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**STAT 51200--FALL 2022**  
**Applied Regression Analysis**

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*Homework #07*

1. Read Chapters 5 and 6 in the text.
2. Do problems: 6.18, 6.19, 6.20, 6.21. Note that the Data for Problem 6.18 can be found on the course's site in the file **TextBookDataSets/CH06PR18.txt**:
3. For the following 5 sub-problems, consider the data given in the file **MathSal.txt**, which describes a data set ( $n = 24$ ) used to evaluate the relation between intermediate and senior level annual salaries of mathematicians ( $Y$ , in thousand dollars) and an index of work quality ( $X1$ ), number of years of experience ( $X2$ ), and an index of grant support success ( $X3$ ).
  - a) Run the multiple linear regression with quality, experience, and publications as the explanatory variables and salary as the response variable. Summarize the regression results by giving the fitted regression equation, the value of  $R^2$ , and the results of the significance test for the null hypothesis that the three regression coefficients for the explanatory variables are all zero (give null and alternative hypotheses, test statistic with degrees of freedom,  $p$ -value, and brief conclusion in words).
  - b) Give 95% confidence intervals (do not use a Bonferroni correction) for regression coefficients of quality, experience, and grants support based on the multiple regression. Describe the results of the hypothesis tests for the individual regression coefficients (give null and alternative hypotheses, test statistic with degrees of freedom,  $p$ -value, and a brief conclusion in words). What is the relationship between these results and the confidence intervals?
  - c) Plot the residuals versus the *predicted* salary and *each* of the explanatory variables (i.e., 4 residual plots). Are there any unusual patterns?
  - d) Examine the assumption of normality for the residuals using a qqplot and histogram. State your conclusions.
  - e) Predict the salary for a mathematician with quality index equal to 6.2, 8 years of experience, and grant support index equal to 5.9. Provide a 95% prediction interval with your prediction.