

Group Project

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```
rm(list=ls())

## -- Attaching packages ----- tidyverse 1.3.0 --

## v ggplot2 3.3.2      v purrr  0.3.4
## v tibble  3.0.4      v dplyr  1.0.2
## v tidyr   1.1.2      v stringr 1.4.0
## v readr   1.4.0      v forcats 0.5.0

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()

## corrrplot 0.84 loaded

## Loading required package: lattice

##
## Attaching package: 'caret'

## The following object is masked from 'package:purrr':
##
##     lift

## Classes and Methods for R developed in the
## Political Science Computational Laboratory
## Department of Political Science
## Stanford University
## Simon Jackman
## hurdle and zeroinfl functions by Achim Zeileis

# Creating new variable names for the datasets we will use for this assignment.
data(mlc_churn)
cust <- mlc_churn

load("Customers_To_Predict.RData")

## Warning: namespace 'pbdZMQ' is not available and has been replaced
## by .GlobalEnv when processing object '.pbd_env'
```

```
test <- data.frame(Custmers_to_predict)
```

Making Life Easier with Variable Names

```
# Renamed variables to make it easier to work with.
cust$area_code <- as.factor(sub("area_code_", "", cust$area_code))
cust %>%
  rename(
    acct_length = account_length,
    intl_plan = international_plan,
    vm_plan = voice_mail_plan,
    num_vm_mess = number_vmail_messages,
    tot_day_min = total_day_minutes,
    tot_day_calls = total_day_calls,
    tot_day_chg = total_day_charge,
    tot_eve_min = total_eve_minutes,
    tot_eve_calls = total_eve_calls,
    tot_night_min = total_night_minutes,
    tot_night_calls = total_night_calls,
    tot_night_chg = total_night_charge,
    tot_intl_min = total_intl_minutes,
    tot_intl_calls = total_intl_calls,
    tot_intl_chg = total_intl_charge,
    num_cust_serv_calls = number_customer_service_calls
  ) -> cust
cust
```

```
## # A tibble: 5,000 x 20
##   state acct_length area_code intl_plan vm_plan num_vm_mess tot_day_min
##   <fct>      <int> <fct>      <fct>      <fct>      <int>      <dbl>
##  1 KS          128 415      no        yes         25       265.
##  2 OH          107 415      no        yes         26       162.
##  3 NJ          137 415      no        no           0       243.
##  4 OH           84 408      yes       no           0       299.
##  5 OK           75 415      yes       no           0       167.
##  6 AL          118 510      yes       no           0       223.
##  7 MA          121 510      no        yes         24       218.
##  8 MO          147 415      yes       no           0       157.
##  9 LA          117 408      no        no           0       184.
## 10 WV          141 415      yes       yes          37       259.
## # ... with 4,990 more rows, and 13 more variables: tot_day_calls <int>,
## #   tot_day_chg <dbl>, tot_eve_min <dbl>, tot_eve_calls <int>,
## #   total_eve_charge <dbl>, tot_night_min <dbl>, tot_night_calls <int>,
## #   tot_night_chg <dbl>, tot_intl_min <dbl>, tot_intl_calls <int>,
## #   tot_intl_chg <dbl>, num_cust_serv_calls <int>, churn <fct>
```

```
# The types in the dataset all look good but will have to create some dummy variables. Will do that next
str(cust)
```

```
## tibble [5,000 x 20] (S3: tbl_df/tbl/data.frame)
## $ state      : Factor w/ 51 levels "AK","AL","AR",...: 17 36 32 36 37 2 20 25 19 50 ...
```

```
## $ acct_length      : int [1:5000] 128 107 137 84 75 118 121 147 117 141 ...
## $ area_code        : Factor w/ 3 levels "408","415","510": 2 2 2 1 2 3 3 2 1 2 ...
## $ intl_plan        : Factor w/ 2 levels "no","yes": 1 1 1 2 2 2 1 2 1 2 ...
## $ vm_plan          : Factor w/ 2 levels "no","yes": 2 2 1 1 1 1 2 1 1 2 ...
## $ num_vm_mess       : int [1:5000] 25 26 0 0 0 0 24 0 0 37 ...
## $ tot_day_min       : num [1:5000] 265 162 243 299 167 ...
## $ tot_day_calls     : int [1:5000] 110 123 114 71 113 98 88 79 97 84 ...
## $ tot_day_chg       : num [1:5000] 45.1 27.5 41.4 50.9 28.3 ...
## $ tot_eve_min       : num [1:5000] 197.4 195.5 121.2 61.9 148.3 ...
## $ tot_eve_calls     : int [1:5000] 99 103 110 88 122 101 108 94 80 111 ...
## $ total_eve_charge   : num [1:5000] 16.78 16.62 10.3 5.26 12.61 ...
## $ tot_night_min     : num [1:5000] 245 254 163 197 187 ...
## $ tot_night_calls   : int [1:5000] 91 103 104 89 121 118 118 96 90 97 ...
## $ tot_night_chg     : num [1:5000] 11.01 11.45 7.32 8.86 8.41 ...
## $ tot_intl_min      : num [1:5000] 10 13.7 12.2 6.6 10.1 6.3 7.5 7.1 8.7 11.2 ...
## $ tot_intl_calls    : int [1:5000] 3 3 5 7 3 6 7 6 4 5 ...
## $ tot_intl_chg      : num [1:5000] 2.7 3.7 3.29 1.78 2.73 1.7 2.03 1.92 2.35 3.02 ...
## $ num_cust_serv_calls: int [1:5000] 1 1 0 2 3 0 3 0 1 0 ...
## $ churn             : Factor w/ 2 levels "yes","no": 2 2 2 2 2 2 2 2 2 2 ...
```

```
tail(cust)
```

```
## # A tibble: 6 x 20
##   state acct_length area_code intl_plan vm_plan num_vm_mess tot_day_min
##   <fct>      <int> <fct>      <fct>      <fct>      <int>      <dbl>
## 1 NC          75 408      no        no          0        171.
## 2 HI          50 408      no        yes         40        236.
## 3 WV         152 415      no        no          0        184.
## 4 DC          61 415      no        no          0        141.
## 5 DC         109 510      no        no          0        189.
## 6 VT          86 415      no        yes         34        129.
## # ... with 13 more variables: tot_day_calls <int>, tot_day_chg <dbl>,
## #   tot_eve_min <dbl>, tot_eve_calls <int>, total_eve_charge <dbl>,
## #   tot_night_min <dbl>, tot_night_calls <int>, tot_night_chg <dbl>,
## #   tot_intl_min <dbl>, tot_intl_calls <int>, tot_intl_chg <dbl>,
## #   num_cust_serv_calls <int>, churn <fct>
```

```
colMeans(is.na(cust))
```

```
##           state      acct_length      area_code      intl_plan
##           0           0           0           0
##      vm_plan      num_vm_mess      tot_day_min      tot_day_calls
##           0           0           0           0
##      tot_day_chg      tot_eve_min      tot_eve_calls      total_eve_charge
##           0           0           0           0
##      tot_night_min      tot_night_calls      tot_night_chg      tot_intl_min
##           0           0           0           0
##      tot_intl_calls      tot_intl_chg      num_cust_serv_calls      churn
##           0           0           0           0
```

```
summary(cust)
```

```
##      state      acct_length  area_code  intl_plan  vm_plan
## WV       : 158    Min.      : 1.0    408:1259  no :4527  no :3677
## MN       : 125    1st Qu.: 73.0    415:2495  yes: 473  yes:1323
## AL       : 124    Median   :100.0    510:1246
## ID       : 119    Mean      :100.3
## VA       : 118    3rd Qu.:127.0
## OH       : 116    Max.      :243.0
## (Other):4240
##      num_vm_mess      tot_day_min      tot_day_calls      tot_day_chg      tot_eve_min
## Min.      : 0.000    Min.      : 0.0    Min.      : 0    Min.      : 0.00    Min.      : 0.0
## 1st Qu.: 0.000    1st Qu.:143.7    1st Qu.: 87    1st Qu.:24.43    1st Qu.:166.4
## Median : 0.000    Median   :180.1    Median   :100    Median   :30.62    Median   :201.0
## Mean      : 7.755    Mean      :180.3    Mean      :100    Mean      :30.65    Mean      :200.6
## 3rd Qu.:17.000    3rd Qu.:216.2    3rd Qu.:113    3rd Qu.:36.75    3rd Qu.:234.1
## Max.      :52.000    Max.      :351.5    Max.      :165    Max.      :59.76    Max.      :363.7
##
##      tot_eve_calls      total_eve_charge      tot_night_min      tot_night_calls
## Min.      : 0.0    Min.      : 0.00    Min.      : 0.0    Min.      : 0.00
## 1st Qu.: 87.0    1st Qu.:14.14    1st Qu.:166.9    1st Qu.: 87.00
## Median :100.0    Median   :17.09    Median   :200.4    Median   :100.00
## Mean      :100.2    Mean      :17.05    Mean      :200.4    Mean      : 99.92
## 3rd Qu.:114.0    3rd Qu.:19.90    3rd Qu.:234.7    3rd Qu.:113.00
## Max.      :170.0    Max.      :30.91    Max.      :395.0    Max.      :175.00
##
##      tot_night_chg      tot_intl_min      tot_intl_calls      tot_intl_chg
## Min.      : 0.000    Min.      : 0.00    Min.      : 0.000    Min.      :0.000
## 1st Qu.: 7.510    1st Qu.: 8.50    1st Qu.: 3.000    1st Qu.:2.300
## Median : 9.020    Median   :10.30    Median   : 4.000    Median   :2.780
## Mean      : 9.018    Mean      :10.26    Mean      : 4.435    Mean      :2.771
## 3rd Qu.:10.560    3rd Qu.:12.00    3rd Qu.: 6.000    3rd Qu.:3.240
## Max.      :17.770    Max.      :20.00    Max.      :20.000    Max.      :5.400
##
##      num_cust_serv_calls      churn
## Min.      :0.00      yes: 707
## 1st Qu.:1.00      no :4293
## Median :1.00
## Mean      :1.57
## 3rd Qu.:2.00
## Max.      :9.00
##
```

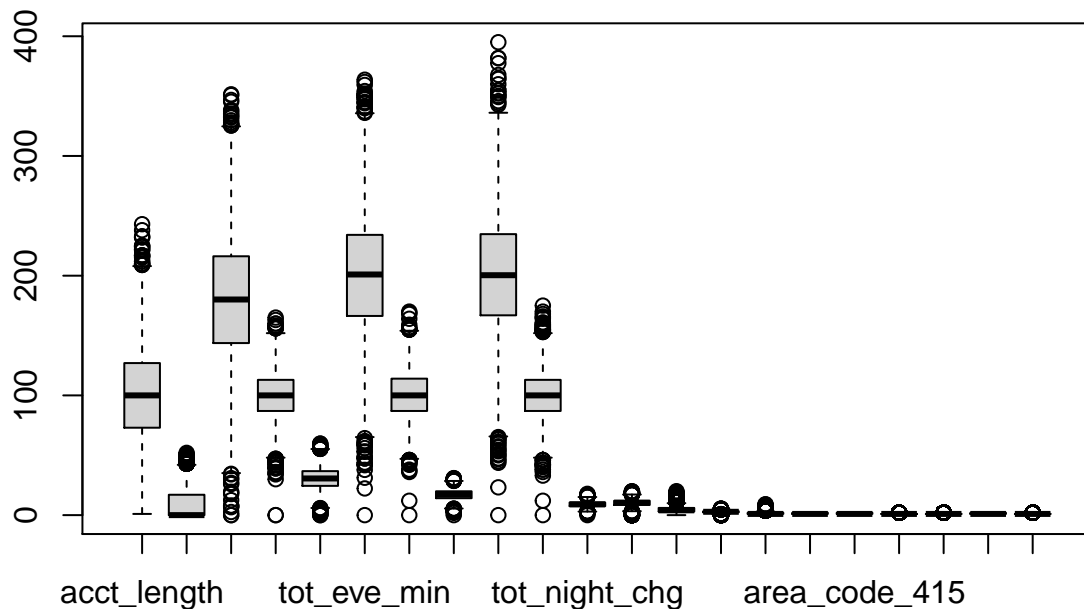
Creating dummy variables for area_code, intl_plan, vm_plan, and churn to separate each of the factors

```
cust %>%
  dummy_cols(c("area_code",
               "intl_plan",
               "vm_plan",
               "churn"),
             remove_selected_columns = TRUE) -> cust

cust <- cust[, c(-20, -22, -25)]

cust[, 17:22] <- lapply(cust[, 17:22], factor)
```

```
# May be a few outliers but, to be honest, nothing seems so extreme that I think it is worth changing.
boxplot(cust[, 2:22])
```

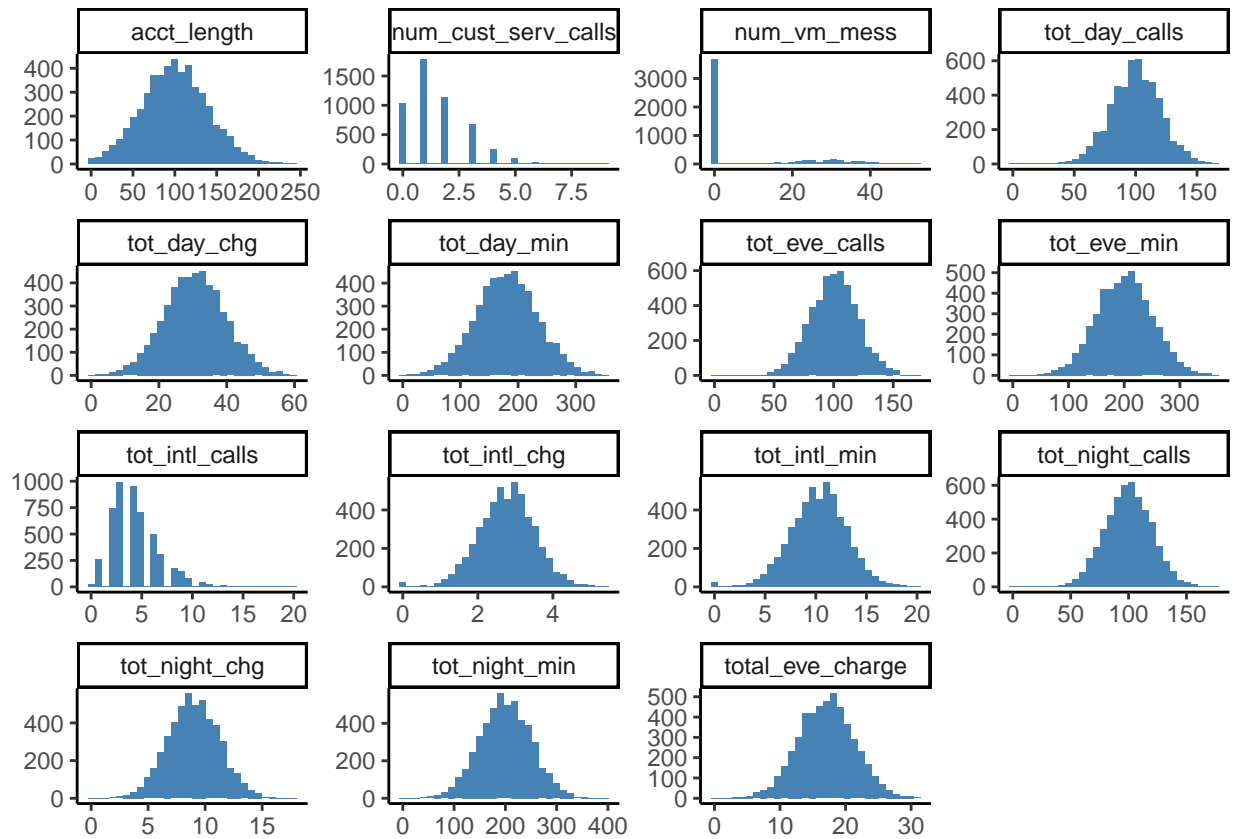


```
cust %>%
  filter(tot_day_calls < 1)
```

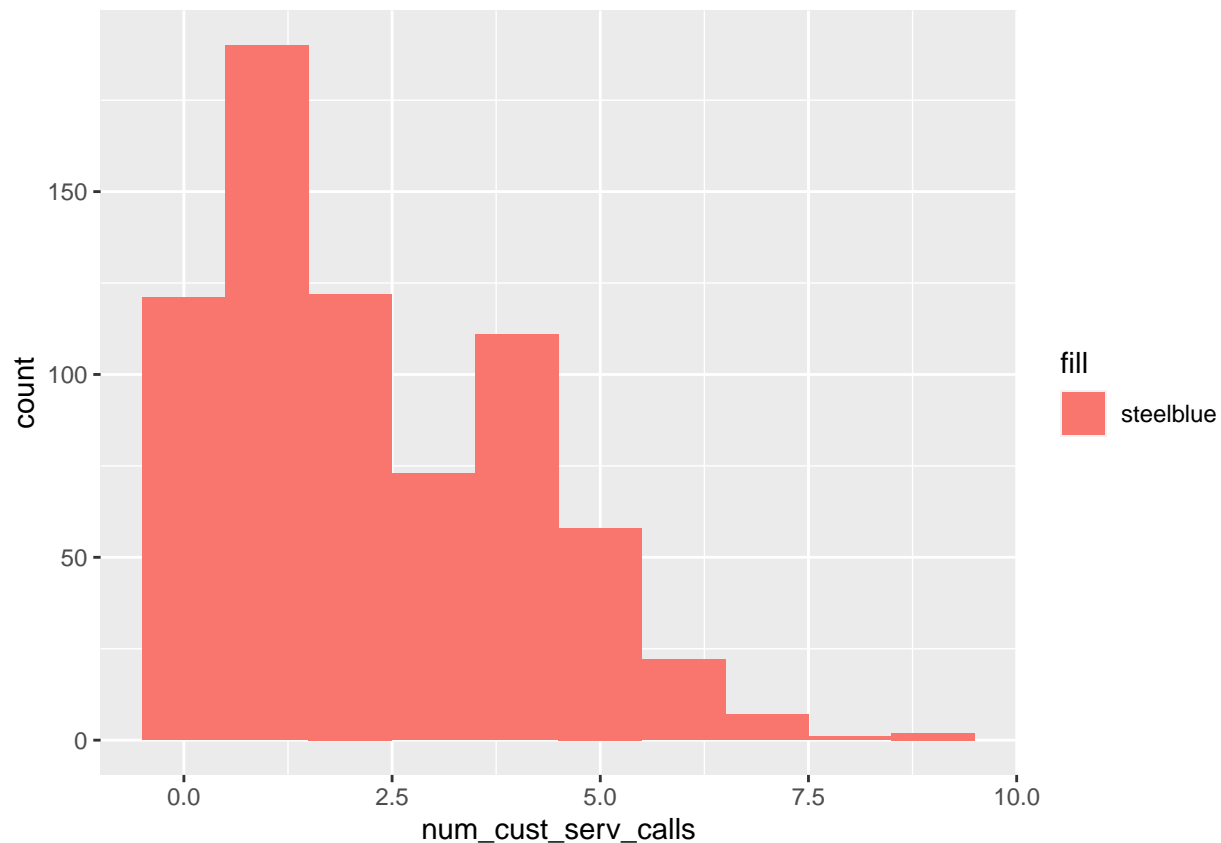
```
## # A tibble: 2 x 22
##   state acct_length num_vm_mess tot_day_min tot_day_calls tot_day_chg
##   <fct>      <int>      <int>      <dbl>      <int>      <dbl>
## 1 SD          98          0          0          0          0
## 2 VT         101          0          0          0          0
## # ... with 16 more variables: tot_eve_min <dbl>, tot_eve_calls <int>,
## #   total_eve_charge <dbl>, tot_night_min <dbl>, tot_night_calls <int>,
## #   tot_night_chg <dbl>, tot_intl_min <dbl>, tot_intl_calls <int>,
## #   tot_intl_chg <dbl>, num_cust_serv_calls <int>, area_code_408 <fct>,
## #   area_code_415 <fct>, area_code_510 <fct>, intl_plan_yes <fct>,
## #   vm_plan_yes <fct>, churn_yes <fct>
```

```
cust[2:16] %>%
  gather(key = Variable, value = Value) %>%
  ggplot() +
    geom_histogram(aes(x = Value), fill = "steelblue") +
    facet_wrap(~Variable, scales='free') +
    theme_classic() +
    theme(aspect.ratio = 0.5, axis.title = element_blank(), panel.grid = element_blank())
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



```
cust %>%
  filter(churn_yes == 1) %>%
  ggplot(mapping = aes(x = num_cust_serv_calls)) +
  geom_histogram(aes(fill = "steelblue"), binwidth = 1)
```



```
cust %>%
  count(churn_yes)
```

```
## # A tibble: 2 x 2
##   churn_yes     n
##   <fct>       <int>
## 1 0         4293
## 2 1          707
```

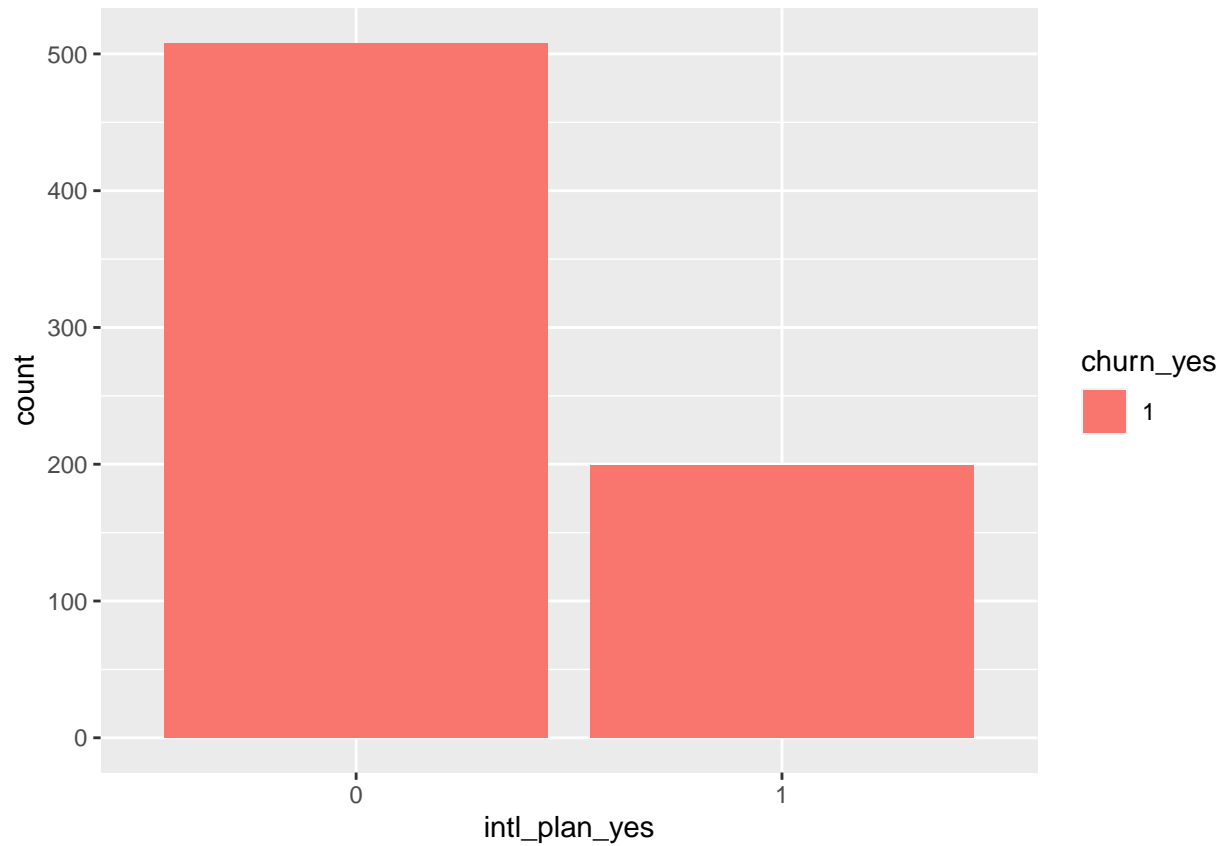
```
cust %>%
  filter(churn_yes == 1 & num_cust_serv_calls >= 1 & num_cust_serv_calls <= 4)%>%
  summarise("% churned after making betw 1 and 4 cust service calls" = n()/707*100)
```

```
## # A tibble: 1 x 1
##   '% churned after making betw 1 and 4 cust service calls'
##                                     <dbl>
## 1                                     70.2
```

```
cust %>%
  filter(churn_yes== 1) -> churn_cust
```

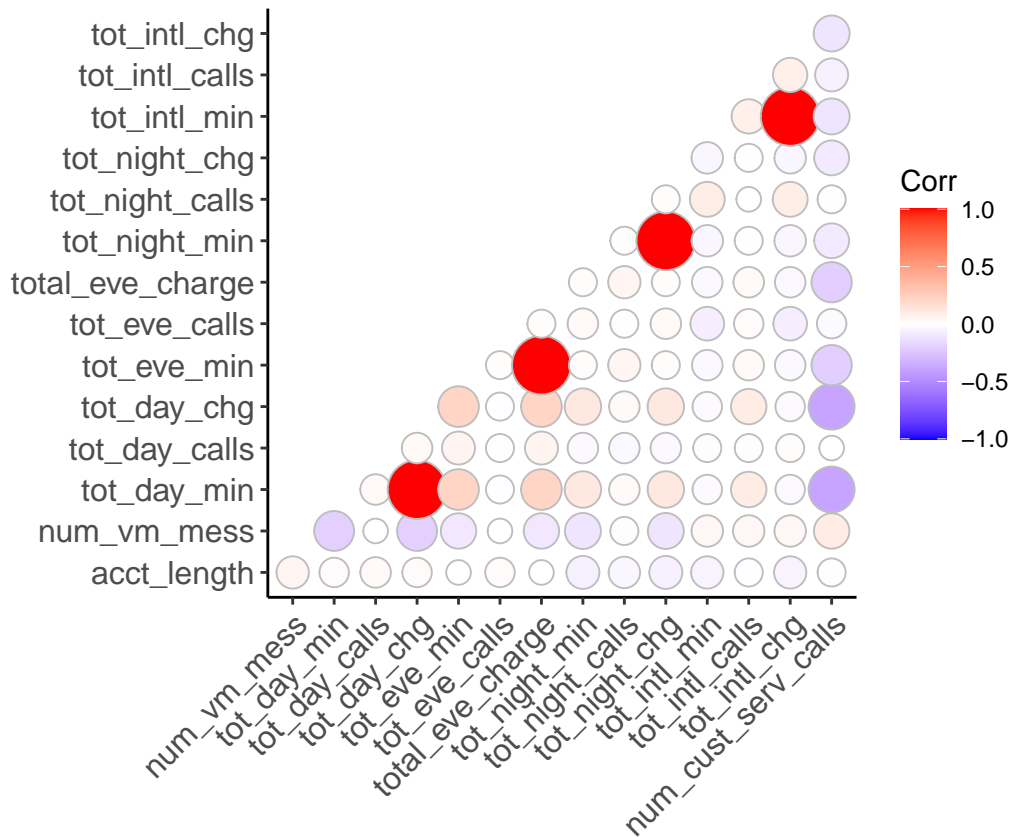
```
cust %>%
  filter(churn_yes== 1) %>%
  ggplot(mapping = aes(x = intl_plan_yes)) +
  geom_histogram(aes(fill = churn_yes), stat = "count")
```

```
## Warning: Ignoring unknown parameters: binwidth, bins, pad
```



Most customers churn when they make 1 to 3 customer service calls. Also, about 30% of customers churn if they have a international plan.

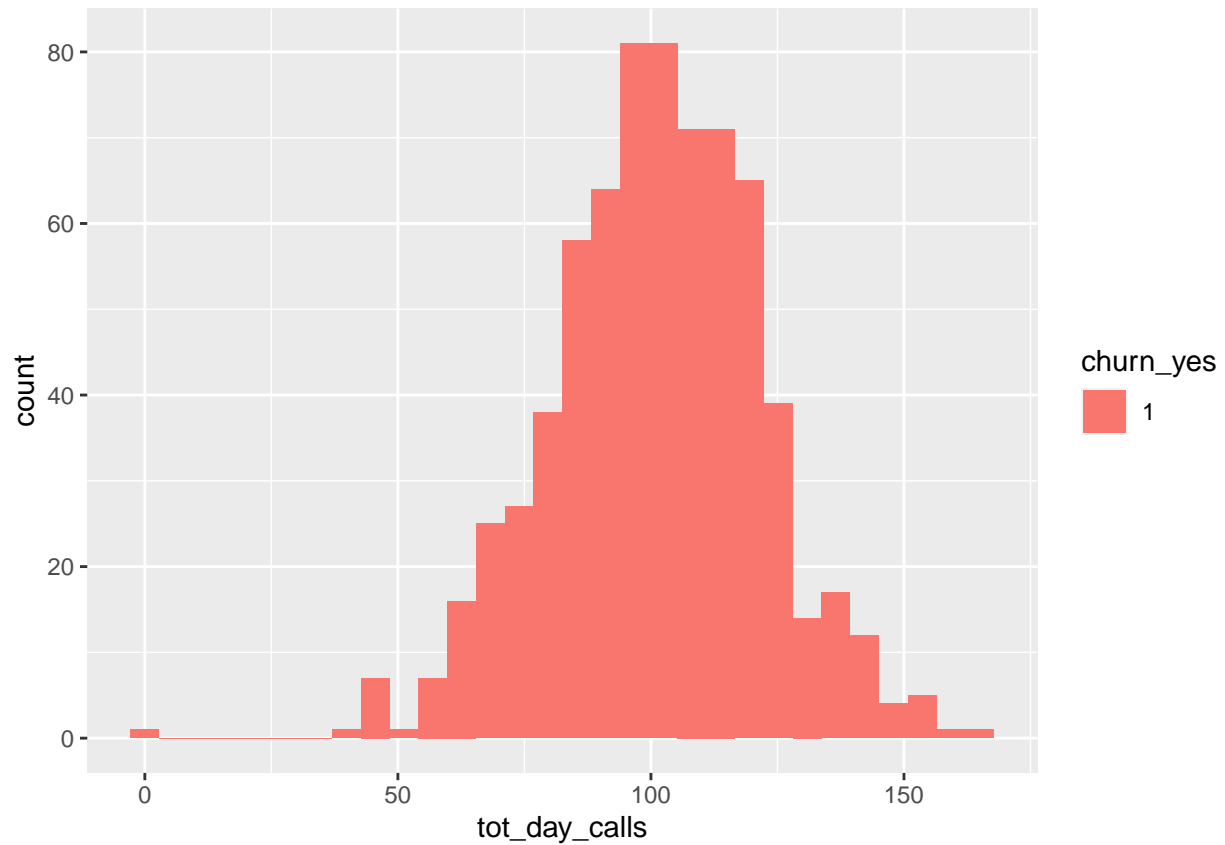
```
cor(churn_cust[, 2:16]) -> cc  
ggcorrplot(cc, method = "circle", type = "lower", ggtheme = ggplot2::theme_classic)
```

Some positive correlation between number of customer service calls and total day charges also total day minutes. Actually, most of the variables have some positive correlation to customer service calls except total day calls, total evening calls, account length, and total night calls.

```
churn_cust %>%
  ggplot(mapping = aes(x = tot_day_calls)) +
  geom_histogram(aes(fill = churn_yes))
```

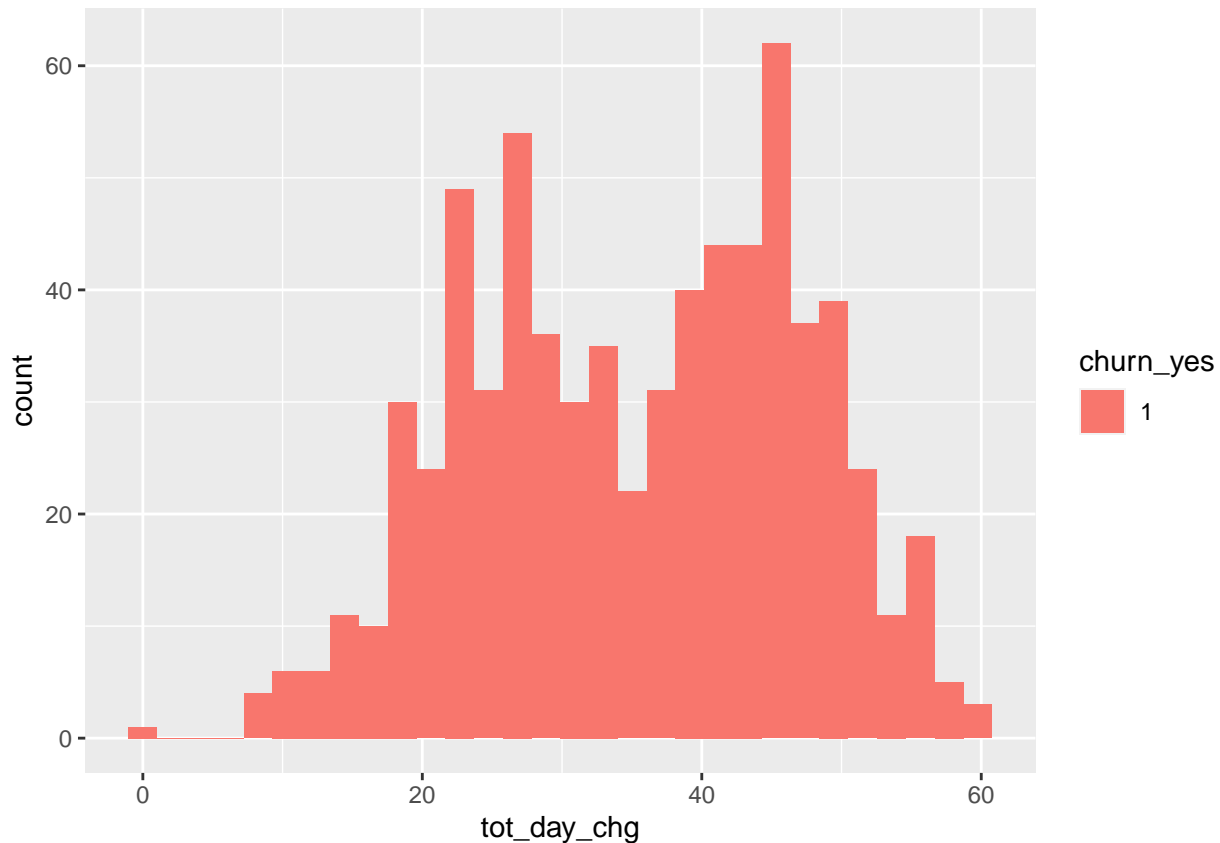
```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



Most of the people seem to churn between 75 to 125 calls per day.

```
churn_cust %>%  
  ggplot(mapping = aes(x = tot_day_chg)) +  
  geom_histogram(aes(fill = churn_yes))
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



Most people churn when charges are between 20 to 50 per day.

Based on the above, I might suggest that the reason people are churning is that the cost of daily phone call charges during the day are too much. FYI I think this data is really old as I remember when Cell Phone companies used to charge more for calls made during the day than the evening...

```
# Partitioning the dataset into train and validation sets.
set.seed(15)
tra_val <- createDataPartition(cust$churn_yes, list = FALSE, p = .8)
train <- cust[tra_val, ]
```

```
## Warning: The 'i' argument of '['()' can't be a matrix as of tibble 3.0.0.
## Convert to a vector.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_warnings()' to see where this warning was generated.
```

```
valid <- cust[-tra_val, ]
```

```
norm <- preprocess(train, method = c("scale", "center"))
train <- predict(norm, train)

summary(train)
```

```
##      state      acct_length      num_vm_mess      tot_day_min
## WV      : 124      Min.      :-2.4987      Min.      :-0.5762      Min.      :-3.339290
```

```
## MN      : 104    1st Qu.: -0.6923    1st Qu.: -0.5762    1st Qu.: -0.677937
## AL      : 97     Median : -0.0149    Median : -0.5762    Median : 0.001754
## OH      : 96     Mean    : 0.0000    Mean    : 0.0000    Mean    : 0.000000
## ID      : 93     3rd Qu.: 0.6625    3rd Qu.: 0.6733    3rd Qu.: 0.670334
## NJ      : 93     Max.    : 3.5728    Max.    : 3.2456    Max.    : 3.170560
## (Other):3394
## tot_day_calls    tot_day_chg        tot_eve_min        tot_eve_calls
## Min.    : -5.075602  Min.    : -3.339354  Min.    : -3.53701  Min.    : -4.458807
## 1st Qu.: -0.661373  1st Qu.: -0.677890  1st Qu.: -0.67859  1st Qu.: -0.663570
## Median : -0.001775  Median : 0.001911  Median : 0.01035  Median : -0.005729
## Mean    : 0.000000  Mean    : 0.000000  Mean    : 0.00000  Mean    : 0.000000
## 3rd Qu.: 0.657822  3rd Qu.: 0.670817  3rd Qu.: 0.67166  3rd Qu.: 0.702715
## Max.    : 3.296212  Max.    : 3.171046  Max.    : 3.20239  Max.    : 3.536491
##
## total_eve_charge  tot_night_min    tot_night_calls    tot_night_chg
## Min.    : -3.5361  Min.    : -3.09433  Min.    : -4.387094  Min.    : -3.09284
## 1st Qu.: -0.6795  1st Qu.: -0.66675  1st Qu.: -0.650206  1st Qu.: -0.66505
## Median : 0.0103  Median : -0.01005  Median : -0.002478  Median : -0.01209
## Mean    : 0.0000  Mean    : 0.00000  Mean    : 0.000000  Mean    : 0.00000
## 3rd Qu.: 0.6722  3rd Qu.: 0.67622  3rd Qu.: 0.695074  3rd Qu.: 0.67593
## Max.    : 3.2013  Max.    : 3.57512  Max.    : 3.734411  Max.    : 3.57700
##
## tot_intl_min      tot_intl_calls    tot_intl_chg        num_cust_serv_calls
## Min.    : -3.68557  Min.    : -1.8180  Min.    : -3.686659  Min.    : -1.1938
## 1st Qu.: -0.63440  1st Qu.: -0.5874  1st Qu.: -0.628489  1st Qu.: -0.4310
## Median : 0.01173  Median : -0.1773  Median : 0.009737  Median : -0.4310
## Mean    : 0.00000  Mean    : 0.0000  Mean    : 0.000000  Mean    : 0.0000
## 3rd Qu.: 0.62196  3rd Qu.: 0.6431  3rd Qu.: 0.621371  3rd Qu.: 0.3317
## Max.    : 3.38596  Max.    : 6.3857  Max.    : 3.387020  Max.    : 5.6710
##
## area_code_408 area_code_415 area_code_510 intl_plan_yes vm_plan_yes churn_yes
## 0:2995        0:1985        0:3022        0:3611        0:2932        0:3435
## 1:1006        1:2016        1: 979        1: 390        1:1069        1: 566
##
##
##
##
##
```

```
# Creating a model for logistic regression based upon all the variables. I will create another logistic
model1 <- glm(churn_yes~., family = "binomial", data = train)
summary(model1)
```

```
##
## Call:
## glm(formula = churn_yes ~ ., family = "binomial", data = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.1239  -0.4847  -0.3016  -0.1628   3.2176
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -3.134e+00  6.580e-01  -4.763 1.91e-06 ***
```

## stateAL	5.381e-01	7.421e-01	0.725	0.468356
## stateAR	9.838e-01	7.519e-01	1.308	0.190740
## stateAZ	7.306e-01	7.745e-01	0.943	0.345549
## stateCA	2.010e+00	7.516e-01	2.675	0.007483 **
## stateCO	6.791e-01	7.625e-01	0.891	0.373157
## stateCT	1.226e+00	7.242e-01	1.693	0.090393 .
## stateDC	7.744e-01	7.742e-01	1.000	0.317205
## stateDE	4.898e-01	7.551e-01	0.649	0.516549
## stateFL	6.173e-01	7.596e-01	0.813	0.416423
## stateGA	8.287e-01	7.573e-01	1.094	0.273803
## stateHI	2.882e-01	8.066e-01	0.357	0.720808
## stateIA	9.718e-01	7.905e-01	1.229	0.218904
## stateID	6.985e-01	7.411e-01	0.943	0.345934
## stateIL	7.138e-02	8.042e-01	0.089	0.929274
## stateIN	6.697e-01	7.472e-01	0.896	0.370096
## stateKS	8.408e-01	7.412e-01	1.134	0.256606
## stateKY	9.899e-01	7.392e-01	1.339	0.180531
## stateLA	7.616e-01	8.043e-01	0.947	0.343660
## stateMA	1.224e+00	7.280e-01	1.682	0.092645 .
## stateMD	1.123e+00	7.135e-01	1.574	0.115391
## stateME	1.465e+00	7.150e-01	2.048	0.040516 *
## stateMI	1.484e+00	7.143e-01	2.078	0.037713 *
## stateMN	1.158e+00	7.101e-01	1.631	0.102931
## stateMO	7.419e-01	7.605e-01	0.975	0.329335
## stateMS	1.094e+00	7.291e-01	1.500	0.133641
## stateMT	2.055e+00	7.025e-01	2.925	0.003445 **
## stateNC	5.518e-01	7.545e-01	0.731	0.464593
## stateND	2.730e-01	7.925e-01	0.344	0.730540
## stateNE	3.153e-01	8.033e-01	0.392	0.694705
## stateNH	9.399e-01	7.440e-01	1.263	0.206458
## stateNJ	1.693e+00	6.965e-01	2.431	0.015070 *
## stateNM	6.506e-01	7.641e-01	0.851	0.394494
## stateNV	1.454e+00	7.186e-01	2.023	0.043095 *
## stateNY	1.043e+00	7.233e-01	1.441	0.149460
## stateOH	1.058e+00	7.213e-01	1.466	0.142528
## stateOK	7.562e-01	7.503e-01	1.008	0.313511
## stateOR	1.037e+00	7.173e-01	1.446	0.148198
## statePA	2.942e-01	8.214e-01	0.358	0.720230
## stateRI	6.277e-02	8.026e-01	0.078	0.937655
## stateSC	1.393e+00	7.424e-01	1.877	0.060543 .
## stateSD	6.270e-01	7.728e-01	0.811	0.417228
## stateTN	1.081e+00	7.401e-01	1.460	0.144266
## stateTX	1.500e+00	7.045e-01	2.129	0.033279 *
## stateUT	1.442e+00	7.183e-01	2.007	0.044771 *
## stateVA	8.492e-03	7.909e-01	0.011	0.991433
## stateVT	3.919e-01	7.555e-01	0.519	0.603960
## stateWA	2.046e+00	7.044e-01	2.905	0.003677 **
## stateWI	1.434e-01	8.005e-01	0.179	0.857845
## stateWV	1.173e+00	6.977e-01	1.681	0.092835 .
## stateWY	1.635e-01	7.573e-01	0.216	0.829065
## acct_length	7.681e-02	5.268e-02	1.458	0.144851
## num_vm_mess	3.424e-01	2.331e-01	1.469	0.141906
## tot_day_min	1.869e+02	1.696e+02	1.102	0.270331
## tot_day_calls	9.778e-03	5.284e-02	0.185	0.853208

```
## tot_day_chg      -1.861e+02  1.695e+02  -1.098  0.272310
## tot_eve_min      1.387e+00  8.036e+01   0.017  0.986233
## tot_eve_calls    -2.516e-02  5.352e-02  -0.470  0.638184
## total_eve_charge -9.732e-01  8.036e+01  -0.012  0.990338
## tot_night_min     6.899e+00  4.250e+01   0.162  0.871041
## tot_night_calls  -4.381e-02  5.308e-02  -0.825  0.409216
## tot_night_chg    -6.663e+00  4.250e+01  -0.157  0.875406
## tot_intl_min      6.686e+00  1.416e+01   0.472  0.636805
## tot_intl_calls    -1.746e-01  5.676e-02  -3.076  0.002097 **
## tot_intl_chg      -6.428e+00  1.416e+01  -0.454  0.649851
## num_cust_serv_calls 6.876e-01  4.975e-02  13.822  < 2e-16 ***
## area_code_4081    6.734e-02  1.520e-01   0.443  0.657757
## area_code_4151    2.134e-03  1.315e-01   0.016  0.987050
## area_code_5101      NA         NA         NA         NA
## intl_plan_yes1     2.328e+00  1.430e-01  16.282  < 2e-16 ***
## vm_plan_yes1      -1.854e+00  5.462e-01  -3.394  0.000689 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##    Null deviance: 3261.7  on 4000  degrees of freedom
## Residual deviance: 2409.9  on 3931  degrees of freedom
## AIC: 2549.9
##
## Number of Fisher Scoring iterations: 6
```

```
varImp(model1)
```

```
##              Overall
## stateAL      0.72515618
## stateAR      1.30839248
## stateAZ      0.94325869
## stateCA      2.67456524
## stateCO      0.89057595
## stateCT      1.69333043
## stateDC      1.00021843
## stateDE      0.64867439
## stateFL      0.81264286
## stateGA      1.09434753
## stateHI      0.35737948
## stateIA      1.22944797
## stateID      0.94250571
## stateIL      0.08875791
## stateIN      0.89629437
## stateKS      1.13444916
## stateKY      1.33912093
## stateLA      0.94695782
## stateMA      1.68160723
## stateMD      1.57441732
## stateME      2.04844752
## stateMI      2.07796097
## stateMN      1.63080845
## stateMO      0.97545380
```

```

## stateMS          1.49989795
## stateMT          2.92493254
## stateNC          0.73130415
## stateND          0.34440742
## stateNE          0.39247764
## stateNH          1.26336646
## stateNJ          2.43069533
## stateNM          0.85149651
## stateNV          2.02278929
## stateNY          1.44144154
## stateOH          1.46644000
## stateOK          1.00788312
## stateOR          1.44592752
## statePA          0.35815114
## stateRI          0.07821706
## stateSC          1.87682117
## stateSD          0.81123889
## stateTN          1.46008886
## stateTX          2.12870520
## stateUT          2.00679581
## stateVA          0.01073699
## stateVT          0.51871441
## stateWA          2.90458280
## stateWI          0.17911758
## stateWV          1.68062764
## stateWY          0.21590068
## acct_length      1.45796170
## num_vm_mess      1.46873096
## tot_day_min      1.10230009
## tot_day_calls    0.18502634
## tot_day_chg      1.09775899
## tot_eve_min      0.01725559
## tot_eve_calls    0.47023905
## total_eve_charge 0.01210992
## tot_night_min    0.16233690
## tot_night_calls  0.82527450
## tot_night_chg    0.15679612
## tot_intl_min     0.47217001
## tot_intl_calls   3.07618309
## tot_intl_chg     0.45396852
## num_cust_serv_calls 13.82170417
## area_code_4081   0.44301226
## area_code_4151   0.01623066
## intl_plan_yes1   16.28176408
## vm_plan_yes1     3.39400328

```

I ran a grid search algorithm and the best AIC model was the one below.

```

model3 <- glm(churn_yes ~ acct_length + num_vm_mess + tot_day_min + tot_day_calls +
  tot_day_chg + tot_eve_min + total_eve_charge + tot_night_min +
  tot_night_chg + tot_intl_min + tot_intl_calls + tot_intl_chg +
  num_cust_serv_calls + area_code_415 + intl_plan_yes + vm_plan_yes +
  tot_day_min:num_cust_serv_calls + tot_day_min:tot_day_chg +
  tot_intl_min:intl_plan_yes + tot_eve_min:num_cust_serv_calls +
  tot_day_min:vm_plan_yes + tot_day_min:tot_eve_min + tot_day_chg:tot_night_min +

```

```

tot_intl_calls:intl_plan_yes + tot_day_chg:intl_plan_yes +
tot_eve_min:vm_plan_yes + num_cust_serv_calls:intl_plan_yes +
tot_night_chg:vm_plan_yes + tot_night_min:num_cust_serv_calls +
acct_length:num_vm_mess + total_eve_charge:tot_night_min +
tot_intl_min:tot_intl_calls + num_cust_serv_calls:vm_plan_yes +
tot_day_calls:total_eve_charge + tot_night_min:vm_plan_yes +
total_eve_charge:num_cust_serv_calls + intl_plan_yes:vm_plan_yes +
num_vm_mess:area_code_415 + tot_eve_min:total_eve_charge +
tot_intl_chg:num_cust_serv_calls + tot_day_calls:num_cust_serv_calls +
tot_day_chg:num_cust_serv_calls + tot_intl_calls:vm_plan_yes +
tot_eve_min:tot_night_chg + tot_day_min:tot_night_chg + acct_length:tot_night_chg +
acct_length:tot_night_min + tot_intl_calls:num_cust_serv_calls, family = "binomial", data = train)

modell1 <- glm(churn_yes~., family = "binomial", data = train)
summary(modell1)

```

```

##
## Call:
## glm(formula = churn_yes ~ ., family = "binomial", data = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.1239  -0.4847  -0.3016  -0.1628   3.2176
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -3.134e+00  6.580e-01  -4.763  1.91e-06 ***
## stateAL       5.381e-01  7.421e-01   0.725  0.468356
## stateAR       9.838e-01  7.519e-01   1.308  0.190740
## stateAZ       7.306e-01  7.745e-01   0.943  0.345549
## stateCA       2.010e+00  7.516e-01   2.675  0.007483 **
## stateCO       6.791e-01  7.625e-01   0.891  0.373157
## stateCT       1.226e+00  7.242e-01   1.693  0.090393 .
## stateDC       7.744e-01  7.742e-01   1.000  0.317205
## stateDE       4.898e-01  7.551e-01   0.649  0.516549
## stateFL       6.173e-01  7.596e-01   0.813  0.416423
## stateGA       8.287e-01  7.573e-01   1.094  0.273803
## stateHI       2.882e-01  8.066e-01   0.357  0.720808
## stateIA       9.718e-01  7.905e-01   1.229  0.218904
## stateID       6.985e-01  7.411e-01   0.943  0.345934
## stateIL       7.138e-02  8.042e-01   0.089  0.929274
## stateIN       6.697e-01  7.472e-01   0.896  0.370096
## stateKS       8.408e-01  7.412e-01   1.134  0.256606
## stateKY       9.899e-01  7.392e-01   1.339  0.180531
## stateLA       7.616e-01  8.043e-01   0.947  0.343660
## stateMA       1.224e+00  7.280e-01   1.682  0.092645 .
## stateMD       1.123e+00  7.135e-01   1.574  0.115391
## stateME       1.465e+00  7.150e-01   2.048  0.040516 *
## stateMI       1.484e+00  7.143e-01   2.078  0.037713 *
## stateMN       1.158e+00  7.101e-01   1.631  0.102931
## stateMO       7.419e-01  7.605e-01   0.975  0.329335
## stateMS       1.094e+00  7.291e-01   1.500  0.133641

```



```

## stateMT          2.055e+00  7.025e-01  2.925 0.003445 **
## stateNC          5.518e-01  7.545e-01  0.731 0.464593
## stateND          2.730e-01  7.925e-01  0.344 0.730540
## stateNE          3.153e-01  8.033e-01  0.392 0.694705
## stateNH          9.399e-01  7.440e-01  1.263 0.206458
## stateNJ          1.693e+00  6.965e-01  2.431 0.015070 *
## stateNM          6.506e-01  7.641e-01  0.851 0.394494
## stateNV          1.454e+00  7.186e-01  2.023 0.043095 *
## stateNY          1.043e+00  7.233e-01  1.441 0.149460
## stateOH          1.058e+00  7.213e-01  1.466 0.142528
## stateOK          7.562e-01  7.503e-01  1.008 0.313511
## stateOR          1.037e+00  7.173e-01  1.446 0.148198
## statePA          2.942e-01  8.214e-01  0.358 0.720230
## stateRI          6.277e-02  8.026e-01  0.078 0.937655
## stateSC          1.393e+00  7.424e-01  1.877 0.060543 .
## stateSD          6.270e-01  7.728e-01  0.811 0.417228
## stateTN          1.081e+00  7.401e-01  1.460 0.144266
## stateTX          1.500e+00  7.045e-01  2.129 0.033279 *
## stateUT          1.442e+00  7.183e-01  2.007 0.044771 *
## stateVA          8.492e-03  7.909e-01  0.011 0.991433
## stateVT          3.919e-01  7.555e-01  0.519 0.603960
## stateWA          2.046e+00  7.044e-01  2.905 0.003677 **
## stateWI          1.434e-01  8.005e-01  0.179 0.857845
## stateWV          1.173e+00  6.977e-01  1.681 0.092835 .
## stateWY          1.635e-01  7.573e-01  0.216 0.829065
## acct_length      7.681e-02  5.268e-02  1.458 0.144851
## num_vm_mess      3.424e-01  2.331e-01  1.469 0.141906
## tot_day_min      1.869e+02  1.696e+02  1.102 0.270331
## tot_day_calls    9.778e-03  5.284e-02  0.185 0.853208
## tot_day_chg      -1.861e+02  1.695e+02  -1.098 0.272310
## tot_eve_min      1.387e+00  8.036e+01  0.017 0.986233
## tot_eve_calls    -2.516e-02  5.352e-02  -0.470 0.638184
## total_eve_charge -9.732e-01  8.036e+01  -0.012 0.990338
## tot_night_min    6.899e+00  4.250e+01  0.162 0.871041
## tot_night_calls  -4.381e-02  5.308e-02  -0.825 0.409216
## tot_night_chg    -6.663e+00  4.250e+01  -0.157 0.875406
## tot_intl_min     6.686e+00  1.416e+01  0.472 0.636805
## tot_intl_calls   -1.746e-01  5.676e-02  -3.076 0.002097 **
## tot_intl_chg     -6.428e+00  1.416e+01  -0.454 0.649851
## num_cust_serv_calls 6.876e-01  4.975e-02  13.822 < 2e-16 ***
## area_code_4081   6.734e-02  1.520e-01  0.443 0.657757
## area_code_4151   2.134e-03  1.315e-01  0.016 0.987050
## area_code_5101    NA          NA          NA          NA
## intl_plan_yes1    2.328e+00  1.430e-01  16.282 < 2e-16 ***
## vm_plan_yes1     -1.854e+00  5.462e-01  -3.394 0.000689 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 3261.7 on 4000 degrees of freedom
## Residual deviance: 2409.9 on 3931 degrees of freedom
## AIC: 2549.9
##

```

```
## Number of Fisher Scoring iterations: 6
```

```
summary(model3) # This model performs well as many of the variables are significant statistically. Also
```

```
##
## Call:
## glm(formula = churn_yes ~ acct_length + num_vm_mess + tot_day_min +
##      tot_day_calls + tot_day_chg + tot_eve_min + total_eve_charge +
##      tot_night_min + tot_night_chg + tot_intl_min + tot_intl_calls +
##      tot_intl_chg + num_cust_serv_calls + area_code_415 + intl_plan_yes +
##      vm_plan_yes + tot_day_min:num_cust_serv_calls + tot_day_min:tot_day_chg +
##      tot_intl_min:intl_plan_yes + tot_eve_min:num_cust_serv_calls +
##      tot_day_min:vm_plan_yes + tot_day_min:tot_eve_min + tot_day_chg:tot_night_min +
##      tot_intl_calls:intl_plan_yes + tot_day_chg:intl_plan_yes +
##      tot_eve_min:vm_plan_yes + num_cust_serv_calls:intl_plan_yes +
##      tot_night_chg:vm_plan_yes + tot_night_min:num_cust_serv_calls +
##      acct_length:num_vm_mess + total_eve_charge:tot_night_min +
##      tot_intl_min:tot_intl_calls + num_cust_serv_calls:vm_plan_yes +
##      tot_day_calls:total_eve_charge + tot_night_min:vm_plan_yes +
##      total_eve_charge:num_cust_serv_calls + intl_plan_yes:vm_plan_yes +
##      num_vm_mess:area_code_415 + tot_eve_min:total_eve_charge +
##      tot_intl_chg:num_cust_serv_calls + tot_day_calls:num_cust_serv_calls +
##      tot_day_chg:num_cust_serv_calls + tot_intl_calls:vm_plan_yes +
##      tot_eve_min:tot_night_chg + tot_day_min:tot_night_chg + acct_length:tot_night_chg +
##      acct_length:tot_night_min + tot_intl_calls:num_cust_serv_calls,
##      family = "binomial", data = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.3815  -0.3639  -0.1651  -0.0624   3.8560
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    -3.56906    0.22760  -15.681  < 2e-16 ***
## acct_length      0.18630    0.06654   2.800  0.00512 **
## num_vm_mess      0.38983    0.28765   1.355  0.17534
## tot_day_min     518.56670   219.04406   2.367  0.01791 *
## tot_day_calls   -0.06970    0.06926  -1.006  0.31423
## tot_day_chg    -517.28606   219.04097  -2.362  0.01820 *
## tot_eve_min      81.98465   103.59169   0.791  0.42870
## total_eve_charge -81.35228   103.59327  -0.785  0.43227
## tot_night_min   -50.39245    58.25188  -0.865  0.38700
## tot_night_chg    50.69713    58.25040   0.870  0.38412
## tot_intl_min      7.24003    17.05365   0.425  0.67117
## tot_intl_calls  -0.07154    0.08303  -0.862  0.38887
## tot_intl_chg    -7.05646    17.05470  -0.414  0.67905
## num_cust_serv_calls  1.18702    0.08052  14.742  < 2e-16 ***
## area_code_4151  -0.10988    0.13296  -0.826  0.40857
## intl_plan_yes1    2.66168    0.20114  13.233  < 2e-16 ***
## vm_plan_yes1    -2.12068    0.69434  -3.054  0.00226 **
## tot_day_min:num_cust_serv_calls -299.31623   175.78324  -1.703  0.08861 .
## tot_day_min:tot_day_chg      0.54287    0.04662  11.644  < 2e-16 ***
## tot_intl_min:intl_plan_yes1    1.35657    0.19794   6.854  7.20e-12 ***
## tot_eve_min:num_cust_serv_calls -159.65789    85.29265  -1.872  0.06122 .
```

```

## tot_day_min:vm_plan_yes1      -1.07864    0.16497   -6.539  6.21e-11 ***
## tot_day_min:tot_eve_min        0.47061    0.06323    7.443  9.85e-14 ***
## tot_day_chg:tot_night_min      69.77118   46.95393    1.486  0.13729
## tot_intl_calls:intl_plan_yes1  -0.96848    0.17788   -5.444  5.20e-08 ***
## tot_day_chg:intl_plan_yes1     -0.73092    0.16220   -4.506  6.60e-06 ***
## tot_eve_min:vm_plan_yes1       -0.57258    0.17741   -3.227  0.00125 **
## num_cust_serv_calls:intl_plan_yes1 -0.76519    0.15509   -4.934  8.06e-07 ***
## tot_night_chg:vm_plan_yes1    -318.60461  142.02538   -2.243  0.02488 *
## tot_night_min:num_cust_serv_calls -0.18921    0.05879   -3.218  0.00129 **
## acct_length:num_vm_mess        0.20644    0.07825    2.638  0.00834 **
## total_eve_charge:tot_night_min  71.19028   44.60521    1.596  0.11049
## tot_intl_min:tot_intl_calls     0.14273    0.06496    2.197  0.02802 *
## num_cust_serv_calls:vm_plan_yes1  0.43939    0.15672    2.804  0.00505 **
## tot_day_calls:total_eve_charge  0.16134    0.06516    2.476  0.01329 *
## tot_night_min:vm_plan_yes1     318.06833  142.01489    2.240  0.02511 *
## total_eve_charge:num_cust_serv_calls 159.28413   85.29617    1.867  0.06184 .
## intl_plan_yes1:vm_plan_yes1     0.92269    0.40597    2.273  0.02304 *
## num_vm_mess:area_code_4151     -0.29807    0.15230   -1.957  0.05034 .
## tot_eve_min:total_eve_charge    0.10734    0.04756    2.257  0.02401 *
## tot_intl_chg:num_cust_serv_calls -0.11584    0.05983   -1.936  0.05285 .
## tot_day_calls:num_cust_serv_calls  0.08847    0.05668    1.561  0.11854
## tot_day_chg:num_cust_serv_calls 298.51828  175.78054    1.698  0.08946 .
## tot_intl_calls:vm_plan_yes1     0.30881    0.17724    1.742  0.08145 .
## tot_eve_min:tot_night_chg      -71.01069   44.60234   -1.592  0.11137
## tot_day_min:tot_night_chg      -69.43228   46.95412   -1.479  0.13921
## acct_length:tot_night_chg      -88.48917   53.17043   -1.664  0.09606 .
## acct_length:tot_night_min       88.39733   53.17298    1.662  0.09642 .
## tot_intl_calls:num_cust_serv_calls -0.08955    0.06284   -1.425  0.15414
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 3261.7  on 4000  degrees of freedom
## Residual deviance: 1711.3  on 3952  degrees of freedom
## AIC: 1809.3
##
## Number of Fisher Scoring iterations: 7

```

```
anova(model1, model3, test = "Chisq")
```

```

## Analysis of Deviance Table
##
## Model 1: churn_yes ~ state + acct_length + num_vm_mess + tot_day_min +
## tot_day_calls + tot_day_chg + tot_eve_min + tot_eve_calls +
## total_eve_charge + tot_night_min + tot_night_calls + tot_night_chg +
## tot_intl_min + tot_intl_calls + tot_intl_chg + num_cust_serv_calls +
## area_code_408 + area_code_415 + area_code_510 + intl_plan_yes +
## vm_plan_yes
## Model 2: churn_yes ~ acct_length + num_vm_mess + tot_day_min + tot_day_calls +
## tot_day_chg + tot_eve_min + total_eve_charge + tot_night_min +
## tot_night_chg + tot_intl_min + tot_intl_calls + tot_intl_chg +
## num_cust_serv_calls + area_code_415 + intl_plan_yes + vm_plan_yes +
## tot_day_min:num_cust_serv_calls + tot_day_min:tot_day_chg +

```

```
## tot_intl_min:intl_plan_yes + tot_eve_min:num_cust_serv_calls +
## tot_day_min:vm_plan_yes + tot_day_min:tot_eve_min + tot_day_chg:tot_night_min +
## tot_intl_calls:intl_plan_yes + tot_day_chg:intl_plan_yes +
## tot_eve_min:vm_plan_yes + num_cust_serv_calls:intl_plan_yes +
## tot_night_chg:vm_plan_yes + tot_night_min:num_cust_serv_calls +
## acct_length:num_vm_mess + total_eve_charge:tot_night_min +
## tot_intl_min:tot_intl_calls + num_cust_serv_calls:vm_plan_yes +
## tot_day_calls:total_eve_charge + tot_night_min:vm_plan_yes +
## total_eve_charge:num_cust_serv_calls + intl_plan_yes:vm_plan_yes +
## num_vm_mess:area_code_415 + tot_eve_min:total_eve_charge +
## tot_intl_chg:num_cust_serv_calls + tot_day_calls:num_cust_serv_calls +
## tot_day_chg:num_cust_serv_calls + tot_intl_calls:vm_plan_yes +
## tot_eve_min:tot_night_chg + tot_day_min:tot_night_chg + acct_length:tot_night_chg +
## acct_length:tot_night_min + tot_intl_calls:num_cust_serv_calls
## Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1 3931 2409.9
## 2 3952 1711.3 -21 698.62
```

```
# A test IIA hypothesis (independence of irrelevant alternatives) for a multinomial logit model. Basic
list(model1 = pR2(model1)["McFadden"],
      model3 = pR2(model3)["McFadden"])
```

```
## fitting null model for pseudo-r2
## fitting null model for pseudo-r2
```

```
## $model1
## McFadden
## 0.2611485
##
## $model3
## McFadden
## 0.4753362
```

```
model1_data <- augment(model1) %>%
  mutate(index = 1:n())
```

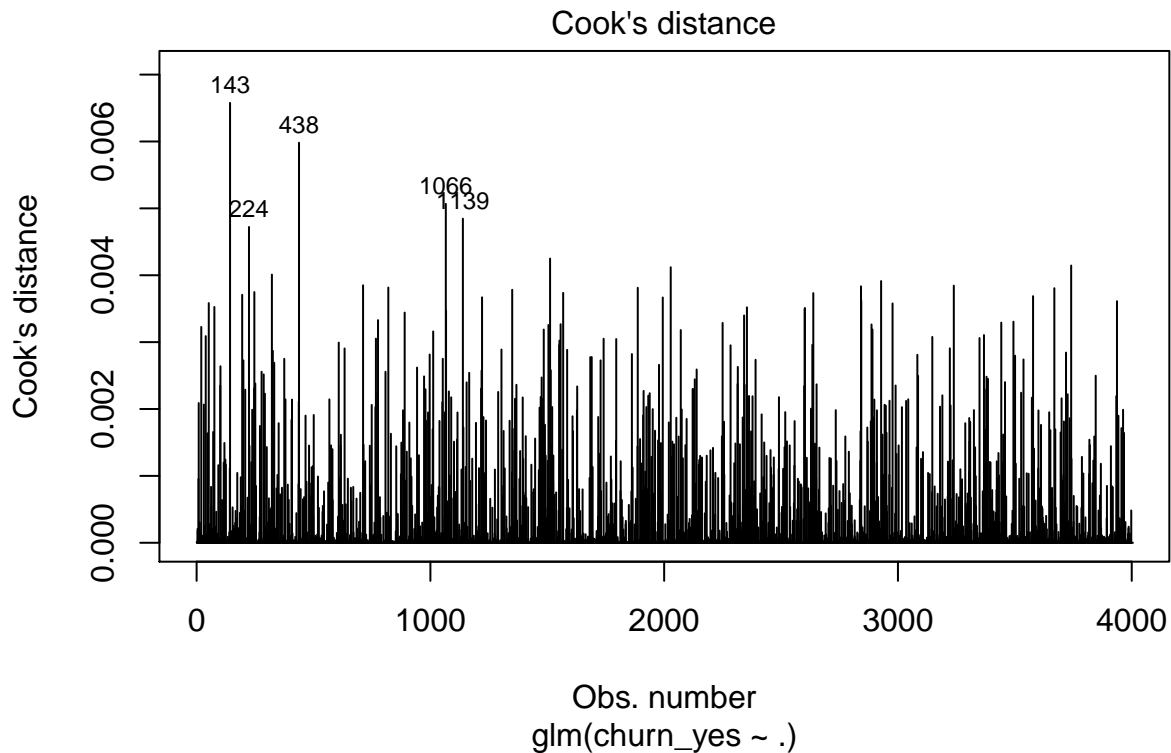
```
model3_data <- augment(model1) %>%
  mutate(index = 1:n())
```

```
model1_data %>% # Used to estimate the influence of a data point when performing a least-squares regre
  filter(abs(.std.resid) > 3)
```

```
## # A tibble: 4 x 29
## churn_yes state acct_length num_vm_mess tot_day_min tot_day_calls tot_day_chg
## <fct> <fct> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 1 SD -0.0651 -0.576 -3.34 -5.08 -3.34
## 2 1 SD -0.241 -0.576 -0.506 1.17 -0.506
## 3 1 WY 1.47 -0.576 -0.239 -1.63 -0.239
## 4 1 IN -0.316 -0.576 -1.81 -0.306 -1.81
## # ... with 22 more variables: tot_eve_min <dbl>, tot_eve_calls <dbl>,
## # total_eve_charge <dbl>, tot_night_min <dbl>, tot_night_calls <dbl>,
## # tot_night_chg <dbl>, tot_intl_min <dbl>, tot_intl_calls <dbl>,
```

```
## # tot_intl_chg <dbl>, num_cust_serv_calls <dbl>, area_code_408 <fct>,
## # area_code_415 <fct>, area_code_510 <fct>, intl_plan_yes <fct>,
## # vm_plan_yes <fct>, .fitted <dbl>, .resid <dbl>, .std.resid <dbl>,
## # .hat <dbl>, .sigma <dbl>, .cooksds <dbl>, index <int>
```

```
plot(model1, which = 4, id.n = 5)
```



```
model1_data %>%
  top_n(5, .cooksds)
```

```
## # A tibble: 5 x 29
## # churn_yes state acct_length num_vm_mess tot_day_min tot_day_calls tot_day_chg
## # <fct> <fct> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 1 AK 0.637 -0.576 -2.26 -0.306 -2.26
## 2 1 SD 1.09 2.95 0.176 -0.205 0.176
## 3 1 AK 0.261 -0.576 -0.139 -2.13 -0.139
## 4 1 SD -0.0651 -0.576 -3.34 -5.08 -3.34
## 5 1 IL -0.291 0.820 -1.25 0.709 -1.25
## # ... with 22 more variables: tot_eve_min <dbl>, tot_eve_calls <dbl>,
## # total_eve_charge <dbl>, tot_night_min <dbl>, tot_night_calls <dbl>,
## # tot_night_chg <dbl>, tot_intl_min <dbl>, tot_intl_calls <dbl>,
## # tot_intl_chg <dbl>, num_cust_serv_calls <dbl>, area_code_408 <fct>,
## # area_code_415 <fct>, area_code_510 <fct>, intl_plan_yes <fct>,
## # vm_plan_yes <fct>, .fitted <dbl>, .resid <dbl>, .std.resid <dbl>,
## # .hat <dbl>, .sigma <dbl>, .cooksds <dbl>, index <int>
```

```
# Now checking how well the models perform on the validation set.
valid <- predict(norm, valid)
```

```
test_m1 <- predict(model1, newdata = valid, type = "response")
```

```
## Warning in predict.lm(object, newdata, se.fit, scale = 1, type = if (type == :
## prediction from a rank-deficient fit may be misleading
```

```
test_m3 <- predict(model3, newdata = valid, type = "response")
```

```
list(
  model1 = table(valid$churn_yes, test_m1 > 0.5) %>%
    prop.table() %>%
    round(3),
  model3 = table(valid$churn_yes, test_m3 > 0.5) %>%
    prop.table() %>%
    round(3)
)
```

```
## $model1
##
##      FALSE TRUE
##  0 0.837 0.022
##  1 0.112 0.029
##
## $model3
##
##      FALSE TRUE
##  0 0.843 0.016
##  1 0.065 0.076
```

```
table(valid$churn_yes, test_m1 > .5)
```

```
##
##      FALSE TRUE
##  0   836   22
##  1   112   29
```

```
table(valid$churn_yes, test_m3 > .5)
```

```
##
##      FALSE TRUE
##  0   842   16
##  1    65   76
```

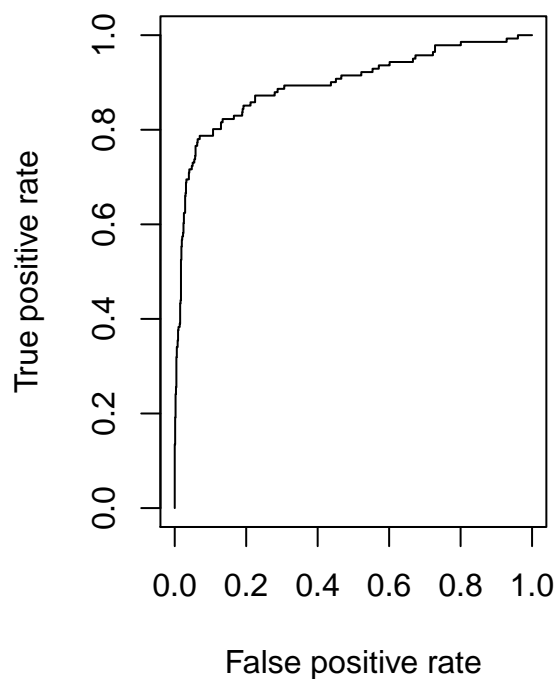
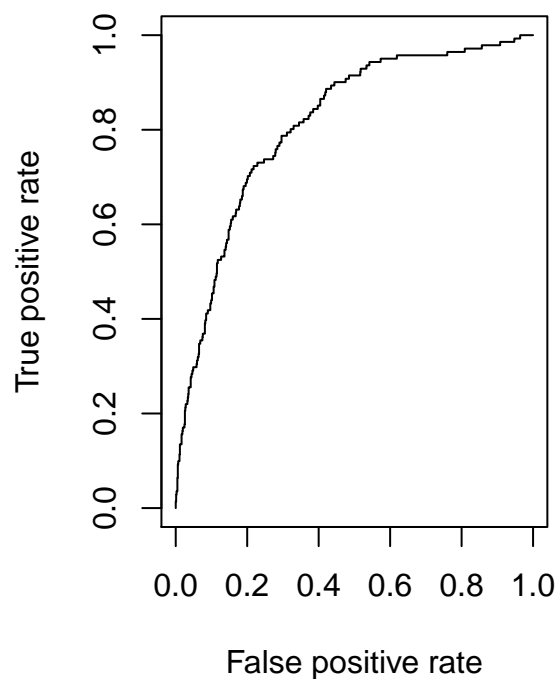
ROC AND AUC

```
library(ROCR)

par(mfrow=c(1, 2))

prediction(test_m1, valid$churn_yes) %>%
  performance(measure = "tpr", x.measure = "fpr") %>%
  plot()

prediction(test_m3, valid$churn_yes) %>%
  performance(measure = "tpr", x.measure = "fpr") %>%
  plot()
```



```
# model 2 AUC
prediction(test_m1, valid$churn_yes) %>%
  performance(measure = "auc") %>%
  .@y.values
```

```
## [[1]]
## [1] 0.8117509
```

```
# model 2 AUC
prediction(test_m3, valid$churn_yes) %>%
  performance(measure = "auc") %>%
  .@y.values
```

```
## [[1]]  
## [1] 0.8972788
```

,