

Nick McLough - 950337388 - Lab 7

CprE 281 QUIZ 5
ELECTRICAL AND COMPUTER
ENGINEERING
IOWA STATE UNIVERSITY

Initial Stuff and Basics
Assigned Date: Week 07

Instructions

Complete the question below to the best of your ability. Once complete, upload a PDF of your work to canvas.

Questions

P1. Number Conversion (3 x 20p each = 60p)

- Find the 32-bit floating point representation for the real number 42_{10} .
- Find the 32-bit floating point representation for the real number -9_{10} .
- Convert $10E90000_{16}$ (a 32-bit float stored in IEEE 754 format) to decimal.

P2. (40 points). Implement the following functions using Shannon's expansion:

- Implement $F(a,b,c) = a \cdot b + a \cdot \bar{c} + a \cdot b \cdot \bar{c}$ using only 2-to-1 MUXs
- Implement $F(a,b,c) = a \cdot b + a \cdot \bar{c} + a \cdot b \cdot \bar{c}$ using only 4-to-1 MUXs

P1) a) 42_{10}

$42/2 = 21$	0
$21/2 = 10$	1
$10/2 = 5$	0
$5/2 = 2$	1
$2/2 = 1$	0
	1

$42_{10} = 101010$

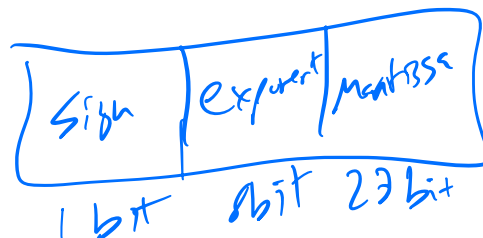
$\frac{101010}{5+127} \times 2^5$

$5+127 = 132$

$132/2 = 66$	0
$66/2 = 33$	0
$33/2 = 16$	1
$16/2 = 8$	0
$8/2 = 4$	0
$4/2 = 2$	0
	1

1000100_2

$01000100.01010 = 42_{10}$



- sign bit

$$\begin{array}{r} 9/2 = 4 \quad 1 \\ 4/2 = 2 \quad 0 \\ 2/2 = 1 \quad 0 \\ \hline 1 \end{array}$$

$$\begin{aligned} & \rightarrow 1001_2 \\ & = \underline{1.001} = 1.001 \times 2^3 \\ & \quad \quad \quad \text{3 decimal places} \end{aligned}$$

$$\underline{3 + 127 = 130}$$

$3 + 127 = 130$
 $1000010_2 =$
 $130/2 = 65 \quad 0$
 $65/2 = 32 \quad 1$
 $32/2 = 16 \quad 0$
 $16/2 = 8 \quad 0$
 $8/2 = 4 \quad 0$
 $4/2 = 2 \quad 0$
 $2/2 = 1 \quad 0$

1	1000010	001000000000000000000000 = -9 ₁₀
sign	exponent	mantissa

p1) C) $10E90600_{16}$ stored in IEEE 754 to decimal.

$$E = 14$$

$$\begin{array}{r} 14/2 = 7 \quad 0 \\ 7/2 = 3 \quad 1 \\ 3/2 = 1 \quad 1 \end{array}$$

1110₂

$$9 = 1001$$

$1 = 0001$

$$0 = 0000$$

sign	exponent				mantissa								
0	0	0	1	0000	1110	1	001	0000	0000	0000	0000	0000	2
↓				↓	↓	↓	↓	↓	↓	↓	↓	↓	
1				0	E	1	0	0	0	0	0	0	

positive

$$001\ 00001_2 =$$

$$2^0 \times 1 = 1$$

$$2^5 \times 1 = 32 + 1 = \underline{33}$$

$$\text{exponent} = 33_{10}$$

$$33 - 127 = -94$$

$$M = 0.1101001\ 0000\ 0000\ 0000\ 0000$$

$$\hookrightarrow 2^{-1} + 2^{-2} + 2^{-4} + 2^{-7}$$

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{16} + \frac{1}{128} = 0.8203125$$

$$-1(1 + 0.8203125) \times 2^{-94}$$

$$= -1.8203125 \times 2^{-94}$$

in decimal

P2) a)

$$a.b + a.\bar{c} + a.b.\bar{c}$$

2 to 1 MUXs

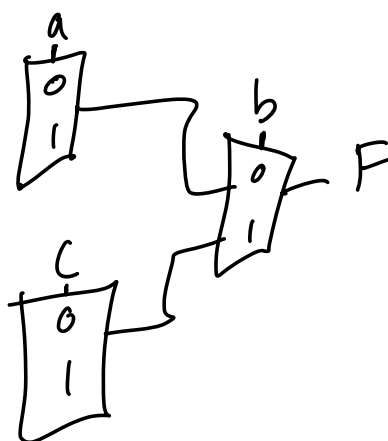
b)

$$a.b + a.\bar{c} + a.b.\bar{c}$$

4 to 1 MUXs

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

$$= A\bar{B}\bar{C} + AB\bar{C} + ABC$$



b)

