

# **TTIC 31230, Fundamentals of Deep Learning**

David McAllester, Autumn 2022

Diffusion Image Modeling Timeline

# Improved Denoising Diffusion Probabilistic Models

## Nichol and Dhariwal, February 2021

This paper provides a method for training an “uncertainty level” for each color channel of each pixel.

Later papers in the code base use these uncertainty levels to weight guidance strength for each color channel of each pixel in “guided diffusion”.

Guided diffusion with channel-level guiding strength is used in DALLE-2.

## Getting Per-Pixel Decoder Uncertainty

Per-pixel decoder uncertainty will be estimated by optimizing the VAE bound on cross-entropy loss.

These papers call it the variational lower bound (VLB) rather than the ELBO.

The paper is written from the perspective of simply optimizing the VLB.

## Why Optimize the VLB?

We can compare any two models of a distribution by computing upper bounds on cross-entropy loss for each model.

Since gradient descent on corss entropy (GPT-3) is so successful, maybe we shuld also be doing **graduate student descent** on cross entropy.

In other words, cross entropy may be an undervalued metric for comparing different systems trained with different architectures.

# Improved Cross-Entropy Loss

For image models the cross entropy is generally referred to as negative log likelihood (or NLL) and is measured in bits per image channel.

Model	ImageNet	CIFAR
Glow (Kingma & Dhariwal, 2018)	3.81	3.35
Flow++ (Ho et al., 2019)	3.69	3.08
PixelCNN (van den Oord et al., 2016c)	3.57	3.14
SPN (Menick & Kalchbrenner, 2018)	3.52	-
NVAE (Vahdat & Kautz, 2020)	-	2.91
Very Deep VAE (Child, 2020)	3.52	2.87
PixelSNAIL (Chen et al., 2018)	3.52	2.85
Image Transformer (Parmar et al., 2018)	3.48	2.90
Sparse Transformer (Child et al., 2019)	3.44	<b>2.80</b>
Routing Transformer (Roy et al., 2020)	<b>3.43</b>	-
DDPM (Ho et al., 2020)	3.77	3.70
DDPM (cont flow) (Song et al., 2020b)	-	2.99
Improved DDPM (ours)	<b>3.53</b>	<b>2.94</b>

## Rewriting the VLB

For a progressive VAE with layers  $z_0, \dots, z_L$  where  $z_0 = y$  the VLB is

$$\begin{aligned} -\ln p_{\text{gen}}(z_0) &\leq E_{\text{enc}} - \ln \frac{p_{\text{gen}}(z_L, \dots, z_0)}{p_{\text{enc}}(z_1, \dots, z_L | z_0)} \\ &= E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \frac{\ln p_{\text{dec}}(z_{\ell-1} | z_{\ell})}{\ln p_{\text{enc}}(z_{\ell} | z_{\ell-1})} \end{aligned}$$

## Rewriting the VLB

$$\begin{aligned} -\ln p_{\text{gen}}(z_0) &\leq E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})}{p_{\text{enc}}(z_{\ell}|z_{\ell-1})} \\ &= E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})}{p_{\text{enc}}(z_{\ell}|z_{\ell-1}, z_0)} \\ &= E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})p(z_{\ell-1}|z_0)}{p_{\text{enc}}(z_{\ell}, z_{\ell-1}|z_0)} \\ &= E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})p_{\text{enc}}(z_{\ell-1}|z_0)}{p_{\text{enc}}(z_{\ell-1}|z_{\ell}, z_0)p_{\text{enc}}(z_{\ell}|z_0)} \end{aligned}$$

## Rewriting the VLB

$$\begin{aligned}
-\ln p_{\text{gen}}(z_0) &\leq E_{\text{enc}} - \ln p_{\text{pri}}(z_L) - \sum_{\ell} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})}{p_{\text{enc}}(z_{\ell-1}|z_{\ell}, z_0)} - \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_0)}{p_{\text{enc}}(z_{\ell}|z_0)} \\
&= E_{\text{enc}} - \ln \frac{p_{\text{pri}}(z_L)}{p_{\text{enc}}(z_L|z_0)} - \sum_{\ell \geq 2} \ln \frac{p_{\text{dec}}(z_{\ell-1}|z_{\ell})}{p_{\text{enc}}(z_{\ell-1}|z_{\ell}, z_0)} - \ln p_{\text{dec}}(z_0|z_1) \\
&= E_{\text{enc}} \left\{ \begin{array}{l} KL(p_{\text{enc}}(z_L|z_0), p_{\text{pri}}(z_L)) \\ + \sum_{\ell \geq 2} KL(p_{\text{enc}}(z_{\ell-1}|z_{\ell}, z_0), p_{\text{dec}}(z_{\ell-1}|z_{\ell})) \\ - \ln p_{\text{dec}}(z_0|z_1) \end{array} \right.
\end{aligned}$$

## Rewriting the VLB

$$-\ln p_{\text{gen}}(z_0) \leq E_{\text{enc}} \left\{ \begin{array}{l} KL(p_{\text{enc}}(z_L|z_0), p_{\text{pri}}(z_L)) \\ + \sum_{\ell \geq 2} KL(p_{\text{enc}}(z_{\ell-1}|z_\ell, z_0), p_{\text{dec}}(z_{\ell-1}|z_\ell)) \\ - \ln p_{\text{dec}}(z_0|z_1) \end{array} \right.$$

All of the KL-divergences can be computed analytically from Gaussians. This reduces the variance in estimating the bound.

Nichol and Dhariwal compute  $-\ln p_{\text{dec}}(z_0|z_1)$  by treating each image channel as a discrete set of 256 values and computing the probability that a draw from the computed Gaussian rounds to the actual discrete value.

## Optimizing Per-Channel Decoder Variances

We now introduce a decoder network  $\tilde{\sigma}_\Psi(z_\ell, \ell) \in R^d$  to give the decoder noise level.

$$\text{dec}(z_\ell, \ell) = \frac{1}{\sqrt{1 - \sigma_\ell^2}} (z_\ell - \sigma_\ell \epsilon(z_\ell, \ell)) + \tilde{\sigma}_\Psi(z_\ell, \ell) \odot \delta \quad \delta \sim \mathcal{N}(0, I)$$

The decoder noise network  $\tilde{\sigma}_\Psi(z_\ell, \ell) \in R^d$  is trained with the VLB objective.

This improves the value of the VLB.

## Optimizing Per-Channel Decoder Variances

$$\text{dec}(z_\ell, \ell) = \frac{1}{\sqrt{1 - \sigma_\ell^2}} (z_\ell - \sigma_\ell \epsilon(z_\ell, \ell)) + \tilde{\sigma}_\Psi(z_\ell, \ell) \odot \delta \quad \delta \sim \mathcal{N}(0, I)$$

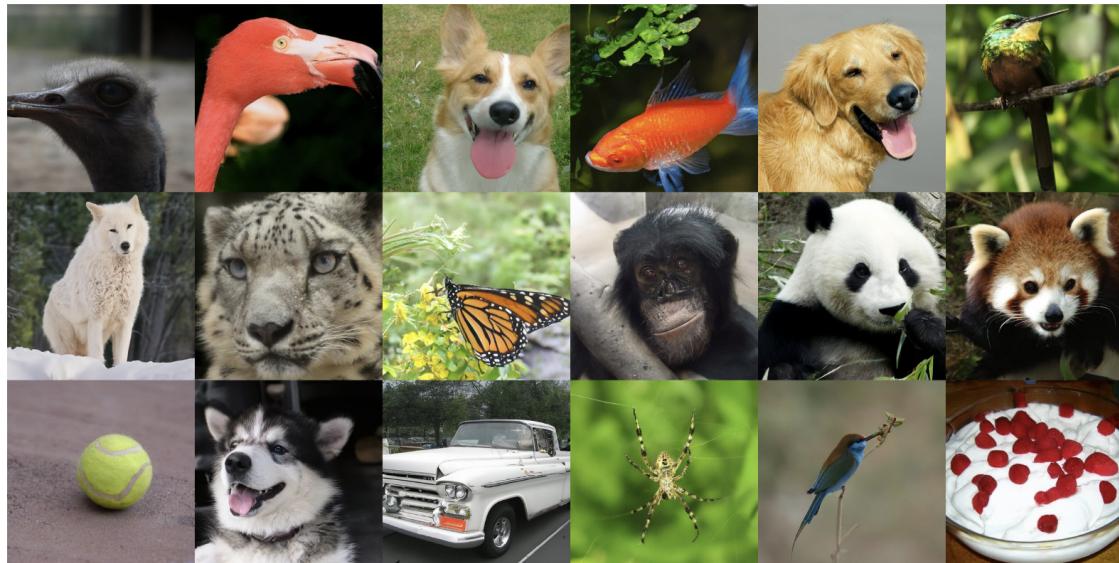
One can interpret  $\tilde{\sigma}(z_\ell, \ell)[i]$  is a level of uncertainty in the decoder value  $\epsilon(z_\ell, \ell)[i]$ .

The more uncertainty the model has in  $\epsilon(z_\ell, \ell)[i]$  the more guidance should be used in adjusting it.

# Diffusion Models Beat GANs on Image Synthesis

## Dharwali and Nichol, May 2021

This paper introduces guided diffusion as a way of handling class-conditional diffusion models.



Guided diffusion is used in DALLE-2.

## Class-Conditional Image Generation

We assume training data consisting of  $(x, y)$  pairs and we want to generate from the distribution  $P(y|x)$ . For example class-conditional image generation.

Previous approaches, such as StyleGAN, have trained a model (a GAN) for each class.

Here we will train a single model which takes the class label as input.

It seems that this can be made to work for VAEs but not for GANS without an auto-encoder component.

## Conditional Diffusion Models

An obvious approach is to draw a pair  $(x, y)$  and pass the conditioning information  $x$  to the image generator.

It is a weakness of GANs that we need a separate model for each  $x$ .

It seems to be a weakness of diffusion models that this natural approach to conditioning fails.

## Classifier Guidance

We assume a distribution on pairs  $(x, y)$ .

We also assume **a classifier**  $P(x|y)$ . For example  $x$  might be the ImageNET label for image  $y$ .

We will generate an image by using  $P(x|y)$  to “guide” generation from the unconditional model  $\epsilon(z_\ell, \ell)$ .

Guidance will be based on the score-matching interpretation of diffusion models where  $\epsilon(z_\ell, \ell)$  is interpreted as  $-\nabla_z \ln p(z)$ .

## Class-Conditional Generation

$$z_{\ell-1} = \frac{1}{\sqrt{1 - \sigma_\ell^2}} (z_\ell - \sigma_\ell \epsilon(z_\ell, \ell)) + \tilde{\sigma}_\ell \odot \delta$$

Score-matching interprets  $\epsilon(z_\ell, \ell)$  as  $-\nabla_z \ln p(z)$ .

$$p(z|x) = \frac{P(z)P(x|z)}{P(x)} \propto p(z)P(x|z)$$

We want a step in direction  $\nabla_z \ln p(z)P(x|z)$ . They use

$$\text{dec}(z_\ell, \ell) = \frac{1}{\sqrt{1 - \sigma_\ell^2}} (z_\ell - \sigma_\ell \epsilon(z_\ell, \ell)) + \tilde{\sigma}_\ell \odot \delta + s\tilde{\sigma} \odot \nabla_z \ln P(x|z)$$

## Classifier Guidance

$$\text{dec}(z_\ell, \ell) = \frac{1}{\sqrt{1 - \sigma_\ell^2}} (z_\ell - \sigma_\ell \epsilon(z_\ell, \ell)) + \tilde{\sigma}_\ell \odot \delta + \textcolor{red}{s} \tilde{\sigma} \odot \nabla_z \ln P(x|z)$$

Here  $s$  is called the scale of the guidance.

Empirically it was found that  $s > 1$  is needed to get good class-specificity of the generated image.

However, increasing  $s$  decreases diversity so we have a diversity/quality trade off.

## Other Improvements

Various architectural choices in the U-Net were optimized based on FID score (not NLL).

These improvements are used in DALLE-2.

## Classifier-Free Diffusion Guidance

Ho and Salimans, December 2021 (NeurIPS workshop)

Classification diffusion guidance uses a classification model  $P(x|y)$ .

This paper introduces “classifier-free” diffusion guidance.

Classifier-free diffusion guidance is used in DALLE-2.

## Classifier-Free Diffusion Guidance

5% of the time we set  $x = \emptyset$  where  $\emptyset$  is a fixed value unrelated to the image.

The decoder then uses

$$\tilde{\epsilon}(z_\ell, \ell, x) = s\epsilon(z_\ell, \ell, x) - (s - 1)\epsilon(z_\ell, \ell, \emptyset)$$

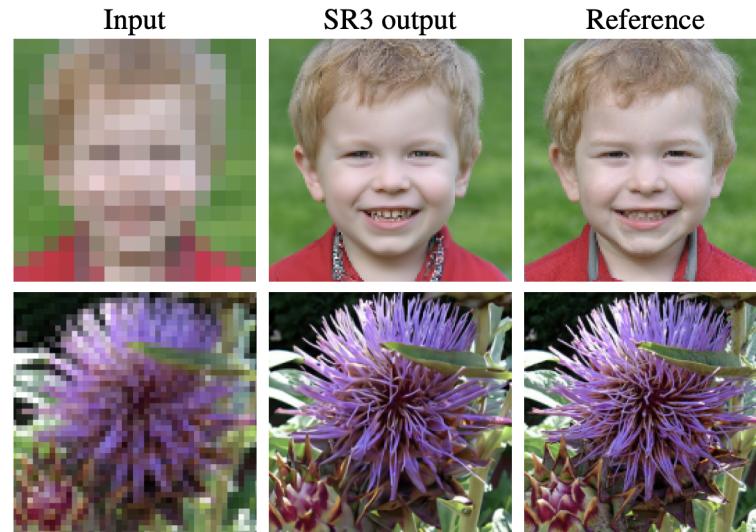
where  $s \geq 1$  controls the relative weight of the two terms.

DALLE-2 incorporates the channel-level uncertainties  $\tilde{\sigma}$  as weights on classifier-free diffusion guidance provided by CLIP.

# Image Super-Resolution via Iterative Refinement

## Saharia, Ho et al., April 2021

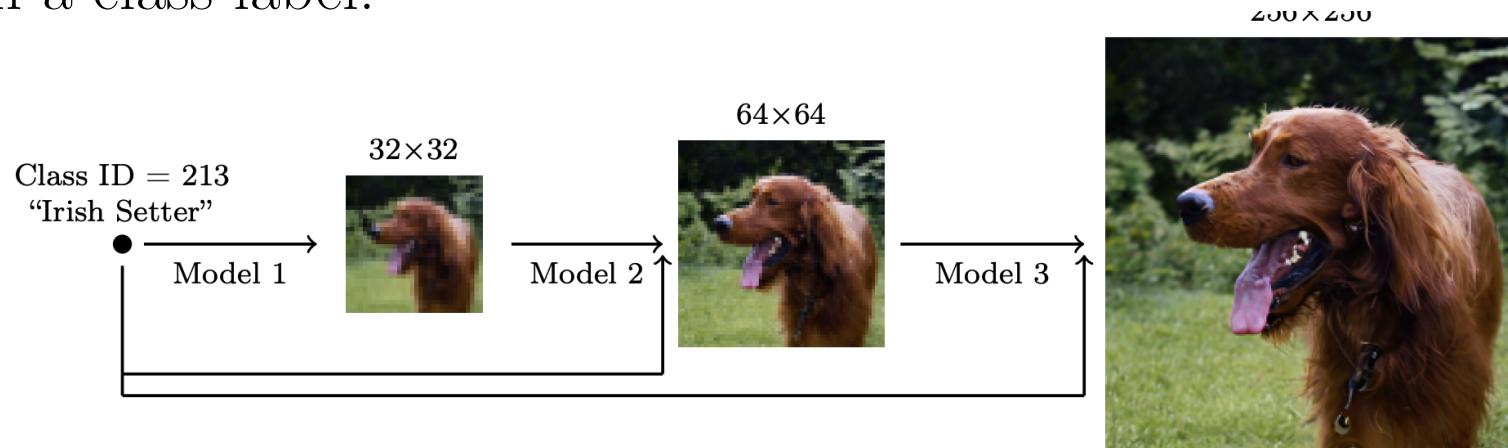
They construct a super-resolution diffusion model as conditional model for pairs for pairs  $(x, y)$  with  $x$  is a downsampling of  $y$ .



# Cascaded Diffusion Models ...

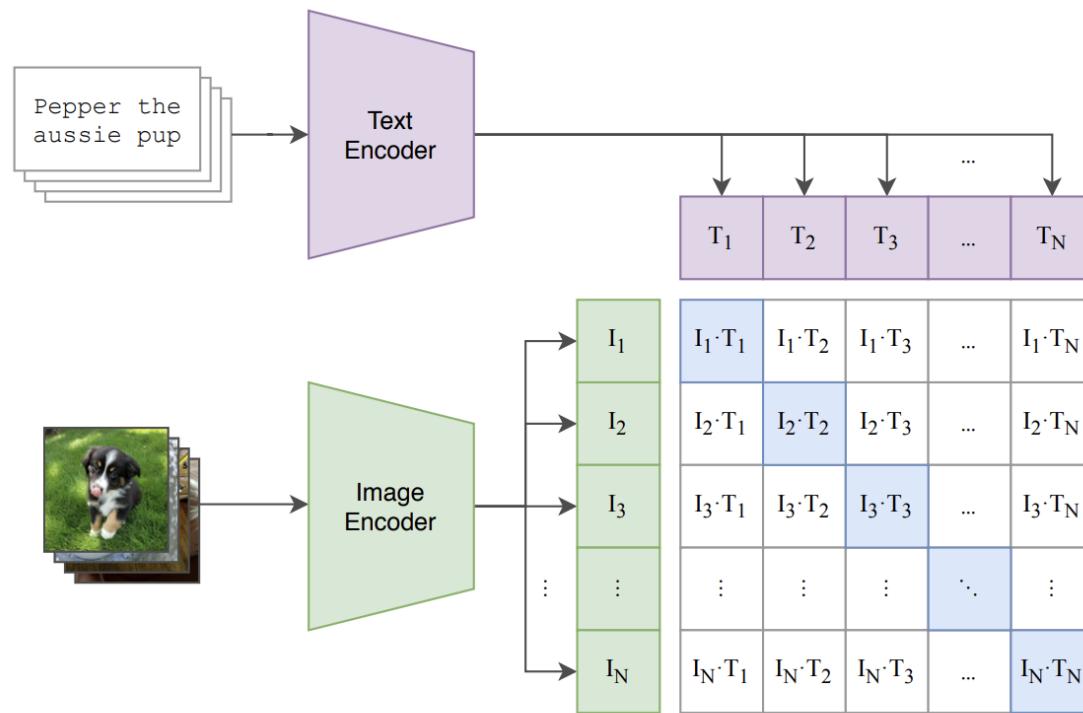
Ho, Saharia et al, May 2021

A series of super-resolution diffusion models each conditioned on a class label.



This architecture is used in DALLE-2.

# CLIP Does Contrastive Coding



CLIP is used in DALLE-2 and in DALLE-2's predecessor GLIDE.

# GLIDE: Towards Photorealistic Image Generation ...

**Nichol, Dhariwal, Ramesh, et al., December 2021**

GLIDE compares two forms of diffusion guidance.

- (a) Classifier-free guidance based on comparing conditioned and unconditioned decoding directions.
- (b) Classifier guidance based on CLIP.

## Classifier-free (self-guided) GLIDE

$$\tilde{\epsilon}(z_\ell, \ell, x) = s\epsilon(z_\ell, \ell, x) - (s-1)\epsilon(z_\ell, \ell, \emptyset)$$

Classifier-free GLIDE does not use CLIP.

The classifier-free guidance differs from the original version in that here we are conditioning on text rather than as Imagenet labels.

The text is transformed to a feature vector by a transformer before being fed to the decoder.

## CLIP-guided GLIDE

Let  $C_I(y)$  be the CLIP vector for image  $y$  and let  $C_T(x)$  be the CLIP vector for text  $x$ .

$$z_{\ell-1} = \frac{1}{\sqrt{1 - \sigma_\ell^2}} \left( z_\ell - \sigma_\ell \epsilon(z_\ell, \ell) + s \tilde{\sigma} \odot \nabla_z C_T(x)^\top C_I(z) \right) + \tilde{\sigma}_\ell \odot \delta$$

Here CLIP is re-trained to handle noised images.

## Upsampling

Both GLIDE versions use diffusion upsampling to go from  $64 \times 64$  to  $256 \times 256$ .

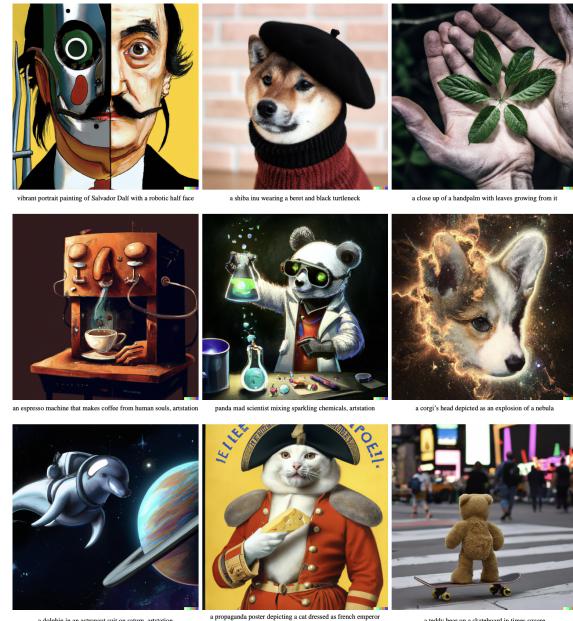
The GLIDE paper concludes that the classifier-free model taking raw text as input is superior to the CLIP-guided model.

# DALL·E-2

Ramesh, Nichol, Dhariwal, et al., March 2022

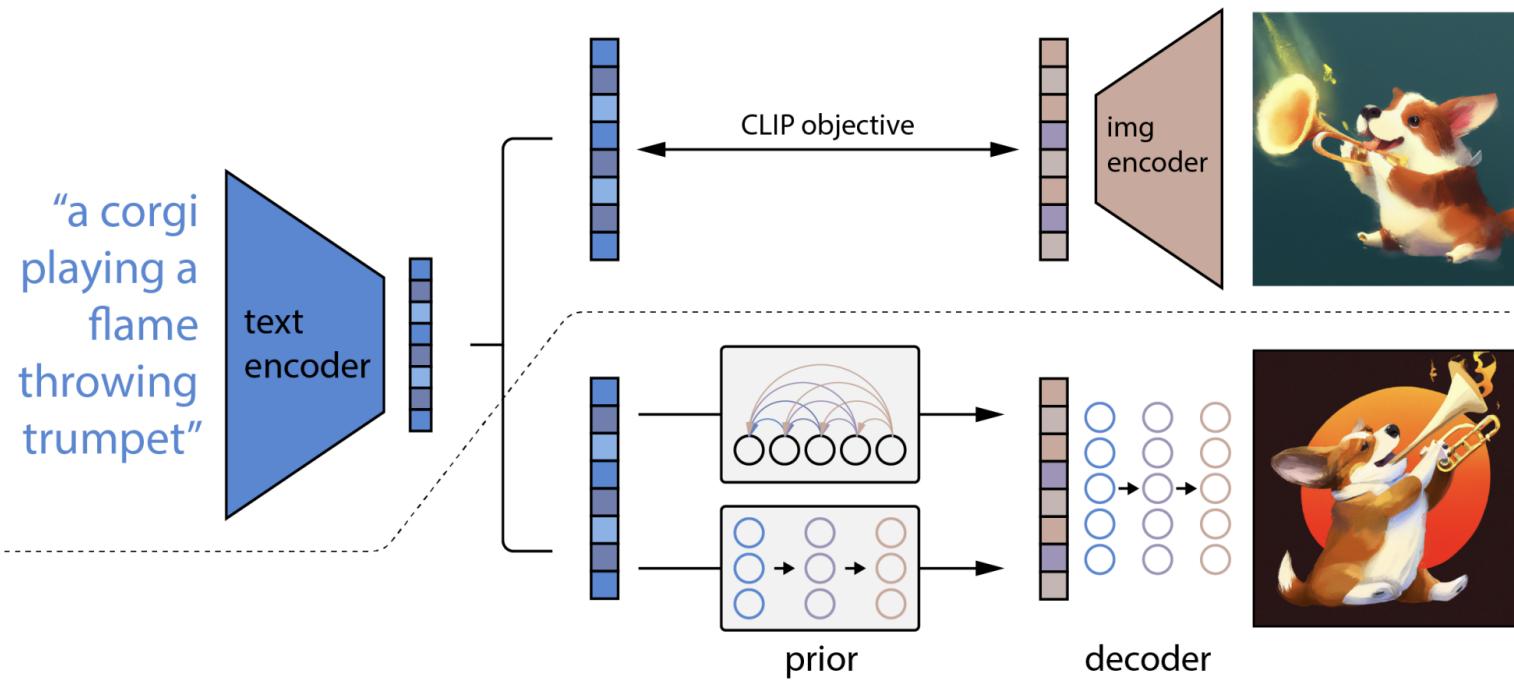


panda mad scientist mixing sparkling chemicals, artstation



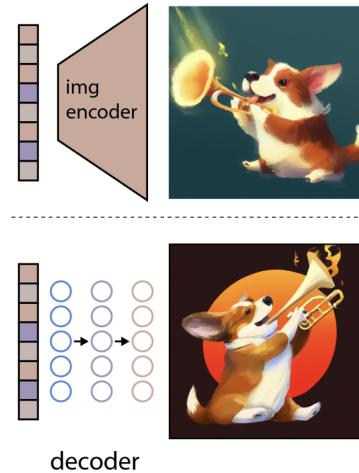
CLIP-guided DALLE-2 is similar in quality to self-guided GLIDE but is more diverse.

# DALL·E-2



This figure is misleading. The lines in the figure do not correspond to the actual data paths of DALLE-2.

# A Conditional Image Auto-Encoder



Let  $C_I(y)$  denote the CLIP embedding of image  $y$ .

$C_I(y)$  is the encoder of an auto-encoder for  $y$  given  $x$ .

$P(C_I(y)|x)$  is the optimal prior for this auto-encoder.

$P(y|C_I(y), x)$  is the optimal decoder.

In DALLE-2 the prior and the decoder both see the text  $x$ .

## Putting it all Together

We are given text  $x$ .

Draw  $\hat{C}$  from the prior  $P(C_I(y)|x)$

Do diffusion decoding with two upsampling models:

compute  $\tilde{z}_{\ell-1}$  using  $\hat{\epsilon} = s\epsilon(z_\ell, \ell, x) - (s-1)\epsilon(z_\ell, \ell, \emptyset)$

$z_{\ell-1} = \hat{z}_{\ell-1} + s'\tilde{\sigma} \odot \nabla_z \hat{C}^\top C_I(z)$

## The Prior

They experiment with two priors  $P(C_I(y)|x)$ .

An autoregressive model and a conditional diffusion model.

They say both priors use self-guidance.

## The Autoregressive Prior

First do PCA on the distribution of vectors  $C_I(y)$  to reduce their dimensionality from 1024 to 319.

Sort the eigenvectors in decreasing order of eigenvalue.

Quantize each of 319 values into 1024 discrete buckets.

We train a transformer to take the text sequence  $x$  followed by the text embedding  $C_T(x)$  and to predict a string of 319 symbols with a vocabulary of size 1024 which can be converted back into the vector  $\hat{C}$ .

## The Diffusion Prior

Let  $z_\ell$  be the noising of  $C_I(y)$  to level  $\ell$ . For the decoder they train a transformer to take the text string  $x$ , the text embedding  $C_T(x)$ , the noised image embedding  $z_\ell$ , and the level  $\ell$ . A final “classifier token” is added to the end of this string and vector computed for that token by the transformer is used as a prediction of  $C_I(y)$ . This predictor  $f(x, z_\ell, \ell)$  is trained on the objective

$$f^* = \operatorname{argmin}_f E_{x,y,z_\ell,\ell} \|f(x, z_\ell, \ell) - C_I(y)\|^2$$

## Sampling $\hat{C}$ from the Diffusion Prior

The paper does not describe the decoding process that computes  $z_{\ell-1}$  from  $z_\ell$  but the following seems reasonable.

$$z_{\ell-1} = f(x, z_\ell, \ell) + \tilde{\sigma}\delta \quad \delta \sim \mathcal{N}(0, I)$$

They can draw samples of  $\hat{C}$  using different values  $\delta$

$$z_0 = f(x, z_1, 1) + \tilde{\sigma}\delta \quad \delta \sim \mathcal{N}(0, I)$$

They draw two samples  $\hat{C}$  and  $\hat{C}'$  and use the one with larger inner product with  $C_T(x)$ .

## Progressive VAEs

Diffusion models are a special case of progressive VAEs.

A progressive VAE has layers of latent variables  $z_1, \dots, z_L$ .

It is not clear whether diffusion models are the best way to do this.

It could be that the important idea is simply having large  $L$  with  $I(z_0, z_\ell)$  going from  $H(z_0)$  to 0 as  $\ell$  goes from 0 to  $L$ .

**END**