Homework #1

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Information Theory

Problem 2.3): Let $\mathbb{P}^n$ be the set of all n-dimensional probability vectors. Futhermore, let $\vec{p}$ be any element of $\mathbb{P}^n$ ($\vec{p} \in \mathbb{P}^n$) and define $\vec{p}$ as $\vec{p} = (p_1, p_2, \ldots, p_i, \ldots, p_n)$, where $i \in \mathbb{Z}^+ \ni i \leq n$. By the definition of a probability space, we must have

$$\vec{p} \cdot \vec{1} = \sum_{i=1}^{n} \{p_i\} = 1 \, , \ \ \forall \vec{p} \in \mathbb{P}^n,$$

where $\vec{1} = (1, 1, \ldots, 1, \ldots, 1)$ is the n-dimensional vector having the value 1 for each of its components. It is clear that, $p_i \log_2 [p_i] \geq 0$ hold $\forall i \in \mathbb{Z}^+ \ni i \leq n$. Moreover, it is also clear that $p_i \log_2 [p_i] = 0$ only for the case where $p_i = 0$ or $p_i = 1$.