The Iowa Gambling Task

The <u>lowa Gambling Task</u> is a psychological task thought to simulate real-life decision making. There are 4 decks for participants to choose from. Each time they choose a deck they get either a reward, a penalty or a mixture of both. The aim is to get the most money. Two of the decks contain more penalties and two contain more rewards. It was found that most people tended to stick to the "good" decks after roughly 50 selections.



Decks A and B are known as the "good" decks because they have a positive net outcome whereas decks C and D have a negative net outcome. There are slight differences in these outcomes in each study. There are three different payloads:

- 1. In Fridberg, Maia, and Worthy, deck C has a variable loss of either -25, -50, or -75.
- 2. In Horstmann, Streingroever, and Wetzels, they maintain the loss of deck C as a constant of -50.
- 3. In Kjome, Premkumar, and Wood, the schedules of rewards and losses in such a way that the net outcome of the "bad" decks decreases by 150 every 10 cards and the net outcome of the "good" decks increases by 25 every 10 cards

My objective was to clean and process the <u>data</u> and perform clustering analysis on it to gain insights into the lowa Gambling Task and real-life decision making. Another target was to find a way to perform clustering on the data while preserving the privacy of each individual lab.

Data Processing

This is where I cleaned and processed the datasets that were given. I did this in three steps:

- 1. Data cleaning
- 2. Merging the Data
- 3. Aggregating the Data

```
import pandas as pd
import numpy as np
```

Firstly, I read in each dataset and used pandas.DataFrame.head() to get an idea of what the datasets looked like.

```
choice_100 = pd.read_csv("./data/choice_100.csv")
choice_150 = pd.read_csv("./data/choice_150.csv")
choice_95 = pd.read_csv("./data/choice_95.csv")
index_100 = pd.read_csv("./data/index_100.csv")
index_150 = pd.read_csv("./data/index_150.csv")
index_95 = pd.read_csv("./data/index_95.csv")
lo_100 = pd.read_csv("./data/lo_100.csv")
lo_150 = pd.read_csv("./data/lo_150.csv")
lo_95 = pd.read_csv("./data/lo_95.csv")
wi_100 = pd.read_csv("./data/lo_100.csv")
wi_150 = pd.read_csv("./data/wi_150.csv")
wi_150 = pd.read_csv("./data/wi_150.csv")
wi_95 = pd.read_csv("./data/wi_95.csv")
```

```
print(choice_100.head())
print(index_100.head())
print(lo_100.head())
print(wi_100.head())
```

```
Choice_1 Choice_2 Choice_3 Choice_4 Choice_5 Choice_6 Choice_7
Subj_1
                                  2
                                            4
Subj_2
                                            4
                                                                          3
Subj_3
                                   3
                                                      4
                                                                          4
Subj_4
                        3
                                   4
                                            2
                                                      1
                                                                4
                                                                          3
                                            2
Subj_5
              1
                                  2
                                                                3
                                                                          4
        Choice_8 Choice_9
                          Choice_10
                                           Choice_91 Choice_92
                                                                 Choice_93 \
                                      . . .
Subj_1
                                   2
                                                   1
                                                              1
                                      . . .
                                   2
                                                              2
Subj_2
                                                                         3
                                      . . .
                                                              2
Subj_3
               4
                        4
                                   3
                                                   3
                                                                         1
Subj_4
              2
                        2
                                   2
                                      . . .
                                                   4
                                                              2
                                                                         3
                                   1 ...
Subj_5
       Choice_94 Choice_95 Choice_96 Choice_97 Choice_98 Choice_99
Subj_1
                          2
                                     2
                                                4
Subj_2
               4
                          2
                                     4
                                                4
                                                           2
                                                                      2
Subj_3
Subj 4
               4
                          3
                                     4
                                                1
                                                           4
                                                                      3
               2
                          3
                                     3
                                                3
                                                           3
Subj_5
        Choice_100
Subj_1
Subj_2
                4
Subj_3
                2
Subj_4
Subj_5
[5 rows x 100 columns]
  Subj
           Study
0
    1
       Horstmann
        Horstmann
2
     3
       Horstmann
3
     4 Horstmann
4
     5
       Horstmann
        Losses_1 Losses_2 Losses_3 Losses_4 Losses_5 Losses_6 Losses_7 \
Subj 1
                                  0
                                                      0
            -200
                     -150
                                         -250
            0
Subj_2
                      0
                                  0
                                          0
                                                      0
                                                                0
                                                                         - 50
Subj_3
              0
                        0
                                - 50
                                         -300
                                                      0
                                                             - 1250
                                                                          0
Subj_4
            -250
                       -50
                                  0
                                          0
                                                    -200
                                                               0
                                                                          0
Subj_5
            0
                        0
                                   0
                                         -1250
        Losses_8 Losses_9
                          Losses_10
                                      ... Losses_91 Losses_92
                                                                Losses 93 \
                                                                      -350
Subj_1
                        0
                                   0 ...
                                                   0
                                                              0
              0
Subj_2
              0
                        0
                                   0
                                                   0
                                                              0
                                                                       0
                                      ...
Subj_3
                         0
                                 -50
                                                              0
                                                                       -200
                                      . . .
                               -1250 ...
Subj_4
              0
                        0
                                                   0
                                                              0
                                                                         0
                                                              0
                                                                         0
Subj_5
              0
                        0
                                   0
                                                   0
        Losses_94 Losses_95 Losses_96 Losses_97 Losses_98
Subj_1
            _ 0
                      - 0
                                     0
                                                0
                                                           0
                                                                      0
Subj_2
             -250
                       -1250
                                     0
                                                0
                                                           0
                                                                      0
             0
                        0
                                     0
Subj_3
                                                0
                                                           0
                                                                      0
Subj_4
               0
                         - 50
                                     0
                                                0
                                                           0
                                                                    - 50
Subj_5
           -1250
                          0
                                     0
                                                0
                                                          -50
                                                                      0
       Losses 100
Subj_1
           -1250
Subj_2
                0
Subj_3
                0
Subj_4
                0
Subj_5
                0
[5 rows x 100 columns]
       Wins_1 Wins_2
                       Wins_3 Wins_4 Wins_5 Wins_6 Wins_7 Wins_8 \
Subj_1
          100
                  100
                          100
                                   50
                                           50
                                                  100
                                                          100
                                                                  100
Subj_2
          100
                  100
                           50
                                   50
                                           50
                                                  100
                                                           50
                                                                  100
Subj_3
           50
                  100
                           50
                                   100
                                           50
                                                  100
                                                           50
                                                                   50
Subj_4
           50
                   50
                           50
                                  100
                                          100
                                                   50
                                                           50
                                                                  100
Subj_5
          100
                  100
                          100
                                  100
                                          100
                                                   50
                                                           50
                                                                  100
        Wins_9 Wins_10 ... Wins_91 Wins_92 Wins_93
                                                       Wins_94 Wins_95
Subj_1
           50
                   100
                        . . .
                                 100
                                          100
                                                   100
                                                            100
                                                                     100
Subj_2
                   100
                                  50
                                          100
                                                    50
                        . . .
                                                             50
Subj_3
           50
                    50
                                   50
                                          100
                                                   100
                                                                      100
                        . . .
Subj_4
          100
                   100
                                  50
                                          100
                                                   50
                                                             50
                                                                      50
                        . . .
Subj_5
           50
                   100
                                 100
                                          100
                                                   100
                                                            100
                                                                      50
        Wins_96 Wins_97
                         Wins_98 Wins_99
Subj_1
            100
                     50
                             100
                                       _
50
                                                100
Subj_2
            50
                     50
                             100
                                      100
                                                 50
                              50
                                      100
Subj_3
            100
                    100
                                                100
Subj_4
            50
                     100
                              50
                                       50
                                                 50
Subj_5
            50
                     50
                              50
                                       50
                                                 50
[5 rows x 100 columns]
```

1. Data Cleaning

My first step was data cleaning. I went through each individual dataframe to see if there were any obvious errors, data type differences or any nulls that needed to be changed.

```
print(choice_95.info(verbose=False))
print(choice_100.info(verbose=False))
print(choice_150.info(verbose=False))
print(index_95.info(verbose=False))
print(index_100.info(verbose=False))
print(index_150.info(verbose=False))
print(lo_95.info(verbose=False))
print(lo_100.info(verbose=False))
print(lo_150.info(verbose=False))
print(vi_95.info(verbose=False))
print(wi_95.info(verbose=False))
print(wi_100.info(verbose=False))
print(wi_150.info(verbose=False))
```

```
<class 'pandas.core.frame.DataFrame'>
Index: 15 entries, Subj_1 to Subj_15
Columns: 95 entries, Choice_1 to Choice_95
dtypes: int64(95)
memory usage: 11.2+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 504 entries, Subj_1 to Subj_504
Columns: 100 entries, Choice_1 to Choice_100
dtvpes: int64(100)
memory usage: 397.7+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 98 entries, Subj_1 to Subj_98
Columns: 150 entries, Choice_1 to Choice_150
dtypes: int64(150)
memory usage: 115.6+ KB
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 15 entries, 0 to 14
Columns: 2 entries, Subj to Study
dtypes: int64(1), object(1)
memory usage: 368.0+ bytes
None
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 504 entries, 0 to 503
Columns: 2 entries, Subj to Study
dtypes: int64(1), object(1)
memory usage: 8.0+ KB
None
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 98 entries, 0 to 97
Columns: 2 entries, Subj to Study
dtypes: int64(1), object(1)
memory usage: 1.7+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 15 entries, Subj_1 to Subj_15
Columns: 95 entries, Losses_1 to Losses_95
dtypes: int64(95)
memory usage: 11.2+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 504 entries, Subj_1 to Subj_504
Columns: 100 entries, Losses_1 to Losses_100
dtypes: int64(100)
memory usage: 397.7+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 98 entries, Subj_1 to Subj_98
Columns: 150 entries, Losses_1 to Losses_150
dtypes: int64(150)
memory usage: 115.6+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 15 entries, Subj 1 to Subj 15
Columns: 95 entries, Wins_1 to Wins_95
dtypes: int64(95)
memory usage: 11.2+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 504 entries, Subj_1 to Subj_504
Columns: 100 entries, Wins_1 to Wins_100
dtypes: int64(100)
memory usage: 397.7+ KB
None
<class 'pandas.core.frame.DataFrame'>
Index: 98 entries, Subj_1 to Subj_98
Columns: 150 entries, Wins_1 to Wins_150
dtypes: int64(150)
memory usage: 115.6+ KB
None
```

```
print(choice_100.isnull().values.any())
print(choice_150.isnull().values.any())
print(choice_95.isnull().values.any())
print(index_100.isnull().values.any())
print(index_150.isnull().values.any())
print(index_95.isnull().values.any())
print(lo_100.isnull().values.any())
print(lo_150.isnull().values.any())
print(lo_95.isnull().values.any())
print(wi_100.isnull().values.any())
print(wi_150.isnull().values.any())
print(wi_95.isnull().values.any())
```

```
False
```

All columns were non-null and of the same type (int64), so I did not need to change any datatypes. The data was already clean

2. Merging the Datasets

In this step, I merged the datasets to include choice, amount won/lost, and index.

I began by changing the column names in the wins and losses datasets to 'Total_{n}'. This made the merging of the two dataframes easier because I was then able to use pandas.DataFrame.add() to get the total amount won or lost for each choice.

```
ld, wd = {}, {}
for i in range(1, 96):
    ld['Losses_' + str(i)] = 'Total_' + str(i)
    wd['Wins_' + str(i)] = 'Total_' + str(i)

lo_95.rename(columns=ld, inplace=True)
wi_95.rename(columns=wd, inplace=True)

total_95 = wi_95.add(lo_95)
total_95
```

	Total_1	Total_2	Total_3	Total_4	Total_5	Total_6	Total_7	Total_8	Total_9	Tot
Subj_1	100	100	100	100	100	100	100	100	-1150	
Subj_2	100	100	50	100	100	100	100	100	100	
Subj_3	50	50	50	100	100	100	100	-50	100	
Subj_4	50	50	100	100	-50	100	100	50	100	
Subj_5	100	100	50	50	50	100	-50	100	100	
Subj_6	100	100	100	100	-50	100	100	50	50	
Subj_7	100	100	50	50	50	50	100	100	100	
Subj_8	50	100	100	50	100	50	100	100	-50	
Subj_9	100	100	100	100	50	50	-50	50	50	
Subj_10	50	100	100	100	50	100	100	50	50	
Subj_11	50	50	0	100	50	100	-50	100	100	
Subj_12	50	50	50	50	100	100	100	100	100	
Subj_13	100	100	50	50	50	100	100	100	-50	
Subj_14	100	100	50	50	100	100	-50	100	50	
Subj_15	100	100	50	50	50	50	50	100	100	
15 rows × 95 columns										

I then joined 'total_95' with 'choice_95' so that the dataframe, 'all_95', now contains the total amount won or lost and the choice that was made for each round. The columns alternate between total and choice because it is easier to understand that way.

```
all_95 = total_95.join(choice_95)

cols = all_95.columns.tolist()
cols = sorted(cols, key = lambda x: int(x.split('_')[-1]))
all_95 = all_95[cols]
all_95
```

	Total_1	Choice_1	Total_2	Choice_2	Total_3	Choice_3	Total_4	Choice_4	Tota
Subj_1	100	2	100	2	100	2	100	2	
Subj_2	100	1	100	2	50	3	100	2	
Subj_3	50	3	50	4	50	3	100	2	
Subj_4	50	4	50	3	100	1	100	1	
Subj_5	100	1	100	2	50	3	50	4	
Subj_6	100	1	100	2	100	1	100	2	
Subj_7	100	1	100	2	50	3	50	4	
Subj_8	50	4	100	2	100	1	50	3	
Subj_9	100	1	100	2	100	1	100	2	
Subj_10	50	4	100	2	100	2	100	1	
Subj_11	50	3	50	3	0	3	100	1	
Subj_12	50	4	50	4	50	4	50	4	
Subj_13	100	1	100	1	50	4	50	3	
Subj_14	100	1	100	2	50	3	50	4	
Subj_15	100	1	100	2	50	3	50	4	

15 rows × 190 columns

I changed the cells in 'index_95' to be in the form 'Subj_{\}' and set that column as the index. I then joined it with 'all_95'.

```
index_95['Subj'] = index_95['Subj'].apply(lambda x: 'Subj_' + str(x))
index_95.set_index('Subj', inplace=True)
index_95.index.name = None
all_95 = all_95.join(index_95)
```

Finally, I added multilevel columns to make each trial separate. I then exported the file in csv format to the data folder in my book.

```
l = []
for i in range(1, 96):
    l.append([i, 'Total_' + str(i)])
    l.append([i, 'Choice_' + str(i)])
l.append(['Name', 'Study'])
all_95.columns = pd.MultiIndex.from_tuples(l)
all_95.to_csv(("./data/all_95.csv"))
print(all_95.head())
```

```
Total_1 Choice_1 Total_2 Choice_2
                                          Total_3 Choice_3
                                                             Total_4 Choice_4
{\sf Subj\_1}
           100
                       2
                             100
                                        2
                                               100
                                                          2
                                                                 100
Subj_2
           100
                             100
                                                50
                                                          3
                                                                 100
Subj_3
            50
                       3
                              50
                                         4
                                                50
                                                          3
                                                                 100
                                                                            2
Subj_4
            50
                       4
                              50
                                        3
                                               100
                                                                 100
Subj_5
           100
                             100
                                                50
                                                                 50
             5
                                     91
                                               92
                                                                   93
       Total_5 Choice_5
                              Choice_91 Total_92 Choice_92 Total_93 Choice_93
                         . . .
Subj_1
           100
                                      4
                                               50
                                                          4
                                                                 -200
                                                                              4
                         . . .
Subj_2
           100
                       2
                                               50
                                                          3
                                                                  50
                                                                              4
                         . . .
                      2 ...
Subj_3
           100
                                      4
                                             -200
                                                          4
                                                                   50
                                                                              4
                                      3
                                               25
Subj_4
           -50
                       1
                         . . .
                                                          3
                                                                   50
                                                                              4
Subj_5
            50
                      3 ...
                                               50
                                                                   50
             94
                                 95
                                                    Name
       Total_94 Choice_94 Total_95 Choice_95
                                                   Study
                                               Fridberg
Subj_1
             50
                        4
                                 50
                                            4
Subj_2
                                 25
                                               Fridberg
Subj_3
             50
                                 50
                                               Fridberg
                                               Fridberg
             50
                                 50
                                            4
Subj_4
                         4
                                             4 Fridberg
Subj_5
             50
                                 50
[5 rows x 191 columns]
```

I repeated this process for the other datasets.

```
ld, wd = \{\}, \{\}
for i in range(1, 101):
    ld['Losses_' + str(i)] = 'Total_' + str(i)
wd['Wins_' + str(i)] = 'Total_' + str(i)
lo\_100.rename(columns=ld, inplace=\textbf{True})
wi_100.rename(columns=wd, inplace=True)
total_100 = wi_100.add(lo_100)
all_100 = total_100.join(choice_100)
cols = all_100.columns.tolist()
cols = sorted(cols, key = lambda x: int(x.split('_')[-1]))
all 100 = all 100[cols]
index_100['Subj'] = index_100['Subj'].apply(lambda x: 'Subj_' + str(x))
index_100.set_index('Subj', inplace=True)
index 100.index.name = None
all_{100} = all_{100.join(index_{100})}
l = []
all_100.to_csv(("./data/all_100.csv"))
print(all_100.head())
```

```
2
             1
                                                3
       Total_1 Choice_1 Total_2 Choice_2 Total_3 Choice_3 Total_4 Choice_4
Subj_1
          -100
                            - <del>5</del>0
                                              100
                      1
                                       1
                                                              -200
Subj_2
           100
                      2
                            100
                                               50
                                                                50
                                                                          4
                                       1
           50
                            100
                                               0
                                                              - 200
                                                                          1
Subj_3
                      4
                                       2
                                                         3
Subj_4
          -200
                      4
                              0
                                       3
                                               50
                                                         4
                                                               100
                                                                          2
Subj_5
           100
                            100
                                              100
                                                             -1150
                                    96
                                              97
                                                                 98
       Total_5 Choice_5 ... Choice_96 Total_97 Choice_97 Total_98 Choice_98
Subj_1
            50
                      3
                                     2
                                              50
                                                         4
                                                                100
                                                                            2
                        . . .
                      3 ...
Subj_2
            50
                                              50
                                                                100
Subj_3
            50
                      4 ...
                                      2
                                             100
                                                                 50
                                                                            4
                                                         2
Subj_4
          -100
                      1 ...
                                      4
                                             100
                                                         1
                                                                 50
                                                                            4
Subj_5
           100
                      2 ...
                                     3
                                              50
                                                         3
                                                                  0
                                                                            3
                                100
                                                      Name
       Total_99 Choice_99 Total_100 Choice_100
                                                     Study
Subj_1
                                             2 Horstmann
             50
                       4
                              -1150
Subj_2
            100
                        2
                                50
                                              4 Horstmann
Subj_3
            100
                                100
                                              2 Horstmann
Subj_4
             0
                                 50
                                              4 Horstmann
                                 50
Subj_5
             50
                                              4 Horstmann
[5 rows x 201 columns]
```

```
ld, wd = \{\}, \{\}
for i in range(1, 151):
    ld['Losses_' + str(i)] = 'Total_' + str(i)
wd['Wins_' + str(i)] = 'Total_' + str(i)
lo_150.rename(columns=ld, inplace=True)
wi_150.rename(columns=wd, inplace=True)
total_150 = wi_150.add(lo_150)
all_150 = total_150.join(choice_150)
cols = all_150.columns.tolist()
cols = sorted(cols, key = lambda x: int(x.split('_')[-1]))
all 150 = all 150[cols]
index_150['Subj'] = index_150['Subj'].apply(lambda x: 'Subj_' + str(x))
index_150.set_index('Subj', inplace=True)
index 150.index.name = None
all_150 = all_150.join(index_150)
for i in range(1, 151):
    l.append([i, 'Total_' + str(i)])
l.append([i, 'Choice_' + str(i)])
l.append(['Name', 'Study'])
all_150.columns = pd.MultiIndex.from_tuples(l)
all_150.to_csv(("./data/all_150.csv"))
print(all_150.head())
```

```
1
                               2
                                                 3
       Total_1 Choice_1 Total_2 Choice_2 Total_3 Choice_3 Total_4 Choice_4
Subj_1
          -200
                       4
                             100
                                         1
                                              -250
                                                           1
                                                                 100
Subj_2
                                                50
                                                                  50
          -150
                       1
                            -250
                                        1
                                                                             3
Subj_3
           100
                       2
                              50
                                         4
                                               100
                                                           1
                                                                  50
Subj_4
            50
                       4
                              50
                                         4
                                                50
                                                           4
                                                                  50
                                                                             4
Subj_5
                                                50
                                      146
                                                147
                                                                      148
       Total_5 Choice_5 ...
                              Choice_146 Total_147 Choice_147 Total_148
Subj_1
            50
                       3
                                                  0
                                                              3
                         . . .
Subj 2
                                                -200
            50
                                                                       50
                         . . . .
Subj_3
                                                 50
           -50
                       1 ...
                                        4
                                                              4
                                                                        50
Subj_4
           -50
                       1
                         . . .
                                        4
                                                 50
                                                              4
                                                                       50
Subj_5
            50
                       4
                                                 50
                                                                        50
                         149
                                               150
                                                                            Name
       Choice_148 Total_149 Choice_149 Total_150 Choice_150
                                                                            Study
                                                            1 Steingroever2011
Subj_1
                2
                          50
                                      4
                                               - 50
Subj_2
                           0
                                               100
                                                             1 Steingroever2011
Subj 3
                          50
                                                50
                                                             4 Steingroever2011
Subj 4
                          50
                                                50
                                                             4 Steingroever2011
Subj_5
                4
                                      4
                          50
                                              -200
                                                             4 Steingroever2011
[5 rows x 301 columns]
```

3. Aggregating the Data

Then, I aggregated the 'all' dataframes into one dataframe and normalised the data.

I began by adding up each choice option so that I had the total number of times A, B, C and D were picked. For the purposes of this task I assumed that 1 was 'A', 2 was 'B' etc. I then added the totals so that I could see the total amount won or lost by each participant. I then added these columns as well as study to a dataframe named 'agg_95'.

```
data = []
for row in all_95.iterrows():
    total, a, b, c, d = 0,0,0,0,0
    for j in range(0, len(list(row[1])) - 1):
        i = list(row[1])[j]
        if j % 2 != 0:
            if i == 1:
               a += 1
            elif i == 2:
                b \ += \ 1
            elif i == 3:
                c += 1
            elif i == 4:
                d += 1
        else:
            total += i
   data.append(['95 ' + row[1].name, total, a, b, c, d, list(row[1])[-1]])
agg_95 = pd.DataFrame(data, columns=['Subj', 'Total', 'A', 'B', 'C', 'D', 'Study'])
agg_95
```

```
Subj Total A
                       B C D
                                    Study
    95_Subj_1
0
              1150 12
                        9
                            3 71 Fridberg
1
    95 Subj 2
               -675 24 26 12 33 Fridberg
    95 Subj 3
               -750 12 35 10 38 Fridberg
 3
    95_Subj_4
               -525
                   11
                       34 12
                               38
                                  Fridberg
    95_Subj_5
               100 10 24 15 46 Fridberg
 4
              1250
5
    95_Subj_6
                     6 18 20 51 Fridberg
6
    95_Subj_7
               -150 19 31
                           8 37 Fridberg
7
    95 Subj 8
               150 12 28 10 45 Fridberg
8
    95_Subj_9
               -575 10 34 12 39 Fridberg
   95_Subj_10
              1475
                     3 20 12
                               60 Fridberg
10
   95_Subj_11
               -350
                   14 40
                            9
                               32 Fridberg
11
   95_Subj_12
               -325
                   15 42 17
                               21
                                  Fridberg
12 95_Subj_13
               450
                   11 30 14 40
                                  Fridberg
13 95_Subj_14
               -425 14 37 17 27 Fridberg
14 95_Subj_15
               450 14 17 23 41 Fridberg
```

This was then repeated for 100 and 150.

```
data = []
for row in all_100.iterrows():
   total, a, b, c, d = 0,0,0,0,0
    for j in range(0, len(list(row[1])) - 1):
       i = list(row[1])[j]
       if j % 2 != 0:
            if i == 1:
               a += 1
            elif i == 2:
               b += 1
            elif i == 3:
               c += 1
            elif i == 4:
               d += 1
   data.append(['100_' + row[1].name, total, a, b, c, d, list(row[1])[-1]])
agg_100 = pd.DataFrame(data, columns=['Subj','Total', 'A', 'B', 'C', 'D', 'Study'])
agg_100
```

```
Subj
                  Total A B C D
                                          Study
       100_Subj_1
  0
                 -1800 21 42 15 22 Horstmann
       100_Subj_2
                  -800 14 35 18 33 Horstmann
  1
  2
       100_Subj_3
                  -450 21 42
                               7 30 Horstmann
  3
                  1200 13 24 28 35 Horstmann
       100_Subj_4
       100_Subj_5
                 -1300 15 31 28 26 Horstmann
  ...
                           ... ... ...
 499 100_Subj_500
                    75 17 29 28 26
                                         Worthy
    100_Subj_501
                   600 14 15 44 27
                                         Worthy
500
                 -1525 27 32 17 24
501 100_Subj_502
                                         Worthy
502 100_Subj_503
                  -750 27 25 23 25
                                         Worthy
                   175 10 24 12 54
503 100 Subj 504
                                         Worthy
504 rows × 7 columns
```

```
data = []
for row in all_150.iterrows():
   total, a, b, c, d = 0,0,0,0,0
    for j in range(0, len(list(row[1])) - 1):
       i = list(row[1])[j]
       if j % 2 != 0:
            if i == 1:
               a += 1
            elif i == 2:
               b += 1
            elif i == 3:
               c += 1
            elif i == 4:
               d += 1
           total += i
   data.append(['150_' + row[1].name, total, a, b, c, d, list(row[1])[-1]])
agg_150 = pd.DataFrame(data, columns=['Subj', 'Total', 'A', 'B', 'C', 'D', 'Study'])
agg_150
```

	Subj	Total	Α	В	С	D	Study
0	150_Subj_1	-550	46	37	29	38	Steingroever2011
1	150_Subj_2	-1600	40	57	19	34	Steingroever2011
2	150_Subj_3	900	19	35	8	88	Steingroever2011
3	150_Subj_4	2200	18	11	10	111	Steingroever2011
4	150_Subj_5	1900	13	1	1	135	Steingroever2011
93	150_Subj_94	300	24	69	13	44	Wetzels
94	150_Subj_95	2150	5	31	46	68	Wetzels
95	150_Subj_96	1450	18	19	37	76	Wetzels
96	150_Subj_97	1200	25	30	44	51	Wetzels
97	150_Subj_98	-1800	11	104	6	29	Wetzels
98 rows × 7 columns							

I then normalised them by dividing each dataframe by the amount of trials it contained.

```
agg_150[['Total', 'A', 'B', 'C', 'D']]/= 150
agg_100[['Total', 'A', 'B', 'C', 'D']]/= 100
agg_95[['Total', 'A', 'B', 'C', 'D']]/= 95
```

I then added in a 'Good' column (the sum of C and D), a 'Bad' column (the sum of A and B), a column for the numeric representation of each study and a column with the payload of the study. I then saved the dataframe as a csv file in the data folder under 'agg_all.csv'.

	Subj	Total	Α	В	С	D	Study	Bad
0	95_Subj_1	12.105263	0.126316	0.094737	0.031579	0.747368	Fridberg	0.221053
1	95_Subj_2	-7.105263	0.252632	0.273684	0.126316	0.347368	Fridberg	0.526316
2	95_Subj_3	-7.894737	0.126316	0.368421	0.105263	0.400000	Fridberg	0.494737
3	95_Subj_4	-5.526316	0.115789	0.357895	0.126316	0.400000	Fridberg	0.473684
4	95_Subj_5	1.052632	0.105263	0.252632	0.157895	0.484211	Fridberg	0.357895
612	150_Subj_94	2.000000	0.160000	0.460000	0.086667	0.293333	Wetzels	0.620000
613	150_Subj_95	14.333333	0.033333	0.206667	0.306667	0.453333	Wetzels	0.240000
614	150_Subj_96	9.666667	0.120000	0.126667	0.246667	0.506667	Wetzels	0.246667
615	150_Subj_97	8.000000	0.166667	0.200000	0.293333	0.340000	Wetzels	0.366667
616	150_Subj_98	-12.000000	0.073333	0.693333	0.040000	0.193333	Wetzels	0.766667
617 rd	ws × 11 column	IS						

The data was then ready for me to use in my cluster analysis.

Cluster Analysis

Cluster analysis or clustering is the task of grouping a set of objects in such a way that objects in the same group are more similar to each other than to those in other groups.

```
import numpy as np
import pandas as pd
import statsmodels.api as sm
import matplotlib.pyplot as plt
import seaborn as sns
sns.set()
sns.set_palette('gnuplot2', n_colors=10)
from sklearn.cluster import KMeans
from collections import Counter
from sklearn.metrics import silhouette_score
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler
```

```
all_95 = pd.read_csv("./data/all_95.csv", header = [0,1], index_col=0)
all_100 = pd.read_csv("./data/all_100.csv", header = [0,1], index_col=0)
all_150 = pd.read_csv("./data/all_150.csv", header = [0,1], index_col=0)
df = pd.read_csv("./data/agg_all.csv", index_col=0)
df
```

	Subj	Total	Α	В	С	D	Study	Bad
0	95_Subj_1	12.105263	0.126316	0.094737	0.031579	0.747368	Fridberg	0.221053
1	95_Subj_2	-7.105263	0.252632	0.273684	0.126316	0.347368	Fridberg	0.526316
2	95_Subj_3	-7.894737	0.126316	0.368421	0.105263	0.400000	Fridberg	0.494737
3	95_Subj_4	-5.526316	0.115789	0.357895	0.126316	0.400000	Fridberg	0.473684
4	95_Subj_5	1.052632	0.105263	0.252632	0.157895	0.484211	Fridberg	0.357895
612	150_Subj_94	2.000000	0.160000	0.460000	0.086667	0.293333	Wetzels	0.620000
613	150_Subj_95	14.333333	0.033333	0.206667	0.306667	0.453333	Wetzels	0.240000
614	150_Subj_96	9.666667	0.120000	0.126667	0.246667	0.506667	Wetzels	0.246667
615	150_Subj_97	8.000000	0.166667	0.200000	0.293333	0.340000	Wetzels	0.366667
616	150_Subj_98	-12.000000	0.073333	0.693333	0.040000	0.193333	Wetzels	0.766667
617 rd	ws × 11 column	S						

1. The Optimal Number of Clusters

There are two methods to find the optimal number of clusters for a dataset, the Elbow Method and the Silhouette Method.

1.1 The Elbow Method

This is the most common method for determining the optimal number of clusters. To do this you must calculate the Within-Cluster-Sum of Squared Errors (WSS) for different values of k, and choose the k for which WSS first starts to diminish. In a plot of WSS-versus-k, this is visible as an elbow.

```
def elbow_score(x):
    distortions = []
    K = range(1,11)
    for k in K:
        kmeanModel = KMeans(n_clusters=k)
        kmeanModel.fit(x)
        distortions.append(kmeanModel.inertia_)
    plt.plot(K, distortions, 'bx-')
    plt.xlabel('k')
    plt.ylabel('Distortion')
    plt.title('The Elbow Method showing the optimal k')
    plt.show()
```

1.2 The Silhouette Method

This is a method to find the optimal number of clusters k. The silhouette value measures how similar a point is to its own cluster (cohesion) compared to other clusters (separation). A high value is desirable. This is the formula: $[s(i) = \frac{b(i)}{\max(a(i), b(i))}]$

NOTE: s(i) is defined to be equal to zero if i is the only point in the cluster. This is to prevent the number of clusters from increasing significantly with many single-point clusters.

 $a(i) \text{ is the measure of the similarity of the point } i \text{ to its own cluster.} \\ \text{ (a(i) = \frac{1}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}{\left(\frac{1}}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}{\left(\frac{1}}\right)}}\right)}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}\right)}}\right)}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}\right)}{\left(\frac{1}}{\left(\frac{1}}\right)}{\left(\frac{1}}{\left(\frac{1}}\right)}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}\right)}}\right)}{\left(\frac{1}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}\right)}{\left(\frac{1}}\right)}{\left(\frac{1}}{\left(\frac{1}}\right)}}{\left(\frac{1}}{\left(\frac{1}\right)}{\left(\frac{1}}\right)}}{\left(\frac{1}}\right)}}{\left(\frac{1}}{\left(\frac{1}\right)}}}}{\left(\frac{1}}{\left(\frac{1}\right)}{\left(\frac{1}}\right)}}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}}\right)}{\left(\frac{1}}{\left(\frac{1}}{\left(\frac{1}\right)}}\right)}{\left(\frac{1}}{\left(\frac{1}}$

```
def sil_value(x):
    sil = []
    kmax = 10

# dissimilarity would not be defined for a single cluster, thus, minimum number of
clusters should be 2
    for k in range(3, kmax+1):
        kmeans = KMeans(n_clusters = k).fit(x)
        labels = kmeans.labels_
        sil.append(silhouette_score(x, labels, metric = 'euclidean'))
    return sil

# https://medium.com/analytics-vidhya/how-to-determine-the-optimal-k-for-k-means-
708505d204eb
```

2. Clustering the Data

I chose to perform clustering on the total amount won or lost compared to the amount the participants chose the deck 'C'. I thought this would be interesting because C was a "good" deck but had frequent losses. The losses also depended on the payload of the study. I wanted to see if the clusters had any relationship to the payload.

I also wanted to cluster the data comparing the total amount won or lost to the amount of times the participants chose a "good" deck. This would be interesting to see if there was anything in particular that defined each of these clusters.

2.1 Performing Clustering on Deck C

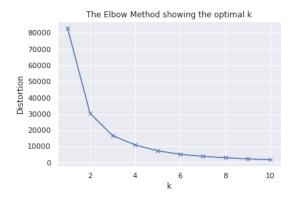
I began by making a dataframe with just 'Total' and 'C' columns.

```
c = df.iloc[:,[1,4]]
c
```

	Total	С				
0	12.105263	0.031579				
1	-7.105263	0.126316				
2	-7.894737	0.105263				
3	-5.526316	0.126316				
4	1.052632	0.157895				
612	2.000000	0.086667				
613	14.333333	0.306667				
614	9.666667	0.246667				
615	8.000000	0.293333				
616	-12.000000	0.040000				
617 rows × 2 columns						

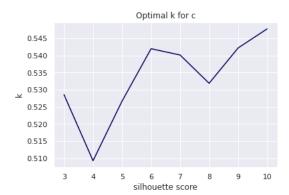
I then used the elbow method and the silhouette method to find the optimal number of clusters.

```
elbow_score(c)
```



```
c_sil = sil_value(c)

plt.plot([3,4,5,6,7,8,9,10], c_sil)
plt.title('Optimal k for c')
plt.xlabel('silhouette score')
plt.ylabel('k')
plt.show()
```



It was not completely clear from the elbow method whick value I should use for k. It looked to be between 3 and 7. In the silhouette method the peak was at 10 but there was also a slightly lower peak at 7. For this reason I chose 7 as my k and made 7 clusters.

I used sklearn.cluster.KMeans to create the clusters and fit them to the data.

```
c_kmeans = KMeans(7)
c_kmeans.fit(c)

KMeans(n_clusters=7)
```

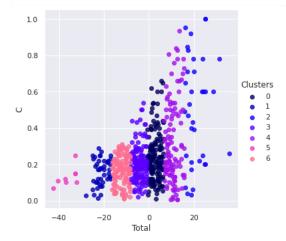
I then find the identified clusters in c.

```
c_identified_clusters = c_kmeans.fit_predict(c)
c_identified_clusters
```

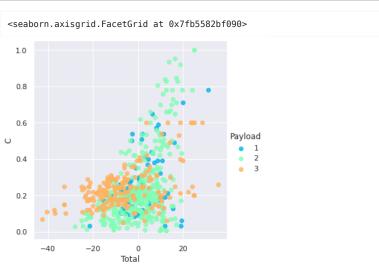
```
array([4, 3, 3, 3, 0, 4, 3, 0, 3, 4, 3, 3, 0, 3, 0, 1, 3, 3, 4, 6, 6, 0,
      6, 4, 3, 0, 0, 0, 3, 0, 0, 6, 6, 3, 0, 3, 0, 6, 0, 4, 4, 3, 0, 3,
      0,\ 4,\ 3,\ 0,\ 3,\ 4,\ 3,\ 0,\ 6,\ 1,\ 4,\ 0,\ 0,\ 0,\ 6,\ 6,\ 3,\ 3,\ 3,
                                                                 0, 1, 0,
      6, 1, 4, 0, 0, 3, 3, 3, 6, 0, 2, 3,
                                           4, 6, 0, 0, 0, 4, 4,
                                                                 6, 2, 0,
      4, 3, 0, 6, 0, 3, 4, 0, 3, 0, 4, 6, 3, 4, 1, 3, 6, 4, 0, 4, 4, 3,
      0, 3, 3, 0, 0, 4, 0, 6, 4, 0, 0, 4,
                                           3, 4, 4, 0, 1, 0, 0,
      1, 3, 4, 0, 4, 4, 6, 0, 0, 3, 4, 4, 0, 3, 4, 3, 3, 4, 4, 4, 0, 6,
                                           3, 6, 3, 0, 0, 0, 1, 0, 6, 0,
      6, 0, 2, 0, 3, 3, 6, 4, 3, 4, 3, 4,
            3, 6, 3, 4, 4, 0,
         1,
                               3, 6, 1, 0,
                                           3, 5,
                                                 Θ,
                                                     4,
                                                        4, 3, 0,
                                                                 1, 0,
      0, 0, 0, 3, 4, 4, 3, 0, 0, 0, 2, 0, 4, 3, 3, 3, 4, 3, 4, 3, 4, 3,
         4, 4, 6, 2, 0, 0, 6, 2, 4, 3, 0,
                                           3, 0, 4, 0, 0, 6, 0,
                                                                 2, 6, 6,
      3, 0, 4, 3, 6, 0, 4, 3, 3, 4, 4, 6, 4, 0, 3, 3, 6, 0, 4, 3, 4, 1,
      0,\ 6,\ 6,\ 6,\ 4,\ 0,\ 0,\ 1,\ 4,\ 4,\ 0,\ 6,\ 4,\ 3,\ 0,\ 6,\ 3,\ 6,\ 3,\ 2,\ 1,\ 3,
      4, 4, 6, 0, 0, 0, 3, 0, 4, 6, 3, 6,
                                           6, 4, 6, 2,
                                                        1, 2, 3,
      6, 2, 6, 2, 1, 2, 4, 0, 2, 0, 6, 2, 3, 4, 0, 2, 6, 2, 0, 6, 4, 1,
          3, 6, 1, 3, 6, 3,
                               3, 0, 3, 6,
                                           1, 6, 6, 6,
                                                        2,
                                                           4, 1,
                            1.
                                                                 6. 6. 3.
      5, 3, 3, 6, 6, 0, 4, 3, 3, 1, 6, 4, 0, 6, 0, 6, 3, 3, 6, 6, 1, 0,
      3, 0, 4, 6, 6, 3, 3, 3, 1, 1, 6, 6, 3, 6, 6, 3, 1, 4, 6,
                                                                 4, 4, 4,
         2, 3, 0, 6, 3, 6, 5, 0, 0, 3, 6,
                                           3, 3, 6, 6, 6, 4, 3,
                                                                 1, 0,
       3, 6, 4, 6, 6, 1, 6, 3, 4, 6, 0, 6, 3, 2, 3, 5, 1, 0, 2, 3, 6, 3,
      1, 6, 0, 6, 3, 0, 6, 6, 6, 5, 6, 3,
                                           3, 6,
                                                 1, 1,
                                                        3, 1, 6,
                                                                 3, 1, 6,
      6, 4, 6, 3, 3, 2, 3, 6, 1, 1, 1, 2,
                                           5, 5,
                                                 3, 1, 6, 2, 6, 1, 4, 1,
      3, 4, 3, 0, 1, 3, 3, 3, 6, 3, 3, 3, 6, 3, 3, 3, 3, 3, 1, 6, 3,
      0, 6, 6, 2, 0, 3, 3, 3, 0, 0, 6, 3, 0, 3, 6, 0, 4, 4, 6, 0, 2, 0,
       2, 4, 3, 4, 6, 0, 4, 3, 4, 0, 4, 4, 3, 6, 3, 0, 6, 4, 6, 1, 0, 6,
      6, 6, 2, 1, 0, 4, 2, 0, 0, 0, 0, 0, 3, 6, 4, 0, 0, 3, 6, 0, 4, 3,
      0, 2, 6, 2, 3, 0, 2, 0, 3, 4, 4, 6, 0, 0, 0, 4, 4, 2, 0, 0, 0, 4,
      0, 4, 0, 4, 4, 6, 0, 6, 3, 3, 4, 3, 0, 4, 4, 4, 6, 4, 0, 4, 4, 4,
      6], dtype=int32)
```

This is a graph of the data with the different clusters shown in different colours.

```
<seaborn.axisgrid.FacetGrid at 0x7fb5582df650>
```



Then, for a comparison, I plotted the data using colour to differentiate payload.



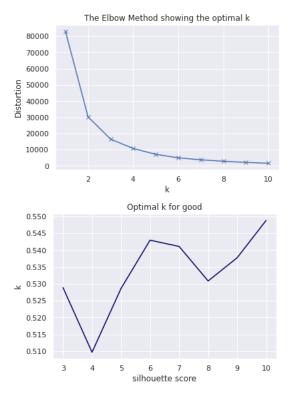
As you can see the datapoints in cluster 6 all chose c less and had the highest loss in the study. All of these data points were in payload 3. This makes sense because these people obviously chose C less because they were getting frequent losses from it and those losses were growing as they went. Most of the people who chose C the most were in payload 2 which is where the losses in C were constant.

2.2 Performing Clustering on "Good" Decks

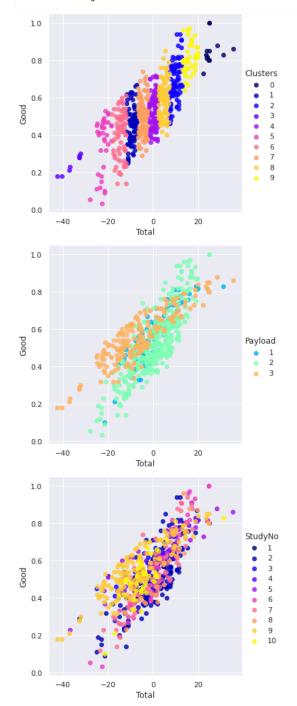
Now I would like to cluster the data based on the "good" card decks to see if there is any insight to be gleamed from it.

```
good = df.iloc[:,[1,7]]
elbow_score(good)
good_sil = sil_value(good)
good_k = good_sil.index(max(good_sil)) + 2

plt.plot([3,4,5,6,7,8,9,10], good_sil)
plt.title('Optimal k for good')
plt.xlabel('silhouette score')
plt.ylabel('k')
plt.show()
```



There is no clear k from the elbow plot, and the peak at 10 is a fair bit higher than any other peak in the silhouette plot. Therefore, I chose to make 10 clusters this time.



As you can see from the two graphs, there is obviously a strong correlation between picking "good" decks and winning more money. There does not seem to be any correlation between payload and "good" decks though. Maia et al. frequently asked the participants about their knowledge of the decks at regular intervals during the task. This is study number 4 and is shown in yellow on the graph. Nothing major stands out about this study except there were less people who chose the "bad" decks. It is hard to see because the datapoints for study 4 are all in the centre of the graph but there are a lot less of their datapoints under 0.4 than the other studies.

2.3 Further Analysis of "Good" Decks

I would now like to look more closely at clusters 7 and 9 because they are the most extreme on each side. It is said that after about 50 choices most people begin to see the patterns ang go for the "good" decks more consistently. I want to see if the people in cluster 9 seemed to figure out the pattern and the people in cluster 7 did not.

I began by getting the number of the good cluster (9) and the bad cluster (7). This is just in case the cluster numbers change at some point.

```
good_cluster = good_data_with_clusters[good_data_with_clusters['Total'] ==
max(good_data_with_clusters['Total'])]['Clusters'].iloc(0)[0]
bad_cluster = good_data_with_clusters[good_data_with_clusters['Total'] ==
min(good_data_with_clusters['Total'])]['Clusters'].iloc(0)[0]
```

I then found the subjects of the cluster so that I could find out whether they belonged to 95, 100, or 150. I then looked at the choices they made after the first 50 rounds and did some analysis on that.

```
good_subj_1 = list(good_data_with_clusters[good_data_with_clusters['Clusters'] ==
bad_cluster]['Subj'])
good_subj_1
good lst = []
for i in good_subj_1:
    n, idx = i.split('_', 1)
if n == '100':
        good\_lst.append(list(all\_100[all\_100.index == idx].values[0])[101::2])
    elif n == '150':
        good\_lst.append(list(all\_150[all\_150.index == idx].values[0])[101::2])
    elif n == '95':
        good_lst.append(list(all_95[all_95.index == idx].values[0])[101::2])
good_d = \{ a' : 0, b' : 0, c' : 0, d' : 0 \}
good_l, no_bad = [], []
for i in good_lst:
    c = Counter(i)
    good_d['a'] += c[1]
good_d['b'] += c[2]
    good_d['c'] += c[3]
    good_d['d'] += c[4]
    if c[1] + c[2] != 0:
        good_l.append((c[3] + c[4]) / (c[1] + c[2]))
    else:
        no_bad.append(c)
print(good d)
print(len([x for x in good_l if x < .5]))</pre>
print(len(good_l))
print(no_bad)
print(np.mean(good_l))
```

```
{'a': 67, 'b': 239, 'c': 46, 'd': 48}
6
8
[]
0.3690945336047337
```

This cluster chose 'B' the most and 6 out of 8 people were twice as likely to choose "bad" decks over "good" decks. This shows that the people in this cluster probably did not see the pattern and got distracted by the infrequent losses in Deck R

The mean of the ratios between good and bad is 0.369, which shows that the participants in the cluster were far less likely to choose good decks. If the mean was 1 it would mean that the participants chose fairly evenly between the "good" and "bad" decks.

```
good_subj_2 = list(good_data_with_clusters[good_data_with_clusters['Clusters'] ==
good_cluster]['Subj'])
good_subj_2
good lst = []
for i in good subi 2:
    n, idx = i.split('_i, 1)
    if n == '100':
        good_lst.append(list(all_100[all_100.index == idx].values[0])[101::2])
    elif n == '150':
        good_lst.append(list(all_150[all_150.index == idx].values[0])[101::2])
        good_lst.append(list(all_95[all_95.index == idx].values[0])[101::2])
good d = \{'a' : 0, 'b' : 0, 'c' : 0, 'd' : 0\}
good_l, no_bad = [], []
for i in good_lst:
   c = Counter(i)
   good d['a'] += c[1]
   good_d['b'] += c[2]
   good_d['c'] += c[3]
    good_d['d'] += c[4]
   if c[1] + c[2] != 0:
        good_l.append((c[3] + c[4]) / (c[1] + c[2]))
    else:
        no_bad.append(c)
print(good d)
print(len([x for x in good_l if x < 1]))
print(len(good_l))
print(no_bad)
print(np.mean(good_l))
```

```
{'a': 28, 'b': 18, 'c': 516, 'd': 188}
0
8
[Counter({3: 32, 4: 18}), Counter({3: 37, 4: 13}), Counter({3: 50}), Counter({3: 100}),
Counter({3: 100})]
15.049107142857144
```

In this cluster 'C' was chosen the most despite its frequent losses. None of the participants chose the "bad" decks more frequently than the "good" decks, with some people never choosing the bad decks at all. The mean was 15.049 which is very high. This means that the "bad" were barely chosen in comparison to the "good" decks.

For these reasons I think it is safe to assume that a lot of these participants figured out that the decks C and D contained more rewards than penalties.

3. Preserving the Privacy of Each Lab

Next, I wanted to find a way to obtain similar clustering results while preserving the privacy of each lab.

3.1 Using PCA

Principal Component Analysis, or PCA, is a way to reduce the dimensionality of a dataset. It also is able to provide some degree of privacy to the data.

First I dropped the columns that were not numeric and useful.

```
x = df.drop(columns = ['Subj', 'Study', 'StudyNo', 'Payload'])
```

I then performed PCA for two components and added them to a dataframe with the study number and payload.

	principal component 1	principal component 2	StudyNo	Payload
0	-13.875027	-0.317474	1	1
1	5.341599	-0.071472	1	1
2	6.130536	-0.110633	1	1
3	3.761851	-0.107813	1	1
4	-2.819895	-0.101765	1	1
612	-3.757980	-0.293730	8	2
613	-16.102065	-0.053414	8	2
614	-11.436426	-0.046602	8	2
615	-9.766207	-0.009333	8	2
616	10.245009	-0.271539	8	2

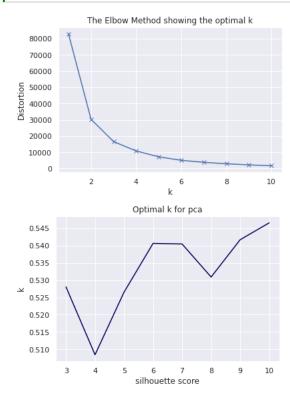
617 rows × 4 columns

I then got the elbow and silhouette scores and chose 7 as my optimal k.

```
elbow_score(principalDf)

pca_sil = sil_value(principalDf)
pca_k = pca_sil.index(max(pca_sil)) + 2

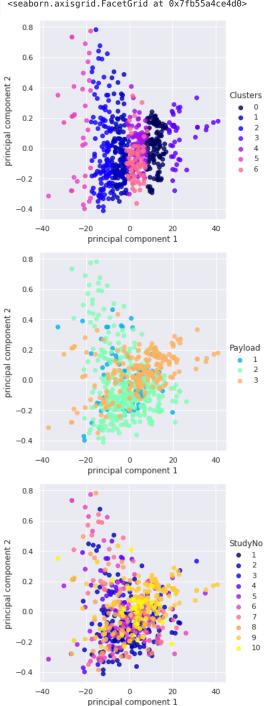
plt.plot([3,4,5,6,7,8,9,10], pca_sil)
plt.title('Optimal k for pca')
plt.xlabel('silhouette score')
plt.ylabel('k')
plt.show()
```



I then clustered the data and made graphs showing the clusters, the payload, and the study.

```
pca_kmeans = KMeans(7)
pca_kmeans.fit(pca_df)
pca_identified_clusters = pca_kmeans.fit_predict(pca_df)
pca_data_with_clusters = pca_df.copy()
pca_data_with_clusters['Clusters'] = pca_identified_clusters
sns.lmplot(data=pca_data_with_clusters, x='principal component 1', y='principal
component 2', hue='Clusters'
                        fit_reg=False, legend=True)
\verb|sns.lmplot(data=pca_data_with_clusters, x='principal component 1', y='principal| \\
component 2', hue='Payload',
                        fit_reg=False, legend=True, palette='rainbow')
sns.lmplot(data=pca_df, x='principal component 1', y='principal component 2',
hue='StudyNo',
                        \label{fit_reg} \texttt{False, legend=True)} \\
```

<seaborn.axisgrid.FacetGrid at 0x7fb55a4ce4d0>



These graphs do not look like the graphs I made before. There is more data in the top left quadrant of the graph. There does not seem to be much correlation between the clusters and the payoff but cluster 4 seems to be made up of majority payload 3 studies. There is no clear connection between these clusters and the studies.

3.2 Using Centroids

To do this I decided to perform clustering on each lab's results separately and then cluster their centroids to see if it gave similar results to clustering the data from all of the labs together. For this example I will use the same analysis as before, the 'Total' and the "good" decks.

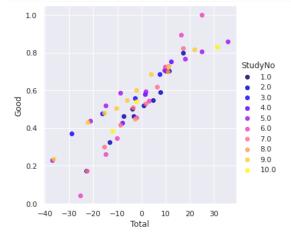
I looped through the studies and got the silhouette score for each study. I then performed k-means clustering on the data from each study. I added the centroid of each cluste to a dataframe called 'centroids'.

```
centroids = pd.DataFrame(columns = ['Total', 'Good', 'StudyNo'])
for study in range(1,11):
    study_df = df[df['StudyNo'] == study]
    study_good = study_df.iloc[:,[1,7]]
    study_good_sil = sil_value(study_good)
    study_good_k = study_good_sil.index(max(study_good_sil)) + 2
       \begin{array}{ll} plt.plot([3,4,5,6,7,8,9,10], & study\_good\_sil) \\ plt.title('Optimal k for \{\}'.format(study\_df['Study'].iloc(0)[0])) \end{array} 
#
      plt.xlabel('silhouette score')
      plt.ylabel('k')
      plt.show()
    study\_good\_kmeans = KMeans(study\_good\_k)
    study_good_kmeans.fit(study_good)
    study_good_identified_clusters = study_good_kmeans.fit_predict(study_good)
    centers = np.array(study_good_kmeans.cluster_centers_)
    for i in centers:
        centroids = centroids.append({'Total': i[0], 'Good': 1-i[1], 'StudyNo': study},
ignore_index=True)
print(centroids)
```

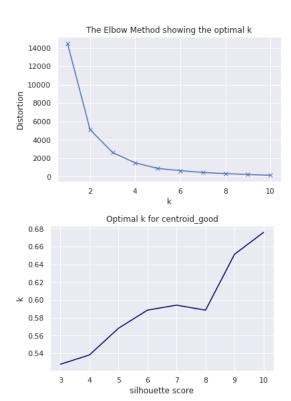
```
Total
                  Good StudyNo
   -3.710526 0.503158
0
                            1.0
   10.052632
              0.705263
                            1.0
   11.500000
              0.703333
                            2.0
   -7.441176 0.462941
                            2.0
    0.803571
              0.518571
                            2.0
4
5
  -13.261905
              0.326190
                            2.0
    4.703704
              0.548889
                            2.0
   -23.000000
              0.173333
                            2.0
   17.200000 0.800000
8
                            2.0
   -3.208333
              0.465000
                            2.0
10
   7.894737
              0.591579
                            2.0
11 -2.741667
              0.558333
                            3.0
12 -28.975000
              0.370000
                            3.0
    7.485714 0.685714
13
                            3.0
14 -16.375000
              0.477500
                            3.0
15
    1.541667
              0.581667
                            4.0
16 12.303571
              0.753571
                            4.0
17
   -8.000000
              0.426250
                            4.0
18 25.050000 0.807500
                            5.0
19
   -8.712500
              0.587500
                            5.0
20 -21.150000
              0.440000
                            5.0
21
   1.700000
              0.592500
                            5.0
22 -36.950000
              0.230000
                            5.0
23 18.016667
              0.766667
                            5.0
24 35.700000
              0.860000
                            5.0
25
   9.366667
              0.706667
                            5.0
26 -14.825000
              0.520000
                            5.0
27 -2.212121
              0.456364
                            6.0
28 9.666667
              0.725926
                            6.0
29 -10.111111 0.346667
                            6.0
30 25.000000
              1.000000
                            6.0
    3.095238
              0.546190
                            6.0
31
32 -25.333333
              0.043333
                            6.0
33 16.285714
              0.893333
                            6.0
34 -14.888889
              0.262222
                            6.0
35 -15.300000
              0.301000
                            7.0
36 6.562500
              0.618750
                            7.0
37
   -3.450000
              0.511000
                            7.0
38 17.285714
              0.825714
                            7.0
39 -8.807692
              0.417692
                            7.0
40
    1.700000
              0.532000
                            7.0
41 -22.750000
              0.175000
                            7.0
42 11.000000
              0.728000
                            7.0
43 10.933333
              0.699333
                            8.0
                            8.0
   -2.793651
              0.450476
45 11.034615
              0.726154
                            9.0
46 - 15.393548
              0.480323
                            9.0
47 - 10.405769
              0.506154
                            9.0
48 -22.326471
              0.432353
                            9.0
49 -36.383333
              0.238333
                            9.0
50 22.042857
              0.815714
                            9.0
   -2.050000
51
             0.600000
                            9.0
52 -5.973214
              0.547500
                            9.0
53
    3.970833
              0.685833
                            9.0
   -2.152174
              0.540870
                           10.0
55 31.250000
              0.830000
                           10.0
56 -12.068182 0.387273
                           10.0
```

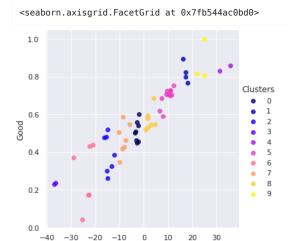
Here is a graph of all the centroids. As you can see, it is similar to the graph for all datapoints when plotting 'Total' and 'Good'. It also still captures that some studies had more variation in their 'Total' or in the amount a "good" deck was chosen. For example, the 6th study had people choosing "good" decks all the time and some people never choosing them. In contrast, the people in study 4 mostly chose a "good" deck somewhere between 40% and 80% of the time.

<seaborn.axisgrid.FacetGrid at 0x7fb544c461d0>



This is where I got the optimal *k* for the centroids data and performed clustering on it.





Total

The clusters show the same as the original clusters that the smaller clusters are on the edge because there are less datapoints there and the ones in the middle are bigger.

Overall, I would say that this method of preserving privacy is fine if you just want to understand the overall picture of the data and see roughly what way the data would look if it was clustered. However if you want to perform deeper analysis on the data it would not be very useful.

Conclusion

There are some interesting insights to be learned from this data when it has been clustered. There are relationships between the amount won or lost and the decks chosen, and the payload for the amount deck C was rewarding or penalising may have impacted the way that participants made their decisions. It is also harder to gain insight into the data as a whole when the privacy of each study is preserved.