RanCh

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Title Tools for abstract discrete Random Choice

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Description This package provides tools for a research project whose purpose is to help us better understand the foundations of stochastic discrete choice. It includes datasets compiled from the literature on context effects and stochastic intransitivity and from some recent experiments. It provides graphical tools to display likelihood function and posterior density contours, as well as regions, in the space of choice probabilities, defined by various stochastic choice axioms, context effects and other conditions.
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binary2ternary

Transform 2nd order barycentric coordinates to 3rd order

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Description

Index

binary2ternary transforms the 2nd order barycentric coordinates of the rows of binary_points into the 3rd order barycentric coordinates of the rows of ternary_points. This is useful for plotting points and line segments of binary choice probabilities on the sides of the 3rd order barycentric coordinate system. The two non-zero columns of the result are specified in the 2-vector ternary_cols.

Usage

```
binary2ternary(binary_points, ternary_cols)
```

Examples

```
binary2ternary(matrix(c(0.6, 0.4), nrow=1), c(2,3)) # returns 1x3 matrix [0 0.6 0.4] binary2ternary(matrix(c(0.6, 0.4), nrow=1), c(3,2)) # returns 1x3 matrix [0 0.4 0.6]
```

compromise_X3 3

compromise_X3

Compromise effect regions

Description

compromise_X3 constructs six regions (all polygons) associated with binary-ternary compromise effects. Below, x and z are the extreme choice objects and y is the between (or compromise) object. The interior of each polygon gives the set of ternary choice probabilities consistent with (1) the two specified binary choice probabilities and (2) one of six compromise effect conditions.

Usage

```
compromise_X3(pyx, pyz)
```

Arguments

рух	scalar, probability $p(y,x)$ of choosing y when presented with choice set $\{x,y\}$.
pyz	scalar, the probability $p(y,z)$ of choosing y when presented with choice set $\{y,z\}.$

Value

named list of six polygons in a barycentric coordinate system. Each polygon is a matrix, with one row for each polygon vertex and one column for each of the three choice objects x,y and z. Element i,j gives the probability of choosing j when presented with choice set $\{x,y,z\}$, at the i'th polygon vertex. The six polygons—triangles except for Cxz, a quadrilateral—are:

Cxyz region where there is a compromise effect with y as target, x as competitor and z as decoy

Czyx region where there is a compromise effect with y as target, z as competitor and x as decoy

Co region where there is neither compromise effect

 $\mathsf{Cx}\ \mathsf{region}\ \mathsf{with}\ \mathsf{only}\ \mathsf{the}\ x\ \mathsf{effect}$

Cz region with only the z effect

Cxz region with both effects

See Also

similarity_X3 for an analogous function for the similarity effect.

Examples

```
C = compromise_X3(0.5, 0.6)
```

dDir

$create_{-}$	P3
Create_	ГЭ

Random Choice Structure for a three-object universe

Description

create_P3 creates a random choice structure for a three-object universe from

Usage

```
create_P3(p12, p23, p13, P1, P2, names = c("x", "y", "z"))
```

Arguments

p12	Probability of chosing object 1 when presented with objects 1 and 2
p23	Probability of chosing object 2 when presented with objects 2 and 3
P1	Probability of chosing object 1 when presented with objects 1, 2 and 3
P2	Probability of chosing object 2 when presented with objects 1, 2 and 3
names	character vector giving names to the three objects
P13	Probability of chosing object 1 when presented with objects 1 and 3

Value

A Random Choice Structure

Examples

```
P = create_P3(21/40, 37/40, 28/40, 19/40, 15/40, names=c('Red', 'Purple', 'Pink'))
P
```

dDir

Dirichlet density function

Description

dDir computes the Dirichlet density at a point p in the regular simplex, for a vector alpha of Dirichlet parameters.

Usage

```
dDir(p, alpha, log = FALSE)
```

Arguments

p	vector of probabilities on the regular simplex
alpha	vector of Dirichlet parameters
log	logical; if TRUE, the log density is returned

Dir2_HD_region 5

Value

density or log density value

Examples

```
f = dDir(c(0.1, 0.3, 0.6), c(2.5, 0.5, 1.0))
```

Dir2_HD_region

Highest Density (HD) region for a second order Dirichlet distribution

Description

Dir2_HD_region constructs a line segment approximating the highest density region of a second order Dirichlet distribution. The line segment is in a second order barycentric coordinate system. This can be used to compute highest prior density and highest posterior density (HPD) regions for a second order Dirichlet-multinomial model (i.e. a beta-binomial model).

Usage

```
Dir2_HD_region(alpha, HD_probability)
```

Arguments

```
alpha vector of three (positive) Dirichlet parameters.

HD_probability scalar in [0,1] giving the probability of the HD region
```

Value

matrix giving polygon approximation of HD region. Each row gives a polygon vertex. The three columns correspond to coordinates in a barycentric coordinate system.

Dir3_HD_region

Highest Density (HD) region for a third order Dirichlet distribution

Description

Dir3_HD_region constructs a polygon approximating the highest density region of a third order Dirichlet distribution. The polygon is in a three-dimensional barycentric coordinate system. This can be used to construct approximate highest prior density and highest posterior density (HPD) regions for a Dirichlet-multinomial model.

Usage

```
Dir3_HD_region(alpha, HD_probability)
```

Arguments

```
alpha vector of three (positive) Dirichlet parameters.

HD_probability scalar in [0,1] giving the probability of the HD region
```

6 log_ML_Dir_mult

Value

matrix giving polygon approximation of HD region. Each row gives a polygon vertex. The three columns correspond to coordinates in a barycentric coordinate system.

 $\begwind {\tt log_ML_DCE_Dir_mult} \begwind {\tt Marginal likelihood for discrete choice experiment, Dirichlet-multinomial model} \\$

Description

log_ML_DCE_Dir_mult computes the marginal likelihood for a model where choice count vectors are independent multinomial across choice sets and choice probability vectors are independent Dirichlet across choice sets.

Usage

```
log_ML_DCE_Dir_mult(A, N, log = TRUE)
```

Arguments

Α	matrix of Dirichlet parameters, each row giving the Dirichlet distribution of the corresponding row of a random choice structure.
N	count matrix with the same dimensions as A, pertaining to the same universe of objects.
log	logical; if TRUE, return the log Bayes factor

log_ML_Dir_mult Log marginal likelihood for Dirichlet-multinomial model

Description

log_ML_Dir_mult computes the log marginal likelihood for a multinomial data generating process and a Dirichlet prior over choice probabilities.

Usage

```
log_ML_Dir_mult(alpha, N, log = TRUE)
```

Arguments

log

alpha vector of Dirichlet parameters

N vector of multinomial counts

logical; if TRUE, return the log marginal likelihood; if FALSE, the marginal likelihood. log=FALSE is usually not recommendend, as underflow is likely.

Value

Marginal likelihood or log marginal likelihood

marginalize 7

	marginalize	Routines for simple manipulations of count matrices and random choice structures.
--	-------------	-----------------------------------------------------------------------------------

Description

Marginalize a count matrix or random choice structure

Usage

```
marginalize(input_N, objects)
```

Arguments

input_N A count matrix
objects A vector of objects to retain

Details

This function takes as input a count matrix or random choice structure on a universe of objects and returns a marginalization of it to a universe that is a subset of the original universe.

Value

A count matrix

Examples

```
N_bce = marginalize(PC_counts, c(2,3,5))
P_abd = marginalize()
N
```

MC_counts

Choice counts in multiple choice experiment

Description

A three dimensional array, 141 by 31 by 5, of count data. Element i,j,k gives the number of times subject i chose object k when presented with choice set j. The choice set index j=1,...,31 encodes a non-empty subset of the universe of the five choice objects a, b, c, d and e, numbered 1, 2, 3, 4, 5. Each digit (or bit) in the binary representation of j is an inclusion indicator: object k is in the set if and only if the k'th digit from the right is 1. For example, the set with b, c, d and e (but not a) is encoded as binary 11110 (decimal 30). Whenever k is not an element of j, the value is NA.

Usage

MC_counts

Format

An object of class array of dimension 141 x 31 x 5.

8 MC_trials

MC_raw

Multiple Choice experiment data

Description

Raw trial-by-trial data from Multiple Choice experiment

Usage

MC_raw

Format

A data frame with 53 variables generated in (WJM) We do not provide documentation, although the variable names are suggestive.

MC_trials

Tibble recording every choice trial in the multiple choice experiment

Description

Tibble recording every choice trial in the multiple choice experiment

Usage

MC_trials

Format

```
A tibble with 18 variables
```

subject subject identifier

trial trial identifier (gives the order in which a subject sees choice sets)

set factor, name of choice set presented: 'ab', 'cde', etc., with objects in alphabetical order

choice factor, choice made by subject: 'a', 'b', 'c', 'd' or 'e'

set_perm factor, order of presentation of objects on screen, left to right

set_card integer, cardinality of choice set (i.e. number of available options)

set_bin binary representation of choice set (binary digits indicate object membership in choice set)

choice_int integer, code for chosen object: a=1, b=2, ..., e=5

ab, ac, ..., de revealed preference indicator: taking column ab as an example, the value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.

multiplicative_X3

multiplicative_X3

Compute a cross section of the multiplicative inequality region

Description

multiplicative_X3 computes the region (a triangle) of ternary probabilities consistent with given binary probabilities and the multiplicative inequality.

Usage

```
multiplicative_X3(P)
```

Arguments

Ρ

A random choice structure

Value

A 3x3 matrix where each row gives one of the three vertices, in barycentric coordinates, of the triangular region where the multiplicative inequality holds.

Examples

```
P = create_P3(0.7, 0.6, 0.8, 0.6, 0.3, 0.1, names = c('x', 'y', 'z')) multiplicative_X3(P)
```

PC_counts

Choice counts in Population Choice experiment

Description

A three dimensional array, 32 by 31 by 5, of count data. Element i,j,k gives the number of subjects that chose object k when presented with choice set j of domain i. The choice set index j=1,...,31 encodes a non-empty subset of the universe of the five choice objects a, b, c, d and e, numbered 1, 2, 3, 4, 5. Each digit (or bit) in the binary representation of j is an inclusion indicator: object k is in the set if and only if the k'th digit from the right is 1. For example, the set with b, c, d and e (but not a) is encoded as binary 11110 (decimal 30) Whenever k is not an element of j, the value is NA.

Usage

PC_counts

Format

An object of class array of dimension 32 x 31 x 5.

See Also

RanCh, under Datasets for a description of the experiment. Other data objects for the experiment include PC_trials for trial-by-trial data, PC_demographics for demographic information and PC_raw for the original raw data.

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PC_demographics

Demographic information for population choice experiment

Description

Demographic information for population choice experiment

Usage

PC_demographics

Format

A data frame with demographic information on subjects

sex Sex of subject: 1 for male, 2 for female

age Age of subject in years

location Province or territory in Canada, 1=Alberta, 2=British Columbia, 3=Manitoba, 4=New Brunswick, 5=Newfoundland/Labrador, 6=Northwest Territories, 7=Nova Scotia, 8=Ontario, 9=Prince Edward Island, 10=Quebec, 11=Saskatchewan, 12=Yukon

See Also

RanCh, under Datasets for a description of the experiment. Other data objects for the experiment include PC_trials for trial-by-trial data, PC_counts for choice count data and PC_raw for the original raw data.

PC_raw

Raw trial-by-trial data from Population Choice experiment

Description

Raw trial-by-trial data from Population Choice experiment

Usage

PC_raw

Format

A data frame with 23 variables

responseid Unused subject identifier

gender Sex of subject: 1 for male, 2 for female

age Age of subject in years

location Province or territory in Canada, 1=Alberta, 2=British Columbia, 3=Manitoba, 4=New Brunswick, 5=Newfoundland/Labrador, 6=Northwest Territories, 7=Nova Scotia, 8=Ontario, 9=Prince Edward Island, 10=Quebec, 11=Saskatchewan, 12=Yukon

set

PC_trials 11

```
block Index (1,...,1024) of pre-constructed random design assigned to subject
consent Whether or not subjects gives consent (1) or not(2). All subjects give consent.
domain Index of choice domain
counts Cardinality of choice set presented
obj1 Object in position 1
obj2 Object in position 2
obj3 Object in position 3, possibly NA
obj4 Object in position 4, possibly NA
obj5 Object in position 5, possibly NA
obj1_text Complete text describing object 1
obj2_text Complete text describing object 2
obj3_text Complete text describing object 3
obj4_text Complete text describing object 4
obj5_text Complete text describing object 5
choice Position of object chosen
expdur Trial duration in ms
intdur Survey duration in minutes
feedback Subject's response to "Please provide any additional feedback about the survey you have
     just completed."
```

See Also

RanCh, under Datasets for a description of the experiment. Other data objects for the experiment include PC_trials for trial-by-trial data, PC_counts for choice count data and PC_demographics for demographic information

PC_trials

Table of choice trials, population choice experiment

Description

Table of choice trials, population choice experiment

Usage

PC_trials

Format

```
A tibble with 20 variables

domain factor, name of choice domain

subject subject identifier

trial trial identifier (gives the order in which a subject sees choice sets)

duration duration of trial in seconds
```

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```
set factor, name of choice set presented: 'ab', 'cde', etc., with objects in alphabetical order
choice factor, choice made by subject: 'a', 'b', 'c', 'd' or 'e'
set_perm factor, order of presentation of objects on screen, left to right
set_card Integer, cardinality of choice set (i.e. number of available options)
set_bin Binary representation of choice set (binary digits indicate object membership in choice set)
choice_int Integer code for chosen object: a=1, b=2, ..., e=5
ab, ac,..., de revealed preference indicator: taking column ab as an example, value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.
```

See Also

RanCh, under Datasets for a description of the experiment. Other data objects for the experiment include PC_counts for choice count data, PC_demographics for demographic information and PC_raw for the original raw data.

plot_HD_Dir3

Plot highest density region for a third order Dirichlet distribution

Description

This function plots the Dirichlet highest density region in barycentric coordinates.

Usage

```
plot_HD_Dir3(A, HD_probability, selection)
```

Arguments

```
HD_probability probability of highest density region alpha vector of Dirichlet parameters
```

Examples

```
plot_HD_Dir3(A, 0.95, c(1,2,3))
```

plot_P3

plot_P3 //	Plot a Random Choice Structure in barycentric coordinates
------------	-----------------------------------------------------------

Description

plot_P3 plots four points specifying a Random Choice Structure for a universe of three objects.

Usage

```
plot_P3(P, perm = c(1, 2, 3), binary_pch = 1, ternary_pch = 20)
```

Arguments

P A random choice structure for a universe of three objects

perm A permutation of (1, 2, 3) specifying which objects in the universe correspond

to the bottom left, top, and bottom right vertex, respectively of the ternary plot.

binary_pch Plotting character (pch) for binary choice probabilities. Defaults to a hollow

circle.

ternary_pch Plotting character (pch) for ternary choice probability. Defaults to a solid circle.

The convention established with the defaults for binary_pch and ternary_pch allow one to distinguish between a binary choice probability and a ternary choice

probability that happens to be on the boundary of the triangle.

Examples

```
 P = create_{P3}(0.7, \ 0.6, \ 0.8, \ 0.6, \ 0.3, \ 0.1, \ names = c('x', \ 'y', \ 'z')) \\ plot_{P3}(P)
```

```
prior_DCE_scalar_alpha
```

One-parameter Dirichlet prior for a RCS

Description

prior_DCE_scalar_alpha computes a matrix of Dirichlet parameters for a one-parameter Dirichlet prior for a random choice structure.

Usage

```
prior_DCE_scalar_alpha(alpha, n_objects)
```

Arguments

alpha univariate parameter for the one-parameter Dirichlet prior.

n_objects number of objects in the universe.

Value

a matrix of Dirichlet parameters with the same dimensions as a count matrix for a universe of the same size.

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proportions

Random Choice Structure from count proportions

Description

proportions takes a count matrix as input, and returns choice proportions as a random choice structure.

Usage

```
proportions(N)
```

Arguments

Ν

A count matrix.

Value

A random choice structure.

Examples

```
PC_P = proportions(PC_counts[1,,])
```

RanCh

RanCh: A package for abstract discrete Random Choice

Description

The RanCh package provides data, graphical tools and inference tools for abstract discrete random choice analysis.

Data sets

NA

regularity 15

regularity

Check if random choice structure satisfies regularity

Description

regularity returns TRUE if the random choice structure P satisfies regularity and false otherwise.

Usage

```
regularity(P)
```

Arguments

Р

A random choice structure

Value

A logical value indicating whether P satisfies regularity.

Examples

```
P = create_P3(0.7, 0.6, 0.8, 0.6, 0.3, 0.1, names = c('x', 'y', 'z'))
regularity(P)
```

regularity_X3

Compute a cross section of the regularity region

Description

regularity_X3 computes the region (a triangle or the empty set) of ternary probabilities consistent with given binary probabilities and the regularity condition.

Usage

```
regularity_X3(P)
```

Arguments

Ρ

A random choice structure.

Value

If the region is empty, the output is NULL. Otherwise, a 3x3 matrix where each row gives one of the three vertices in barycentric coordinates.

Examples

```
 P = create_{P3}(0.7,\ 0.6,\ 0.8,\ 0.6,\ 0.3,\ 0.1,\ names = c('x',\ 'y',\ 'z')) \\ reg\_region = regularity_{L}X3(P)
```

similarity_2_3

set_index

Compute set index

Description

set_index takes a vector of object indices and constructs a set index, which is an index for the set of objects whose indices appear in the given vector. Each digit (or bit) in the binary representation of the resulting set index is an inclusion indicator: object i is in the set if and only if the i'th digit from the right is 1. For example, the set with objects 1, 3, and 4 has index equal to binary 1101, or decimal 13. The set with elements 1, 3 and 4 can be specified as the input vector c(1,3,4) or any permutation thereof, such as c(3,4,1).

Usage

```
set_index(v)
```

Arguments

٧

vector of object indices, in any order

Details

Note that the singleton set with object i is represented as 2^(i-1). The bitwise "or" (bitwAnd in the package bitops) of the set indices of two sets gives the set index of the union; the bitwise "and", the intersection.

Value

a integer index corresponding to the set of objects whose indices are in v

Examples

```
A = set_index(1,3,4) \# Returns (decimal) 13, equal to binary 1101.
```

similarity_2_3

Check if binary-ternary choice probabilities are in similarity effect region

Description

similarity_2_3 returns TRUE if the specified binary and ternary choice probabilities in random choice structure P are in the specified similarity effect region.

Usage

```
similarity_2_3(P, target, competitor, decoy, weak = TRUE,
  two_sided = FALSE)
```

similarity_X3

Arguments

P A random choice structure
target Index of target object
competitor Index of competitor object
decoy Index of decoy object

weak Logical, whether similarity effect is weak or not

Value

A logical value indicating whether the appropriate choice probabilities are in the similarity effect region.

Examples

```
P = create_P3(0.7, 0.6, 0.8, 0.6, 0.3, 0.1, names = c('x', 'y', 'z')) \\ similarity_2_3(P, target=1, competitor=2, decoy=3)
```

similarity_X3

Similarity effect regions

Description

similarity_X3 constructs six regions (all polygons) associated with binary-ternary similary effects. Below, x and y are "similar" choice objects and object z is dissimilar to both x and y. The interior of each polygon gives the set of ternary choice probabilities consistent with (1) the two specified binary choice probabilities and (2) one of six similarity effect conditions.

Usage

```
similarity_X3(pxz, pyz)
```

Arguments

```
pxz scalar, probability of choosing y when presented with choice set \{x, z\}
pyz scalar, probability of choosing y when presented with choice set \{y, z\}
```

Value

named list of six polygons in a barycentric coordinate system. Each polygon is a matrix, with one row for each polygon vertex and one column for each of the three choice objects x, y and z. Element i,j gives the probability of choosing j, when presented with choice set $\{x, y, z\}$, at the i'th polygon vertex. The six polygons—triangles except for Sxy, a quadrilateral—are:

Sxyz region where there is a similarity effect with object x as target, y as decoy and z as competitor Syxz region where there is a similarity effect with object x as target, y as decoy and z as competitor So region where there is neither similarity effect

```
Sx region with only the x effect
Sy region with only the y effect
Sxy region with both effects
```

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See Also

compromise_X3 for an analogous function for the compromise effect.

Examples

```
S = similarity_X3(0.5, 0.6)
```

YG_counts

Choice counts in YouGov experiment

Description

A four dimensional array, 16 by 2 by 15 by 4, of count data. Element h,i,j,k gives the number of subjects who chose object k when presented with choice set j of domain h, in their i'th block of 16 trials. The choice set index j=1,...,15 encodes a non-empty subset of the universe of the four choice objects a, b, c, and d, numbered 1, 2, 3, 4. Each digit (or bit) in the binary representation of j is an inclusion indicator: object k is in the set if and only if the k'th digit from the right is 1. For example, the set with b, c, and d (but not a) is encoded as binary 1110 (decimal 14) Whenever k is not an element of j, the value is NA.

Usage

YG_counts

Format

An object of class array of dimension 16 x 2 x 15 x 4.

YG_demographics

Demographic information for subjects

Description

Demographic information for subjects

Usage

YG_demographics

Format

A data frame with demographic information on subjects

```
sex Sex of subject
educ Educational attainment by subject
region Region of subject's residence in US
race Race of subject
age_range Age range of subject
```

YG_raw 19

YG_raw

YouGov Experiment data

Description

Raw trial-by-trial data from YouGov experiment

Usage

YG_raw

Format

```
A data frame with 17 variables:
```

design

card

domain

combo

perm

choiceset Choice set as a character string

option_1 Object presented in first position: 1, 2, 3 or 4

option_2 Object presented in second position

option_3 Object presented in third position

option_4 Object presented in fourth position

response Object chosen: 1, 2, 3 or 4

order

gender Sex of respondant: 1 for male, 2 for female

educ Education of respondant: 1 for No high school, 2 for High school graduate, 3 for Some college, 4 for 2-year college, 5 for 4-year college, 6 for post-graduate

region Region of respondant: 1 for northeast, 2 for midwest, 3 for south, 4 for west

race Race of respondant: 1 for White, 2 for Black, 3 for Hispanic, 4 for Asian, 5 for Native American, 6 for Mixed, 7 for Other, 8 for Middle Eastern

age_cross Age category of respondant: 1 for 18-34, 2 for 35-54, 3 for 55 and over

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YG_trials

Table of choice trials, population choice experiment

Description

Table of choice trials, population choice experiment

Usage

YG_trials

Format

A tibble with 17 variables

domain factor, name of choice domain

subject subject identifier

block block, equal to 1 or 2, identifying the first or second pass a subject makes through the domains.

trial trial identifier (gives the order in which a subject sees choice sets)

duration duration of trial in seconds

set factor, name of choice set presented: 'ab', 'bcd', etc., with objects in alphabetical order

choice factor, choice made by subject: 'a', 'b', 'c', or 'd'

set_perm factor, order of presentation of objects on screen, left to right

set_card Integer, cardinality of choice set (i.e. number of available options)

set_bin Binary representation of choice set (binary digits indicate object membership in choice set)

choice_int Integer code for chosen object: a=1, b=2, ..., d=4

ab, ac, ..., cd revealed preference indicator: taking column ab as an example, value is 1 if a is revealed preferred to b, -1 if b is revealed preferred to a, 0 otherwise.

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