Proc Review

T. METIN SEZGIN

Implementation

```
proc? : SchemeVal → Bool
(define proc?
  (lambda (val)
     (procedure? val)))
procedure : Var \times Exp \times Env \rightarrow Proc
(define procedure
  (lambda (var body env)
     (lambda (val)
       (value-of body (extend-env var val env)))))
apply-procedure : Proc \times ExpVal \rightarrow ExpVal
(define apply-procedure
  (lambda (proc1 val)
     (proc1 val)))
```

Alternative implementation

Other changes to the interpreter

```
(define-datatype expval expval?
  (num-val
    (num number?))
  (bool-val
    (bool boolean?))
  (proc-val
    (proc proc?)))
(proc-exp (var body)
 (proc-val (procedure var body env)))
(call-exp (rator rand)
 (let ((proc (expval->proc (value-of rator env)))
        (arg (value-of rand env)))
    (apply-procedure proc arg)))
```

LETREC

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PROC is ex; long live LETREC

- PROC had its limitations
 - No recursive procedures
- Define a language with recursive procedures
 - Specification
 - × Syntax
 - × Semantics
 - Representation
 - Implementation

Nuggets of the lecture

- Implementation requires creating representation for recursive procedures
- We need to rethink how we evaluate recursive procedures
- A more elaborate way of representing procedures in the environment is needed

LETREC

• The idea

The new grammar

```
Expression ::= letrec Identifier (Identifier) = Expression in Expression letrec-exp (p-name b-var p-body letrec-body)
```

LETREC

Extend the environment recursively

```
(value-of
   (letrec-exp proc-name bound-var proc-body letrec-body)
     ρ)
= (value-of
     letrec-body
          (extend-env-rec proc-name bound-var proc-body ρ))
```

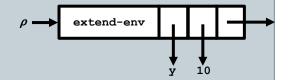
- How should environment lookup work?
 - o If the search variable matches a recursive procedure

```
(apply-env \rho_1 proc-name)
= (proc-val (procedure bound-var proc-body \rho_1))
```

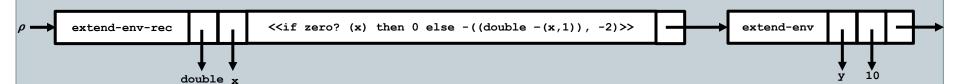
If there is no match

```
(apply-env \rho_1 \ var) = (apply-env \rho \ var)
```

Extended environment



Extended environment



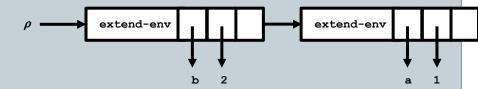
Example

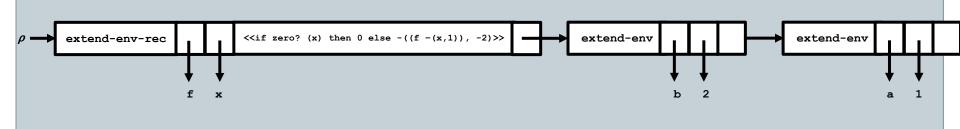
```
(value-of <<letrec double(x) = if zero?(x)</pre>
                                  then 0
                                  else - ((double - (x,1)), -2)
             in (double 6) >> \rho_0)
= (value-of << (double 6) >>
    (extend-env-rec double x <<if zero?(x) ...>> \rho_0))
= (apply-procedure
    (value-of <<double>> (extend-env-rec double x
                             <<if zero?(x) ...>> \rho_0))
    (value-of <<6>> (extend-env-rec double x
                        <<if zero?(x) ...>> \rho_0)))
= (apply-procedure
    (procedure x <<if zero?(x) ...>>
      (extend-env-rec double x <<if zero?(x) ...>> \rho_0))
    [6])
= (value-of
    <<if zero?(x) ...>>
   [x=[6]] (extend-env-rec
                     double x <<if zero?(x) ...>> \rho_0))
= (-
    (value-of
      <<(double - (x,1))>>
      [x=[6]] (extend-env-rec
                        double x <<if zero?(x) ...>> \rho_0))
    -2)
```

Example cont.

```
= (-
    (apply-procedure
      (value-of
        <<double>>
        [x=[6]] (extend-env-rec
                          double x <<if zero?(x) ...>> \rho_0))
      (value-of
        <<- (x,1)>>
        [x=[6]] (extend-env-rec
                          double x <<if zero?(x) ...>> \rho_0)))
    -2)
= (-
    (apply-procedure
      (procedure x <<if zero?(x) ...>>
        (extend-env-rec double x <<if zero?(x) ...>> \rho_0))
      [5])
    -2)
```







The new environment and apply-env

```
(define-datatype environment environment?
  (empty-env)
  (extend-env
    (var identifier?)
    (val expval?)
    (env environment?))
  (extend-env-rec
    (p-name identifier?)
    (b-var identifier?)
    (body expression?)
    (env environment?)))
(define apply-env
  (lambda (env search-var)
    (cases environment env
      (empty-env ()
        (report-no-binding-found search-var))
      (extend-env (saved-var saved-val saved-env)
        (if (eqv? saved-var search-var)
          saved-val
          (apply-env saved-env search-var)))
      (extend-env-rec (p-name b-var p-body saved-env)
        (if (eqv? search-var p-name)
          (proc-val (procedure b-var p-body env))
          (apply-env saved-env search-var))))))
```