



de Louvain

Cryptography l

INGI2347: COMPUTER SYSTEM SECURITY (Spring 2016)

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Plan for today

Lecture 4

What's crypto?



- Symmetric key encryption
- Trusted 3rd parties
- Public key encryption
- Crypto hash functions

κρμπτο γραφη (Cryptography)

- Greek for "secret writing"
- Confidentiality
 - Obscure a message from eaves-droppers
- Integrity
 - Assure recipient that the message was not altered
- Authentication
 - Verify the identity of the source of a message
- Non-repudation
 - Convince a 3rd party that what was said is accurate



Cryptography is everywhere



Secure communication:

web traffic: HTTPS

■ wireless traffic: 802.11i WPA2 (and WEP), GSM, Bluetooth

Encrypting files on disk: EFS, TrueCrypt

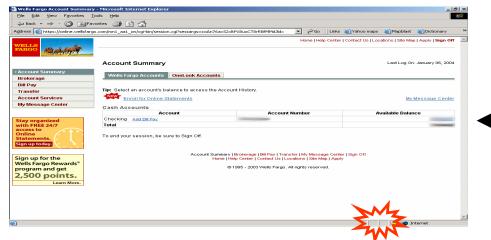
Content protection (e.g. DVD, Blu-ray): CSS, AACS

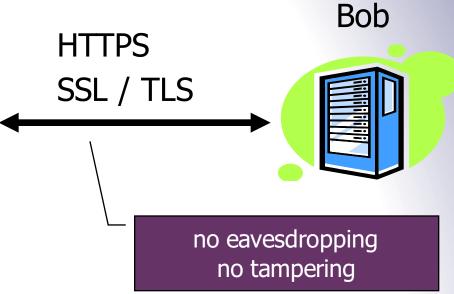
User authentication

... and much much more

Secure communication







Alice

Two main parts

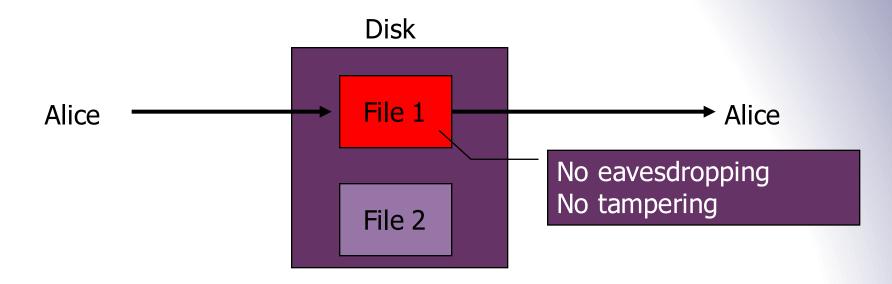
1. Handshake Protocol: **Establish shared secret key** using public-key cryptography

2. Record Layer: **Transmit data using shared secret key**Ensure confidentiality and integrity

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Protected files on disk





Analogous to secure communication:

Alice today sends a message to Alice tomorrow





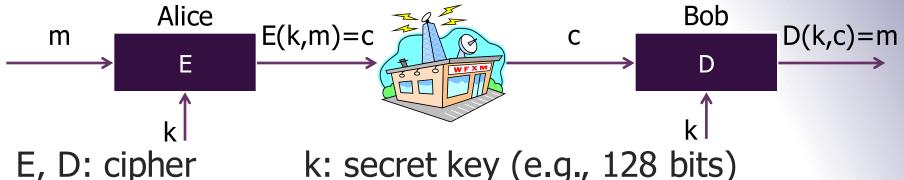


- Encryption algorithm
 - Transforms a plaintext into a ciphertext that is unintelligible for non-authorized parties
 - Usually parametrized with a cryptographic key
- Asymmetric (Public) key cryptography
 - Crypto system: encryption + decryption algorithms + key generation
- Symmetric (Shared) key cryptography
 - Cipher/decipher: symmetric-key encryption/decryption algorithms

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Build block: sym.-key encryption





m, c: plaintext, cipher text

- Same secret key for both encryption and decryption
- Encryption algorithm is publicly known
 - Never use a proprietary algorithm
- Fast in software or hardware implementations



Use Cases



- **Single use key**: (one time key)
 - Key is only used to encrypt one message
 - encrypted email: new key generated for every email
- Multi use key: (many time key)
 - Key used to encrypt multiple messages
 - encrypted files: same key used to encrypt many files
 - SSL: same key used to encrypt many packets
 - Need more machinery than for one-time key



Things To Remember

Cryptography is:

- A tremendous tool
- The basis for many security mechanisms

Cryptography is **NOT**:

- The solution to all security problems
- Reliable unless implemented and used properly
- Something you should try to invent yourself
 - many many examples of broken ad-hoc designs
- Privacy | Steganography | (Encoding|Decoding)



Cryptography is NOT

Privacy

Ability to control how personal information spreads in a community

Steganography

Science of information hiding

Encoding | Decoding

- Code is a system of symbols which represent information
- Encoding transforms information into a codeword
- Decoding recovers information from a codeword

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Cryptanalysis: a rigorous science

Proves or disproves the security of a cryptosystem

- The three steps:
 - Precisely specify threat model
 - Propose a construction
 - Prove that breaking construction under threat mode will solve an underlying hard problem
- Definition of break:
 - Decrypting (totally or partially) a given ciphertext
 - Recovering the key of the cryptosystem
 - Proving a cryptosystem is less secure than what is claimed

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Symmetric-key cryptography

Assumes parties already share a secret key

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Symmetric Ciphers: definition

Def: a **cipher** defined over (K, M, C)

is a pair of "efficient" algs (E, D) where

$$E: K \times M \rightarrow C$$
, $D: K \times C \rightarrow M$

s.t. $\forall m \in M, k \in K: D(k, E(k, m)) = m$

E is often randomized | D is always deterministic



Stream vs. Block Ciphers

Stream ciphers

- Act on the plaintext one symbol at a time
- Examples: RC4, GSM A5-1, Bluetooth E0, CSS, ...
- High speed rate, hardware implementations very cheap
- Security analysis is not well established

Block ciphers

- Act on the plaintext in blocks of symbols
- Examples: DES, 3DES, AES, IDEA, Blowfish, RC5, Kasumi, Safer, ...
- Suited to software implementations on various systems
 - (e.g., 8-bit, 32-bit, 64-bit processors)
- Security analysis is well established

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Stream Ciphers: The One Time Pad (Vernam 1917)

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First example of a "secure" cipher

$$M = C = \{0,1\}^n, \quad K = \{0,1\}^n$$

key = (random bit string as long the message)

$$E(k,m) = k \oplus m$$

$$D(k,c) = k \oplus c$$

key: 1 0 1 1 0 1 0

CT: 1 1 0 1 1 0 1

Indeed:

$$D(k,E(k,m)) = D(k,k \oplus m) = k \oplus (k \oplus m) = (k \oplus k) \oplus m = 0 \oplus m = m$$

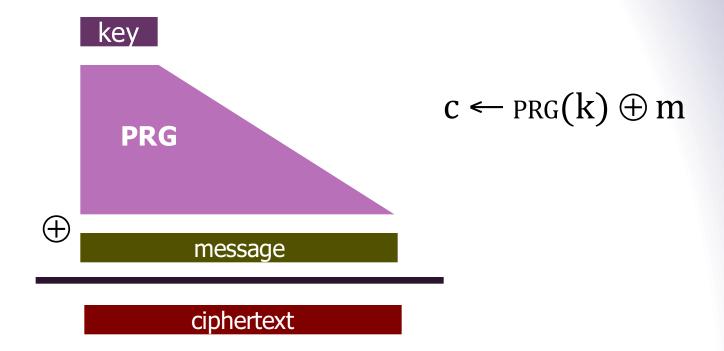
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Stream ciphers (single key use)

Problem: OTP key is as long the message

Solution: Pseudo random key – stream ciphers



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Dangers in using stream ciphers

One time key!! "Two time pad" is insecure:

$$\begin{cases} C_1 \leftarrow m_1 \oplus PRG(k) \\ C_2 \leftarrow m_2 \oplus PRG(k) \end{cases}$$

Eavesdropper does:

$$C_1 \oplus C_2 \rightarrow m_1 \oplus m_2$$

Enough redundancy in English and ASCII encoding that:

$$m_1 \oplus m_2 \rightarrow m_1, m_2$$

What is a secure cipher?

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Attacker's abilities: obtains one ciphertext (for now)

Possible security requirements:

attempt #1: attacker cannot recover secret key

$$E(k,m) = m$$
 Insecure: leaks m

attempt #2: attacker cannot recover all of plaintext

$$E(k, m_0 || m_1) = m_0 || E(k, m_1)$$
 Insecure: leaks m_0

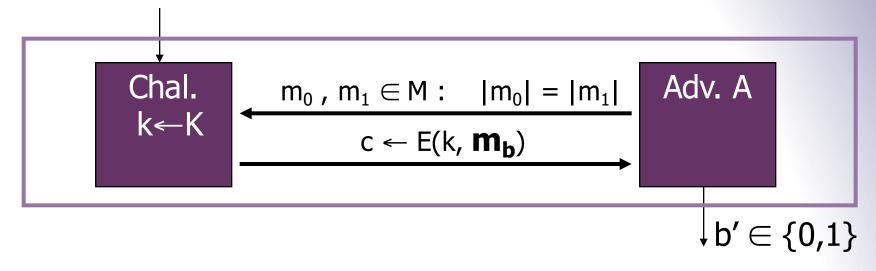
Shannon's information-theoretic perfect secrecy:

ciphertext should reveal no "info" about plaintext

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Semantic Security (one-time key)

For b=0,1 define experiments EXP(0) and EXP(1) as:



for
$$b=0,1$$
: $W_b := [event that EXP(b)=1]$

Sematic Security Advantage of A against E

E is **semantically secure** if for all efficient A $Adv_{SS}[A,E]$ is negligible

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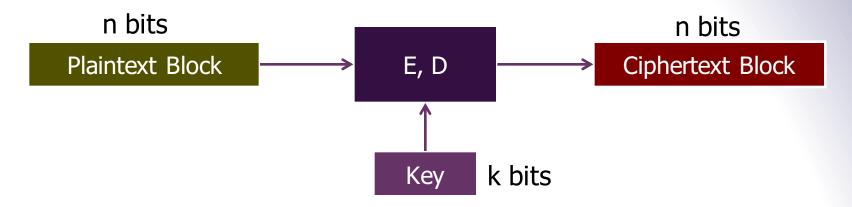
Model of the attacker (also for PK)

- Chosen-plaintext attack (CPA)
 - The adversary has access to an **encryption** oracle: he can choose plaintexts and get their corresponding ciphertexts
- Chosen-ciphertext attack (CCA)
 - The attacker has access to a decryption oracle: he can choose ciphertexts (other than the ciphertext he is challenged with) and get their corresponding plaintext
 - More powerful than CPA



Block Ciphers





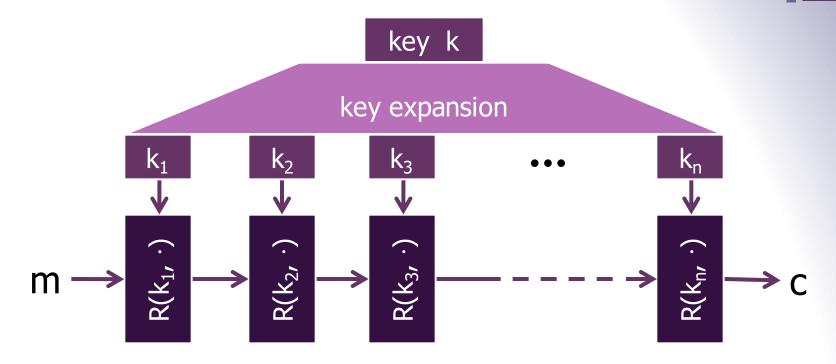
Canonical examples:

1. 3DES: n = 64 bits, k = 168 bits

2. AES: n=128 bits, k=128, 192, 256 bits



Block Ciphers Built by Iteration



R(k,m) is called a round function

for 3DES (n=48), for AES-128 (n=10)

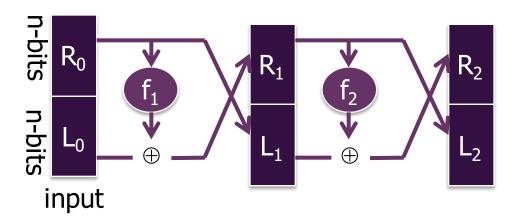


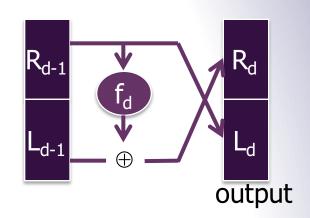
Block Ciphers: DES

(Feistel Network)

Given functions $f_1, ..., f_d$: $\{0,1\}^n \rightarrow \{0,1\}^n$

Goal: build invertible function F: $\{0,1\}^{2n} \rightarrow \{0,1\}^{2n}$

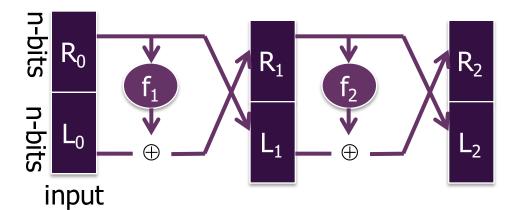


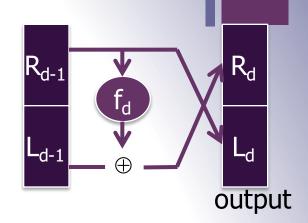


In symbols:
$$\begin{cases} R_i = f_i(R_{i-1}) \oplus L_{i-1} \\ L_i = R_{i-1} \end{cases}$$

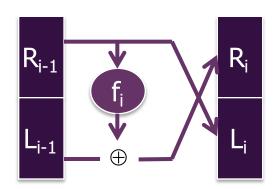


Feistel Network





Feistel network F: $\{0,1\}^{2n} \rightarrow \{0,1\}^{2n}$ is invertible Construct inverse:

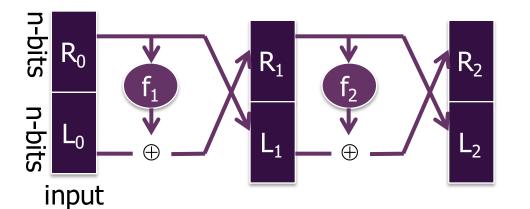


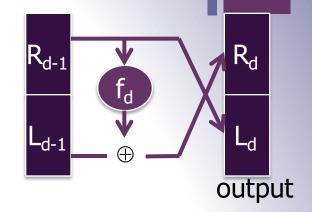
$$\begin{cases} R_{i-1} = L_i \\ L_{i-1} = R_i \end{cases}$$

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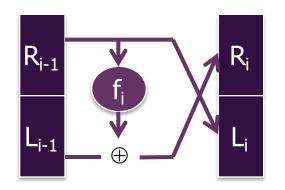
Feistel Network inverse construction

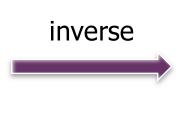


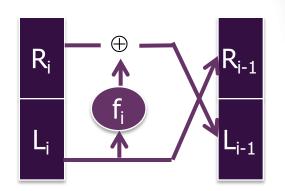


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Feistel network F: $\{0,1\}^{2n} \rightarrow \{0,1\}^{2n}$ is invertible Construct inverse:

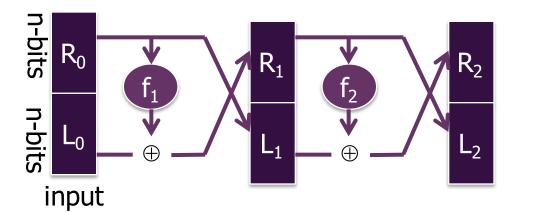


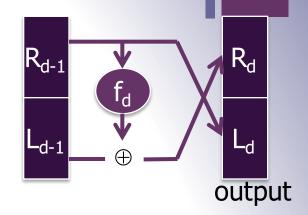






Feistel Network Decryption

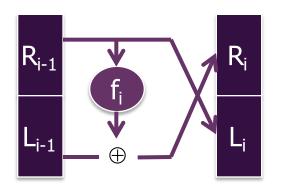




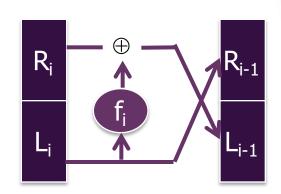
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Feistel network F: $\{0,1\}^{2n} \rightarrow \{0,1\}^{2n}$ is invertible

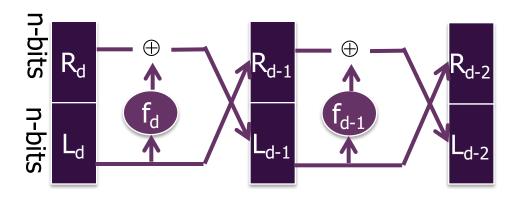
Construct inverse:

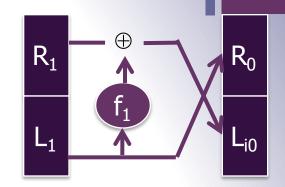


inverse



Feistel Network Decryption





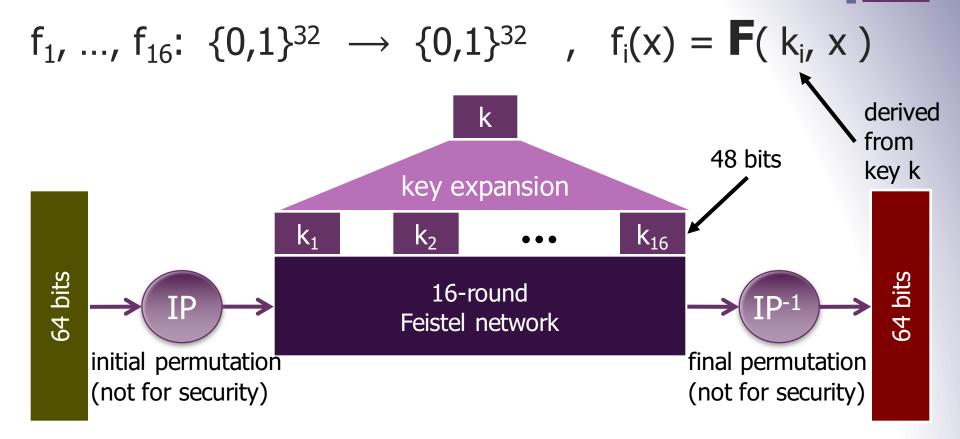
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- Inversion is basically the same circuit, with f₁, ..., f_d applied in reverse order
- General method for building invertible functions (block ciphers) from arbitrary functions
- Used in many block ciphers ... but not AES

input

output

DES: 16-round Feistel Network



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To invert, use keys in reverse order

DES challenge

```
msg = "The unknown messages is: XXXXX ... "

CT = c_1 c_2 c_3 c_4 ...
```

Goal: find $k \in \{0,1\}^{56}$ s.t. DES $(k, m_i) = c_i$ for i=1,2,3

1997: Internet search -- 3 months

1998: EFF machine (deep crack) -- **3 days** (250K \$)

1999: combined search -- 22 hours

2006: COPACOBANA (120 FPGAs) -- 7 days (10K \$)

 \Rightarrow 56-bit ciphers should not be used !! (128-bit key \Rightarrow 2⁷² days)



Triple-DES



Strengthening DES against exhaustive search

- Let $E: K \times M \longrightarrow M$ be a block cipher
- Define **3E**: $K^3 \times M \longrightarrow M$

3E(
$$(k_1,k_2,k_3)$$
, m) = E $(k_1, D(k_2, E(k_3, m)))$

key-size = $3 \times 56 = 168$ bits. $k_1 = k_2 = k_3$ For 3DES: 3×slower than DES.

=> single DES

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Advanced Encryption Standard (AES)

- National Institute of Standards & Technology NIST
 - Computer Security Research Center (CSRC)
 - http://csrc.nist.gov/
- Uses the Rijndael algorithm
 - Invented by Belgian researchersDr. Joan Daemen & Dr. Vincent Rijmen
 - http://jda.noekeon.org/JDA_VRI_Rijndael_V2_1999.pdf
 - Adopted May 26, 2002
 - Key length: 128, 192, or 256 bits
 - Block size: 128 bits
 - If DES could be broken in 1 second, then AES would require 149 trillion years to be broken

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Performance

Crypto++ 5.6.0

[Wei Dai]

AMD Opteron, 2.2 GHz (Linux)

	<u>Cipher</u>	Block/key size	Speed	(MB/sec)
stream	RC4		126	
	RC4 Salsa20/12 Sosemanuk		643	
	Sosemanuk	<	727	

block	3DES AES-128	64/168	13
	AES-128	128/128	109



Problems with Shared Key Crypto

- Compromised key means interceptors can decrypt any ciphertext they've acquired
 - Change keys frequently to limit damage
- Distribution of keys is problematic
 - Keys must be transmitted securely
 - Use couriers?
 - Distribute in pieces over separate channels?



Trusted 3rd Parties

Basic key exchange

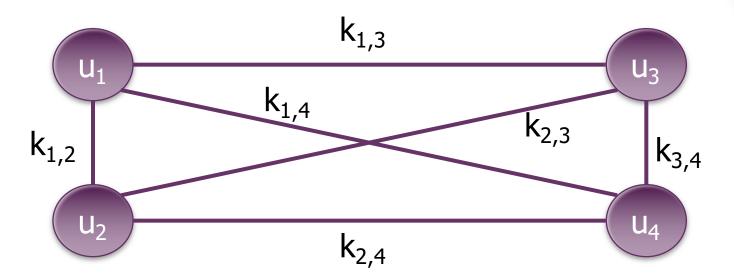
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Key Management

Problem: n users

Storing mutual secret keys is difficult

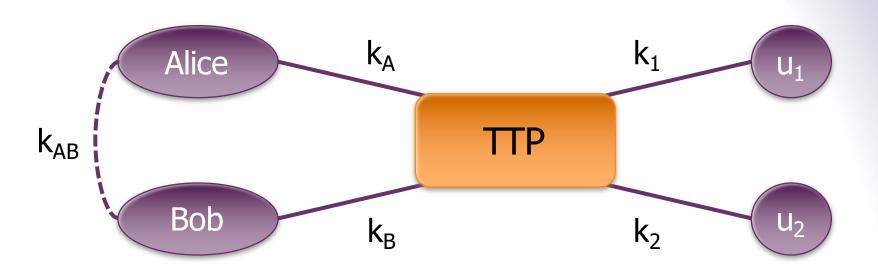


Total: O(n) keys per user; $O(n^2)$ keys in the system



A better solution

Onlined Trusted 3rd Party (TTP)



Every user only remembers one key

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Generating keys: a toy protocol



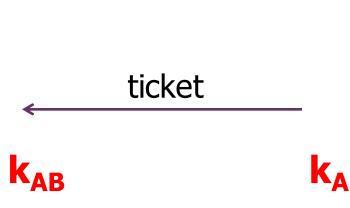
Alice wants a shared key with Bob

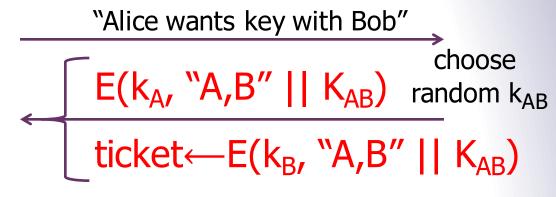
Eavesdropping security only

Bob (k_B)

Alice (k_A)

TTP





(E,D) a CPA-secure cipher: attacker cannot distinguish between an encrypted value and a random one



Generating keys: a toy protocol

Alice wants a shared key with Bob

Eavesdropping security only

Eavesdropper sees:

```
E(k_{A}, "A, B" || k_{AB}) ; E(k_{B}, "A, B" || k_{AB})
```

(E,D) is CPA-secure \Rightarrow eavesdropper learns nothing about k_{AB}

- TTP needed for every key exchange, knows all session keys
- In a corporate environment environment might make sense
 - Example: Kerberos system



Toy protocol: insecure against active attacks



Example: insecure against replay attacks

Attacker records session between Alice and Bob

For example a book order

Attacker replays session to Bob

Bob thinks Alice is ordering another copy of book

Key question



Can we generate shared keys without an online TTP?

Answer: yes!

Starting point of public-key cryptography:

- Merkle (1974), Diffie-Hellman (1976), RSA (1977)
- Further references:
 - More recently: ID-based enc. (BF 2001), Functional enc. (BSW 2011)

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Public key cryptography

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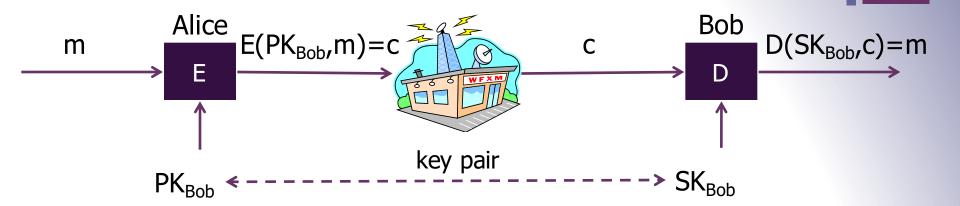
Asymmetric or Public Key Crypto

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- Sender encrypts using a *public* key
- Receiver decrypts using a *private* key
- Only the private key must be kept secret!
 - Public key can be distributed at will
- Constructions generally rely on hard problems from number theory or algebra (e.g., FACT)
- Can be used for digital signatures
- Examples: RSA, El Gamal, DSA



Public Key Encryption



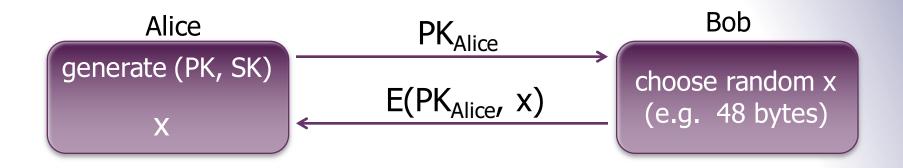
PK: public key, SK: secret key (e.g., 1024 bits)

Example: Bob generates (PK_{Bob}, SK_{Bob}) and gives PK_{Bob} to Alice



Applications

Session setup (for now, only eavesdropping security)



Non-interactive applications: (e.g., Email)

- Bob sends email to Alice encrypted using PK_{Alice}
- Note: Bob needs PK_{Alice} (public key management)



Public Key Encryption

<u>Def</u>: a public-key cryptosys. is a triple of algs. (G, E, D)

- G(): randomized alg. outputs a key pair (PK, SK)
- E(PK, m): randomized alg. that takes $m \in M$ and outputs $c \in C$
- D(SK, c): deterministic alg. that takes $c \in C$ and outputs $m \in M$ or \bot

Consistency: $\forall (PK, SK)$ output by G:

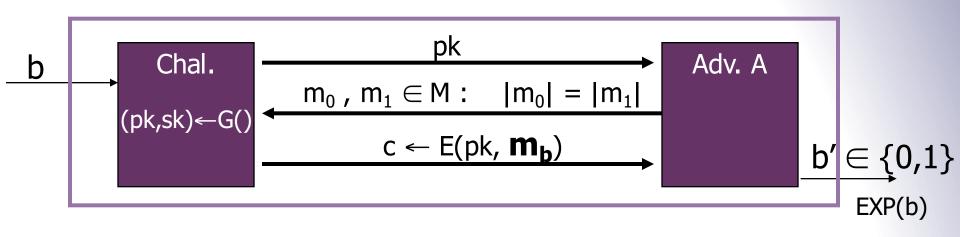
 $\forall m \in M$: D(SK, E(PK, m)) = m

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Semantic Security

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For b=0,1 define experiments EXP(0) and EXP(1) as:



<u>Def</u>: E = (G, E, D) is sem. secure if for all efficient A:

$$Adv_{SS}[A,E] = Pr[EXP(0)=1] - Pr[EXP(1)=1] < negligible$$



Establishing a shared secret



Alice

<u>Bob</u>

$$(pk, sk) \leftarrow G()$$

"Alice", pk

choose random $x \in \{0,1\}^{128}$

"Bob",
$$c \leftarrow E(pk,x)$$

 $D(sk,c) \rightarrow x$

x shared secret



Security (eavesdropping)

Adversary sees pk, E(pk, x) and wants $x \in M$

```
Semantic security \Rightarrow adversary cannot distinguish \{ pk, E(pk, x), x \} from \{ pk, E(pk, x), rand \in M \}
```

 \Rightarrow can derive session key from x

Note: protocol is vulnerable to man-in-the-middle

Insecure against man in the middle



The protocol is insecure against **active** attacks

```
Alice
                                  MiTM
                                                                    Bob
(pk, sk) \leftarrow G()
                              (pk', sk') \leftarrow G()
            "Alice", pk
                              →||"Alice", pk′
                                                               choose random
                                                                x \in \{0,1\}^{128}
                                               "Bob", E(pk', x)
                    x \leftarrow D(sk', E(pk', x))
          "Bob", E(pk, x)
```



Trade-offs for Public Key Crypto

- More computationally expensive than symmetric (shared) key crypto
 - Algorithms are harder to implement
 - Require more complex machinery
- More formal justification of difficulty
 - Hardness based on complexity-theoretic results
- A principal needs 1 private key and 1 public key
 - Number of keys for pair-wise communication is O(n)



RSA Algorithm



- Proposed in 1979
- They won the 2002 Turing award for this work

Has withstood years of cryptanalysis

- Not a guarantee of security!
- But a strong vote of confidence
 - Further reading: Twenty years of attacks on the RSA cryptosystem,
 D. Boneh, Notices of the AMS, 1999
- Hardware implementations:

■ 1000 x slower than DES



RSA at a High Level

- Public and private key are derived from secret prime numbers
 - Today at least 1024 bits to ensure security (4096 bits is better)
- Plaintext message (a sequence of bits)
 - Treated as a (large!) binary number
- Encryption is modular exponentiation
- To break the encryption, conjectured that one must be able to factor large numbers
 - Not known to be in P (polynomial time algorithms)

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Crypto hash functions

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- Take a variable length string
- Produce a fixed length digest

$$h: \left\{0,1\right\}^* \rightarrow \left\{0,1\right\}^n$$

- (Non-cryptographic) Examples:
 - Parity (or byte-wise XOR)
 - CRC
- Realistic Example:
 - The NIST Secure Hash Algorithm (SHA) takes a message of less than 2⁶⁴ bits and produces a digest of 160 bits



Cryptographic Hashes

- Create a hard-to-invert summary of input data
- Like a check-sum or error detection code
 - Uses a cryptographic algorithm internally
 - More expensive to compute
- Sometimes called a Message Digest
- Examples:
 - Secure Hash Algorithm (SHA)
 - Message Digest (MD4, MD5)



Desired Properties

One way hash function

■ Given a hash value y, it should be infeasible to find m s.t. h(m)=y

Collision resistance

■ It should be infeasible to find two different messages m_1 and m_2 s.t. $h(m_1)=h(m_2)$

Random oracle property

- h(m) is indistinguishable from a random n-bit value
- Attacker must spend a lot of effort to be able to modify the message without altering the hash value



Any questions?



