

Rubin Observatory

PSF Photometry

LSSTC DSFP | The Internet | August 2020



Beyond aperture photometry

- We've looked at aperture photometry, where the goal is simply to count up all the photons that we can attribute to a given star.
- This totally works! But we can do better, in two ways:
 - 1) We really should understand the statistical basis for our measurement.
 - Doing so will tell us how to make the best measurement
 - 2) We know that aperture fluxes cannot be optimal
 - Depending on where we set the aperture, we're either throwing away information outside that aperture, or we're including pixels with lots of noisy sky and little signal.

Maximum Likelihood estimate

- For each pixel, we have a model that we want to compare to the measured value for that pixel in an image, in the presence of noise.
- Going to follow the notation of Portillo, Speagle, Finkbeiner 2020; classic reference is King 1983.
- Our PSF is $p(x, y)$, and our model for a star given a flux f is $f p(x, y)$. The PSF must be normalized, $\sum_{x,y} p(x, y) = 1$, and we require the image to be background-subtracted.

Maximum Likelihood estimate

- Because the noise on each pixel is uncorrelated with the noise on other pixels, the likelihood for the flux measurement is the product of the likelihoods on each individual pixel.
- Let \hat{f} represent the measured flux in pixel i , and assuming Gaussian noise

$$\mathcal{L}(x, y, f) = \frac{1}{\sqrt{2\pi\sigma^2}} \prod_i \exp((\hat{f}_i - fp_i(x, y))^2 / (2\sigma^2))$$

- Taking the log likelihood gives us a sum over the model comparisons

$$\ln \mathcal{L}(x, y, f) = -\frac{N}{2} \ln(2\pi\sigma^2) - \frac{1}{2\sigma^2} \sum_i (\hat{f}_i - fp_i(x, y))^2$$

- Find the maximum of the likelihood by setting the partial derivative w.r.t. f to zero, solve for f_{ML}

$$\partial_f \mathcal{L}(x, y, f_{\text{ML}}) = \frac{1}{\sigma^2} \sum_i \hat{f}_i p_i(x, y) - f_{\text{ML}} p_i^2(x, y) = 0$$

- Which gives us a nice solution for the flux

$$f_{\text{ML}}(x, y) = \frac{\sum_i \hat{f}_i p_i(x, y)}{\sum_i p_i^2(x, y)}$$

- To say in words what this means:
 - To measure the flux, we take the product of the PSF model and the image pixels, sum that product, and divide by a normalization.

- PSF photometry can also be thought of as a pixel weighting scheme. To demonstrate, if $p(x, y) = 1/N$, N being the number of pixels in your sum, then:

$$f_{\text{ML}} = \frac{\sum_i \hat{f}_i (1/N)}{\sum_i (1/N^2)} = \frac{\sum_i \hat{f}/N}{N/N^2} = \sum_i \hat{f}_i$$

- That's aperture photometry!

“Where” to do PSF photometry?

- We skipped a step: how do we know where to put the PSF model?
- Few steps to that process:
 - 1) Matched filter — Convolve the image with the PSF, finding regions with significant flux
 - 2) Peak finding
 - 3) Centroiding

- Convolution — heard about this in the earlier talk
- Once we have the detection image, we need to make a list of possible sources to measure. (We don't want to run photometry on every above-background pixel)
- Use a “peak-finding” algorithm; we want to identify pixels that have a greater value than all of their immediate neighbors.
- That “peak” gives us the starting point for photometry

Centroiding

- Peaks give us an integer pixel, but we can measure the position of the source more accurately than that.
- There are several different centroiding algorithms available, usually designed to be robust even when the PSF is poorly known.
- SDSS and Rubin Observatory use successive quartic interpolations.
- An easier algorithm to think about is to compute the mean of the pixel positions in x or y , *weighted by the measured flux*.

PSF Determination

- One more piece of the puzzle: we need to construct the PSF model.
- First we need “PSF Candidates” — sources on the image that have the right size/shape to be stars, with no close neighbors
- There’s a bootstrap problem here, we need some rough guess at the PSF size before we know what would be good candidates

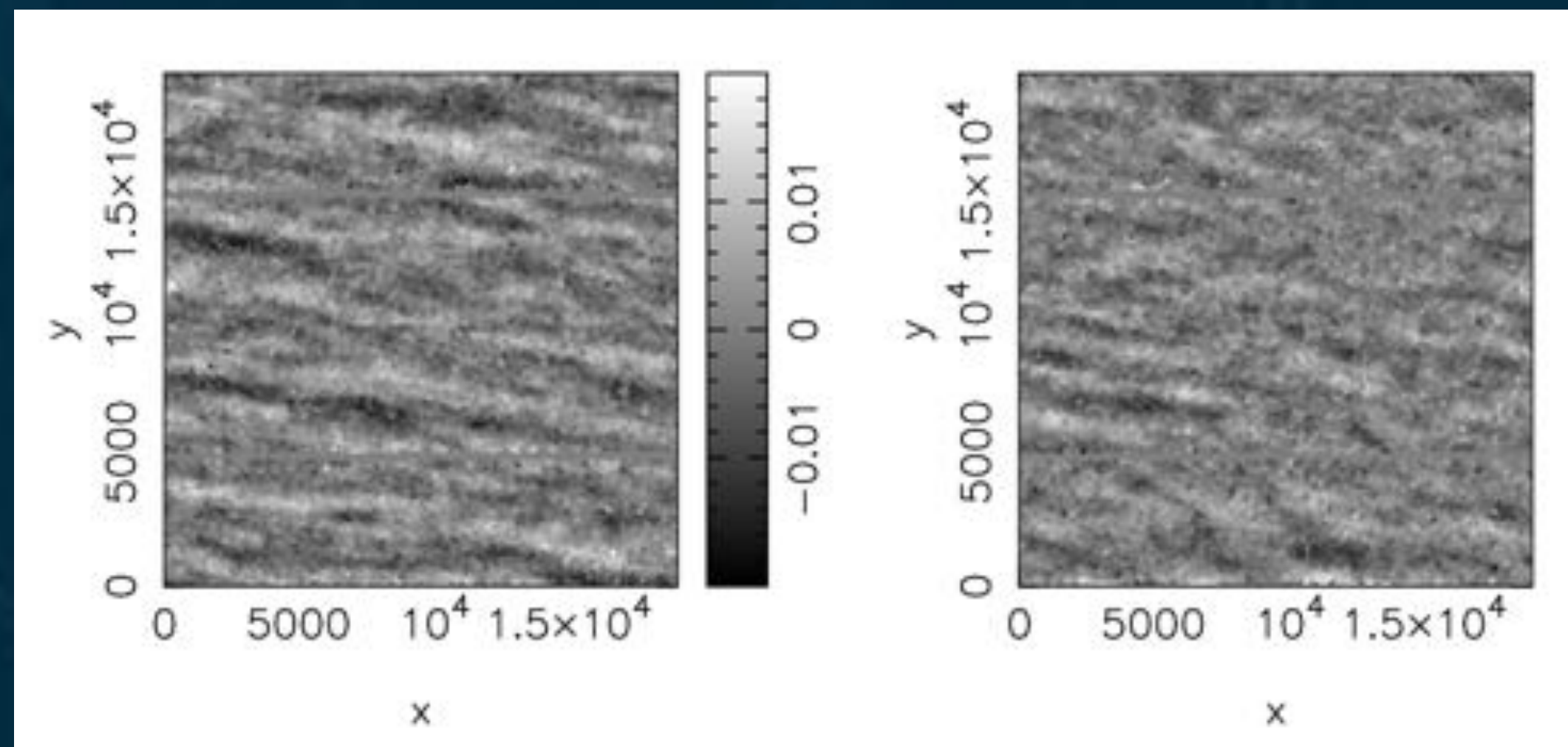
PSF Determination

- With PSF candidates in hand, there are a few different algorithms:
 - Model fitting, using Gaussian or a Moffat function (Gaussian core + Lorentizan wings)
 - Fitting to basis functions (e.g. SDSS). Similar to model fitting, but the basis functions are designed to capture the range of variation in the PSF.
 - “Pixel Basis” fitting, where candidates are resampled to a higher-resolution pixel grid, then each pixel is fit separately to capture spatial variation. Used by PSFEx (part of Source Extractor).

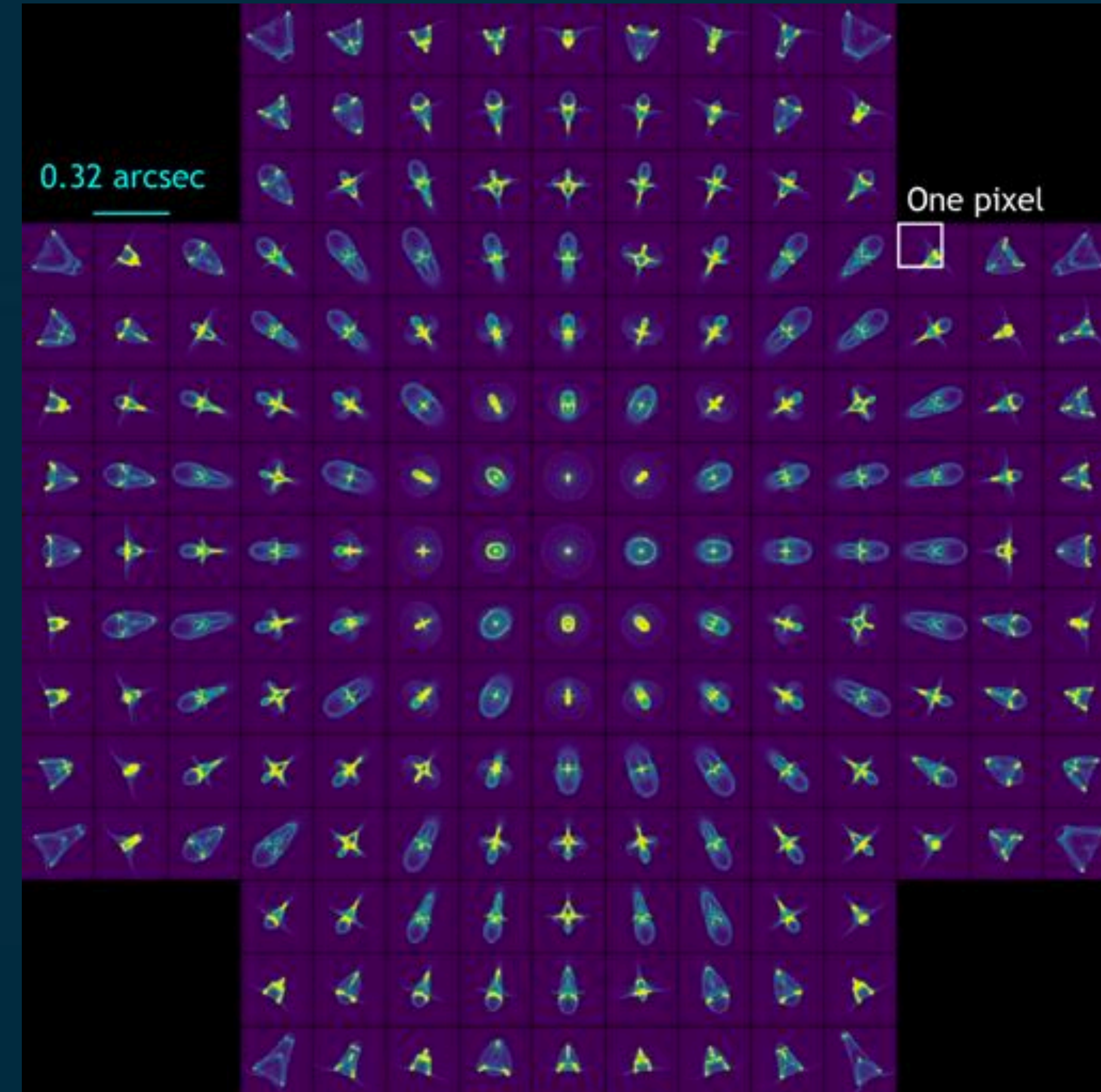
PSF Determination for Rubin Observatory

- Goal is to model the optics and the atmosphere *separately*
- Important for galaxy shape measurements, weak lensing.

CFHT PSF shape residuals (Heymans et al. 2012)



Rubin Obs. Optical PSF model (Meyers)



Recap

- Photometry is often an iterative process.
 - Detection (with a PSF guess)
 - PSF Determination
 - Detection (now with the new PSF)
 - Centroiding
 - PSF Flux measurement

Photometric Calibration



Photometric Calibration

- Let's start simple.
- Our goal when photometering an image is to report how bright the objects are relative to some agreed-on standard.
- Typically today, you're most likely to either Pan-STARRS (PS1) or Gaia stars as your "standards".
- Gaia covers the whole sky; PS1 covers 3/4ths of the sky slightly deeper/denser, and with grizy filters.

- Ideally, there are “calibration” stars in your image
- You know the magnitude of the calibration stars, and you can measure how many counts they created in your image.
- Simple calibration: $\text{mag} = -2.5 \log(\text{counts}) + \text{ZP}$
 - With your calibration stars, solve for the “zero point” ZP.
- For all other stars, compute the magnitude using the measured zeropoint.
- This works because CCDs are very *linear* in their response; makes relative photometry very robust.

- There are a few important details that this leaves out:
 - Why are Gaia, PS1, or eventually LSST magnitudes good for calibration? How did they calibrate their images?
 - Is the zero point all that matters? What about comparing different surveys?
 - Absolute calibration: what actually defines how bright a magnitude is?

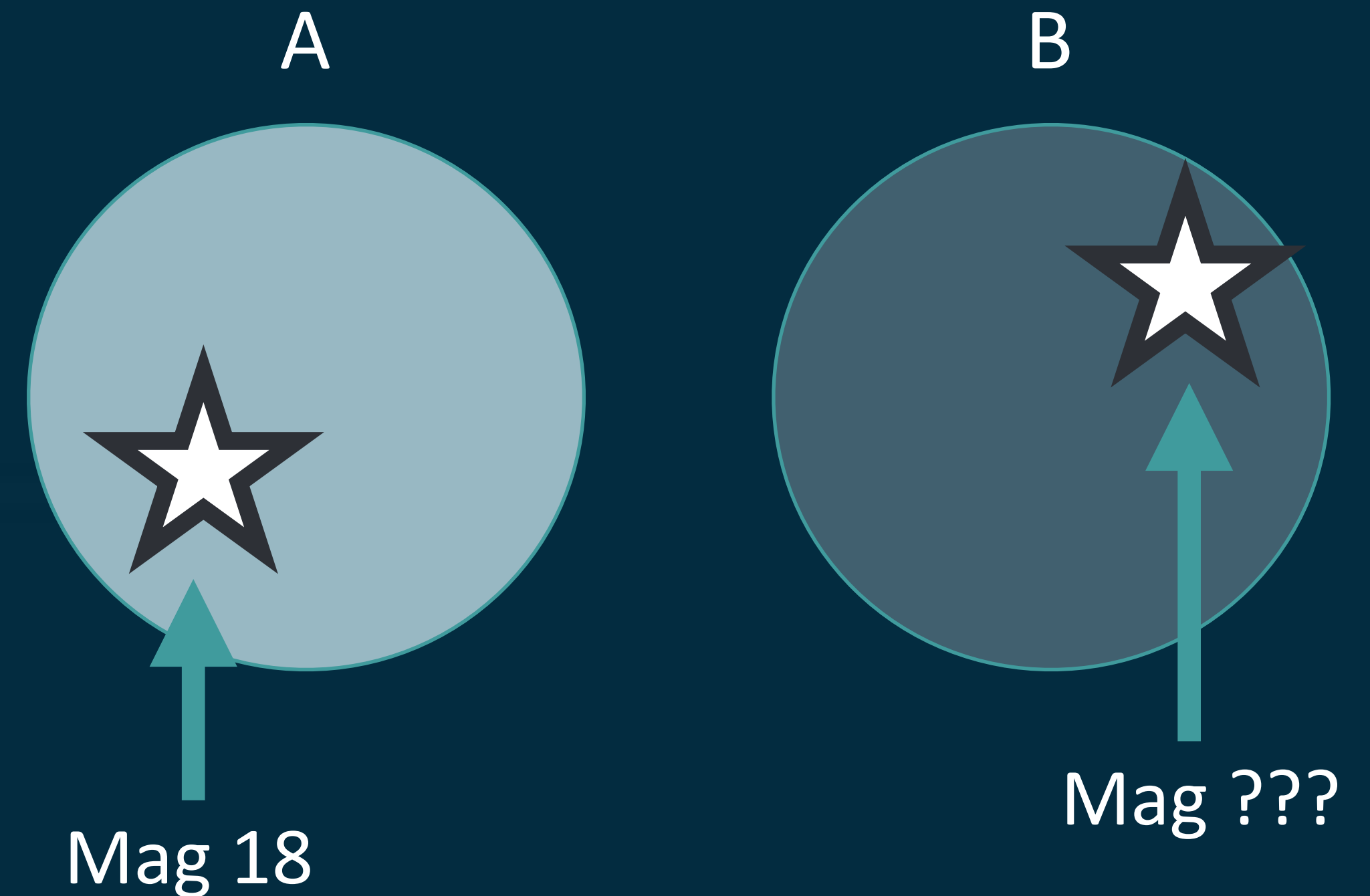
Survey Calibration

- Let's say I'm running a big survey.
- I have two fields, A and B.



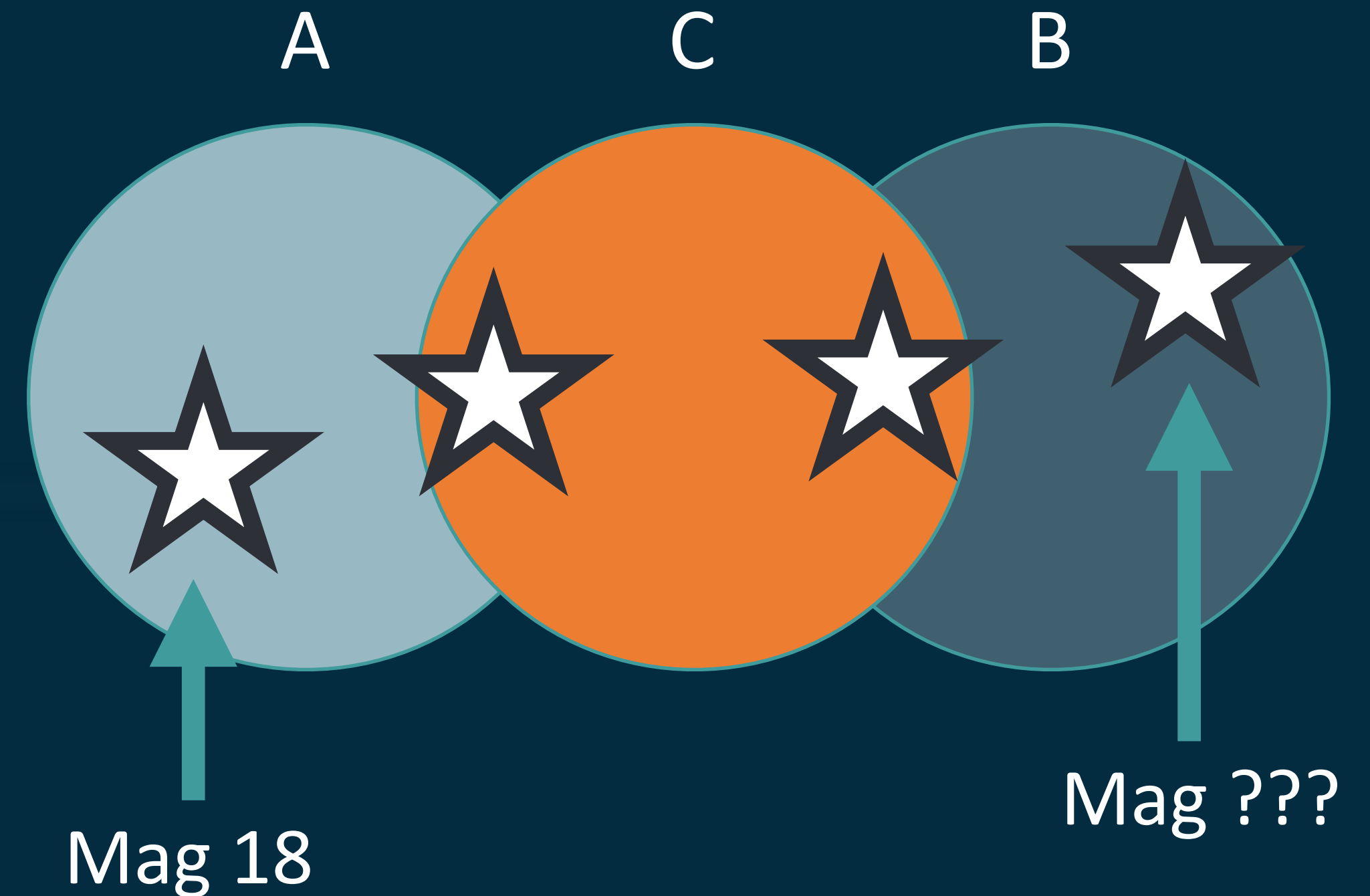
Survey Calibration

- Let's say I'm running a big survey.
- I have two fields, A and B.
- A has a calibrated star, magnitude 18
- B doesn't have any calibration stars, but it has a star I'm interested in.
- Bad news, survey ended, so I'm out of luck.



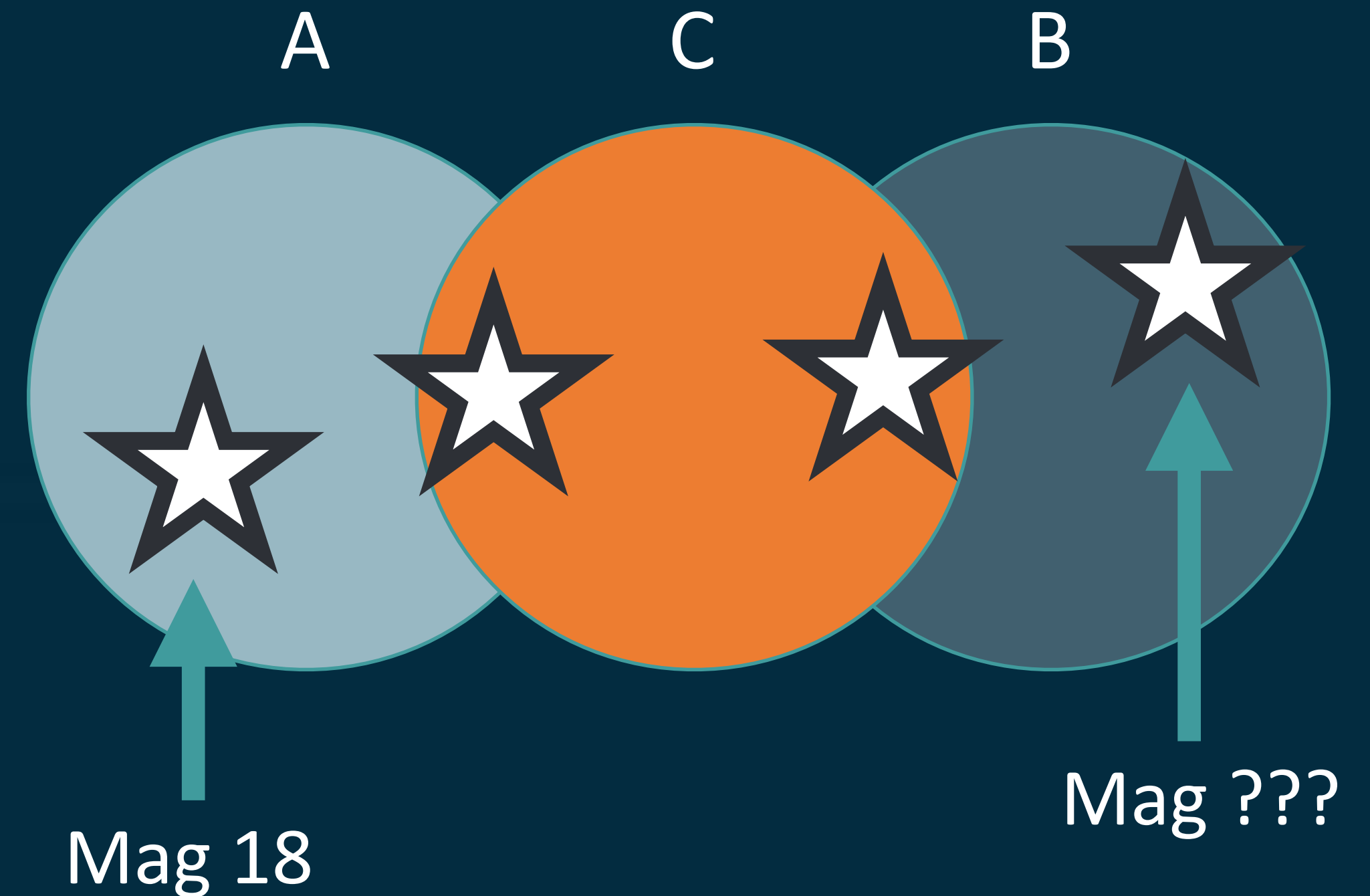
Survey Calibration

- A survey extension is approved!
- If I take Exposure C, it will have some stars that overlap Exposure A, and some stars that overlap Exposure B.
- Exposures A and C must “agree” on how bright the stars they share in common are. I.e., I calculate a zero point for C that minimizes the residual of the stars shared with A.
- The same minimization can be done between exposures C and B.



Survey Calibration

- The exciting part is that we don't need to solve B and C separately, we can solve the whole survey simultaneously.
- Concept extends to arbitrary numbers of exposures.
- Linear least-squares minimization problem, lots of standard techniques for handling large problems like this.



- What is this accomplishing?
- We know that there are many effects that can change the throughput of the telescope from night to night, exposure to exposure. (Sometimes called a “gray” term, no color dependence)
- E.g., if we observe a field low in the sky (high airmass), more of those photons are scattered/extincted than when we observe the field high in the sky.
- The “traditional” technique was to identify and correct these effects individually, but with survey-scale data we can build and solve a model for multiple photometric effects simultaneously.

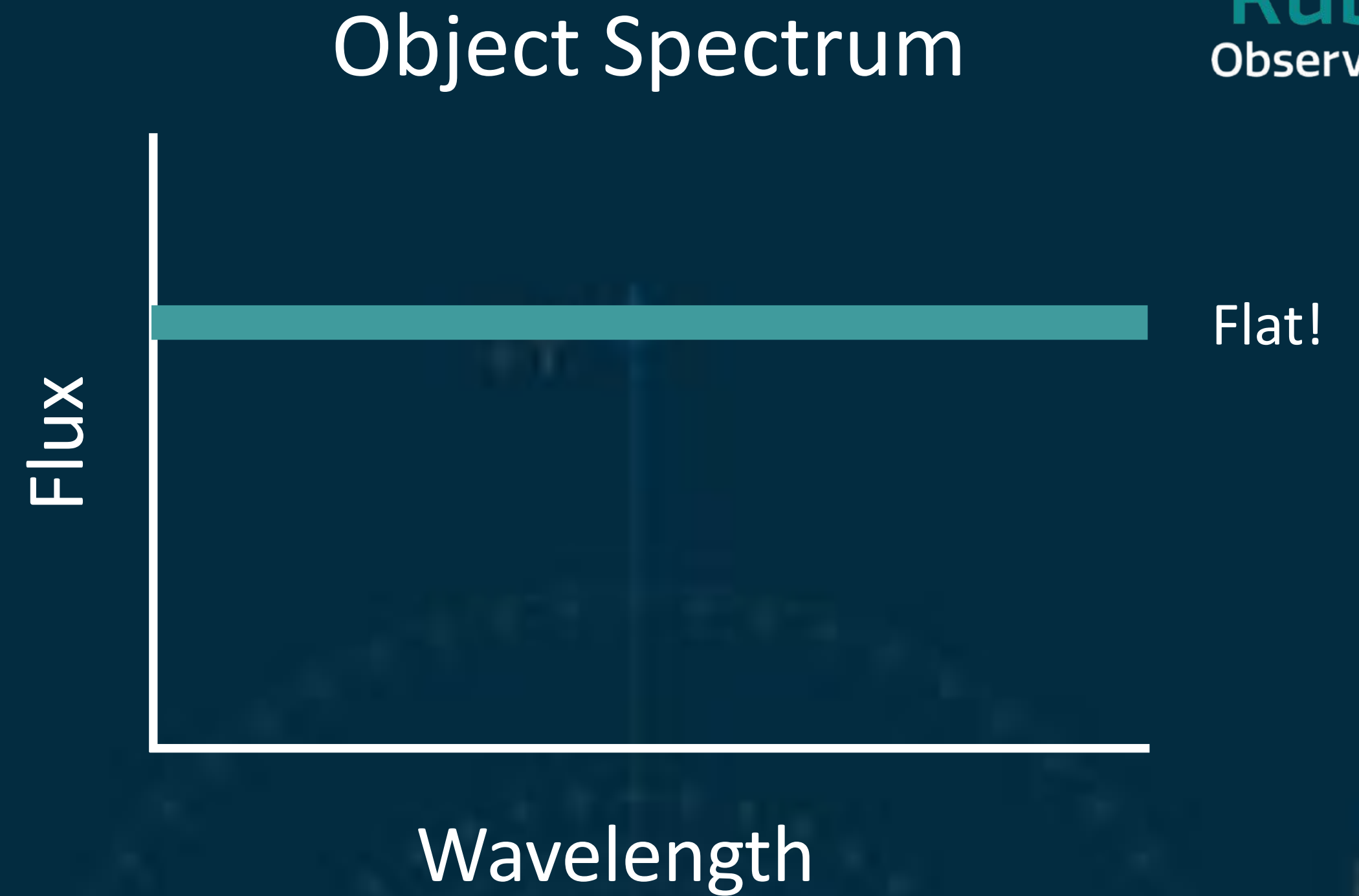
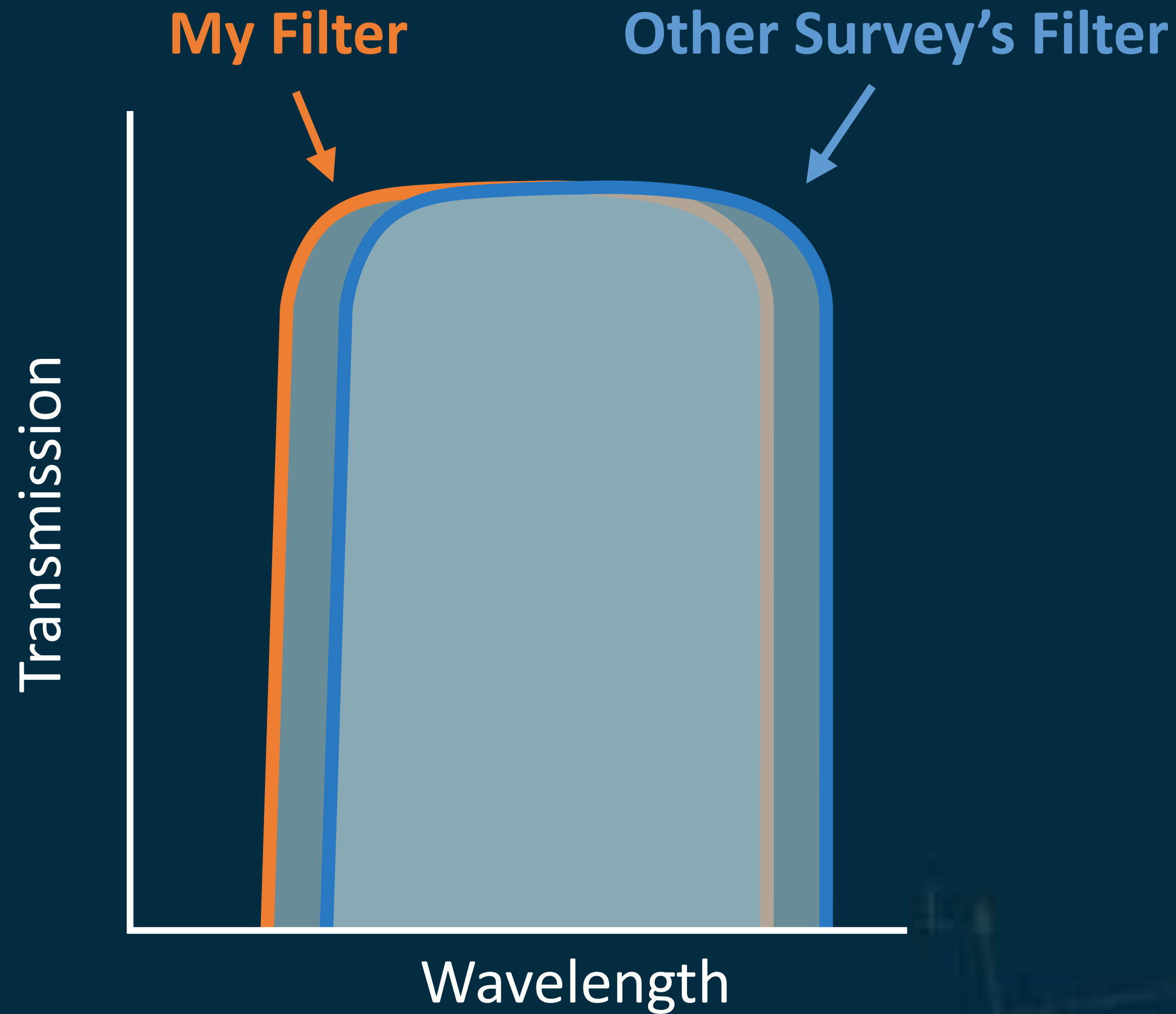
- The result is that we can treat PS1 or Gaia as a consistent photometric system.
- (That doesn't mean perfect, and we still haven't talked about absolute calibration)
- More info in the respective survey's papers:
 - SDSS: Padmanabhan et al. 2008, [arXiv:astro-ph/0703454](#)
 - Pan-STARRS: Schlafly et al. 2012, [arXiv:astro-ph/1201.2208](#)
 - DES: Burke et al. 2018, [arXiv:astro-ph/1706.01542](#)

Short Break



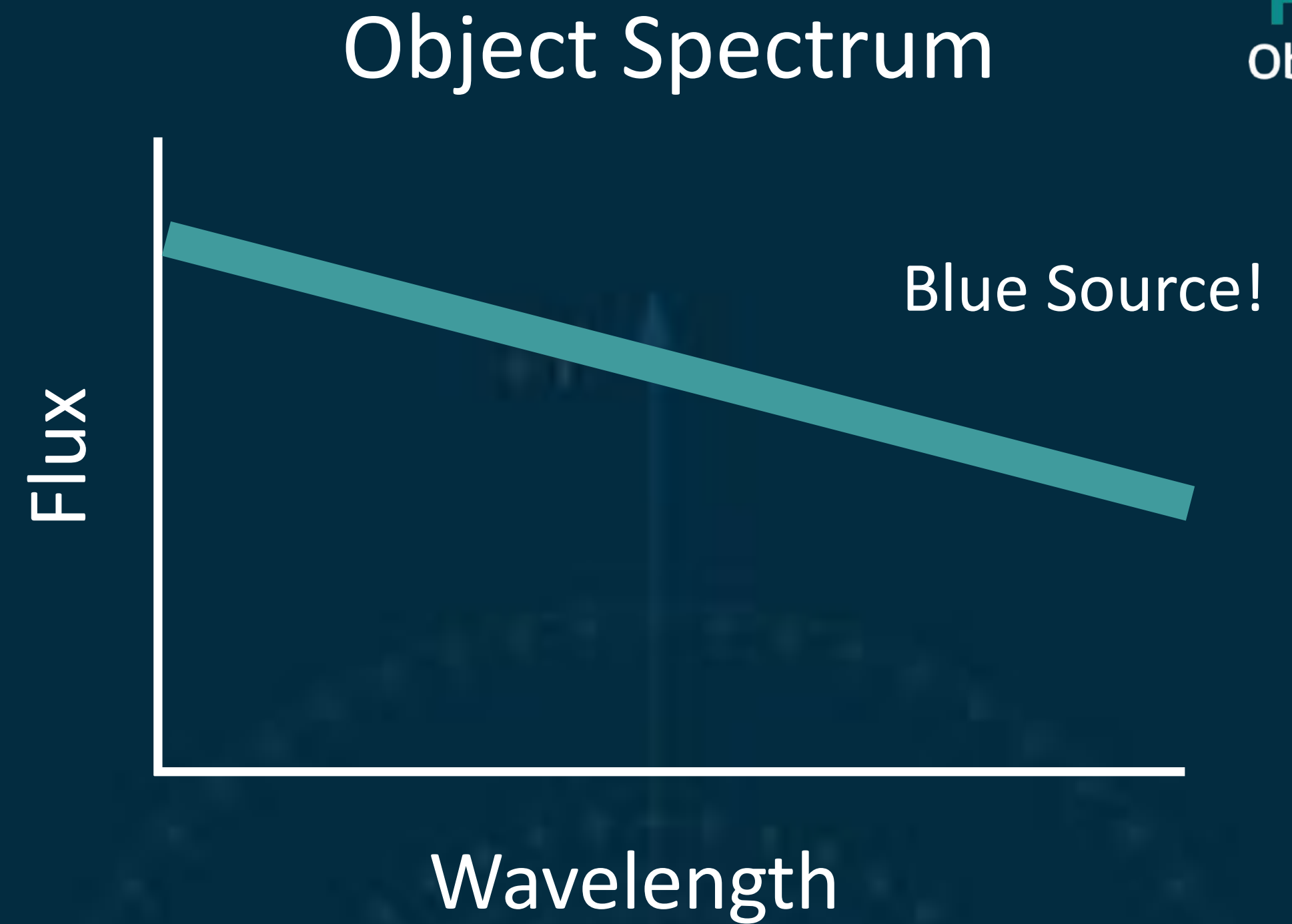
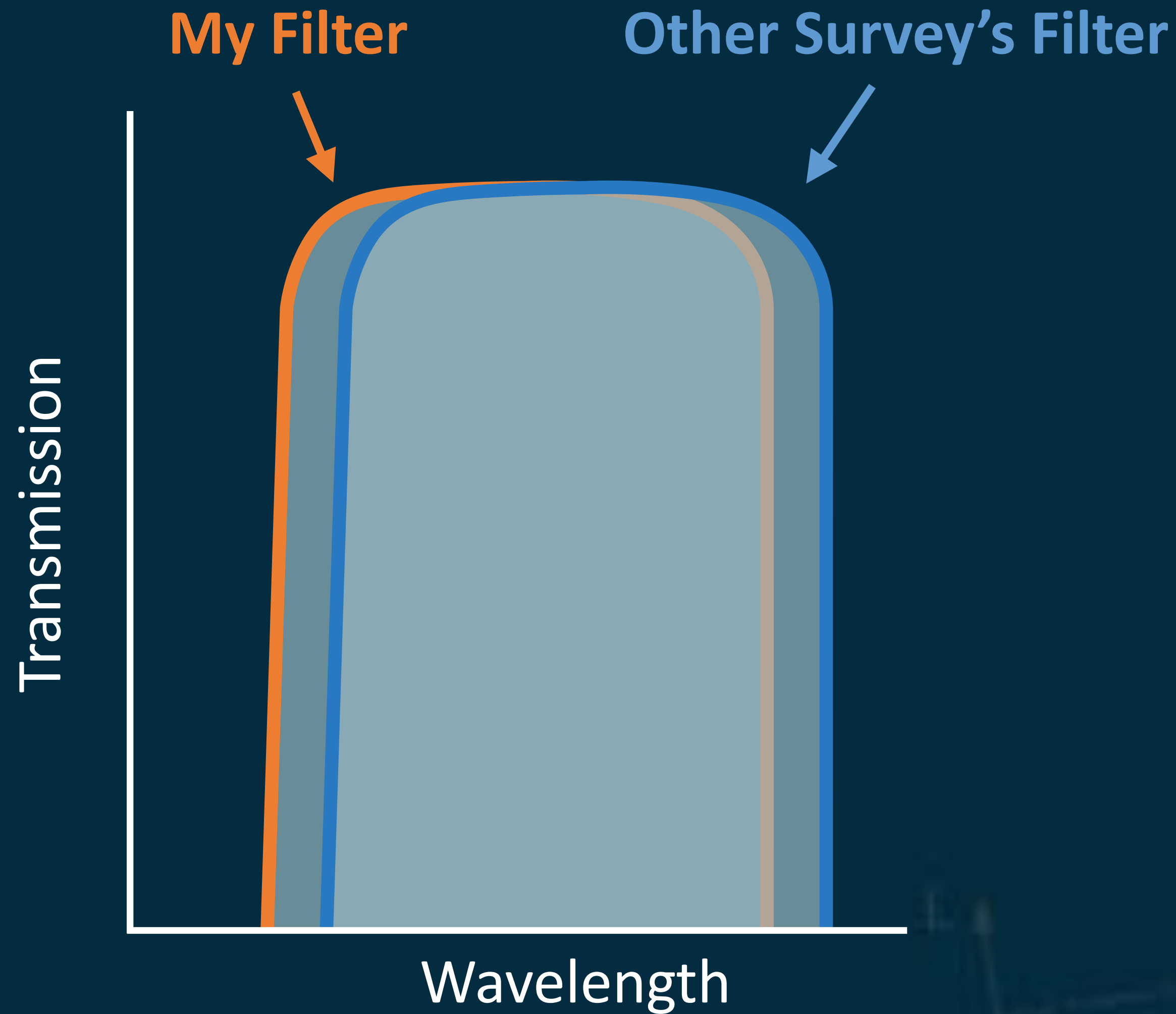
Color

- So far we've only dealt with "gray" terms; no spectral dependence at all.
- The modern challenge for surveys like LSST is that there is spectral dependence everywhere



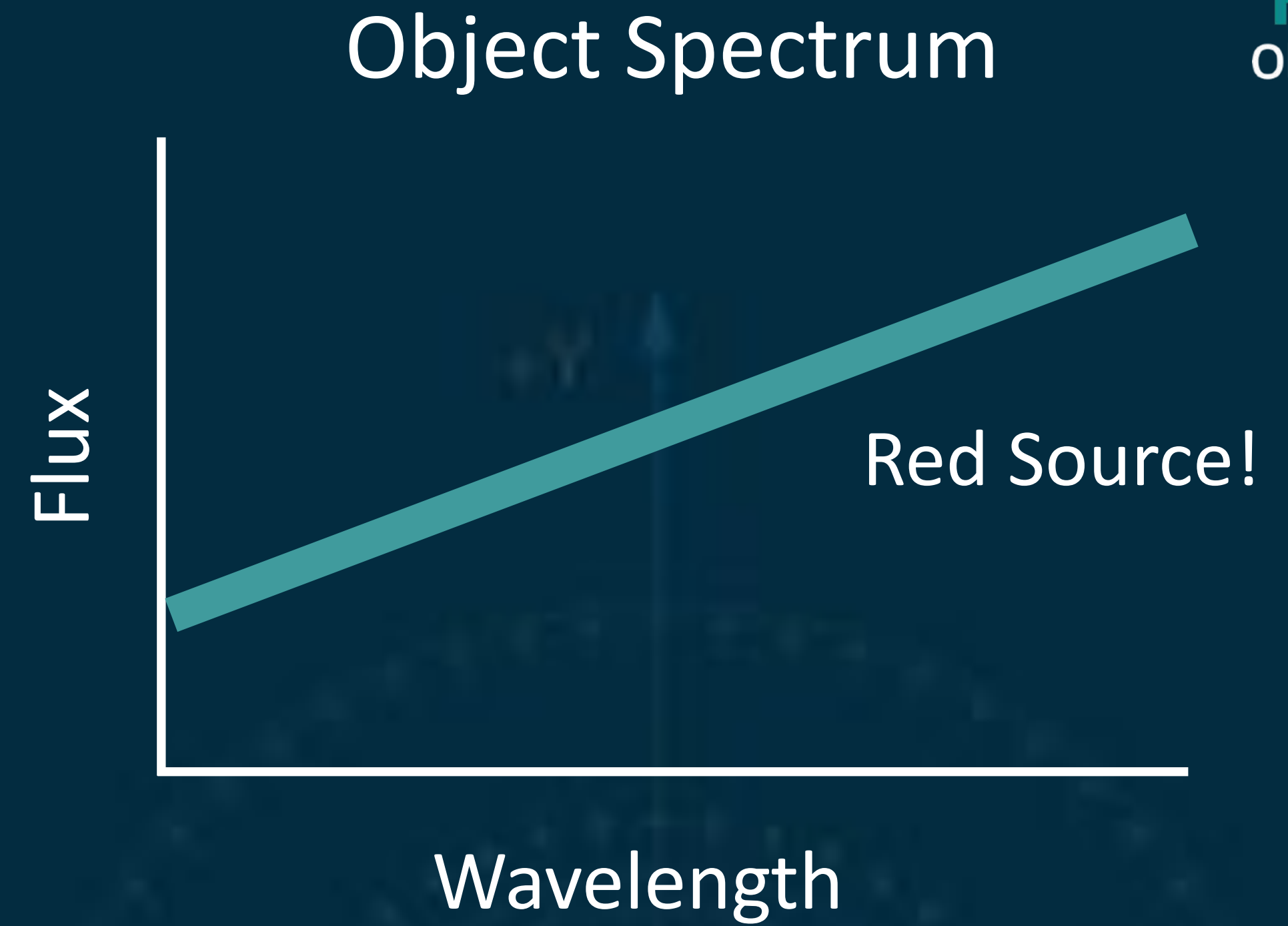
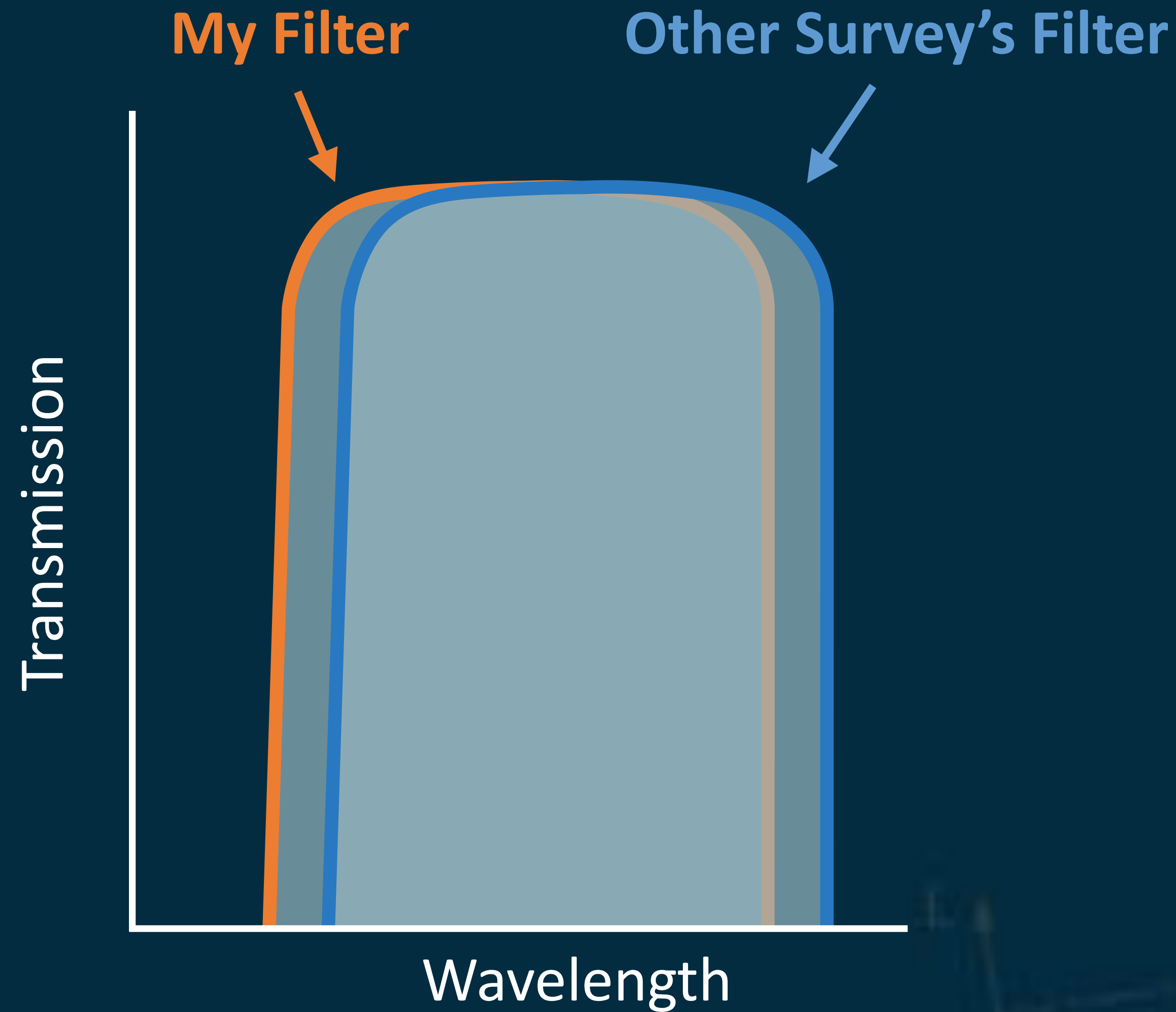
Measured Flux

Other Survey	1.0
My Survey	1.0



Measured Flux

Other Survey	1.0
My Survey	1.1



Measured Flux

Other Survey	1.0
My Survey	0.9

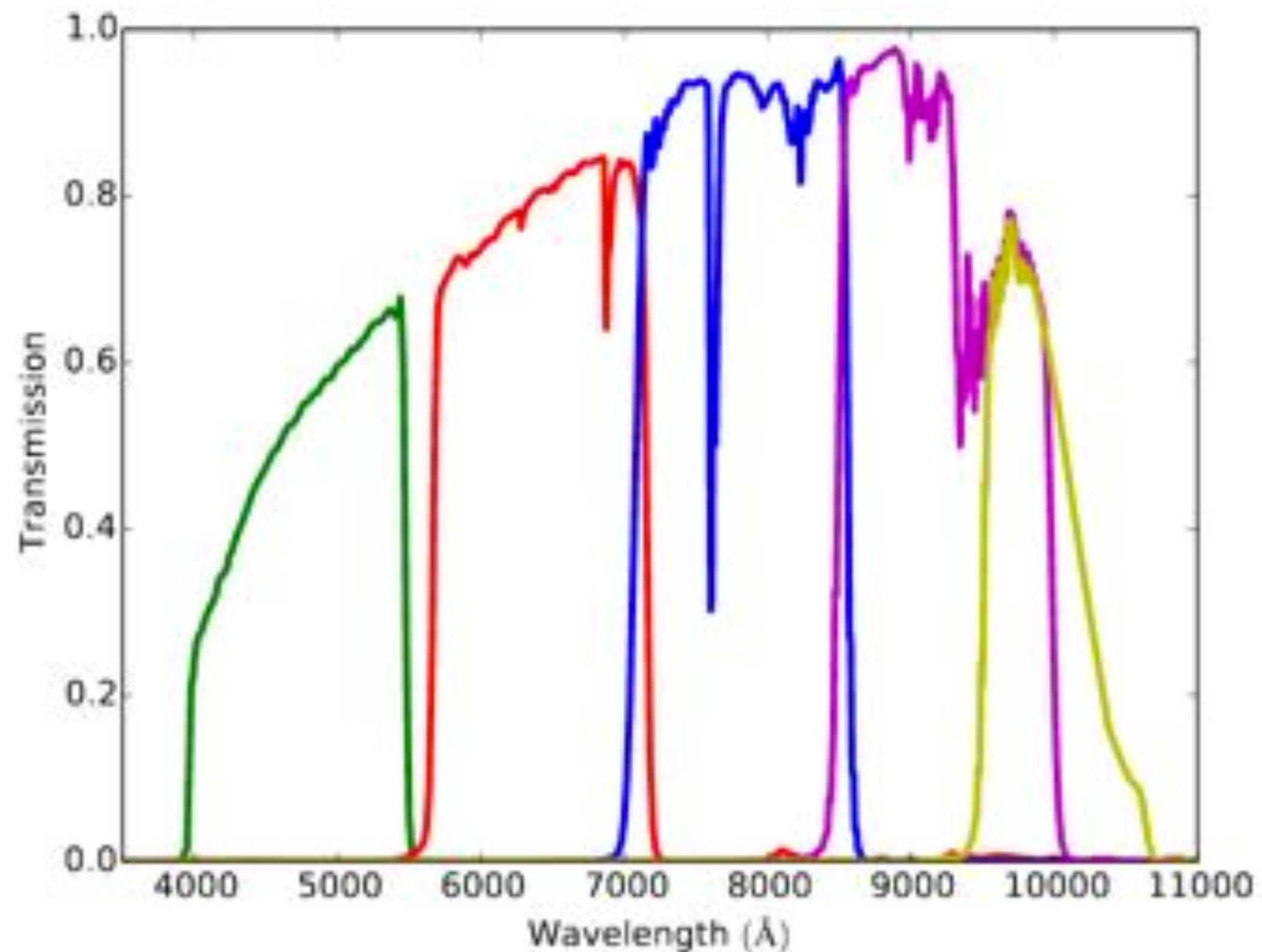
Color terms

- Every image will have both blue and red sources present, so there's no adjustment to the zero point that will correct for both.
- Optimistically this might be “just noise” that I've added, but it's a systematic effect that could affect science.
- Traditional solution is to adopt a “color term”, so that my measurement becomes something like:
 - $\text{mag} = -2.5 \log(\text{counts}) + \text{ZP} + C(\text{g-r})$
 - where C is a constant, and (g-r) is the color of the star that I'm measuring. (picking g and r as arbitrary example filters)

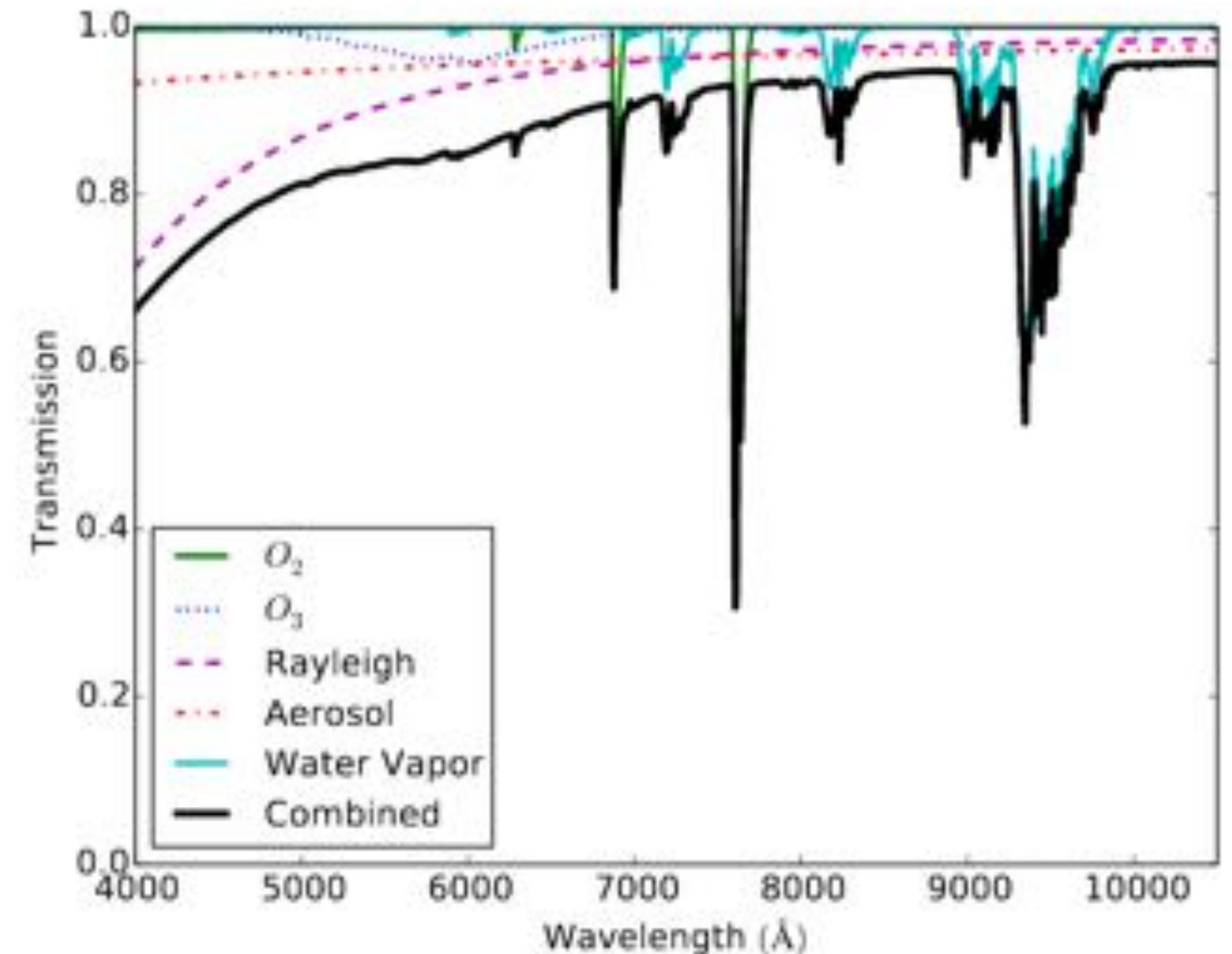
- Color terms might be sufficient if we're just correcting fixed filter edge differences. But reality is more complicated:
- “Total” passband throughput, including the atmosphere, changes over time.
 - => Even within a survey, with fixed hardware, chromatic variation is present between exposures.

- Individual atmospheric components vary within a night

DES Passbands, including atmosphere



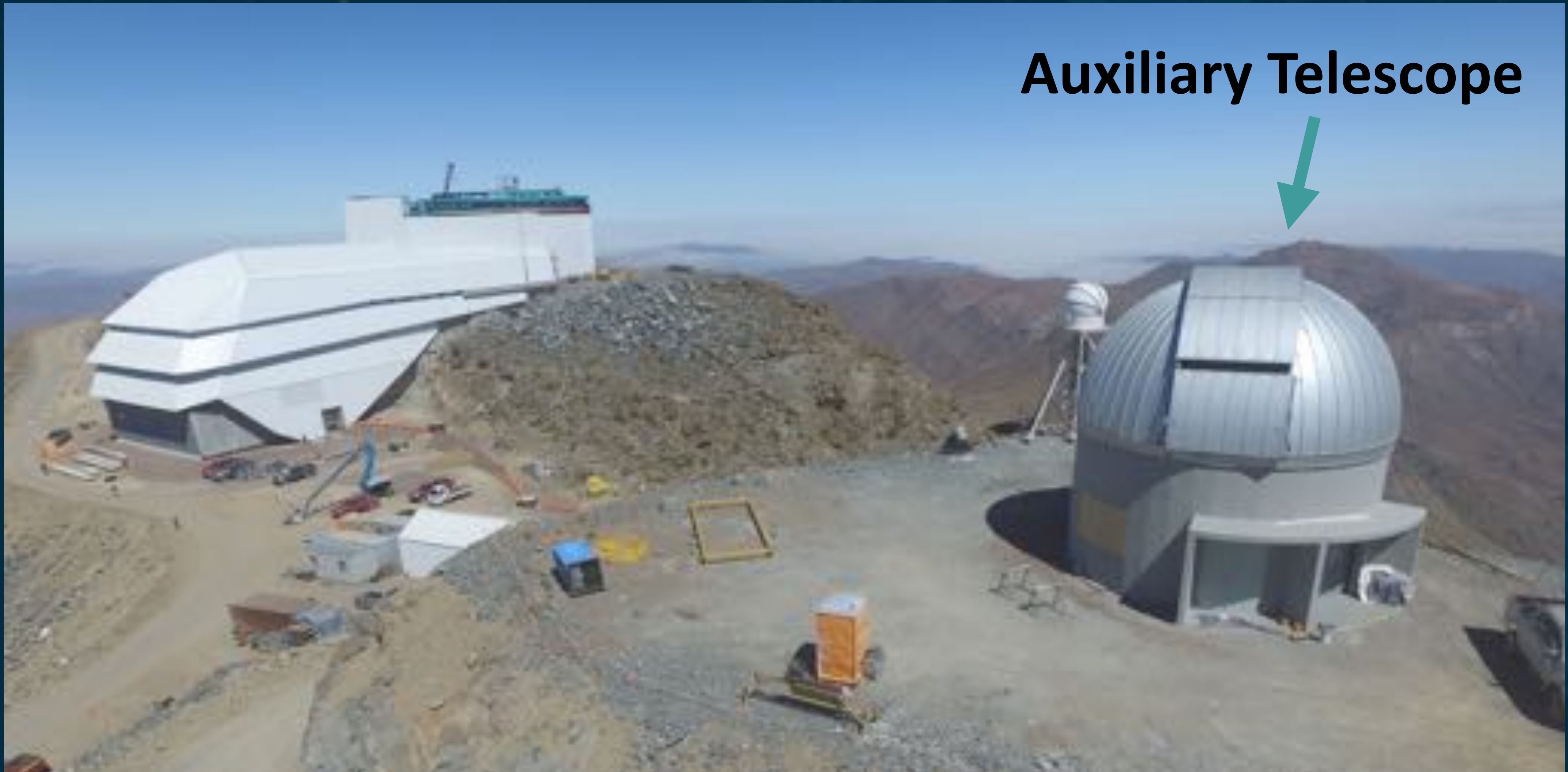
Model Atmosphere



From Burke et al. 2017

Rubin Observatory plans

Auxiliary Telescope



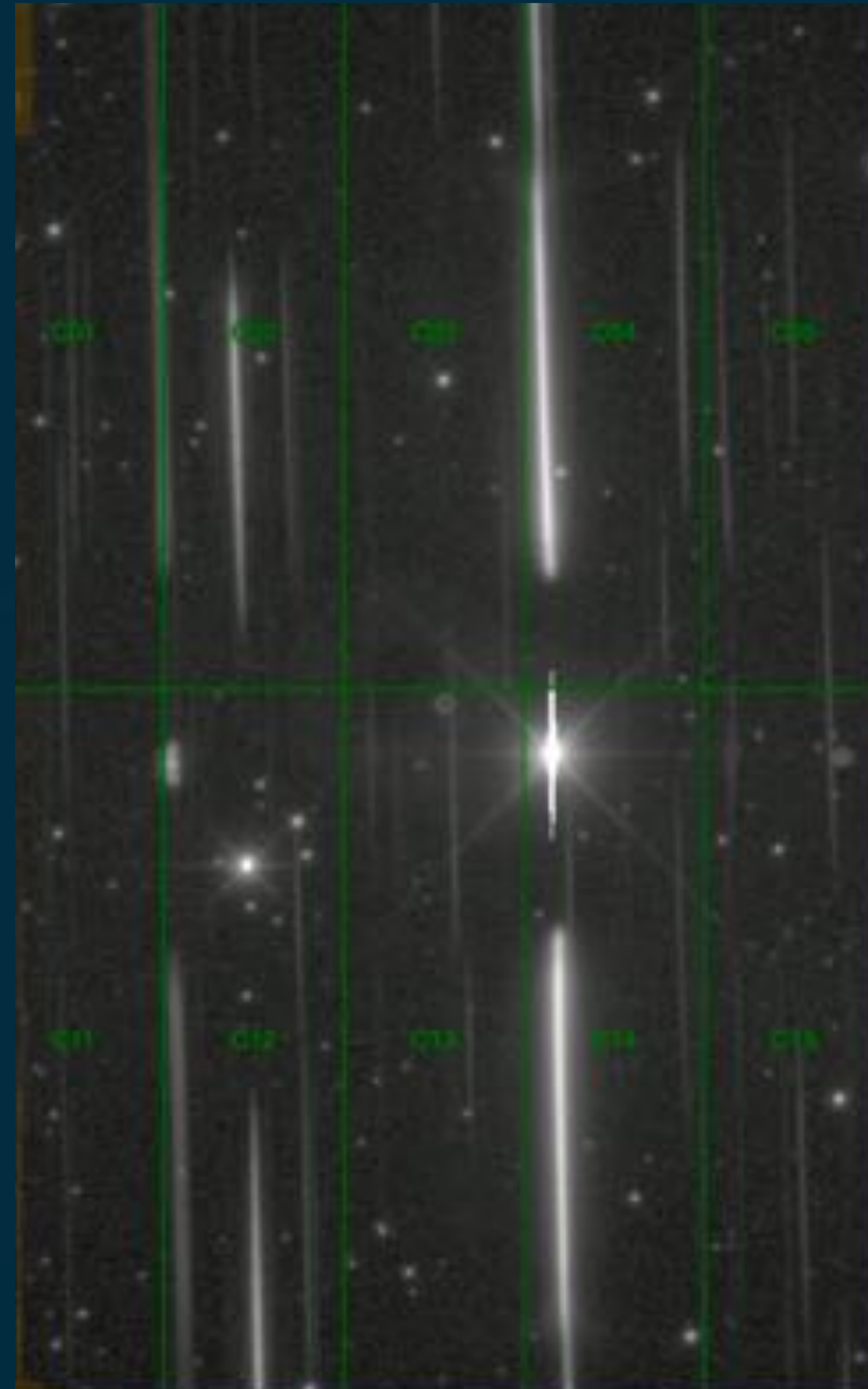
Auxiliary Telescope

- AuxTel continuously takes spectra of standard stars, with broad wavelength coverage
- Fit atmospheric models to these spectra, tells us what the “effective” passbands are for the main survey.



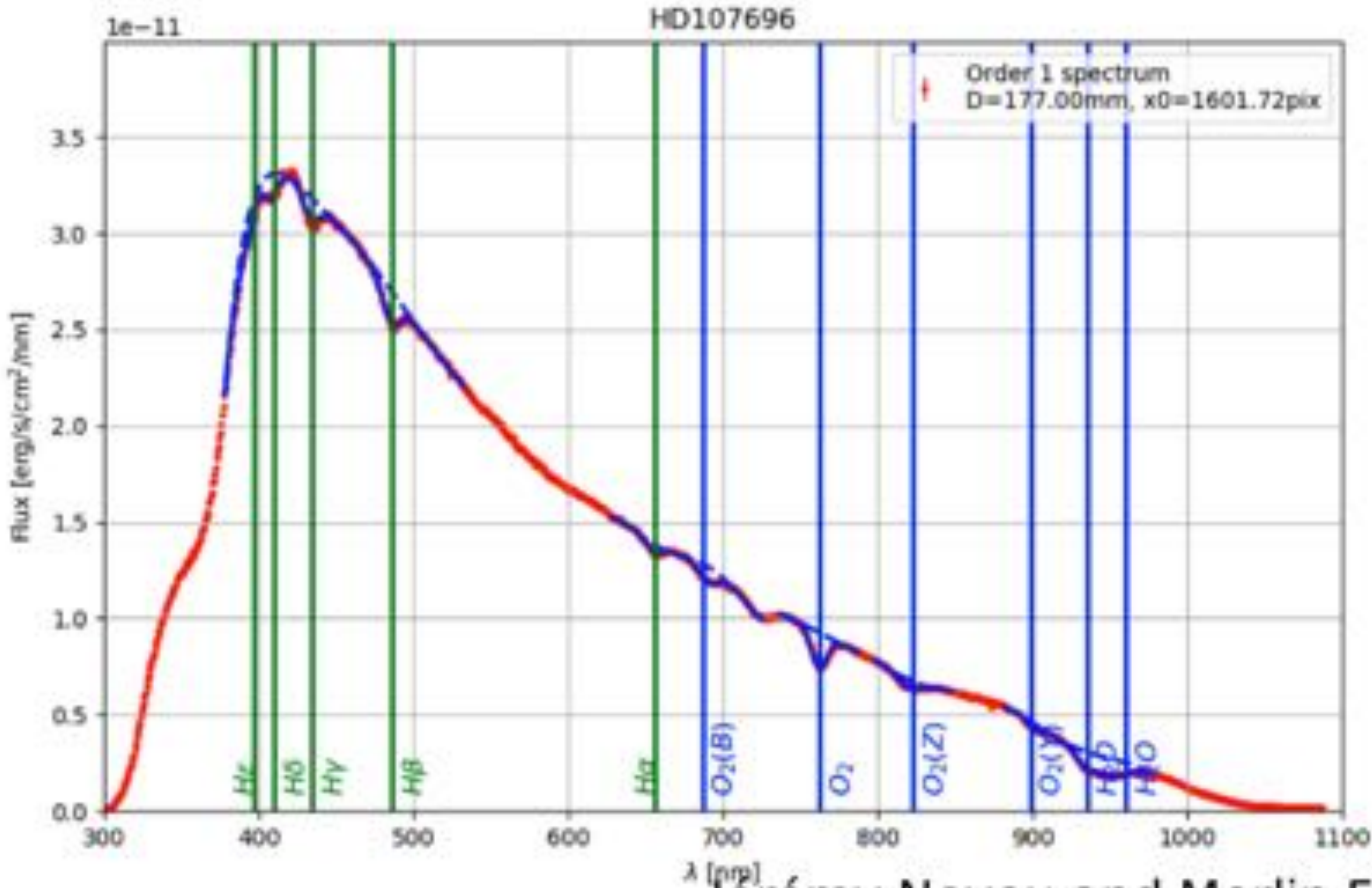
Auxiliary Telescope

- AuxTel continuously takes spectra of standard stars, with broad wavelength coverage
- Fit atmospheric models to these spectra, tells us what the “effective” passbands are for the main survey as a function of time, for each night of observing.



Rubin
Observatory





Jérémy Neveu and Merlin Fisher-Levine

Summarizing Photometric Calibration

- Large surveys “self-calibrate” to create their own internally-consistent magnitude system
- System is tied to an external “absolute” calibration for physical flux, using a small set of calibrators.
- Measured magnitudes are dependent on the exact bandpass used for measurement.
- Bandpasses change from survey to survey, from night to night within a survey, and even within a night.
- Accurate bandpass calibration is at the forefront of improving photometric accuracy.