

# RanCh

July 16, 2019

**Title** Tools for abstract discrete Random Choice

**URL** <http://github.com/mccauslw/RanCh>

**BugReports** <http://github.com/mccauslw/RanCh/issues>

**Version** 0.0.0.9000

**Description** This package provides tools for a research project whose purpose is to help us better understand the foundations of stochastic discrete choice. It includes datasets compiled from the literature on context effects and stochastic intransitivity and from some recent experiments. It provides graphical tools to display likelihood function and posterior density contours, as well as regions, in the space of choice probabilities, defined by various stochastic choice axioms, context effects and other conditions.

**Imports** klaR,  
MASS,  
bitops,  
Smisc,  
ggtern

**Depends** R (>= 3.6.0)

**License** CC0

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 6.1.1

**Suggests** knitr,  
rmarkdown

**VignetteBuilder** knitr

## R topics documented:

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binary2ternary

*Transform 2nd order barycentric coordinates to 3rd order*

---

## Description

binary2ternary transforms the 2nd order barycentric coordinates of the rows of `binary_points` into the 3rd order barycentric coordinates of the rows of `ternary_points`. This is useful for plotting points and line segments of binary choice probabilities on the sides of the 3rd order barycentric coordinate system. The two non-zero columns of the result are specified in the 2-vector `ternary_cols`.

**Usage**

```
binary2ternary(binary_points, ternary_cols)
```

**Arguments**

`binary_points` matrix of points, with each row a 2-vector on the 1-simplex  
`ternary_cols` 2-vector specifying the columns of the result corresponding to the two columns of `binary_points`

**Value**

matrix of points, with each row a 3-vector on the 2-simplex. The first element of `ternary_cols` gives the column of the result that takes the values of the first column of `binary_points`; the second element gives the column of the result taking the values of the second column of `binary_points`. The remaining column of the result is set to zero.

**Examples**

```
binary2ternary(matrix(c(0.6, 0.4), nrow=1), c(2,3)) # returns 1x3 matrix [0 0.6 0.4]
binary2ternary(matrix(c(0.6, 0.4), nrow=1), c(3,2)) # returns 1x3 matrix [0 0.4 0.6]
```

---

BM\_terms

---

*Compute Block-Marschack terms from a random choice structure*


---

**Description**

`BM_terms` returns a matrix of the same dimensions as the input matrix, a random choice structure  $P$ . The non-NA terms are all non-negative if and only if the random choice structure  $P$  satisfies random utility.

**Usage**

```
BM_terms(P)
```

**Arguments**

$P$  A random choice structure. Element  $P[A, x]$  is the probability that  $x$  is chosen when choice set  $A$  is presented.

**Value**

A matrix of Block-Marschak terms. If  $Q$  is the result, then for all random rankings of the elements of the universe of objects than induce the random choice structure  $P$ , element  $Q[A, x]$  is the probability that  $x$  is ranked higher than any other element of choice set  $A$  and lower than any element in the complement of  $A$  in the universe of objects. If  $x \notin A$ , then  $Q[A, x]$  has value NA. The RCS  $P$  satisfies random utility if and only if for all  $x \in A \subseteq T$ ,  $Q_A(x) \geq 0$

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
Q <- BM_terms(P)
Q
```

---

|            |  |
|------------|--|
| compromise | <i>Check if choice probabilities exhibit compromise effect</i> |
|------------|--|

---

### Description

compromise returns TRUE if the specified binary and ternary choice probabilities in random choice structure P are in the specified compromise effect region.

### Usage

```
compromise(P, target, competitor, decoy, two_sided = FALSE)
```

### Arguments

|            |  |
|------------|--|
| P          | matrix, random choice structure  |
| target     | index of target object   |
| competitor | index of competitor object   |
| decoy      | index of decoy object  |
| two_sided  | logical value indicating whether the compromise inequality is to hold also for competitor and decoy exchanged. |

### Value

A logical value indicating whether the appropriate choice probabilities are in the similarity effect region.

### Examples

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
compromise(P, target=1, competitor=2, decoy=3)
```

---

|               |                                  |
|---------------|----------------------------------|
| compromise_X3 | <i>Compromise effect regions</i> |
|---------------|----------------------------------|

---

### Description

compromise\_X3 constructs six regions (all polygons) associated with binary-ternary compromise effects. Below,  $x$  and  $z$  are the extreme choice objects and  $y$  is the between (or compromise) object. The interior of each polygon gives the set of ternary choice probabilities consistent with (1) the two specified binary choice probabilities and (2) one of six compromise effect conditions.

### Usage

```
compromise_X3(pyx, pyz)
```

### Arguments

|     |   |
|-----|---|
| pyx | scalar, probability $p(y, x)$ of choosing $y$ when presented with choice set $\{x, y\}$ . |
| pyz | scalar, probability $p(y, z)$ of choosing $y$ when presented with choice set $\{y, z\}$ . |

Value

named list of six polygons in a barycentric coordinate system. Each polygon is a matrix, with one row for each polygon vertex and one column for each of the three choice objects  $x, y$  and  $z$ . Element  $i, j$  gives the probability of choosing  $j$  when presented with choice set  $\{x, y, z\}$ , at the  $i$ 'th polygon vertex. The six polygons—triangles except for Cxz, a quadrilateral—are:

Cxyz region where there is a compromise effect with  $y$  as target,  $x$  as competitor and  $z$  as decoy

Czyx region where there is a compromise effect with  $y$  as target,  $z$  as competitor and  $x$  as decoy

Co region where there is neither compromise effect

Cx region with only the  $x$  effect

Cz region with only the  $z$  effect

Cxz region with both effects

See Also

[similarity\\_X3](#) for an analogous function for the similarity effect.

Examples

```
C <- compromise_X3(0.5, 0.6)
```

---

|           |  |
|-----------|--|
| create_P3 | <i>Random Choice Structure for a three-object universe</i> |
|-----------|--|

---

Description

create\_P3 creates a random choice structure for a three-object universe from

Usage

```
create_P3(p12, p23, p13, P1, P2, names = c("x", "y", "z"))
```

Arguments

- p12 Probability of chosing object 1 when presented with objects 1 and 2
- p23 Probability of chosing object 2 when presented with objects 2 and 3
- p13 Probability of chosing object 1 when presented with objects 1 and 3
- P1 Probability of chosing object 1 when presented with objects 1, 2 and 3
- P2 Probability of chosing object 2 when presented with objects 1, 2 and 3
- names character vector giving names to the three objects

Value

A Random Choice Structure

Examples

```
P <- create_P3(21/40, 37/40, 28/40, 19/40, 15/40, names=c('Red', 'Purple', 'Pink'))
P
```

---

|      |                                   |
|------|-----------------------------------|
| dDir | <i>Dirichlet density function</i> |
|------|-----------------------------------|

---

**Description**

dDir computes the Dirichlet density at a point  $p$  in the regular simplex, for a vector  $\alpha$  of Dirichlet parameters.

**Usage**

```
dDir(p, alpha, log = FALSE)
```

**Arguments**

|          |  |
|----------|--|
| $p$      | vector of probabilities on the regular simplex |
| $\alpha$ | vector of Dirichlet parameters                 |
| log      | logical; if TRUE, the log density is returned  |

**Value**

density or log density value

**Examples**

```
f <- dDir(c(0.1, 0.3, 0.6), c(2.5, 0.5, 1.0))
```

---

|                |  |
|----------------|--|
| dDir3_quantile | <i>Quantile of density value for third order Dirichlet</i> |
|----------------|--|

---

**Description**

dDir3\_quantile computes an approximation of the given quantile of a third order Dirichlet density value, under that Dirichlet distribution.

**Usage**

```
dDir3_quantile(quantile, alpha, normalized = FALSE)
```

**Arguments**

|            |  |
|------------|--|
| quantile   | the quantile of the desired density value  |
| $\alpha$   | a vector of Dirichlet parameters   |
| normalized | binary; if TRUE, return the quantile as a fraction of the maximum density value; if FALSE, return the unnormalized quantile. |

**Value**

The value of the quantile, normalized or not

---

|                |  |
|----------------|--|
| Dir2_HD_region | <i>Highest Density (HD) region for a second order Dirichlet distribution</i> |
|----------------|--|

---

**Description**

Dir2\_HD\_region constructs a line segment approximating the highest density region of a second order Dirichlet distribution. The line segment is in a second order barycentric coordinate system. This can be used to compute highest prior density and highest posterior density (HPD) regions for a second order Dirichlet-multinomial model (i.e. a beta-binomial model).

**Usage**

```
Dir2_HD_region(alpha, HD_probability)
```

**Arguments**

alpha                      vector of three (positive) Dirichlet parameters.  
 HD\_probability   scalar in  $[0, 1]$  giving the probability of the HD region

**Value**

matrix giving polygon approximation of HD region. Each row gives a polygon vertex. The three columns correspond to coordinates in a barycentric coordinate system.

---

|                |   |
|----------------|---|
| Dir3_HD_region | <i>Highest Density (HD) region for a third order Dirichlet distribution</i> |
|----------------|---|

---

**Description**

Dir3\_HD\_region constructs a polygon approximating the highest density region of a third order Dirichlet distribution. The polygon is in a three-dimensional barycentric coordinate system. This can be used to construct approximate highest prior density and highest posterior density (HPD) regions for a Dirichlet-multinomial model.

**Usage**

```
Dir3_HD_region(alpha, HD_probability)
```

**Arguments**

alpha                      vector of three (positive) Dirichlet parameters.  
 HD\_probability   scalar in  $[0, 1]$  giving the probability of the HD region

**Value**

matrix giving polygon approximation of HD region. Each row gives a polygon vertex. The three columns correspond to coordinates in a barycentric coordinate system.

---

|                     |   |
|---------------------|---|
| log_ML_DCE_Dir_mult | <i>Marginal likelihood for DCE, Dirichlet-multinomial model</i> |
|---------------------|---|

---

### Description

log\_ML\_DCE\_Dir\_mult computes the marginal likelihood for a model where choice count vectors are independent multinomial across choice sets and choice probability vectors are independent Dirichlet across choice sets.

### Usage

```
log_ML_DCE_Dir_mult(Alpha, N, log = TRUE)
```

### Arguments

|       |   |
|-------|---|
| Alpha | matrix of Dirichlet parameters, each row giving the Dirichlet distribution of the corresponding row of a random choice structure. |
| N     | count matrix with the same dimensions as Alpha, pertaining to the same universe of objects.                                       |
| log   | logical; if TRUE, return the log Bayes factor   |

---

|                                  |  |
|----------------------------------|--|
| log_ML_DCE_scalar_alpha_Dir_mult | <i>Marginal likelihood for DCE, scalar Dirichlet multinomial model</i> |
|----------------------------------|--|

---

### Description

log\_ML\_DCE\_scalar\_alpha\_Dir\_mult computes the marginal likelihood for a model where choice probability vectors  $P_A$  are mutually independent, and

$$P_A(x_1, \dots, x_{|A|}) \sim \text{Di}(\alpha/|A|, \dots, \alpha/|A|)$$

, and choices are conditionally independent multinomial.

### Usage

```
log_ML_DCE_scalar_alpha_Dir_mult(alpha, N, log = TRUE)
```

### Arguments

|       |   |
|-------|---|
| alpha | scalar determining Dirichlet parameters       |
| N     | count matrix                                  |
| log   | logical; if TRUE, return the log Bayes factor |



---

|                    |  |
|--------------------|--|
| log_ML_DCE_uniform | <i>Marginal likelihood for DCE, discrete uniform model</i> |
|--------------------|--|

---

### Description

log\_ML\_DCE\_uniform computes the marginal likelihood for a model (without parameters) where choices are mutually independent and for each choice set choices are discrete uniform on the choice set.

### Usage

```
log_ML_DCE_uniform(N, log = TRUE)
```

### Arguments

|     |   |
|-----|---|
| N   | count matrix                                  |
| log | logical; if TRUE, return the log Bayes factor |

---

|                         |   |
|-------------------------|---|
| log_ML_DCE_uniform_mult | <i>Marginal likelihood for DCE, uniform multinomial model</i> |
|-------------------------|---|

---

### Description

log\_ML\_DCE\_uniform\_mult computes the marginal likelihood for a model (without parameters) where choice probability vectors are mutually independent and uniformly distributed, choices are conditionally independent multinomial.

### Usage

```
log_ML_DCE_uniform_mult(N, log = TRUE)
```

### Arguments

|     |   |
|-----|---|
| N   | count matrix                                  |
| log | logical; if TRUE, return the log Bayes factor |

---

log\_ML\_DCE\_vector\_alpha\_Dir\_mult

*Marginal likelihood for DCE, vector Dirichlet multinomial model*


---

### Description

log\_ML\_DCE\_vector\_alpha\_Dir\_mult computes the marginal likelihood for a model where choice probability vectors  $P_A$  are mutually independent, and

$$P_A(x_1, \dots, x_{|A|}) \sim \text{Di}(u_1, \dots, u_{|A|})$$

, and choices are conditionally independent multinomial.

### Usage

```
log_ML_DCE_vector_alpha_Dir_mult(u, N, log = TRUE)
```

### Arguments

|     |   |
|-----|---|
| u   | vector determining Dirichlet parameters       |
| N   | count matrix                                  |
| log | logical; if TRUE, return the log Bayes factor |

---

log\_ML\_Dir\_mult

*Log marginal likelihood for Dirichlet-multinomial model*


---

### Description

log\_ML\_Dir\_mult computes the log marginal likelihood for a multinomial data generating process and a Dirichlet prior over choice probabilities.

### Usage

```
log_ML_Dir_mult(alpha, n, log = TRUE)
```

### Arguments

|       |   |
|-------|---|
| alpha | vector of Dirichlet parameters  |
| n     | vector of multinomial counts  |
| log   | logical; if TRUE, return the log marginal likelihood; if FALSE, the marginal likelihood. log=FALSE is usually not recommendend, as underflow is likely. |

### Value

Marginal likelihood or log marginal likelihood

---

|             |  |
|-------------|--|
| marginalize | <i>Routines for simple manipulations of count matrices and random choice structures.</i> |
|-------------|--|

---

**Description**

Marginalize a count matrix or random choice structure

**Usage**

```
marginalize(input_N, objects)
```

**Arguments**

|         |                               |
|---------|-------------------------------|
| input_N | A count matrix                |
| objects | A vector of objects to retain |

**Details**

This function takes as input a count matrix or random choice structure on a universe of objects and returns a marginalization of it to a universe that is a subset of the original universe.

**Value**

A count matrix

**Examples**

```
N_bce <- marginalize(PC_counts['Beer',,], c(2, 3, 5)) # Marginalize data first
P_bce_1 <- proportions(N_bce)                       # then compute proportions
P <- proportions(PC_counts['Beer',,])                # Compute proportions first
P_bce_2 <- marginalize(P, c(2, 3, 5))                # then marginalize. Gives same result.
```

---

|           |  |
|-----------|--|
| MC_counts | <i>Choice counts in multiple choice experiment</i> |
|-----------|--|

---

**Description**

A 141 by 31 by 5 array of count data. Element  $i, j, k$  gives the number of times subject  $i$  chose object  $k$  when presented with choice set  $j$ . The choice set index  $j=1,\dots,31$  encodes a non-empty subset of the universe of the five choice objects a, b, c, d and e, numbered 1, 2, 3, 4, 5. Whenever  $k$  is not an element of  $j$ , the value is NA.

**Usage**

```
MC_counts
```

**Format**

An object of class array of dimension 141 x 31 x 5.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [MC\\_trials](#), a table of choice trial data, and [MC\\_raw](#), a table of raw data. [set\\_index](#) describes how the choice set index encodes the choice set.

MC\_raw

*Multiple Choice experiment data***Description**

Raw trial-by-trial data from Multiple Choice experiment

**Usage**

MC\_raw

**Format**

A data frame with 53 variables generated in (WJM) We do not provide documentation, although the variable names are suggestive.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [MC\\_trials](#), a table of choice trial data, and [MC\\_counts](#), an array of choice count data.

MC\_trials

*Table of choice trial data from the Multiple Choice experiment***Description**

Table of choice trial data from the Multiple Choice experiment

**Usage**

MC\_trials

**Format**

A tibble with 18 variables

subject subject identifier

trial trial identifier (gives the order in which a subject sees choice sets)

set factor, name of choice set presented: 'ab', 'cde', etc., with objects in alphabetical order

choice factor, choice made by subject: 'a', 'b', 'c', 'd' or 'e'

set\_perm factor, order of presentation of objects on screen, left to right

set\_card integer, cardinality of choice set (i.e. number of available options)

set\_bin binary representation of choice set (binary digits indicate object membership in choice set)

choice\_int integer, code for chosen object: a=1, b=2, ..., e=5

ab, ac, ..., de revealed preference indicator: taking column ab as an example, the value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [MC\\_counts](#), an array of choice count data, and [MC\\_raw](#), a table of raw data.

---

|                   |  |
|-------------------|--|
| multiplicative_X3 | <i>Compute a cross section of the multiplicative inequality region</i> |
|-------------------|--|

---

**Description**

`multiplicative_X3` computes the region (a triangle) of ternary probabilities consistent with given binary probabilities and the multiplicative inequality.

**Usage**

```
multiplicative_X3(P)
```

**Arguments**

P                      A random choice structure

**Value**

A 3x3 matrix where each row gives one of the three vertices, in barycentric coordinates, of the triangular region where the multiplicative inequality holds.

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
multiplicative_X3(P)
```

---

|           |   |
|-----------|---|
| PC_counts | <i>Array of choice count data from the Population Choice experiment</i> |
|-----------|---|

---

**Description**

A 32 by 31 by 5 array of count data. Element  $i, j, k$  gives the number of subjects that chose object  $k$  when presented with choice set  $j$  of domain  $i$ . The choice set index  $j=1,\dots,31$  encodes a non-empty subset of the universe of the five choice objects a, b, c, d and e, numbered 1, 2, 3, 4, 5. Whenever  $k$  is not an element of  $j$ , the value is NA.

**Usage**

```
PC_counts
```

**Format**

An object of class array of dimension 32 x 31 x 5.

See Also

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [PC\\_trials](#), a table of choice trial data, [PC\\_demographics](#), a table of demographic information, and [PC\\_raw](#), a table of raw data. [set\\_index](#) describes how the choice set index encodes the choice set.

---

|                 |   |
|-----------------|---|
| PC_demographics | <i>Table of demographic information from the Population Choice experiment</i> |
|-----------------|---|

---

Description

Table of demographic information from the Population Choice experiment

Usage

PC\_demographics

Format

A data frame with demographic information on subjects

sex Sex of subject: 1 for male, 2 for female

age Age of subject in years

location Province or territory in Canada, 1=Alberta, 2=British Columbia, 3=Manitoba, 4=New Brunswick, 5=Newfoundland/Labrador, 6=Northwest Territories, 7=Nova Scotia, 8=Ontario, 9=Prince Edward Island, 10=Quebec, 11=Saskatchewan, 12=Yukon

See Also

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [PC\\_trials](#), a table of choice trial data, [PC\\_counts](#), a matrix of choice count data, and [PC\\_raw](#), a table of raw data.

---

|        |  |
|--------|--|
| PC_raw | <i>Table of raw data from Population Choice experiment</i> |
|--------|--|

---

Description

Table of raw data from Population Choice experiment

Usage

PC\_raw

**Format**

A data frame with 23 variables

responseid Unused subject identifier

gender Sex of subject: 1 for male, 2 for female

age Age of subject in years

location Province or territory in Canada, 1=Alberta, 2=British Columbia, 3=Manitoba, 4=New Brunswick, 5=Newfoundland/Labrador, 6=Northwest Territories, 7=Nova Scotia, 8=Ontario, 9=Prince Edward Island, 10=Quebec, 11=Saskatchewan, 12=Yukon

set

block Index (1,...,1024) of pre-constructed random design assigned to subject

consent Whether or not subjects gives consent (1) or not(2). All subjects give consent.

domain Index of choice domain

counts Cardinality of choice set presented

obj1 Object in position 1

obj2 Object in position 2

obj3 Object in position 3, possibly NA

obj4 Object in position 4, possibly NA

obj5 Object in position 5, possibly NA

obj1\_text Complete text describing object 1

obj2\_text Complete text describing object 2

obj3\_text Complete text describing object 3

obj4\_text Complete text describing object 4

obj5\_text Complete text describing object 5

choice Position of object chosen

expdur Trial duration in ms

intdur Survey duration in minutes

feedback Subject's response to "Please provide any additional feedback about the survey you have just completed."

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [PC\\_trials](#), a table of choice trial data, [PC\\_counts](#), a matrix of choice count data, and [PC\\_demographics](#), a table of demographic information

---

|           |   |
|-----------|---|
| PC_trials | <i>Table of choice trial data from the Population Choice experiment</i> |
|-----------|---|

---

**Description**

Table of choice trial data from the Population Choice experiment

**Usage**

```
PC_trials
```

**Format**

A tibble with 20 variables

domain factor, name of choice domain

subject subject identifier

trial trial identifier (gives the order in which a subject sees choice sets)

duration duration of trial in seconds

set factor, name of choice set presented: 'ab', 'cde', etc., with objects in alphabetical order

choice factor, choice made by subject: 'a', 'b', 'c', 'd' or 'e'

set\_perm factor, order of presentation of objects on screen, left to right

set\_card Integer, cardinality of choice set (i.e. number of available options)

set\_bin Binary representation of choice set (binary digits indicate object membership in choice set)

choice\_int Integer code for chosen object: a=1, b=2, ..., e=5

ab, ac, ..., de revealed preference indicator: taking column ab as an example, value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [PC\\_counts](#), an array of choice count data, [PC\\_demographics](#), a table of demographic information, and [PC\\_raw](#), a table of raw data.

---

|              |  |
|--------------|--|
| plot_HD_Dir3 | <i>Plot highest density regions for RCS with 3 objects</i> |
|--------------|--|

---

**Description**

This function plots the Dirichlet highest density (HD) regions in barycentric coordinates for the three binary choice probability and one ternary choice probability vectors of a random RCS

**Usage**

```
plot_HD_Dir3(Alpha, HD_probability, selection)
```



**Arguments**

Alpha                      matrix of Dirichlet parameters specifying the distribution of an RCD

HD\_probability      scalar in  $[0, 1]$  giving the probability of the HD region

selection                3-vector specifying the three columns of A to use for plotting

**Examples**

```
library(klaR)
N_bce <- marginalize(PC_counts['Beer', , ], c(2, 3, 5)) # Counts for objects 2, 3, 5
prior_Alpha <- prior_DCE_scalar_alpha(2.0, 3) # Parameters of simple conjugate prior
post_Alpha <- prior_Alpha + N_bce # Posterior parameters
triplot(label=c('b', 'c', 'e')) # Set up ternary plot
plot_HD_Dir3(post_Alpha, 0.90, c(1,2,3)) # Plot HPD regions
```

plot\_P3

*Plot a Random Choice Structure in barycentric coordinates***Description**

plot\_P3 plots four points specifying a Random Choice Structure for a universe of three objects.

**Usage**

```
plot_P3(P, perm = c(1, 2, 3), binary_pch = 1, ternary_pch = 20)
```

**Arguments**

P                      A random choice structure for a universe of three objects

perm                    A permutation of (1, 2, 3) specifying which objects in the universe correspond to the bottom left, top, and bottom right vertex, respectively of the ternary plot.

binary\_pch              Plotting character (pch) for binary choice probabilities. Defaults to a hollow circle.

ternary\_pch             Plotting character (pch) for ternary choice probability. Defaults to a solid circle. The convention established with the defaults for binary\_pch and ternary\_pch allow one to distinguish between a binary choice probability and a ternary choice probability that happens to be on the boundary of the triangle.

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
plot_P3(P)
```

---

prior\_DCE\_scalar\_alpha

*One-parameter Dirichlet prior for a RCS*

---

### Description

prior\_DCE\_scalar\_alpha computes a matrix of Dirichlet parameters for a one-parameter Dirichlet prior for a random choice structure.

### Usage

```
prior_DCE_scalar_alpha(alpha, n_objects)
```

### Arguments

|           |   |
|-----------|---|
| alpha     | univariate parameter for the one-parameter Dirichlet prior. |
| n_objects | number of objects in the universe.                          |

### Value

a matrix of Dirichlet parameters with the same dimensions as a count matrix for a universe of the same size.

---

prior\_DCE\_uniform

*Uniform prior for a RCS*

---

### Description

prior\_DCE\_uniform computes a matrix of Dirichlet parameters for the uniform prior over a random choice structure.

### Usage

```
prior_DCE_uniform(n_objects)
```

### Arguments

|           |                                    |
|-----------|------------------------------------|
| n_objects | number of objects in the universe. |
|-----------|------------------------------------|

### Value

a matrix of Dirichlet parameters all set to one, so that all choice probability vectors are uniformly distributed.

---

prior\_DCE\_vector\_alpha

*Vector Dirichlet prior for a RCS*

---

### Description

prior\_DCE\_vector\_alpha computes a matrix of Dirichlet parameters for a vector Dirichlet prior for a random choice structure.

### Usage

```
prior_DCE_vector_alpha(u)
```

### Arguments

u                      vector parameter for the vector Dirichlet prior.

### Value

a matrix of Dirichlet parameters for the vector Dirichlet prior.

---

proportions

*Random Choice Structure from count proportions*

---

### Description

proportions takes a count matrix as input, and returns choice proportions as a random choice structure.

### Usage

```
proportions(N)
```

### Arguments

N                      A count matrix.

### Value

A random choice structure.

### Examples

```
PC_P <- proportions(PC_counts[1,,])
```

---

|       |   |
|-------|---|
| RanCh | <i>RanCh: A package for abstract discrete Random Choice</i> |
|-------|---|

---

### Description

The RanCh package provides data, graphical tools and inference tools for abstract discrete random choice analysis.

### Data sets

NA

---

|                |  |
|----------------|--|
| random_utility | <i>Check if random choice structure satisfies random utility</i> |
|----------------|--|

---

### Description

random\_utility returns TRUE if the random choice structure P satisfies random utility and FALSE otherwise.

### Usage

```
random_utility(P)
```

### Arguments

P                      A random choice structure

### Value

A logical value indicating whether P satisfies random utility.

### Examples

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
random_utility(P)
```

---

|      |                                  |
|------|----------------------------------|
| rDir | <i>Dirichlet random variates</i> |
|------|----------------------------------|

---

**Description**

rDir draws from the Dirichlet distribution

**Usage**

```
rDir(n, alpha)
```

**Arguments**

|       |                                |
|-------|--------------------------------|
| n     | number of draws                |
| alpha | vector of Dirichlet parameters |

**Value**

matrix with n rows, each a draw from the Dirichlet distribution

**Examples**

```
library(klaR)
p <- rDir(1000, c(1, 1, 1)) # Uniform distribution on 2-simplex
triplot(label=c('x', 'y', 'z'))
plot(tritrafo(p))
```

---

|                 |  |
|-----------------|--|
| RDS_2011_counts | <i>Choice count data from the Regenwetter, Dana and Davis-Stober (2011) experiment</i> |
|-----------------|--|

---

**Description**

A 3 by 18 by 31 by 5 array of count data. Element  $h, i, j, k$  gives the number of times subject  $i$  chose object  $k$  when presented with choice set  $j$  of domain  $h$ . Domain names are "Cash 1", "Cash 2" and "Noncash", explained in the paper. The choice set index  $j \in \{1, \dots, 31\}$  encodes a non-empty subset of the universe of the four choice objects a, b, c, d, and e, numbered 1, 2, 3, 4, 5. Whenever  $k$  is not an element of  $j$ , the value is NA.

**Usage**

```
RDS_2011_counts
```

**Format**

An object of class array of dimension 3 x 18 x 31 x 5.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. [set\\_index](#) describes how the choice set index encodes the choice set.

---

|            |  |
|------------|--|
| regularity | <i>Check if random choice structure satisfies regularity</i> |
|------------|--|

---

**Description**

regularity returns TRUE if the random choice structure P satisfies regularity and FALSE otherwise.

**Usage**

```
regularity(P)
```

**Arguments**

P                      A random choice structure

**Value**

A logical value indicating whether P satisfies regularity.

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
regularity(P)
```

---

|               |   |
|---------------|---|
| regularity_X3 | <i>Compute a cross section of the regularity region</i> |
|---------------|---|

---

**Description**

regularity\_X3 computes the region (a triangle or the empty set) of ternary probabilities consistent with given binary probabilities and the regularity condition.

**Usage**

```
regularity_X3(P)
```

**Arguments**

P                      A random choice structure.

**Value**

If the region is empty, the output is NULL. Otherwise, a 3x3 matrix where each row gives one of the three vertices in barycentric coordinates.

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
reg_region <- regularity_X3(P)
```

ru

*Helper function for random\_utility and BM\_terms, below.***Description**

ru tests whether or not a random choice structure satisfies random utility

**Usage**

```
ru(P, compute_Q)
```

**Arguments**

|            |  |
|------------|--|
| P          | matrix, a random choice structure  |
| compute_Q, | a logical value indicating whether or not to compute $Q$ , the matrix of Block-Marschak terms corresponding to $P$ . If compute_Q is true, output is a list with elements $Q$ and is_ru, where is_ru is a boolean value that is TRUE or FALSE according to whether or not $P$ satisfies random utility. If compute_Q is FALSE, output is TRUE or FALSE according to whether or not $P$ satisfies random utility. |

**Value**

A logical value indicating whether  $P$  satisfies random utility.

set\_index

*Compute set index***Description**

set\_index takes a vector  $v$  of object indices and constructs a set index, an index for the set of objects whose indices are elements of  $v$ . Each digit (or bit) in the binary representation of the resulting set index is an inclusion indicator: object  $i$  is in the set if and only if the  $i$ 'th digit from the right is 1. For example, the set with objects 1, 3, and 4 has index equal to binary 1101, or decimal 13. The set with elements 1, 3 and 4 can be specified as the input vector c(1,3,4) or any permutation thereof, such as c(3,4,1).

**Usage**

```
set_index(v)
```

**Arguments**

|   |  |
|---|--|
| v | vector of object indices, in any order |
|---|--|

**Details**

Note that the singleton set with object  $i$  is represented as  $2^{i-1}$ . The bitwise "or" (bitwOr) of the set indices of two sets is the set index of their union; the bitwise "and" (bitwAnd), the set index of their intersection.

**Value**

An integer index corresponding to the set of objects whose indices are elements of  $v$ .

**Examples**

```
A <- set_index(c(1,3,4)) # Returns (decimal) 13, equal to binary 1101.
```

---

|            |  |
|------------|--|
| similarity | <i>Check if choice probabilities exhibit similarity effect</i> |
|------------|--|

---

**Description**

similarity returns TRUE if the specified binary and ternary choice probabilities in random choice structure  $P$  are in the specified similarity effect region.

**Usage**

```
similarity(P, target, competitor, decoy, two_sided = FALSE)
```

**Arguments**

|            |  |
|------------|--|
| $P$        | matrix, random choice structure  |
| target     | index of target object   |
| competitor | index of competitor object   |
| decoy      | index of decoy object  |
| two_sided  | logical value indicating whether the similarity inequality is to hold also for target and decoy exchanged. |

**Value**

A logical value indicating whether the appropriate choice probabilities are in the similarity effect region.

**Examples**

```
P <- create_P3(0.7, 0.6, 0.8, 0.6, 0.3, names = c('x', 'y', 'z'))
similarity(P, target=1, competitor=2, decoy=3)
```



---

|               |                                  |
|---------------|----------------------------------|
| similarity_X3 | <i>Similarity effect regions</i> |
|---------------|----------------------------------|

---

### Description

similarity\_X3 constructs six regions (all polygons) associated with binary-ternary similarity effects. Below,  $x$  and  $y$  are "similar" choice objects and object  $z$  is dissimilar to both  $x$  and  $y$ . The interior of each polygon gives the set of ternary choice probabilities consistent with (1) the two specified binary choice probabilities and (2) one of six similarity effect conditions.

### Usage

```
similarity_X3(pxz, pyz)
```

### Arguments

|     |   |
|-----|---|
| pxz | scalar, probability of choosing $y$ when presented with choice set $\{x, z\}$ |
| pyz | scalar, probability of choosing $y$ when presented with choice set $\{y, z\}$ |

### Value

named list of six polygons in a barycentric coordinate system. Each polygon is a matrix, with one row for each polygon vertex and one column for each of the three choice objects  $x$ ,  $y$  and  $z$ . Element  $i, j$  gives the probability of choosing  $j$ , when presented with choice set  $\{x, y, z\}$ , at the  $i$ 'th polygon vertex. The six polygons—triangles except for Sxy, a quadrilateral—are:

Sxyz region where there is a similarity effect with object  $x$  as target,  $y$  as decoy and  $z$  as competitor

Syxz region where there is a similarity effect with object  $x$  as target,  $y$  as decoy and  $z$  as competitor

So region where there is neither similarity effect

Sx region with only the  $x$  effect

Sy region with only the  $y$  effect

Sxy region with both effects

### See Also

[compromise\\_X3](#) for an analogous function for the compromise effect.

### Examples

```
S <- similarity_X3(0.5, 0.6)
```

---

T\_1969\_counts

*Choice count data from the Tversky (1969) experiment*


---

### Description

An 8 by 31 by 5 array of count data. Element  $i, j, k$  gives the number of times subject  $i$  chose object  $k$  when presented with choice set  $j$ . The choice set index  $j \in \{1, \dots, 7\}$  encodes a non-empty subset of the universe of the three choice objects  $x, y$ , and  $z$ , numbered 1, 2, 3. Whenever  $k$  is not an element of  $j$ , the value is NA.

### Usage

```
T_1969_counts
```

### Format

An object of class array of dimension 8 x 31 x 5.

### See Also

[RanCh](#), under Datasets for a description of the experiment. [set\\_index](#) describes how the choice set index encodes the choice set.

---

T\_1972\_counts

*Choice count data from the Tversky (1972) experiment*


---

### Description

A four dimensional array, 3 by 8 by 7 by 3, of count data. Element  $h, i, j, k$  gives the number of times subject  $i$  chose object  $k$  when presented with choice set  $j$  of domain  $h$ . Domain names are "Dots", "Gambles" and "Applicants", explained in the paper. The choice set index  $j \in \{1, \dots, 7\}$  encodes a non-empty subset of the universe of the three choice objects  $x, y$ , and  $z$ , numbered 1, 2, 3. Whenever  $k$  is not an element of  $j$ , the value is NA.

### Usage

```
T_1972_counts
```

### Format

An object of class array of dimension 3 x 8 x 7 x 3.

### See Also

[RanCh](#), under Datasets for a description of the experiment. [set\\_index](#) describes how the choice set index encodes the choice set.

YG\_counts

*Array of choice count data from the YouGov experiment***Description**

A four dimensional array, 16 by 2 by 15 by 4, of count data. Element  $h, i, j, k$  gives the number of subjects who chose object  $k$  when presented with choice set  $j$  of domain  $h$ , in their  $i$ 'th block of 16 trials. The choice set index  $j = 1, \dots, 15$  encodes a non-empty subset of the universe of the four choice objects a, b, c, and d, numbered 1, 2, 3, 4. Whenever  $k$  is not an element of  $j$ , the value is NA.

**Usage**

YG\_counts

**Format**

An object of class array of dimension 16 x 2 x 15 x 4.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [YG\\_trials](#), a table of choice trial data, [YG\\_demographics](#), a table of demographic information, and [YG\\_raw](#), a table of raw data. [set\\_index](#) describes how the choice set index encodes the choice set.

YG\_demographics

*Table of demographic information from the YouGov experiment***Description**

Table of demographic information from the YouGov experiment

**Usage**

YG\_demographics

**Format**

A data frame with demographic information on subjects

sex Sex of subject

educ Educational attainment by subject

region Region of subject's residence in US

race Race of subject

age\_range Age range of subject

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [YG\\_trials](#), a table of choice trial data, [YG\\_counts](#), a matrix of choice count data, and [YG\\_raw](#), a table of raw data.

YG\_raw

*Table of choice trial data from the YouGov experiment***Description**

Table of choice trial data from the YouGov experiment

**Usage**

YG\_raw

**Format**

A data frame with 17 variables:

design

card

domain

combo

perm

choiceset Choice set as a character string

option\_1 Object presented in first position: 1, 2, 3 or 4

option\_2 Object presented in second position

option\_3 Object presented in third position

option\_4 Object presented in fourth position

response Object chosen: 1, 2, 3 or 4

order

gender Sex of respondent: 1 for male, 2 for female

educ Education of respondent: 1 for No high school, 2 for High school graduate, 3 for Some college, 4 for 2-year college, 5 for 4-year college, 6 for post-graduate

region Region of respondent: 1 for northeast, 2 for midwest, 3 for south, 4 for west

race Race of respondent: 1 for White, 2 for Black, 3 for Hispanic, 4 for Asian, 5 for Native American, 6 for Mixed, 7 for Other, 8 for Middle Eastern

age\_cross Age category of respondent: 1 for 18-34, 2 for 35-54, 3 for 55 and over

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [YG\\_trials](#), a table of choice trial data, [YG\\_counts](#), a matrix of choice count data, and [YG\\_demographics](#), a table of demographic information

YG\_trials

*Table of choice trials data from the YouGov experiment***Description**

Table of choice trials data from the YouGov experiment

**Usage**

```
YG_trials
```

**Format**

A tibble with 17 variables

domain factor, name of choice domain

subject subject identifier

block block, equal to 1 or 2, identifying the first or second pass a subject makes through the domains.

trial trial identifier (gives the order in which a subject sees choice sets)

duration duration of trial in seconds

set factor, name of choice set presented: 'ab', 'bcd', etc., with objects in alphabetical order

choice factor, choice made by subject: 'a', 'b', 'c', or 'd'

set\_perm factor, order of presentation of objects on screen, left to right

set\_card Integer, cardinality of choice set (i.e. number of available options)

set\_bin Binary representation of choice set (binary digits indicate object membership in choice set)

choice\_int Integer code for chosen object: a=1, b=2, ..., d=4

ab, ac, ..., cd revealed preference indicator: taking column ab as an example, value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.

**See Also**

[RanCh](#), under Datasets for a description of the experiment. Other data objects for the experiment include [YG\\_counts](#), an array of choice count data, [YG\\_demographics](#), a table of demographic information, and [YG\\_raw](#), a table of raw data.

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