

Marci M. McBride

CSE 122

HW 1

#3. Part a)

```
I. sum = 0;
   for (i = 0; i < n; i++)
       sum++;
```

Line	Cost	N
C1	1	1
C2	2	N+1
C3	1	n

$$T(n) = C1(1) + C2(N+1) + C3(n)$$

$$= n(C2+C3) + C2 + C1$$

$$T(n) = 3n+3 = 3(n+1)$$

```
II. sum = 0;
    for (i = 0; i < n; i++)
        for (j = 0; j < n; j++)
            sum++;
```

Line	Cost	N
C1	1	1
C2	2	N+1
C3	2	N(n+1)
C4	1	N ²

$$T(n) = C1(1) + C2(N+1) + C3(n(n+1)) + C4(N^2)$$

$$T(n) = 1 + 2n + 2 + 2(n^2+n) + n^2$$

$$= 3n^2 + 4n + 3$$

```
III. sum = 0;
     for (i = 0; i < n; i++)
         for (j = 0; j < n * n; j++)
             sum++;
```

Line	Cost	N
C1	1	1
C2	2	N+1
C3	2	N(n ² +1)
C4	1	N ³

$$T(n) = C1(1) + C2(N+1) + C3(n(n^2+1)) + C4(N^3)$$

$$T(n) = 1 + 2n + 2 + 2(n^3+n) + n^3$$

$$=3n^3 + 4n + 3$$

```
IV. sum = 0;
    for (i = 0; i < n; i++)
        for(j = 0; j < i; j++)
            sum++;
```

Line	Cost	N
C1	1	1
C2	2	N+1
C3	2	N(n+1)/2
C4	1	n(n-1)/2

$$T(n) = C1(1) + C2(N+1) + C3(n(n+1)/2) + C4(n(n-1)/2)$$

$$T(n) = 1 + 2n + 2 + n^2 + n + (n^2 - n)/2$$

$$T(n) = (3n^2 + 5n + 6)/2$$

```
V. sum = 0;
    for (i = 0; i < n; i++)
        for(j = 0; j < i * i; j++)
            for(k = 0; k < j; k++)
                sum++;
```

Line	Cost	N
C1	1	1
C2	2	N+1
C3	2	(n-1)((n(2n-7)+12)/6)
C4	2	(n-1) (n-2) (6n ³ -27n ² +47n-30)/60
C5	1	(n-1) (n-2) (n-3) (2n ² -3n)/20

$$T(n) = C1(1) + C2(N+1) + C3((n-1)((n(2n-7)+12)/6)) + C4((n-1) (n-2) (6n^3 - 27n^2 + 47n - 30)/60) + C5((n-1) (n-2) (n-3) (2n^2 - 3n)/20)$$

$$T(n) = 1 + 2n + 2 + 2((n-1)((n(2n-7)+12)/6)) + 2((n-1) (n-2) (6n^3 - 27n^2 + 47n - 30)/60) + ((n-1) (n-2) (n-3) (2n^2 - 3n)/20)$$

$$T(n) = (6n^5 - 45n^4 + 140n^3 - 225n^2 + 224n - 50)/10$$