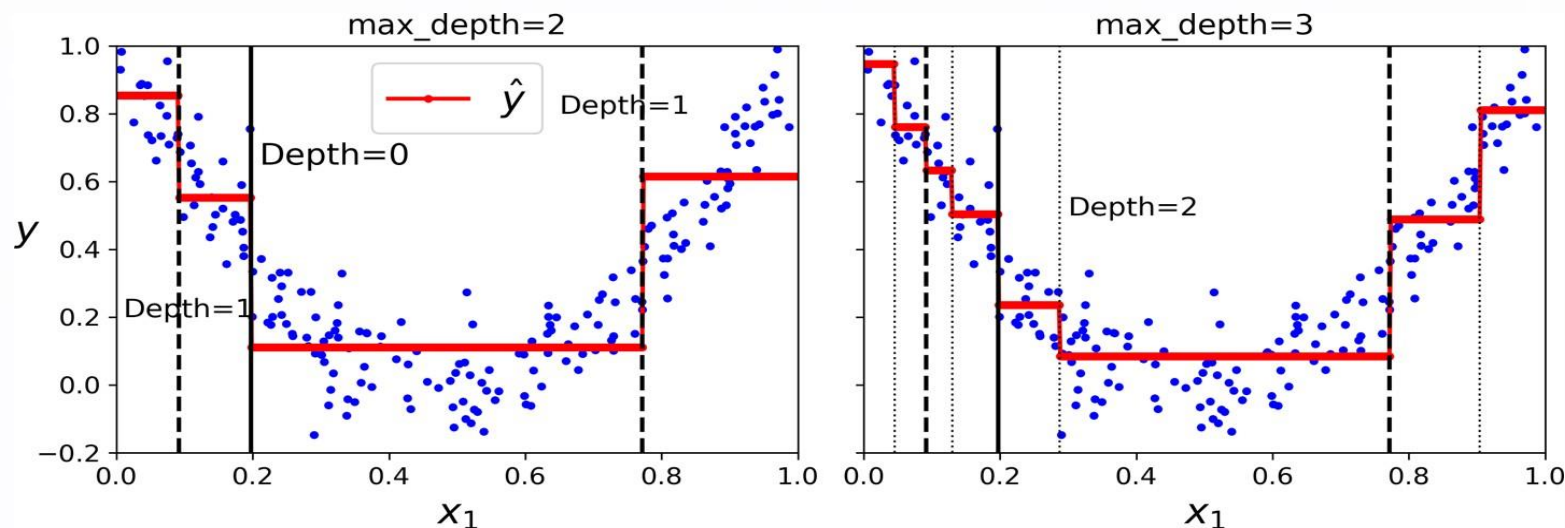


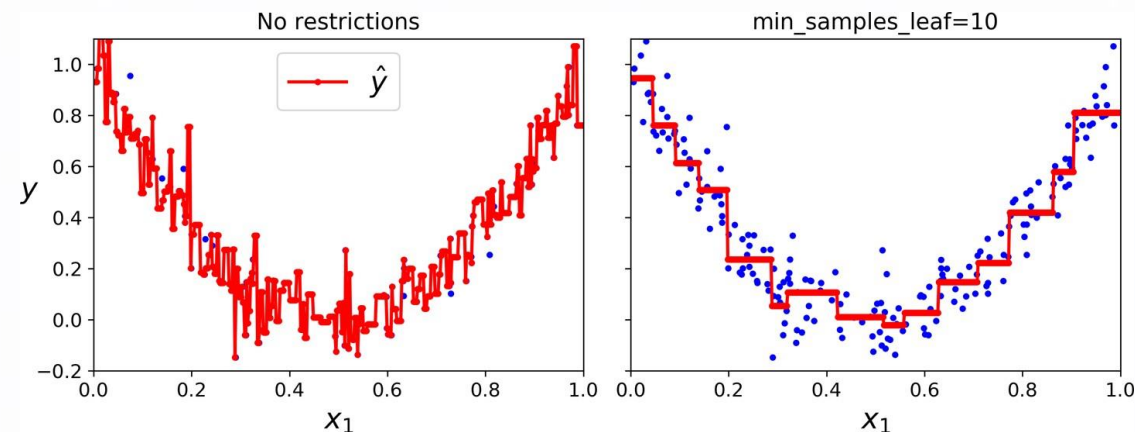
Figure 6-5. Predictions of two Decision Tree regression models

The CART algorithm works mostly the same way as earlier, except that instead of trying to split the training set in a way that minimizes impurity, it now tries to split the training set in a way that minimizes the MSE.

Equation 6-4. CART cost function for regression

$$J(k, t_k) = \frac{m_{\text{left}}}{m} \text{MSE}_{\text{left}} + \frac{m_{\text{right}}}{m} \text{MSE}_{\text{right}} \quad \text{where} \quad \begin{cases} \text{MSE}_{\text{node}} = \sum_{i \in \text{node}} (\hat{y}_{\text{node}} - y^{(i)})^2 \\ \hat{y}_{\text{node}} = \frac{1}{m_{\text{node}}} \sum_{i \in \text{node}} y^{(i)} \end{cases}$$

Just like for classification tasks, **Decision Trees are prone to overfitting when dealing with regression tasks.** Without any regularization (i.e., using the default hyperparameters), you get the predictions on the left in **Figure 6-6**. These predictions are obviously overfitting the training set very badly. Just setting `min_samples_leaf=10` results in a much more reasonable model, represented on the right in **Figure 6-6**.



- DTs have a few limitations. First, as you may have noticed, **Decision Trees love orthogonal decision boundaries (all splits are perpendicular to an axis)**, which makes them sensitive to training set rotation.
- For example, **Figure 6-7** shows a simple linearly separable dataset: on the left, a Decision Tree can split it easily, while on the right, after the dataset is rotated by  $45^\circ$ , the decision boundary looks unnecessarily convoluted.

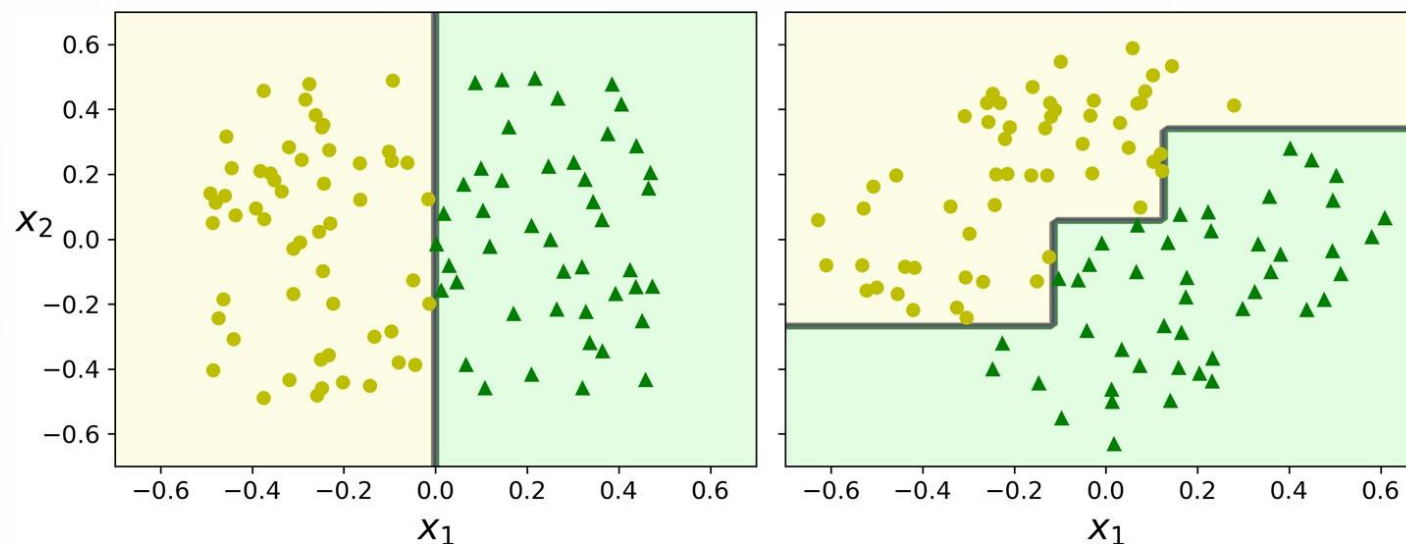


Figure 6-7. Sensitivity to training set rotation

- More generally, the main issue with Decision Trees is that **they are very sensitive to small variations in the training data**.
- For example, if you just remove the widest *Iris versicolor* from the iris training set (the one with petals 4.8 cm long and 1.8 cm wide) and train a new Decision Tree, you may get the model represented in **Figure 6-8**.
- As you can see, it looks very different from the previous Decision Tree (**Figure 6-2**). Actually, since the training algorithm used by Scikit-Learn is stochastic, you may get very different models even on the same training data (unless you set the `random_state` hyperparameter).

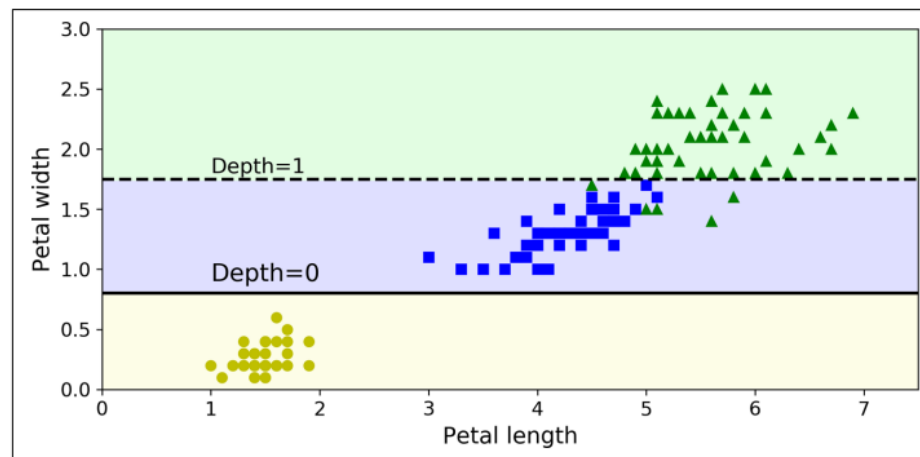


Figure 6-8. Sensitivity to training set details

**Random Forests** can limit this instability by averaging predictions over many trees, as we will see in the next chapter