

CHEM 571A - Problem Set #3

Due Friday September 7th

1. *McQuarrie 4-11*: Evaluate the commutator $[\hat{A}, \hat{B}]$, where \hat{A} and \hat{B} are given below

\hat{A}	\hat{B}
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(a) $\frac{d^2}{dx^2}$	x
(b) $\frac{d}{dx} - x$	$\frac{d}{dx} + x$
(c) $\int_0^x dx$	$\frac{d}{dx}$
(d) $\frac{d^2}{dx^2} - x$	$\frac{d^2}{dx^2} + x^2$

2. *McQuarrie 5-14*: The force constant of $^{35}\text{C}^{35}\text{Cl}$ is $319 \text{ N} \cdot \text{m}^{-1}$. Calculate the fundamental vibrational frequency and the zero-point energy of $^{35}\text{C}^{35}\text{Cl}$ (in the harmonic approximation).
3. *McQuarrie 5-19*: The vibrational term of a diatomic molecule is given to good approximation by

$$G(\nu) = \left(\nu + \frac{1}{2}\right) \tilde{\omega}_e - \left(\nu + \frac{1}{2}\right)^2 \tilde{x}_e \tilde{\omega}_e$$

where ν is the vibrational quantum number. Show that the spacing between adjacent levels ΔG is given by

$$\Delta G = \tilde{\omega}_e \{1 - 2\tilde{x}_e(\nu + 1)\}$$

Also show that the maximum vibrational quantum number is given by

$$\nu_{\max} = \frac{1}{2\tilde{x}_e} - 1$$

Use the above result to compute the dissociation energy, D_e , of the molecule.'

4. *McQuarrie 5-22*: Show that $\psi_0(x)$ and $\psi_1(x)$ for the harmonic oscillator are orthogonal.