

MSc Computational Science
joint programme UvA/VU



A DIFFUSION-BASED MODEL OF SPATIAL INTERACTIONS IN *ASPERGILLUS* SPP. GERMINATION

INTERMEDIATE PRESENTATION DECEMBER

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OUTLINE



1 Introduction

2 3D Diffusion

Experiment assumptions

Experiment results

3 Discussion

Permeation

4 Next Steps

Educated guess of D'

Physical derivation of D'

Mathematical derivation of D'

Numerical estimation of D'

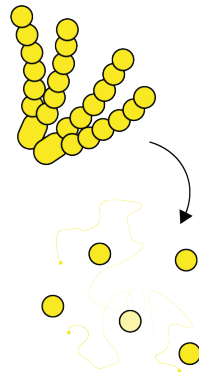
The effect of spore density

INTRODUCTION



Hypothesis

- » Upon inoculation in an aqueous medium, a germination inhibitor diffuses away from the conidium.
 - Experiments have highlighted **1-octen-3-ol** as a likely candidate [2, 3, 4]
- » Once its concentration at the spore falls below a certain threshold, the conidium breaks dormancy and enters a swelling phase.
 - It has been observed that in a **externally non-inhibited** spore swelling begins around **4 hours** from inoculation
- » An increased density of spores drives the local inhibitor concentration high, reducing overall germination.
 - Densities above 10^5 spores/mL exhibit germination inhibition [4, 5]



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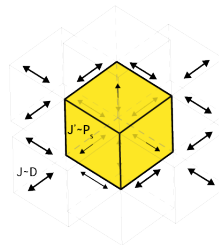
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3D DIFFUSION



Experiment assumptions

- » Assumptions as in **Experiment 2: Slow release**, but in 3 dimensions
- » Diffusion/permeation can occur over a larger surface area, in more spatial directions
- » For memory considerations, a smaller lattice edge length is taken: $L = 128 \times 5 \mu\text{M} = 640 \mu\text{M}$
- » Total lattice volume: $V = 2.62 \times 10^{-4} \text{ mL}$ (larger than in 2D system)



3D DIFFUSION



Results: comparison

- » Dimensionality of diffusion plays a role, but not as decisive as rate of permeation.

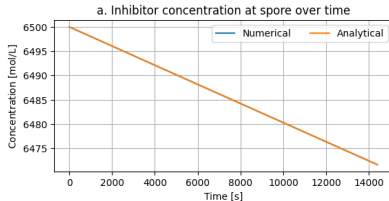


Figure: Results from Experiment 2
(2D system with permeation)

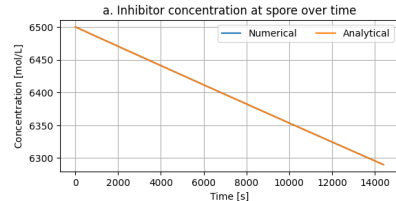


Figure: Results from Experiment 2
(3D system with permeation)

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DISCUSSION



Estimations

- » Some quantities can be inferred by fixing specific parameters.
- » If swelling begins at $t = 4$ h immediately upon inhibitor drop below the threshold of 10 mM and
 1. if **cell membrane is limiting permeation** from within the spore, then the initial concentration is:

$$c_0 \approx 1.033 \times 10^{-5} \text{ mol/mL} \quad (1)$$

2. if **spore is completely filled with 1-octen-3-ol**, then the permeation coefficient through the barrier is:

$$P_s = \frac{125 \mu\text{m}^3}{14\,400 \text{ s} \cdot 150 \mu\text{m}^2} \ln \frac{6.5 \times 10^3 \text{ mol/mL}}{10^{-5} \text{ mol/mL}} \approx 0.001\,174 \mu\text{m/s} \quad (2)$$

3. or if **cell wall is completely filled with 1-octen-3-ol**, then a diffusion coefficient through the cell wall can be computed

»

$$c_0 = c_{\text{out}} - \frac{c_{\text{out}} - c_{\text{in}}(t)}{\exp\left(-\frac{P_s A t}{V}\right)} \quad (3)$$

»

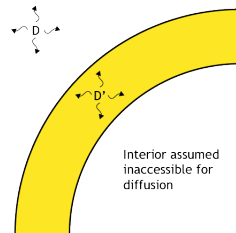
$$P_s = \frac{V_s}{tA} \ln \left(\frac{\Delta c(0)}{\Delta c(t)} \right) \quad (4)$$

DISCUSSION



Estimations

- » **Option 1** means that the concentration drop until break of dormancy is very small. Can the system be this sensitive?
- » Estimating P_s like in **Option 2** needs to be done with a more realistic initial concentration - hard to determine proportion of cell volume filled with inhibitor.
- » **Option 3** should consider that the cell wall is **not a barrier**, but a **source region with a different diffusion constant D'** .



DISCUSSION



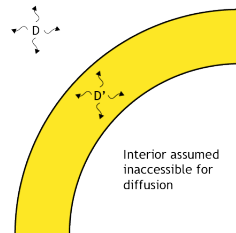
Cell wall diffusivity

- » An equation describing the relationship between D and P_s is:

$$P_s = \frac{K}{d}D, \quad (5)$$

where K is a partition coefficient and d is the thickness of the permeating barrier.

- » But P_s cannot be known without the assumption that the concentration originates from **beyond** the barrier.
- » Therefore, a different **mathematical relation** needs to be derived or **numerical simulations** need to be fitted to find D' .



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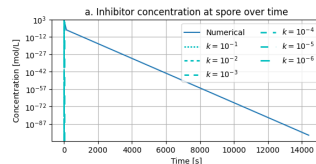
The effect of spore density

NEXT STEPS



Educated guess of D'

- » The diffusion coefficient is not always known but it can be related to comparable systems.
- » Diffusion of glucose through a cellulose film has $D \approx 1.7 \times 10^{-11} \text{ m}^2/\text{s} = 17 \mu\text{m}^2/\text{s}$
- » Results of 3D simulation with this diffusivity show a concentration drop to 10^{-12} mol/mL in the first 15 minutes.



NEXT STEPS



Physical derivation of D'

- » The diffusion coefficient can be estimated e.g. using the Einstein relation:

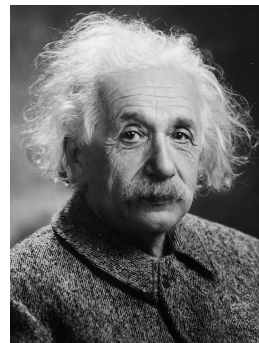
$$D = \mu k_B T, \quad (6)$$

where μ is the mobility of a particle (a factor relating the drift velocity to an applied force $\langle \vec{v} \rangle = \mu \vec{f}$,

- » of the Stokes-Einstein relation:

$$D = \frac{k_B T}{6\pi\eta a}, \quad (7)$$

where η is the viscosity of the medium and a is the radius of the particle.

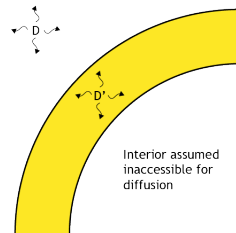


NEXT STEPS



Mathematical derivation of D'

- » An attempt at an analytical derivation can be done using Fick's laws and Random Walk models.
- » Fixing a starting concentration c_0 , the diffusivity of the surrounding medium D , the end concentration in the cell wall $c(t_i)$ and the time for inhibitor release t_i — D' can be expressed.
- » Might be non-trivial to solve depending on what is assumed at the interface.

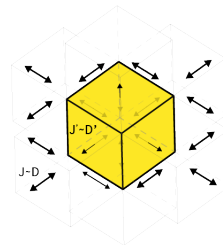


NEXT STEPS



Numerical estimation of D'

- » The diffusion coefficient can be approximated by stochastic simulations.
- » Running for various D' candidates, recording the threshold release time t'_i and optimising towards $|t'_i - t_i|$, where $t_i = 4$ h
- » The resulting D' can be related to other physical properties, verifying consistency with the properties of 1-octen-3-ol and the cell wall layers.
- » D' may have a more complex interpretation, e.g. the cumulative effect of different cell wall layers.



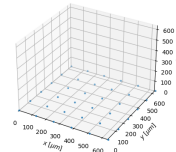
NEXT STEPS



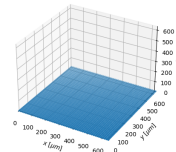
The effect of spore density

- » Assume we find a reasonable D' .
- » Is it consistent with spore-density-dependent inhibition?
- » Different spore densities need to be simulated to observe saturation effects (10^4 , 10^5 , ... 10^9 spores/mL).
- » Start with a regular grid of spores, then try other distributions.
- » Results should be related to observed decrease in germination percentage.
- » **If there is a slow-release system that reaches germination threshold for 1 spore, does it explain increased rates of inhibition for high spore densities?**

Spore density: 10^5 spores/mL



Spore density: 10^7 spores/mL





- [1] Nicklaus Carter, Julia Towne, and David J. Neivandt. “Finite element analysis of glucose diffusivity in cellulose nanofibril peripheral nerve conduits”. In: *Cellulose* 28 (2021), pp. 2791–2803. URL: <https://api.semanticscholar.org/CorpusID:231858923>.
- [2] Gilma Silva Chitarra et al. “1-Octen-3-ol inhibits conidia germination of *Penicillium paneum* despite of mild effects on membrane permeability, respiration, intracellular pH, and changes the protein composition.”. In: *FEMS microbiology ecology* 54 1 (2005), pp. 67–75. URL: <https://api.semanticscholar.org/CorpusID:24273006>.
- [3] Gilma Silva Chitarra et al. “Germination of *Penicillium paneum* Conidia Is Regulated by 1-Octen-3-ol, a Volatile Self-Inhibitor”. In: *Applied and Environmental Microbiology* 70 (2004), pp. 2823–2829. URL: <https://api.semanticscholar.org/CorpusID:19828197>.



- [4] Erika Herrero-García et al. “8-Carbon oxylipins inhibit germination and growth, and stimulate aerial conidiation in *Aspergillus nidulans*.”. In: *Fungal biology* 115 4-5 (2011), pp. 393–400. URL: <https://api.semanticscholar.org/CorpusID:33687383>.
- [5] Maryam Ijadpanahsaravi et al. “The impact of inter- and intra-species spore density on germination of the food spoilage fungus *Aspergillus niger*.”. In: *International journal of food microbiology* 410 (2023), p. 110495. URL: <https://api.semanticscholar.org/CorpusID:265268197>.