

Title: Four plots for SVMs

The general form of the mathematics for a linear support vector machine are quite straightforward.

Support Vector Machines are Supervised tools.

SEE: https://rpubs.com/mzc/mlwr_svm_concrete (https://rpubs.com/mzc/mlwr_svm_concrete)

Therefore, given a set of labeled pairs of data:

$$(x_i, y_i), \quad i = 1, \dots, l \quad \text{where} \quad x_i \in R^n \quad \text{and} \quad y \in \{1, -1\}^l$$

$$\text{Such that } f(x_i) = \begin{cases} \geq 0; & y_i = 1 \\ < 0; & y_i = -1 \end{cases}$$

where y is a set of two values which indicate a label, e.g. true or false.

$$\min \frac{1}{2} W^T W + C \sum_{i=1}^l \xi_i$$

$$\text{subject to } y_i(w^T \phi(x_i) + b) \geq (1 - \xi_i) \text{ where } \xi_i \geq 0,$$

C is the penalty parameter, cost, of the error term, such that $C > 0$.

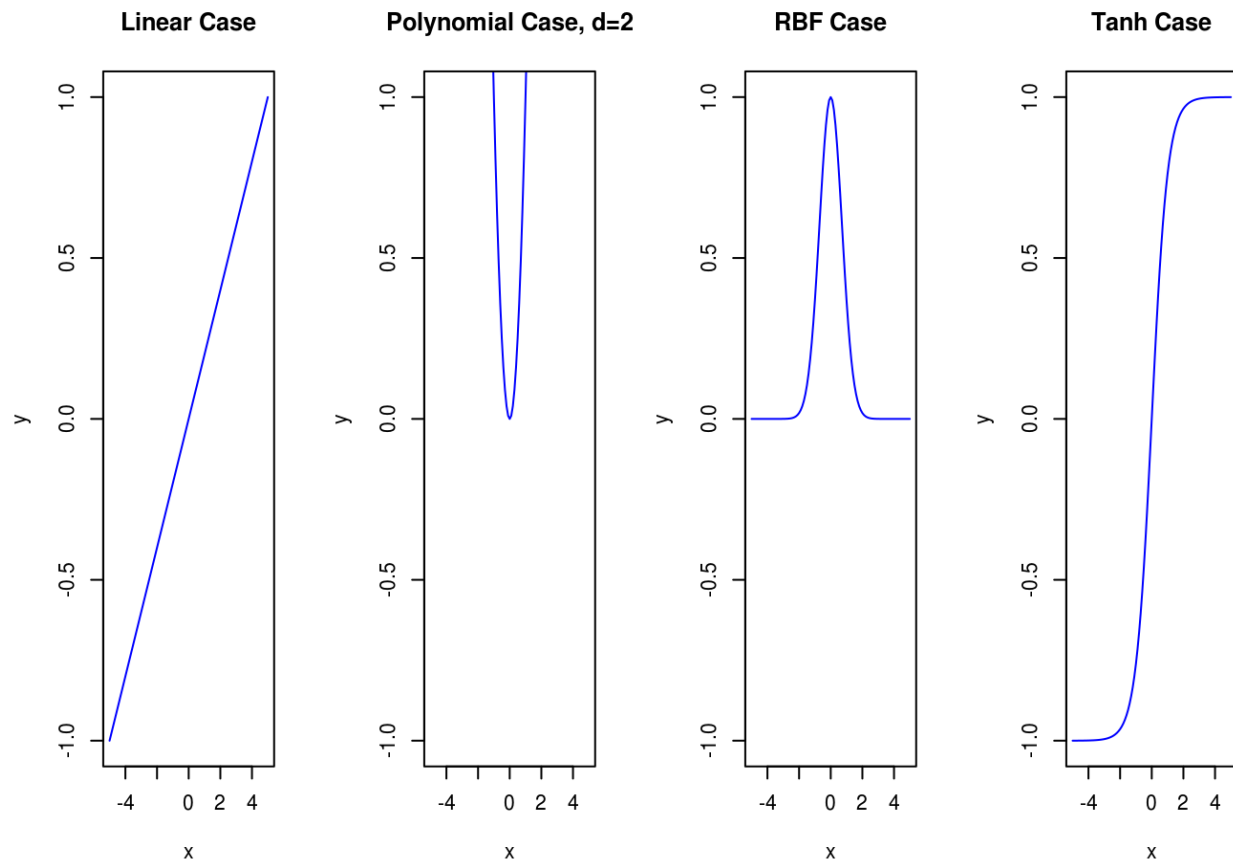
Furthermore, $K(x_i, x_j) \equiv \phi(x_i)^T \phi(x_j)$ is called the kernel function.

The 4 most common SVM formulae are:

1. Linear: $K(x_i, x_j) = \langle x_i, x_j \rangle$
 - The linear kernel does not transform the data at all.
 2. Polynomial: $K(x_i, x_j) = (\gamma x_i^T x_j + r)^d, \gamma > 0$
 - The polynomial kernel has a simple non-linear transform of the data.
 3. Radial Basis Function (RBF): $K(x_i, x_j) = \exp(-\gamma \|x_i^T - x_j\|^2), \gamma > 0$
 - The Gaussian RBF kernel which performs well on many data and is a good default
 4. Sigmoid: $K(x_i, x_j) = \tanh(\gamma x_i^T x_j + r), \gamma > 0$
 - The sigmoid kernel produces a SVM analagous to the activation function similar to a perceptron (<https://cs.stanford.edu/people/eroberts/courses/soco/projects/neural-networks/Neuron/index.html>) with a sigmoid activation function.¹
- Such that γ, r and d are kernel parameters.

There are no reliable rules for which kernel to use with any given data set.

Plots for 4 most common SVM formulae:



EOF

1. https://rpubs.com/mzc/mlwr_svm_concrete (https://rpubs.com/mzc/mlwr_svm_concrete)↵