

presents the

REFERENCE IMPLEMENTATION

also known as the PURPLE PAPER

of the remarkable

DAI CREDIT SYSTEM

issuing a diversely collateralized stablecoin



elucidated by

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Chapter 1

Introduction

The dai credit system, henceforth also "Maker," is a network of Ethereum contracts designed to issue the dai currency token and automatically adjust credit incentives in order to keep its market value stable relative to SDR¹ in the short and medium term.

New dai enters the money supply when a borrower takes out a loan backed by an excess of collateral locked in Maker's token vault. Thus all outstanding dai represents some CDP owner's claim on their collateral. The debt and collateral amounts are recorded in a *collateralized debt position*, or CDP.

Off-chain *price feeds* give Maker knowledge of the market values of dai and the various tokens used as collateral, enabling the system to assess credit risk. If the value of a CDP's collateral drops below a certain multiple of its debt, a decentralized liquidation auction is triggered to sell the collateral for dai to be burned thus settling the debt.

The system issues a separate token with symbol MKR, which behaves like a "share" in Maker itself. When a collateral auction fails to recover the full debt value, the MKR token is diluted by way of a *reverse auction*. The value of MKR, though volatile by design, is backed by the revenue from a *stability fee* imposed on all dai loans and used to buy MKR for burning.

This document is an executable technical specification of the of the Maker smart contracts. It is a draft; be aware that the contents will certainly change before the public launch of the dai.

¹ "Special Drawing Rights" (ticker symbol XDR), the international reserve asset created by the International Monetary Fund, whose value is derives from a weighted basket of world currencies.

1.1 Reference implementation

The version of this system that will be deployed on the blockchain is written in Solidity, which is a workable smart contract implementation language. This reference implementation is a model of the behavior of those contracts, written as a "literate" Haskell program. The motivations for such a reference implementation include:

- 1. **Comparison**. Checking two free-standing implementations against each other is a well-known way of ensuring that they both behave as intended.
- 2. **Testing**. Haskell lets us use powerful testing tools such as QuickCheck and SmallCheck for comprehensively verifying key properties as a middle ground between unit testing and formal verification.
- 3. **Explicitness**. Coding the contract behavior in Haskell, a purely functional language, enforces explicit description of aspects which Solidity leaves implicit. For example, a Solidity program can read previously unwritten storage and get back a zero value, whereas in Haskell we must give explicit defaults. The state rollback behavior of failed actions is also explicit in the type of the execution function, which may return an error.
- 4. **Typing**. While Solidity does have a static type system, it is not expressive enough to encode the distinctions made by our system. In particular, the two different decimal fixed point number types that we use are typed in Solidity with one and the same uint128 type. In Haskell we can make this distinction explicit.
- 5. **Formality**. The work of translating a Solidity program into a purely functional program opens up opportunities for certain types of formal verification. In particular, this document will be useful for modelling aspects of the system in a proof assistant like Agda, Idris, Coq, or Isabelle. We can also use logical tools for Haskell, such as Liquid Haskell (which provides compile time logical property checking) and sbv (a toolkit for model checking and symbolic execution).
- 6. **Simulation**. Solidity is highly specific to the Ethereum blockchain environment and as such does not have facilities for interfacing with files or other computer programs. This makes the Solidity implementation of the system less useful for doing simulations of the system's economic, game-theoretic, or statistical aspects.

1.2 Limitations

This implementation has a simplified model of Maker's governance authorization. Instead of the "access control list" approach of the DSGuard component, we give full authority to one single address. A future iteration will include the full authorization model.

We also do not currently model the EVM's 256 bit word size, but allow all quantities to grow arbitrarily large. This will also be modelled in a future iteration.

Finally, our model of ERC20 tokens is simplified, and for example does not include the concept of "allowances."

Part I Implementation

Preamble

We replace the default prelude module with our own. This brings in dependencies and hides unneeded symbols. Consult Appendix A to see exactly what is brought into scope.

```
module Maker where
import Prelude () Import nothing from Prelude
import Maker.Prelude Import everything from Maker Prelude
```

We also import our definition of decimal fixed point numbers, listed in Appendix B.

import Maker.Decimal

Chapter 2

Types

We now define the data types used by Maker: numeric types, identifiers, on-chain records, and test model data.

2.1 Numeric types

The system uses two different precisions of decimal fixed point numbers, which we call *wads* and *rays*, having respectively 18 digits of precision (used for token quantities) and 36 digits (used for precise rates and ratios). See Appendix B for details on decimal fixed point numbers and rounding.

```
Define the distinct type for currency quantities  \begin{array}{l} \textbf{newtype} \ \texttt{Wad} = \texttt{Wad} \ (\texttt{Decimal} \ \texttt{E18}) \\ \textbf{deriving} \ (\texttt{Ord}, \texttt{Eq}, \texttt{Num}, \texttt{Real}, \texttt{Fractional}, \texttt{RealFrac}) \\ \textbf{Define the distinct type for rates and ratios} \\ \textbf{newtype} \ \texttt{Ray} = \texttt{Ray} \ (\texttt{Decimal} \ \texttt{E36}) \\ \textbf{deriving} \ (\texttt{Ord}, \texttt{Eq}, \texttt{Num}, \texttt{Real}, \texttt{Fractional}, \texttt{RealFrac}) \\ \end{array}
```

We also define a type for time durations in whole seconds.

```
\label{eq:newtype} \begin{array}{l} \textbf{newtype} \; \texttt{Sec} = \texttt{Sec} \; \texttt{Int} \\ \textbf{deriving} \; (\texttt{Eq}, \texttt{Ord}, \texttt{Enum}, \texttt{Num}, \texttt{Real}, \texttt{Integral}) \end{array}
```

Haskell number types are not automatically converted, so we convert explicitly with a *cast* function.

```
Convert via fractional n/m form. cast :: (Real \ a, Fractional \ b) \Rightarrow a \rightarrow b cast = fromRational \ . \ toRational
```

2.2 Identifiers and addresses

There are several kinds of identifiers used in the system, and we use types to distinguish them. The type parameter a creates distinct types; e.g., Id Foo and Id Bar are incompatible.

```
data Id a = \text{Id String} deriving (Show, Eq, Ord)
```

We define another type for representing Ethereum account addresses.

```
data Address = Address String
  deriving (Ord, Eq, Show)
```

We also have two predefined entity identifiers.

```
The DAI token vault address id_{\mathrm{DAI}} = \mathrm{Id} "DAI" 
A test account with ultimate authority id_{god} = \mathrm{Address} "GOD"
```

2.3 Gem — token model

In this model, all tokens behave in the same simple way.¹ We omit the ERC20 concept of "allowances."

Tokens can be held by CDP owners, by collateral vaults, or by the test driver. We model this distinction with a data type.

```
data Holder = InAccount Address | InVault (Id Jar) | InToy
deriving (Eq, Show, Ord)
```

¹In the real world, token semantics can differ, despite nominally following the ERC20 interface. Maker governance therefore involves due diligence on collateral token contracts.

We now define a Gem as simply a map keeping track of the currency amount held by each holder.

```
data Gem = Gem { ● balanceOf :: Map Holder Wad}
deriving (Eq, Show)
```

2.4 Jar — collateral vaults

2.5 Ilk — CDP type

```
data Ilk = Ilk {
  • jar :: Id Jar, Collateral vault
  mat :: Ray,
                    Liquidation ratio

    axe :: Ray,

                    Liquidation penalty
  • hat :: Wad,
                    Debt ceiling
  tax :: Ray,
                    Stability fee
  • lag::Sec,
                    Price feed limbo duration
  • rho::Sec,
                    Time of latest debt unit adjustment
  • rum :: Wad,
                    Total debt in debt unit
  • chi::Ray
                    Dai value of debt unit
  } deriving (Eq, Show)
```

2.6 Urn — collateralized debt position (CDP)

2.7 Vat — CDP engine

```
\mathtt{data}\ \mathtt{Vat} = \mathtt{Vat}\ \{
```

Table 2.1: CDP record

```
data Urn = Urn  {
  • cat :: Maybe Address, Address of liquidation initiator
  • vow :: Maybe Address, Address of liquidation contract
  • lad :: Address,
  • ilk :: Id Ilk,
                              CDP type
  • art :: Wad,
                              Outstanding debt in debt unit
  • jam::Wad
                              Collateral amount in debt unit
   } deriving (Eq, Show)
  • fix::Wad,
                                  Market price
  • how :: Ray,
                                  Sensitivity
  • par :: Wad,
                                  Target price
                                  Target rate
  • way :: Ray,
  • tau :: Sec,
                                  Last prodded
  • joy :: Wad,
                                  Unprocessed stability fees
  • sin::Wad,
                                  Bad debt from liquidated CDPs
  • jars :: Map (Id Jar) Jar, Collateral tokens
  • ilks :: Map (Id Ilk) Ilk, cdp types
  • urns :: Map (Id Urn) Urn
  } deriving (Eq, Show)
```

2.8 System model

Lens fields

```
makeLenses '' Gem
makeLenses '' Jar
makeLenses '' Ilk
makeLenses '' Urn
makeLenses '' Vat
makeLenses '' System
```

2.9 Default data

```
defaultIlk :: Id Jar \rightarrow Ilk
defaultIlk id_{jar} = Ilk {
   • jar = id_{jar},
   • axe = Ray 1,
   • mat = Ray 1,
   • tax = Ray 1,
   • hat = Wad 0,
   • lag = Sec 0,
   • chi = Ray 1,
   • rum = Wad 0,
   \bullet \ \ \mathtt{rho} = \mathtt{Sec} \ 0
}
emptyUrn :: Id Ilk \rightarrow Address \rightarrow Urn
emptyUrn\ id_{\mathtt{ilk}}\ id_{\mathtt{lad}} = \mathtt{Urn}\ \{
  • vow = Nothing,
   • cat = Nothing,
   • lad = id_{lad},
   • ilk = id_{ilk},
   • art = Wad 0,
   \bullet \ \mathtt{jam} = \mathtt{Wad} \ 0
initialVat :: \mathtt{Ray} \rightarrow \mathtt{Vat}
initialVat how_0 = Vat
```

```
• tau = 0,
   • fix = Wad 1,
   • par = Wad 1,
   • how = how_0,
   • way = \text{Ray } 1,
   • joy = \operatorname{Wad} 0,
   ullet sin = \operatorname{Wad} 0,
   • ilks = \emptyset,
   • urns = \emptyset,
   • jars =
      \textit{singleton id}_{\text{\tiny DAI}}\;\text{Jar}\;\big\{
         \bullet \ \mathtt{gem} = \mathtt{Gem} \ \{
            ullet balanceOf = arnothing
         },
         • tag = Wad 0,
         \bullet zzz = 0
      }
}
initialSystem :: Ray \rightarrow System
initialSystem how_0 = System {
   • vat
                    = initial Vat how_0,
   • era
                    =id_{god},
   • sender
   • accounts = mempty
```

}

Chapter 3

Acts

The *acts* are the basic state transitions of the system.

For details on the underlying "Maker monad," which specifies how the act definitions behave with regard to state and rollback thereof, see chapter 4.

3.1 Assessment

In order to prohibit CDP acts based on risk situation, we define five stages of risk.

```
data Stage = Pride | Anger | Worry | Panic | Grief | Dread
deriving (Eq, Show)
```

We define the function *analyze* that determines the risk stage of a CDP.

```
analyze \, era_0 \, par_0 \, urn_0 \, ilk_0 \, jar_0 =
  if | view vow urn<sub>0</sub> \not\equiv Nothing
        CDP liquidation in progress

ightarrow Dread
     | view cat urn<sub>0</sub> \not\equiv Nothing
        CDP liquidation triggered

ightarrow Grief
     | pro < min
        CDP's collateralization below liquidation ratio
           \to \mathtt{Panic}
     | view zzz jar_0 + view lag ilk_0 < era_0
        CDP type's price limbo exceeded limit

ightarrow Panic
     | view zzz jar_0 < era_0
        CDP type's price feed in limbo

ightarrow Worry
     | cap > view hat ilk_0
        CDP type's debt ceiling exceeded

ightarrow Anger
     otherwise
         No problems

ightarrow Pride
  where
    CDP's collateral value in SDR:
     pro = view jam urn_0 * view tag jar_0
    CDP type's total debt in SDR:
      cap = view rum ilk_0 * cast (view chi ilk_0)
    CDP's debt in SDR:
      con = view art urn_0 * cast (view chi ilk_0) * par_0
    Required collateral as per liquidation ratio:
     min = con * cast (view mat ilk_0)
```

Table 3.1: CDP acts in the five stages of risk

	give	shut	lock	wipe	free	draw	bite	grab	plop
Pride	2	3	3	F	₽	4	_	_	_
Anger	\mathcal{E}	S	₽	S	\oplus	_	_	_	_
Worry	₿	S	S	E	_	_	_	_	_
Panic	₿	5	- 30	E	_	_	(_	_
Grief	₿	_	_	_	_	_	_	\bigcirc	_
Dread	₿	_	_	_	_	_	_	_	\bigcirc
		de	crease r	isk	increa	se risk	unwind risk		
allowed for owner unconditionally allowed for owner if able to repay allowed for owner if collateralization maintained allowed for settler contract allowed for anyone								d	

Now we define the internal act gaze which returns the value of *analyze* after ensuring that the system state is updated.

```
gaze id_{\text{urn}} = \mathbf{do}

Adjust target price and target rate prod

Update debt unit and unprocessed fee revenue id_{\text{ilk}} \leftarrow look \; (\text{vat.urns.} \; ix \; id_{\text{urn.}} \; ilk)

drip id_{\text{ilk}}

Read parameters for risk analysis era<sub>0</sub> \leftarrow use era par<sub>0</sub> \leftarrow use (vat.par) urn<sub>0</sub> \leftarrow look (vat.urns.ix id_{urn.}) ilk<sub>0</sub> \leftarrow look (vat.ilks.ix (view ilk urn<sub>0</sub>)) jar<sub>0</sub> \leftarrow look (vat.jars.ix (view jar ilk<sub>0</sub>))

Return risk stage of CDP return (analyze era<sub>0</sub> par<sub>0</sub> urn<sub>0</sub> ilk<sub>0</sub> jar<sub>0</sub>)
```

Acts on CDPs use gaze to prohibit increasing risk when already risky, and to freeze debt and collateral during liquidation; see Table 3.1.

3.2 Lending

Any user can open one or more accounts with the system using open, specifying a self-chosen account identifier and a CDP type.

```
open id_{\text{urn}} id_{\text{ilk}} = \mathbf{do}

Fail if account identifier is taken none (vat . urns . ix id_{\text{urn}})

Create a CDP record with the sender as owner id_{\text{lad}} \leftarrow use sender initialize (vat . urns . at id_{\text{urn}}) (emptyUrn id_{\text{ilk}} id_{\text{lad}})
```

The owner of a CDP can transfer its ownership at any time using give.

```
give id_{	ext{urn}} \ id_{	ext{lad}} = 	ext{do}

Fail if sender is not the CDP owner id_{sender} \leftarrow use \ sender

owns \ id_{	ext{urn}} \ id_{sender}

Transfer ownership

vat . urns . ix \ id_{	ext{urn}} . lad := id_{	ext{lad}}
```

Unless liquidation has been triggered for a CDP, its owner can use lock to deposit more collateral.

```
lock id_{\text{urn}} \text{ wad}_{\text{gem}} = \mathbf{do}

Fail if sender is not the CDP owner id_{\text{lad}} \leftarrow use \ sender owns id_{\text{urn}} \ id_{\text{lad}}

Fail if liquidation initiated want (gaze id_{\text{urn}}) (\notin [Grief, Dread])

Identify collateral type id_{\text{ilk}} \leftarrow look (vat.urns.ix \ id_{\text{urn}}.ilk) id_{\text{jar}} \leftarrow look (vat.ilks.ix \ id_{\text{ilk}}.jar)

Transfer tokens from owner to collateral vault pull id_{\text{jar}} \ id_{\text{lad}} \ \text{wad}_{\text{gem}}

Record an increase in collateral increase (vat.urns.ix \ id_{\text{urn}}.jam) wad<sub>gem</sub>
```

When a CDP has no risk problems—except that its CDP type's debt ceiling may be exceeded—its owner can use free to withdraw some amount of collateral, as long as the withdrawal would not reduce collateralization below the liquidation ratio.

```
Free id_{\text{urn}} wad_{\text{gem}} = \mathbf{do}

Fail if sender is not the CDP owner id_{\text{lad}} \leftarrow use \ sender owns id_{\text{urn}} \ id_{\text{lad}}

Record a decrease in collateral decrease (vat . urns . ix \ id_{\text{urn}} . jam) wad_{\text{gem}}

Roll back on any risk problem except debt ceiling excess want (gaze id_{\text{urn}}) (\in [Pride, Anger])

Transfer tokens from collateral vault to owner id_{\text{ilk}} \leftarrow look (vat . urns . ix \ id_{\text{urn}} . ilk) id_{\text{jar}} \leftarrow look (vat . ilks . ix \ id_{\text{ilk}} . jar) push id_{\text{jar}} \ id_{\text{lad}} wad_{\text{gem}}
```

When a CDP has no risk problems, its owner can use draw to take out a loan of newly minted dai, as long as the CDP type's debt ceiling is not reached and the loan would not result in undercollateralization.

```
draw id_{urn} wad_{DAI} = do
 Fail if sender is not the CDP owner
    id_{1ad} \leftarrow use sender
    owns id_{\tt urn} id_{\tt lad}
 Update debt unit and unprocessed fee revenue
    id_{\mathtt{ilk}} \leftarrow look \, (\mathtt{vat.urns.} \, ix \, id_{\mathtt{urn}} \, . \, \mathtt{ilk})
    chi_1 \leftarrow drip id_{ilk}
 Denominate loan in debt unit
   let wad_{chi} = wad_{DAI} / cast chi_1
 Increase CDP debt
    increase (vat . urns . ix id_{\mathtt{urn}} . \mathtt{art}) \mathtt{wad}_{\mathtt{chi}}
 Increase total debt of CDP type
    increase (vat . ilks . ix id_{ilk} . rum) wad<sub>chi</sub>
 Roll back on any risk problem
    want (gaze id_{urn}) (\equiv Pride)
 Mint dai and transfer to CDP owner
   mint id_{DAI} wad_{DAI}
   \operatorname{push} id_{\scriptscriptstyle \mathrm{DAI}} id_{\scriptscriptstyle \mathrm{1ad}} \operatorname{wad}_{\scriptscriptstyle \mathrm{DAI}}
```

A CDP owner who has previously loaned dai can use wipe to repay part of their debt as long as liquidation has not been initiated.

```
wipe id_{\text{urn}} \text{ wad}_{\text{DAI}} = \mathbf{do}
```

```
Fail if sender is not the CDP owner
  id_{\mathtt{lad}} \leftarrow use \ sender
  owns idurn idlad
Fail if liquidation initiated
  want (gaze id_{urn}) (\notin [Grief, Dread])
Update debt unit and unprocessed fee revenue
  id_{\texttt{ilk}} \leftarrow look \, (\texttt{vat.urns.} \, ix \, id_{\texttt{urn.}} \, . \, \texttt{ilk})
  chi_1 \leftarrow drip id_{ilk}
Denominate dai amount in debt unit
 let wad_{chi} = wad_{DAI} / cast chi_1
Decrease CDP debt
  decrease (vat . urns . ix idurn . art) wadchi
Decrease total CDP type debt
  decrease (vat.ilks.ix id_{ilk}.rum) wad<sub>chi</sub>
Transfer dai from CDP owner to dai vault
 pull id_{\text{DAI}} id_{\text{lad}} wad_{\text{DAI}}
Destroy reclaimed dai
 burn id_{\text{DAI}} wad_{\text{DAI}}
```

A CDP owner can use shut to close their account—repaying all debt and reclaiming all collateral—if the price feed is up to date and liquidation has not been initiated.

```
shut id_{	ext{urn}} = 	ext{do}

Update debt unit and unprocessed fee revenue id_{	ext{ilk}} \leftarrow look \ (	ext{vat.urns.} ix id_{	ext{urn.}} . 	ext{ilk})

chi_1 \leftarrow drip \ id_{	ext{ilk}}

Reclaim all outstanding dai art_0 \leftarrow look \ (	ext{vat.urns.} ix id_{	ext{urn.}} . 	ext{art})

wipe id_{	ext{urn.}} \ (art_0 * cast \ chi_1)

Reclaim all collateral jam_0 \leftarrow look \ (	ext{vat.urns.} ix id_{	ext{urn.}} . 	ext{jam})

free id_{	ext{urn.}} \ jam_0

Nullify CDP record vat. urns. at id_{	ext{urn.}} := Nothing
```

3.3 Adjustment

```
prod = do
   \mathtt{era}_0 \leftarrow \mathit{use} \ \mathtt{era}
   tau_0 \leftarrow use (vat.tau)
   fix_0 \leftarrow use(vat.fix)
   par_0 \leftarrow use (vat.par)
   \mathsf{how}_0 \leftarrow \mathit{use} \ (\mathsf{vat} \ . \ \mathsf{how})
   way_0 \leftarrow use (vat.way)
   let
    Time difference in seconds
      age = era_0 - tau_0
    Current target rate applied to target price
      par_1 = par_0 * cast (way_0 \uparrow \uparrow age)
    Sensitivity parameter applied over time
      wag = how_0 * fromIntegral age
    Target rate scaled up or down
      way_1 = inj (prj way_0 +
                      if fix_0 < par_0 then wag else -wag)
   vat.par := par_1
   vat.way := way_1
   \mathtt{vat}.\mathtt{tau} := \mathtt{era}_0
   where
    Convert between multiplicative and additive form
      prj x = if x \ge 1 then x - 1 else 1 - 1 / x
      inj x = if x \ge 0 then x + 1 else 1 / (1 - x)
```

```
drip id_{ilk} = do
    {\tt rho}_0 \leftarrow look \, ({\tt vat.ilks.} \, ix \, id_{\tt ilk} \, . \, {\tt rho}) \, \, {\sf Time \, stamp \, of \, previous \, drip}
    \mathsf{tax}_0 \leftarrow look \, (\mathsf{vat.ilks.} \, ix \, id_{\mathtt{ilk}} \, . \, \mathsf{tax}) \, \mathsf{Current} \, \mathsf{stability} \, \mathsf{fee}
     \mathtt{chi}_0 \leftarrow look \, (\mathtt{vat.ilks.} \, ix \, id_{\mathtt{ilk}} \, . \, \mathtt{chi}) \, \, \mathsf{Current \, debt \, unit \, value}
    \mathtt{rum}_0 \leftarrow look \, (\mathtt{vat.ilks.} \, ix \, id_{\mathtt{ilk}} \, . \, \mathtt{rum}) \, \, \mathsf{Current \, total \, debt \, in \, debt \, unit}
     joy_0 \leftarrow look (vat.joy)
                                                                                  Current unprocessed stability fee revenue
    era_0 \leftarrow use era
                                                                                  Current time stamp
    let
         age = era_0 - rho_0
         chi_1 = chi_0 * tax_0 \uparrow \uparrow age
         joy_1 = joy_0 + (cast (chi_1 - chi_0) :: Wad) * rum_0
    \mathtt{vat.ilks.} ix id_{\mathtt{ilk}}.\mathtt{chi} := \mathtt{chi}_1
    \mathtt{vat.ilks.} ix id_{\mathtt{ilk}}.\mathtt{rho} := \mathtt{era}_0
    vat.joy := joy_1
     return chi<sub>1</sub>
```

3.4 Feedback

```
\begin{array}{l} \operatorname{mark}\ id_{\operatorname{jar}}\ \operatorname{tag}_1\ \operatorname{zzz}_1 = \\ \operatorname{auth}\ \$\ \operatorname{\mathbf{do}} \\ \operatorname{vat}\ .\ \operatorname{jars}\ .\ ix\ id_{\operatorname{jar}}\ .\ \operatorname{tag} := \operatorname{tag}_1 \\ \operatorname{vat}\ .\ \operatorname{jars}\ .\ ix\ id_{\operatorname{jar}}\ .\ \operatorname{zzz} := \operatorname{zzz}_1 \end{array} \begin{array}{l} \operatorname{tell}\ \operatorname{wad}_{\operatorname{gem}} = \\ \operatorname{auth}\ \$\ \operatorname{\mathbf{do}} \\ \operatorname{vat}\ .\ \operatorname{fix} := \operatorname{wad}_{\operatorname{gem}} \end{array}
```

3.5 Liquidation

```
bite id_{	ext{urn}} = 	ext{do}

Fail if CDP is not in need of liquidation want \ (	ext{gaze} \ id_{	ext{urn}}) \ (\equiv 	ext{Panic})

Record the sender as the liquidation initiator
```

```
id_{\texttt{cat}} \leftarrow \textit{use sender}
        \mathtt{vat}.\mathtt{urns}.\mathit{ix}\:\mathit{id}_{\mathtt{urn}}.\mathtt{cat}:=\mathtt{Just}\:\mathit{id}_{\mathtt{cat}}
      Read current debt
        \mathtt{art}_0 \leftarrow look \, (\mathtt{vat.urns.} \, ix \, id_{\mathtt{urn}} \, . \, \mathtt{art})
      Update debt unit
        id_{\mathtt{ilk}} \leftarrow look \, (\mathtt{vat.urns.} \, ix \, id_{\mathtt{urn}} \, . \, \mathtt{ilk})
        chi_1 \leftarrow drip id_{ilk}
      Read liquidation penalty ratio
        id_{\texttt{ilk}} \leftarrow look \, (\texttt{vat.urns.} \, ix \, id_{\texttt{urn.}} \, . \, \texttt{ilk})
        axe_0 \leftarrow look (vat.ilks.ix id_{ilk}.axe)
      Apply liquidation penalty to debt
        let art_1 = art_0 * cast axe_0
      Update CDP debt
        vat . urns . ix id_{urn} . art := art<sub>1</sub>
      Record as bad debt
        increase (vat . sin) (art<sub>1</sub> * cast chi<sub>1</sub>)
grab id_{urn} =
    auth $ do
      Fail if CDP is not marked for liquidation
        want (gaze id_{urn}) (\equiv Grief)
      Record the sender as the CDP's settler
        id_{vow} \leftarrow use sender
        \mathtt{vat} . \mathtt{urns} . ix\ id_{\mathtt{urn}} . \mathtt{vow} := \mathtt{Just}\ id_{\mathtt{vow}}
      Forget the CDP's requester of liquidation
        vat . urns . ix id_{urn} . cat := Nothing
plop id_{urn} wad_{DAI} =
    auth $ do
      Fail unless CDP is in liquidation
        want (gaze id_{urn}) (\equiv Dread)
      Forget the CDP's settler
        vat.urns.ix\ id_{urn}.vow := Nothing
      Return some amount of excess auction gains
        \mathtt{vat.urns.}\ ix\ id_{\mathtt{urn}}. \mathtt{jam}:=\mathtt{wad}_{\mathtt{DAI}}
```

```
egin{aligned} {
m heal \ wad_{DAI}} &= \ {
m auth \ \$ \ do} \ & decrease \ {
m (vat.sin) \ wad_{DAI}} \end{aligned} egin{aligned} {
m love \ wad_{DAI}} &= \ {
m auth \ \$ \ do} \ & decrease \ {
m (vat.joy) \ wad_{DAI}} \end{aligned}
```

3.6 Governance

```
form id_{ilk} id_{jar} =
     auth $ do
          initialize (vat . ilks . at id<sub>ilk</sub>)
              (defaultIlk\ id_{jar})
\mathtt{frob}\ \mathtt{how}_1 =
    auth $ do
         \mathtt{vat} \cdot \mathtt{how} := \mathtt{how}_1
chop id_{ilk} axe_1 =
     auth $ do
         \mathtt{vat.ilks.} \ \mathit{ix} \ \mathit{id}_{\mathtt{ilk}} \ . \ \mathtt{axe} := \mathtt{axe}_1
\mathtt{cork}\ id_{\mathtt{ilk}}\ \mathtt{hat}_1 =
    \mathtt{auth} \ \$ \ \mathbf{do}
         \mathtt{vat.ilks.} \ ix \ id_{\mathtt{ilk}} \ . \ \mathtt{hat} := \mathtt{hat}_1
{\tt calm}\; id_{\tt ilk}\; {\tt lag}_1 =
    auth $ do
         \mathtt{vat.ilks.}\ ix\ id_{\mathtt{ilk}}.\mathtt{lag} := \mathtt{lag}_1
```

```
\begin{array}{l} \operatorname{cuff}\, id_{\mathtt{ilk}}\, \mathtt{mat}_1 = \\ \\ \operatorname{auth} \, \$\,\, \mathbf{do} \\ \\ \operatorname{vat} \, .\, \operatorname{ilks} \, .\, ix\,\, id_{\mathtt{ilk}} \, .\, \mathtt{mat} := \mathtt{mat}_1 \\ \\ \operatorname{crop}\, id_{\mathtt{ilk}}\, \operatorname{tax}_1 = \\ \\ \operatorname{auth} \, \$\,\, \mathbf{do} \\ \\ \operatorname{drip}\, id_{\mathtt{ilk}} \\ \\ \operatorname{vat} \, .\, \operatorname{ilks} \, .\, ix\,\, id_{\mathtt{ilk}} \, .\, \operatorname{tax} := \operatorname{tax}_1 \end{array}
```

3.7 Treasury

```
pull id_{jar} id_{lad} wad_{gem} =
    transfer id_{jar} wad_{gem}
        (InAccount id_{lad})
        (InVault
                            id_{jar})
{\tt push}\ id_{\tt jar}\ id_{\tt lad}\ {\tt wad}_{\tt gem} =
    transfer\ id_{jar}\ wad_{gem}
        (InVault
                            id_{iar}
        (InAccount id_{lad})
mint id_{jar} wad_0 =
    zoom \; (\mathtt{vat.jars.} \; ix \; id_{\mathtt{jar}} \, . \, \mathtt{gem}) \; \$ \; \mathbf{do}
        increase\ (balanceOf.\ ix\ (InVault\ id_{\texttt{jar}}))\ \mathtt{wad}_0
\operatorname{burn} id_{\operatorname{jar}} \operatorname{wad}_0 =
    zoom\;({\tt vat.jars.}ix\;id_{\tt jar}.{\tt gem})~\$~\mathbf{do}
        decrease (balanceOf. ix (InVault id_{jar})) wad_0
```

3.8 Manipulation

```
\begin{aligned} & \text{mine } id_{\text{jar}} = \mathbf{do} \\ & \textit{initialize} \left( \text{vat. jars. } at \ id_{\text{jar}} \right) \\ & \left( \text{Jar } \left\{ \right. \\ & \bullet \text{ gem} = \text{Gem} \left( \textit{singleton} \text{ InToy } 1000000000000 \right), \\ & \bullet \text{ tag} = \text{Wad } 0, \\ & \bullet \text{ zzz} = 0 \right\} \right) \end{aligned} \text{hand } dst \ \text{wad}_{\text{gem}} \ id_{\text{jar}} = \mathbf{do} \\ & \textit{transfer } id_{\text{jar}} \ \text{wad}_{\text{gem}} \\ & \text{InToy} \left( \text{InAccount } dst \right) \end{aligned} \text{sire lad} = \mathbf{do} \ \textit{prepend accounts} \ \text{lad}
```

3.9 Other stuff

```
perform :: Act \rightarrow Maker ()
perform x =
   let ?act = x in case x of
      Form id jar \rightarrow form id jar
      Mark jar tag zzz \rightarrow mark jar tag zzz
      Open id ilk \rightarrow open id ilk
      Tell wad

ightarrow tell wad
      Frob ray
                         \rightarrow frob ray
      Prod

ightarrow prod

ightarrow warp t
      Warp t
      Give urn lad \rightarrow give urn lad
      Pull jar lad wad \rightarrow pull jar lad wad
      \mathtt{Lock}\ \mathtt{urn}\ \mathtt{wad} \to \mathtt{lock}\ \mathtt{urn}\ \mathtt{wad}
      Mine id

ightarrow mine id
```

```
{\tt Hand}\;{\tt lad}\;{\tt wad}\;{\tt jar} \to {\tt hand}\;{\tt lad}\;{\tt wad}\;{\tt jar}
       Sire lad

ightarrow sire lad
being :: Act \rightarrow Address \rightarrow Maker ()
being x who = do
   old
             \leftarrow use sender
   sender := who
             \leftarrow perform x
   sender := old
   return y
transfer id_{jar} wad src dst =
 Operate in the token's balance table
   \emph{zoom} \; (\texttt{vat.jars.} \; \emph{ix} \; \emph{id}_{\texttt{jar}} \; . \; \texttt{gem.} \; \emph{balanceOf}) \; \$ \; \mathbf{do}
     Fail if source balance insufficient
       balance \leftarrow look (ix src)
       aver (balance \geqslant wad)
     Decrease source balance
       decrease (ix src) wad
    Increase destination balance
       initialize (at dst) 0
       increase (ix dst) wad
```

Chapter 4

Act framework

4.1 Act descriptions

We define the Maker act vocabulary as a data type.

```
data Act =
    Bite (Id Urn)
   Draw (Id Urn) Wad
    Form (Id Ilk) (Id Jar)
   Free (Id Urn) Wad
   Frob Ray
    Give (Id Urn) Address
    Grab (Id Urn)
    Heal Wad
   Lock (Id Urn) Wad
    Love Wad
   Mark (Id Jar) Wad
                          Sec
    Open (Id Urn) (Id Ilk)
    {\tt Prod}
    Pull (Id Jar) Address Wad
    Shut (Id Urn)
    Tell Wad
    Warp Sec
    Wipe (Id Urn) Wad
    Mine (Id Jar)
    Hand Address Wad
                          (Id Jar)
    Sire Address
```

```
Test acts
| Addr Address
deriving (Eq. Show)
```

Acts can fail. We divide the failure modes into general assertion failures and authentication failures.

```
data Error = AssertError Act | AuthError
deriving (Show, Eq)
```

4.2 The Maker monad

The reader does not need any abstract understanding of monads to understand the code. What they give us is a nice syntax—the **do** notation—for expressing exceptions and state in a way that is still purely functional.

4.3 Asserting

```
aver x = unless \ x \ (throwError \ (AssertError \ ?act))

none x = preuse \ x \gg \lambda case

Nothing \rightarrow return \ ()

Just _- \rightarrow throwError \ (AssertError \ ?act)

look f = preuse \ f \gg \lambda case

Nothing \rightarrow throwError \ (AssertError \ ?act)

Just x \rightarrow return \ x

want m \ p = m \gg (aver \ . p)

notElem x \ xs = \neg \ (elem \ x \ xs)
```

We define owns id_{urn} id_{lad} as an assertion that the given CDP is owned by the given account.

```
owns id_{\tt urn} \ id_{\tt lad} = {f do}

want \ (look \ ({\tt vat.urns.} \ ix \ id_{\tt urn} \ . \ {\tt lad})) \ (\equiv id_{\tt lad})
```

4.4 Modifiers

```
\begin{array}{l} \text{auth } continue = \mathbf{do} \\ s \leftarrow use \ sender \\ unless \ (s \equiv id_{god}) \\ (\textit{throwError} \ \text{AuthError}) \\ continue \end{array}
```

Chapter 5

Sketches for property stuff...

Testing

```
data Parameter =
   Fix | Par | Way
maintains
    :: Eq \ a \Rightarrow Lens' \ System \ a \rightarrow Maker ()
             \rightarrow System \rightarrow Bool
maintains\ p = \lambda m\ {
m sys}_0 
ightarrow
   case exec \operatorname{sys}_0 m \text{ of }
    On success, data must be compared for equality
      Right sys_1 \rightarrow view p sys_0 \equiv view p sys_1
    On rollback, data is maintained by definition
      Left \_ \rightarrow True
changesOnly
    :: Lens' System a \rightarrow Maker ()
    \rightarrow System \rightarrow Bool
changesOnly p = \lambda m sys_0 \rightarrow
   case exec sys<sub>0</sub> m of
    On success, equalize p and compare
      Right sys_1 \rightarrow set \ p \ (view \ p \ sys_1) \ sys_0 \equiv sys_1
    On rollback, data is maintained by definition
      Left _
                     \rightarrow True
```

Appendix A

Prelude

```
module Maker.Prelude (
  module Maker.Prelude,
  module X
) where
import Prelude as X (
 Conversions to and from strings
  Read (..), Show (..),
 Comparisons
  Eq(...), Ord(...),
 Core abstractions
  Functor
               (fmap),
  Applicative (),
  Monad
               (return, (\gg)),
 Numeric classes
  Num (..), Integral (), Enum (),
 Numeric conversions
  Real (..), Fractional (..),
  RealFrac (..),
  fromIntegral,
 Simple types
  Integer, Int, String,
 Algebraic types
  Bool
         (True, False),
```

```
Maybe (Just, Nothing), Either (Right, Left), 
Functional operators (.), (\$), 
Numeric operators (+), (-), (*), (/), (\uparrow), (\uparrow\uparrow), div, 
Utilities all, \neg, elem, 
Constants mempty, \bot, otherwise)
```

We use a typical composition of monad transformers from the mtl library to structure stateful actions. See section 4.2 (*The Maker monad*).

```
import Control.Monad.State as X (
```

MonadState, Type class of monads with state

 $State T, \hspace{1cm} \hbox{Type constructor that adds state to a monad type} \\$

execStateT, Runs a state monad with given initial state

get, Gets the state in a do blockput) Sets the state in a do block

import Control.Monad.Reader as X (

MonadReader, Type class of monads with "environments" *ask*, Reads the environment in a **do** block

local) Runs a sub-computation with a modified environment

import Control.Monad.Writer as X (

MonadWriter, Type class of monads that emit logs

WriterT, Type constructor that adds logging to a monad type

Writer, Type constructor of logging monads runWriterT, Runs a writer monad transformer

execWriterT, Runs a writer monad transformer keeping only logs

execWriter) Runs a writer monad keeping only logs

import Control.Monad.Except as X (

MonadError, Type class of monads that fail
Except, Type constructor of failing monads
throwError, Short-circuits the monadic computation

runExcept) Runs a failing monad

Our numeric types use decimal fixed-point arithmetic.

```
import Data.Fixed as X (
```

Fixed (..), Type constructor for numbers of given precision

HasResolution (..)) Type class for specifying precisions

We rely on the lens library for accessing nested values. There is no need to understand the theory behind lenses to understand this program. The notation $a \cdot b \cdot c$ denotes a nested accessor much like a.b.c in C-style languages; for more details, consult lens documentation¹.

```
import Control.Lens as X (
  Lens'.
  lens.
   makeLenses.
                    Defines lenses for record fields
   makeFields,
                    Defines lenses for record fields
                    Writes a lens
  set,
   use, preuse,
  Zoom (..),
  view, preview, Reads a lens in a do block
  (\&\sim),
                    Lets us use a do block with setters \lozenge Get rid of this.
   ix,
                    Lens for map retrieval and updating
                    Lens for map insertion
   at,
 Operators for partial state updates in do blocks:
  (:=),
                    Replace
  (-=), (+=), Update arithmetically
   (\% =),
                    Update according to function
  (?=))
                    Insert into map
import Control.Lens.Zoom as X
import Control.Lens.Internal.Zoom as X
```

Where the Solidity code uses mapping, we use Haskell's regular tree-based map type².

For sequences of log entries, we use a sequence structure which has better time complexity than regular lists.

```
import Data.Sequence as X (Seq) import qualified Data.Sequence as Sequence
```

Some less interesting imports are omitted from this document.

¹Gabriel Gonzalez's 2013 article *Program imperatively using Haskell* is a good introduction.

²We assume the axiom that Keccak hash collisions are impossible.

Appendix B

Rounding fixed point numbers

This somewhat arcane-looking code implements a wrapper around the base library's decimal fixed point type, only with x*y and x/y operations that do rounding instead of truncation of their intermediate results.

```
module Maker.Decimal (Decimal, E18, E36, Epsilon (...)) where import Data.Fixed newtype HasResolution e \Rightarrow \text{Decimal } e = \text{D (Fixed } e) deriving (Ord, Eq, Real, RealFrac)
```

We want the printed representations of these numbers to look like "0.01" and not "R 0.01".

```
instance HasResolution e \Rightarrow \text{Read (Decimal } e) where readsPrec\ n\ s = fmap\ (\lambda(x,y) \to (D\ x,y))\ (readsPrec\ n\ s) instance HasResolution e \Rightarrow \text{Show (Decimal } e) where show\ (D\ x) = show\ x
```

In the Num instance, we delegate everything except multiplication.

```
instance HasResolution e \Rightarrow \text{Num (Decimal } e) where x \otimes (D \text{ (MkFixed } a)) * D \text{ (MkFixed } b) = D \text{ (MkFixed } (div (a * b + div (resolution x) 2) (resolution x)))}
D \text{ } a + D \text{ } b = D \text{ } (a + b)
D \text{ } a - D \text{ } b = D \text{ } (a - b)
negate \text{ } (D \text{ } a) = D \text{ } (negate \text{ } a)
abs \text{ } (D \text{ } a) = D \text{ } (abs \text{ } a)
```

```
signum (D a) = D (signum a)

fromInteger i = D (fromInteger i)
```

In the Fractional instance, we delegate everything except division.

```
instance HasResolution e \Rightarrow Fractional (Decimal e) where x@(D \text{ (MkFixed } a)) / D \text{ (MkFixed } b) = D \text{ (MkFixed } (div (a * resolution } x + div b 2) b))
recip (D a) = D (recip a)
fromRational r = D (fromRational r)
```

We define the E18 and E36 symbols and their fixed point multipliers.

```
data E18; data E36 instance HasResolution E18 where resolution \_=10 \uparrow (18 :: Integer) instance HasResolution E36 where resolution \_=10 \uparrow (36 :: Integer)
```

The fixed point number types have well-defined smallest increments (denoted ϵ). This becomes useful when verifying equivalences.

```
class Epsilon t where \epsilon :: t instance HasResolution a \Rightarrow Epsilon (Decimal a) where The use of \bot is safe since resolution ignores the value. \epsilon = 1 \ / \ from Integral \ (resolution \ (\bot :: Fixed \ a))
```