

# CT255 Assignment 1

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## Problem 1

Study the code and summarize its functionality (bullet points will do), thereby referencing important lines of source code.

### Main function:

Accepts an argument *arg*, 1 to 64 characters long (**L12, L14**). This argument is sent to the hash function **hashF1()** (**L13**).

The function prints the input and resulting hash (**L18**), then starts searching for hash collisions.

### hashF1() function:

Takes a string input *s*.

Checks whether the string has the required length (**L36**).

The function then creates a 64 bit string out of the input, adding filler alphabetical characters if necessary. (**L40-41**).

Meanwhile, a 4-digit array *hashA* has been created. (**L30**).

The string is iterated through and *hashA* is populated by multiplying the current character's ASCII value (*byPos*) by different numbers:

```
hashA[0] += (byPos * 17); // Note: A += B means A = A + B
hashA[1] += (byPos * 31);
hashA[2] += (byPos * 101);
hashA[3] += (byPos * 79);
```

Next, each digit of *hashA* is replaced with itself modulo 255 (**L51-54**).

Finally, each digit of *hashA* is multiplied by  $(256 \wedge \text{digit position})$ . These numbers are added together to form the hash. If the hash is negative, it is multiplied by -1. This value is then returned.

## Problem 2

Consider the input "Bamb0" (i.e. "Bamb" followed by a zero). The resulting hash value is 1079524045. Enhance the code to search for "Bamb0" hash collisions (i.e., different inputs that create the same hash value → weak collision resistance) via a brute-force search. What collision(s) can you find?

I wrote the following **findMatches()** function to perform this task:

```
private static void findMatches(int stringLength){
    // initialise variables

    char[] randomString =new char[stringLength];
    int matchCounter =0;

    // make 999999 attempts at finding a match

    for (int i=0; i < 999999; i++) {

        // populate the random string

        for (int j = 0; j < stringLength; j++) {
            Random rnd =new Random();

            String alphabet =!"#$%&\\'()*+,-./0123456789:;<=>?
@ABCDEFGHIJKLMNopQRSTUVWXYZ[\\]\\^_`abcdefghijklmnopqrstuvwxyz{|}~?;/.,"

            char c = alphabet.charAt(rnd.nextInt(alphabet.length())); pick
a random character from the alphabet
            randomString[j] = c;

        }

        int result = hashF1(String.valueOf(randomString));

        // check if the generated hash matches our desired hash

        if (result ==1079524045) {
            /* System.out.println(String.format("%s",
String.valueOf(randomString))); // print out string (optional)*/
            matchCounter ++;
        }

    }

    System.out.println(String.format("Number of matches of length %d found:
%d", stringLength, matchCounter));
}
```

```

Assignment 2 CT255_HashFunction1 hashF1
CT255_HashFunction1.java
Run CT255_HashFunction1
I':Dt8kA)4\B:z'9pM44jR
Td+ej*89#A7E5M3wS93E_6~
XPhUS\hD}CY%p1[D-oL'r/'
TsQP+_ts\(\Xj{{1T,C:7}*a
(15snz^oB)Uj`1RTu%W;G>\
o,v~JbH?AQ6P#(v%a#C/,Y4
O\0,6LL3{t!v}UbvFI6<F8
BwNFQFXc?Gv8^nDu5\+^Fc8
_rYKn<)#7n\};D)h/:_XC
g`ky:[V%g0d/bZrFAk9n/G,
u<w;?PW?8^6XnI>y|>*Phe
,36(r\..?8\42(EMuIBq#cNL
pXl80\,-:la\8Zh@u.*Kin\N
?:[ozo,=+UEX{eqW+_0?}#D
JF.@o=r./6W-;A{63r&13bi
Z>d3qoNEq{.$y!5]T}^I51L
DZG=LnFv)mZ\9kQc]SUESFD
\6ZL=pGB6=~| (PM9~4Nr9zP
)+2sMwYL30x#|d\~Th+5q_I
I'+(xL"f\?x8'$.Un^TUcC
BnW7X2+gXY$F30yiSzc^x,
H4iH??!Jh={j^?pkL.mMdo/
,;e'_h%K/>)~\akrzn[,Y+p
0.<4!?!/?T*%\g^0g'.+]R=
!KbVLR~--dD)I(_7.,2S3)e6
~2\fn&w)+$wvI\=|I)n\DLT
Number of matches of length 23 found: 3754

Process finished with exit code 0

```

```

Assignment 2 CT255_HashFunction1 findMatches
CT255_HashFunction1.java
Run CT255_HashFunction1
"C:\Program Files\Java\jdk-19\bin\java.exe" *-ja
Input = Banb0 : Hash = 1079524045
Start searching for collisions
Number of matches of length 0 found: 0
Number of matches of length 1 found: 0
Number of matches of length 2 found: 4525
Number of matches of length 3 found: 5441
Number of matches of length 4 found: 5924
Number of matches of length 5 found: 6075
Number of matches of length 6 found: 5791
Number of matches of length 7 found: 5486
Number of matches of length 8 found: 4930
Number of matches of length 9 found: 4917
Number of matches of length 10 found: 4598
Number of matches of length 11 found: 4492
Number of matches of length 12 found: 4326
Number of matches of length 13 found: 4018
Number of matches of length 14 found: 3926
Number of matches of length 15 found: 3913
Number of matches of length 16 found: 3678
Number of matches of length 17 found: 3859
Number of matches of length 18 found: 3774
Number of matches of length 19 found: 3885
Number of matches of length 20 found: 3826
Number of matches of length 21 found: 3922
Number of matches of length 22 found: 3906
Number of matches of length 23 found: 3931

Process finished with exit code 0

```

## Problem 3

Enhance the code in `hashF1()` to make it more robust, i.e., to reduce the risk of hash collisions. Explain your answer via comments in your code.

To further secure **hashF1()**, I added the following code before the modulo operations:

```
hashA[0] = extraEncryption(hashA[0]);
hashA[0] = extraEncryption(hashA[1]);
hashA[0] = extraEncryption(hashA[2]);
hashA[0] = extraEncryption(hashA[3]);
```

This calls my **extraEncryption()** function:

```
private static int extraEncryption(int x) {
    // perform 5 bit left shift on the number then subtract the original to
    get multiplication by 31
    // similar to Java's own String.hashCode() function
    return ( x << 5 - (x));
}
```

which simply performs a 5-bit bitwise left shift on the operand then subtracts the original operand from the result.

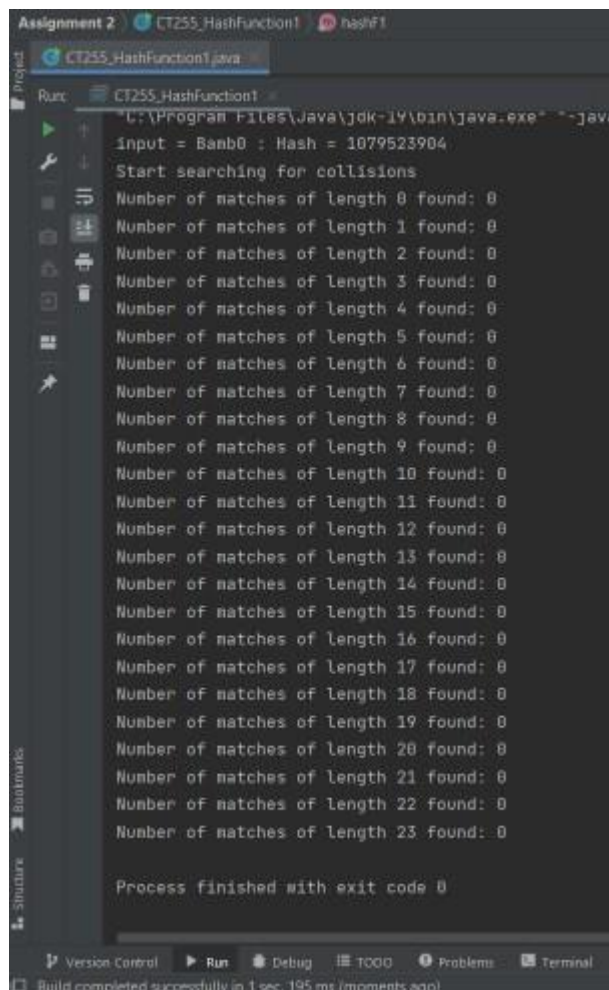
I chose this particular operation because it results in the multiplication of the operand by 31. Java's own **String.hashCode()** function

$$s[0]*31^{(n-1)} + s[1]*31^{(n-2)} + \dots + s[n-1]$$

performs a similar multiplication.

Various reasons behind this multiplication by 31 have been proposed, some due to performance and some due to convenience.

However, in 1997, Goodrich and Tamassia computed that creating a hash code using a cyclic shift of 31, 33, 37, 39, or 41 bits produced fewer than 7 hash collisions when generating hashes from over 50,000 English words. [*Data Structures and Algorithms in Java*, 9.2.3]



```
Assignment 2 [CT255_HashFunction1] hashF1
CT255_HashFunction1.java
Run CT255_HashFunction1
C:\Program Files\Java\jdk-14\bin\java.exe -j...
Input = Bamb0 : Hash = 1079523904
Start searching for collisions
Number of matches of length 0 found: 0
Number of matches of length 1 found: 0
Number of matches of length 2 found: 0
Number of matches of length 3 found: 0
Number of matches of length 4 found: 0
Number of matches of length 5 found: 0
Number of matches of length 6 found: 0
Number of matches of length 7 found: 0
Number of matches of length 8 found: 0
Number of matches of length 9 found: 0
Number of matches of length 10 found: 0
Number of matches of length 11 found: 0
Number of matches of length 12 found: 0
Number of matches of length 13 found: 0
Number of matches of length 14 found: 0
Number of matches of length 15 found: 0
Number of matches of length 16 found: 0
Number of matches of length 17 found: 0
Number of matches of length 18 found: 0
Number of matches of length 19 found: 0
Number of matches of length 20 found: 0
Number of matches of length 21 found: 0
Number of matches of length 22 found: 0
Number of matches of length 23 found: 0

Process finished with exit code 0
Build completed successfully in 1 sec, 195 ms (moments ago)
```

My testing shows that applying the **extraEncryption()** function results in a significantly lower number of hash collisions, therefore I am satisfied that it achieves the desired result.