# Lecture 05 Lists and recursion

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#### **Announcements**

- etutor assignment all parts due on Sunday
- 2. Reading SICP 1.2 (pages 79-126)

## Lecture 04 – review Structures and Patterns in Functional Programming

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### Lecture Nuggets

- Order of growth matters
- Support for compound data allows data abstraction
  - Pairs
  - Lists
  - Others
- Two main patterns when dealing with lists
  - o Consing up − to build
  - o Cdring down − to process



#### Nuggets:

- 1 Order of growth
- 2 Pairs
  - Lists
  - → Others
- 3 Two main Patterns

  - → consing up (building)
    → cdring down (processing)



```
\Rightarrow Pairs (cons cells)

(cons \langle x-exp \rangle \langle y-exp \rangle) => \langle P \rangle (constructor)

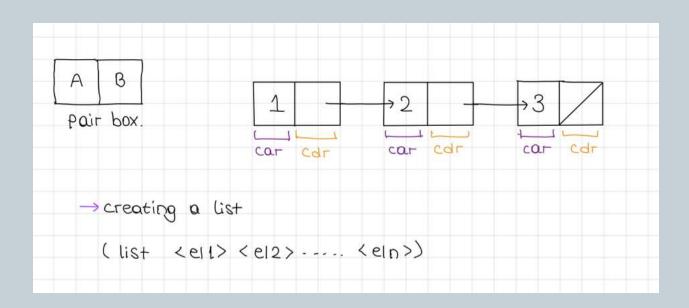
(x-val> \langle y-val \rangle

\Rightarrow returns a pair \langle P \rangle (accessor)

(ar-Part =) \langle x-val \rangle \rightarrow (car \langle P \rangle)

cdr-Part =) \langle y-val \rangle \rightarrow (cdr \langle P \rangle)
```





Nugget

## Support for compound data allows data abstraction



```
Using pair abstractions to build procedures

(define pt (make-point 1 2))
(define p2 (make-point 4 3))

(define streeth-point (lambda (pt scale)
(make-point (* scale (point-x pt)))

(* Scale (point-y p t)))))
```

### Lecture notes – notable contributors

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# Lecture 05 Lists and recursion

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### Lecture Nuggets

- Two main patterns when dealing with lists
  - o Consing up − to build
  - Cdring down to process
- Higher order procedures
- Three more patterns for lists
  - Transforming
  - Filtering
  - Accumulating

Nugget

Two patterns for dealing with lists

#### Common Pattern #1: cons'ing up a list

```
(define (enumerate-interval from to)
 (if (> from to)
     nil
     (adjoin from
           (enumerate-interval
             (+ 1 from)
             to))))
(e-i 2 4)
(if (> 2 4) nil (adjoin 2 (e-i (+ 1 2) 4)))
(if #f nil (adjoin 2 (e-i 3 4)))
(adjoin 2 (e-i 3 4))
(adjoin 2 (adjoin 3 (e-i 4 4)))
(adjoin 2 (adjoin 3 (adjoin 4 (e-i 5 4))))
(adjoin 2 (adjoin 3 (adjoin 4 nil)))
 (adjoin 2 (adjoin 3 -
                                       ))
 (adjoin 2
                                   ==> (2 3 4)
                           COMP 301 SICP
```

#### Common Pattern #2: cdr'ing down a list

```
(define (list-ref lst n)
  (if (= n 0))
      (first lst)
      (list-ref (rest 1st)
                 (- n 1))))
                         (list-ref joe 1)
(define (length 1st)
  (if (null? lst)
      (+ 1 (length (rest lst)))))
```

Nugget

## Higher order procedures

```
Other common patterns
```

```
• 1 + 2 + ... + 100 = (100 * 101)/2
                                                                 100
• 1 + 4 + 9 + ... + 100^2 = (100 * 101 * 201)/6
• 1 + 1/3^2 + 1/5^2 + ... + 1/101^2 = \pi^2/8
(define (sum-integers a b)
  (if (> a b)
     (+a (sum-integers (+ 1 a) b))))
(define (sum-squares a b)
                                        (define (sum term a next b)
  (if (> a b)
                                          (if (> a b)
     (+ (square a)
        (sum-squares (+ 1 a) b))))
(define (pi-sum a b)
                                            (+ (term a)
  (if (> a b)
                                              (sum term (next a) next b))))
    (+ (/ 1 (square a))
   <sub>10/16</sub>(pi-sum (+ a 2) b)))
```

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#### Let's check this new procedure out!

```
(define (sum term a next b)
                                   A higher order procedure!!
 (if (> a b))
   (+ (term a)
     (sum term (next a) next b))))
What is the type of this procedure?
(number → number, number, number → number, number → number
                                  procedure
       procedure
                            procedure
```

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#### **Higher order procedures**

 A higher order procedure: takes a procedure as an argument or returns one as a value

```
(define (sum-integers1 a b)
        (sum (lambda (x) x) | a (lambda (x) (+ x 1)) b))
(define (sum-squares1 a b)
        (sum square a (lambda (x) (+ x 1)) b))
(define (pi-sum1 a b)
      (sum (lambda (x) (/ 1 (square x))) a
           (lambda (x) (+ x 2)) b))
(define (sum term a next b)
(if (> a b))
   (+ (term a)
    (sum term (next a) next b))))
```

#### **Common Pattern #1: Transforming a List**

```
(define (square-list 1st)
  (if (null? lst)
      nil
      (cons (square (car lst))
            (square-list (cdr lst)))))
(define (double-list lst)
  (if (null? lst)
      nil
      (cons (* 2 (car 1st))
            (double-list (cdr lst))))
(define (square-list lst)
  (map square lst))
(define (double-list 1st)
  (map (lambda (x) (* 2 x))
lst))
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```

#### **Common Pattern #1: Transforming a List**

Let's code it together.

#### **Common Pattern #1: Transforming a List**

```
(define (square-list 1st)
  (if (null? 1st)
      nil
      (cons (square (car lst))
            (square-list (cdr lst)))))
(define (double-list lst)
  (if (null? 1st)
      nil
      (cons (* 2 (car 1st))
            (double-list (cdr lst))))
(define (MAP proc 1st)
  (if (null? lst)
      nil
      (cons (proc (car 1st))
            (map proc (cdr lst)))))
(define (square-list 1st)
  (map square 1st))
(define (double-list 1st)
  (map (lambda (x) (* 2 x))
lst))
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```

#### **Common Pattern #2: Filtering a List**

```
(define (keep-it-odd lst)
 (cond ((null? lst) nil)
       ((odd? (car lst))
        (cons (car lst) (keep-it-odd (cdr lst)))
       (else (keep-it-odd (cdr lst)))))
 > (filter odd? '(3 8 1 3 2 4 5 1 3))
 (3 1 3 5 1 3)
```

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#### **Common Pattern #2: Filtering a List**

Let's code it together.

24/28

#### **Common Pattern #2: Filtering a List**

```
(define (keep-it-odd lst)
 (cond ((null? lst) nil)
       ((odd? (car lst))
        (cons (car lst) (keep-it-odd (cdr lst)))
       (else (keep-it-odd (cdr lst)))))
 (define (filter pred 1st)
   (cond ((null? lst) nil)
          ((pred (car lst))
           (cons (car 1st)
                 (filter pred (cdr lst))))
          (else (filter pred (cdr lst)))))
```

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#### **Common Pattern #3: Accumulating Results**

```
(define (add-up 1st)
 (if (null? lst)
     (+ (car 1st)
        (add-up (cdr lst))))
(define (mult-all 1st)
 (if (null? lst)
     (* (car 1st)
        (mult-all (cdr lst))))
> (reduce + 0 '(1 2 3 4 5))
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```

#### **Common Pattern #3: Accumulating Results**

```
(define (add-up 1st)
  (if (null? 1st)
      (+ (car lst)
         (add-up (cdr lst))))
(define (mult-all 1st)
  (if (null? lst)
      (* (car 1st)
         (mult-all (cdr lst))))
(define (REDUCE op init 1st)
  (if (null? lst)
      init
      (op (car lst)
          (reduce op init (cdr lst))))
(define (add-up 1st)
  (reduce + 0 lst))
```

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