

Take Home Exam 1

Max Callaghan

October 2015

1 Part I: Basic Questions [14pt: each 2pt]

Briefly explain why your chosen answer is correct.

1. **Question**

False or true: To judge, whether adding an additional explanatory variable improves the model, I check, whether the R^2 increases.

Answer

This is true to an extent. The R^2 describes how much of the variation in the dependent variable is explained by variation in the independent variables. Therefore, when the R^2 increases, our model is explaining more of the variation in the independent variable. Nevertheless, one should avoid ' R^2 Maximising', especially if explanatory variables are added to the model without theoretical justification. Adding explanatory variables will *always* increase the R^2 , even if this is just due to chance. The Adjusted R^2 adjusts R^2 according to the number of predictors, and can help in avoiding overfitting the model

2. **Question**

False or true: When the panel-specific factors a_i are significant, the fixed-effects estimator will be preferred over pooled OLS.

Answer

True. In a fixed effects model, time-invariant factors are captured by a_i . Where these are significant we can say that the fixed effects captured by a_i are unobservable time-invariant differences across individuals. If these are present, then it is likely that the assumption of i.i.d of our error terms is very likely violated in a pooled OLS model. It is also likely, if the unobservable characteristics of each individual panel observation are correlated with the observable characteristics in our model, that the assumption of exogeneity of the regressors is also very likely violated.

3. Question

False or true: I cannot reject a Null-hypothesis on a single coefficient, when the absolute value of the t -statistic is smaller than the critical value.

Answer

True. At a given sample size and probability threshold, the critical value states the minimum value of t at which we can reject a Null-hypothesis. If t is above the critical value, we can reject the Null-hypothesis that the coefficient is not statistically significant, and if it is lower, we cannot reject it.

4. Question

False or true: The OLS estimators β_h become more accurate, when the variance of the independent variable x_{hit} decreases

Answer

The accuracy of the estimated coefficient is determined by

$$\widehat{Var}(\hat{\beta}_h) = \frac{\hat{\sigma}_\epsilon^2 \frac{1}{NT}}{(1 - R)_h^2 Var(x_{it})}$$

for $k = 1, \dots, k$.

Therefore, when the variance decreases, the estimators β_h become less accurate.

5. Question

Calculate the R^2 of a regression, of which the variance of the realized variable y is equal to 6.4 and the variance of the fitted dependent variable \hat{y} is 5.8

Answer

6. Question

False or true: Including an irrelevant variable does not lead to biased OLS coefficients.

Answer

Including irrelevant variables does not lead to biased OLS coefficients in the relevant variables. It can only make the model less efficient. If the true model is y

7. Question

False or true: When a regressor is endogenous, we have the situation that the dependent variable y_{it} is correlated with the residual ϵ_{it} , $cov(y_{it}, \epsilon_{it}) \neq 0$.

Answer

2 Part 2: GDP Growth and Investment [28pt]

1. Question

Calculate the variances of the GDP growth ($Var(y_{it})$) and investment ($Var(x_{it})$) and their covariance ($Cov(x_{it}, y_{it})$).

Answer

- Population variance of GDP Growth: $\frac{1}{NT} \sum_{i=1}^N \sum_{t=1}^N (y_{it} - \bar{y})^2 = 63.75$
- Population variance of Investment: $\frac{1}{NT} \sum_{i=1}^N \sum_{t=1}^N (x_{it} - \bar{x})^2 = 9.93$

2. Question

Calculate the OLS solution for $\hat{\beta}_0$ and $\hat{\beta}_1$ and write-up the regression equation.

Answer

$$\hat{\beta}_1 = \frac{Cov(x_{it}, y_{it})}{Var(x_{it})} \text{ and } \hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$$
$$\hat{\beta}_1 = 0.335744 \text{ and } \hat{\beta}_0 = -3.9314909$$
$$GDPgrowth_{it} = -3.93 + 0.34 Investment_{it}$$

3. Question

Give an interpretation of the estimated coefficients $\hat{\beta}_0$ and $\hat{\beta}_1$.

Answer

The estimated coefficients tell us that the model predicts that when x (Investment) is 0, y (GDP growth) will be $\hat{\beta}_0 = -3.93$. For every increase in x , y is predicted to increase by 0.34. The model estimates a positive effect of Investment on GDP growth.

4. Question

Add the fitted values of y_{it} , $\hat{y}_{it} = \hat{\beta}_0 + \hat{\beta}_1 x_{it}$, to the table above.

Answer

See excel sheet.

5. Question

Calculate the residuals and add them into the table above.

Answer

See excel sheet. $\epsilon_{it} = \hat{y}_{it} - y_{it}$

6. Question

Draw the regression line into the graph below and mark explicitly, where the regression line cross the y axis and the slope.

Answer

The graph given in the exam is substituted for a similar graph produced by excel that extends the y axis so that the intercept can be drawn.

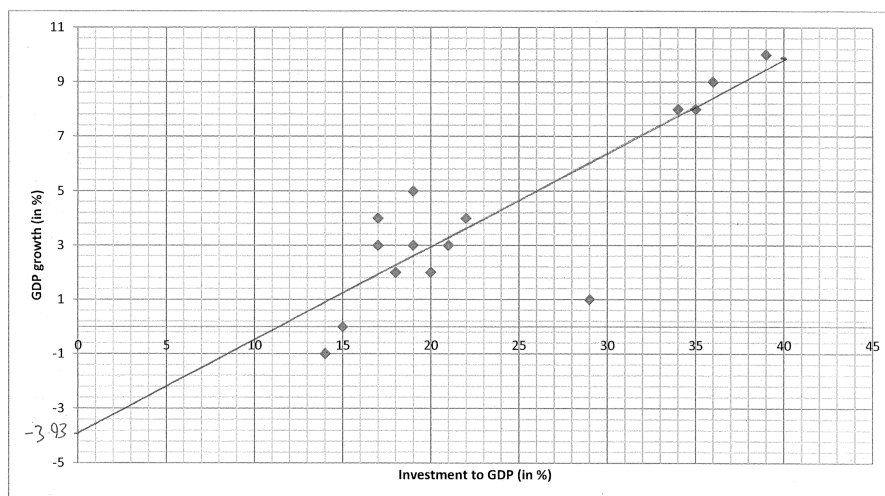


Figure 1: Intercept = -3.93, Slope = 0.34

7. Question

Use graphical inspection to judge, whether this regression suffers from heteroscedasticity.

Answer

It is difficult to make a judgement with so few data points, but the variance at high values of x seems to be smaller than the variance at low values of x . This suggests that the data is, at least to some extent, heteroscedastic.

8. Question

Calculate the standard errors of $\hat{\beta}_1$ (Note: The standard error is the square root of their variances: $s.e.\hat{\beta}_1 = \sqrt{\widehat{Var}(\hat{\beta}_1)}$).

Answer

$$s.e.\beta_1 = \sqrt{\frac{\frac{1}{n-2} \sum_{i=1}^N \sum_{t=1}^T \epsilon_{it}^2}{\sum_{i=1}^N \sum_{t=1}^T (x_{it} - \bar{x})^2}} = 0.055$$

9. Question

Perform a t -test at the 5% significance level to test the hypothesis that the level of investment has a positive impact on GDP growth. Thus, the Null Hypothesis is $H_0 : \beta_1 = 0$. Interpret the result.

Answer

The t -statistic of our hypothesis is given by

$$t = \frac{\hat{\beta}_1 - \hat{\beta}_1^0}{s.e.\hat{\beta}_1} = \frac{0.34 - 0}{0.055} = 6.18$$

Our degrees of freedom are $df = NT - k = 16 - 1 = 15$

With 15 degrees of freedom, the critical value for a t -test at the 5% significance level is 2.131.

Since 6.18 is larger than 2.131, we can reject the null hypothesis that the level of investment has no impact on GDP growth.

10. **Question**

Calculate the R^2 of the regression and interpret the result (Hint: Choose the formula, which seems most convenient given the variables you already have at hand).

Answer

$$R^2 = 1 - \frac{Var(\hat{\epsilon})}{Var(y)} = 0.72$$

3 Part 3: Current Account Imbalances and Exchange Rate Regimes [37pt]

3.1 Regression preparation [6pt]

(a) **Question**

Explain briefly, why we should concentrate on the *absolute* value and not the level of the current account to measure current account imbalances.

Answer

We want to look at current account imbalances. Variation either side of 0 is an imbalance, so we look at the absolute value, and take that as the size of the current account imbalance, regardless of direction.

(b) (i) **Question**

abs_cagdp: A variable that depicts the absolute value of *cagdp* ($|cagdp|$) (Hint: Use Stata help to find out the command to calculate absolute values).

Answer

```
1 _____ Stata code/output _____  
1 cap gen abs_cagdp = abs(cagdp)
```

(ii) **Question**

trade_openness: A variable that measures nominal export relative to GDP plus nominal import to GDP (*imports* + *exports*).

Answer

```
1 _____ Stata code/output _____  
1 cap gen trade_openness = importsgdp + exportsgdp
```

(c) **Question**

We want to focus only on industrial countries. Thus, drop all non-industrial countries from the data set. Indicate, how many observations you have left in your data set.

Answer

Stata code/output

1 <code>drop if ind == 0</code> 2 <code>(1,465 observations deleted)</code>
--

3.2 Model Choice [8pt]

To test your hypothesis, you want to run a pooled OLS regression with *abs_gdp* as dependent variable and regime, *exportsgdp*, *trade_openess*, *finance*, *gdpgrowth* as independent variables

(a) **Question**

Explain, why we do not regress simply the *abs_cagdp* on *regime*, but also add other control variables to the set of regressors? What could be the consequences for the estimators, if one ignores important explanatory variables

Answer

If regime type was the only variable that we thought had an effect on *abs_cagdp*, we would only include regime type. If other variables affect our dependent variable and we do not include them, we risk *omitted variable bias*. When we miss out an independent variable that is both a determinant of the dependent variable *and* correlated with one or more of our independent variables, the coefficient for the included independent variable will be biased because it will contain part of the effects of omitted variables that are correlated with our included variable.

(a) **Question**

Explain, what the consequences are, if we have a multicollinearity problem among the explanatory variables

Answer

Multicollinearity describes a model where the independent variables are correlated with each other. In a case of perfect multicollinearity, there is a linear relationship between at least two of the variables. The variance of the estimated coefficients is given by

$$\widehat{Var}(\hat{\beta}_h) = \frac{\hat{\sigma}_\epsilon^2 \frac{1}{NT}}{(1 - R_h^2) Var(x_{it})} \text{ for } k = 1, \dots, k$$

The greater the relationship between x_{it} and the other independent variables (given by R_h^2), the greater the variance of our estimator. Multicollinearity makes our estimators less precise.

(a) **Question**

Test, whether we have a multicollinearity problem between our explanatory variables. Explain, how you derive your conclusion.

Answer

Stata calculates the Variance Inflation Factor (VIF) for us using the formula

$$VIF(\hat{\beta}_h) = \frac{1}{1 - R_h^2}$$

High values for VIF indicate the presence of multicollinearity. 10 is sometimes used as a cutoff point.

Stata code/output

1	. estat vif		
2			
3	Variable	VIF	1/VIF
4	-----		
5	trade_open~s	118.93	0.008408
6	exportsgdp	116.98	0.008548
7	finance	1.40	0.712628
8	regime	1.20	0.834933
9	gdpgrowth	1.13	0.886961
10	-----		
11	Mean VIF	47.93	

Unsurprisingly, we can detect multicollinearity problems in the high VIF values for both trade openness and exportsgdp. This is because we created trade openness out of a linear combination of exports and imports. So, notwithstanding some degree of variation between the balance or otherwise of exports and imports, they are highly correlated

(a) **Question**

In case you do detect multicollinear variables: What would you recommend to do? Which of the potential multicollinear variables would you drop?

Answer

We created the variable *tradeopenness*, presumably, because we thought that the combination of both exports and imports had an effect on our dependent variable. If we drop it, we are left with just imports; if we drop imports, then we still have the effect of the combination of exports and imports. An alternative would be to use imports and exports separately, but they would most likely still be highly correlated, though to a lesser extent.

3.3 Estimating a pooled OLS regression [15pt]

(a) **Question**

Continue with your preferred set of regressors (meaning: drop if nec-

essary a variable(s) to solve for a potential multicollinearity problem (see Question 2.c)) and estimate the determinants of *abs_cagdp* with *pooled OLS*.

Answer

```

----- Stata code/output -----
1 reg abs_cagdp regime trade_openness finance gdpgrowth
2 outtex, file(pooled.tex) labels level detail ///
3 legend key(stab) replace

```

Table 1: Estimation results : regress

Variable	Coefficient	(Std. Err.)
regime	-0.701**	(0.158)
trade.openness	0.029**	(0.002)
finance	0.106	(0.085)
gdpgrowth	0.107*	(0.049)
Intercept	1.842**	(0.276)
<hr/>		
N	818	
R ²	0.213	
F _(4,813)	54.870	
<hr/>		
Significance levels :	† : 10%	* : 5% ** : 1%

(a) **Question**

Answer

(a) **Question**

Answer