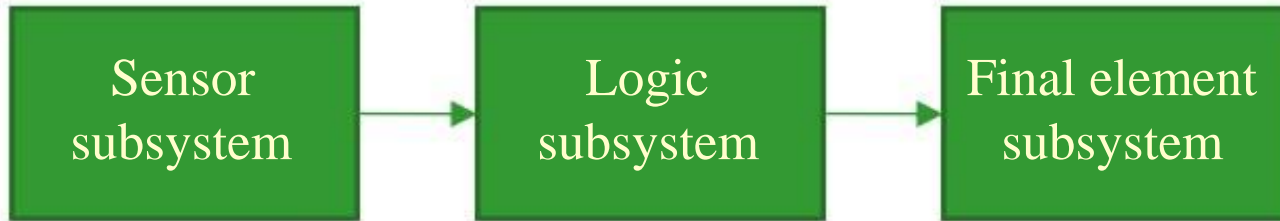


# Redundancy Analysis

Alan Harding



# Sub-system structure



## Sensor subsystem components

- Sensors
- Barriers
- Input conditioning circuits
- etc.

## Final element components

- Actuators
- Barriers
- Output conditioning circuits
- etc.

## Logic subsystem components

- Processors
- Computers
- Scanning devices
- etc.

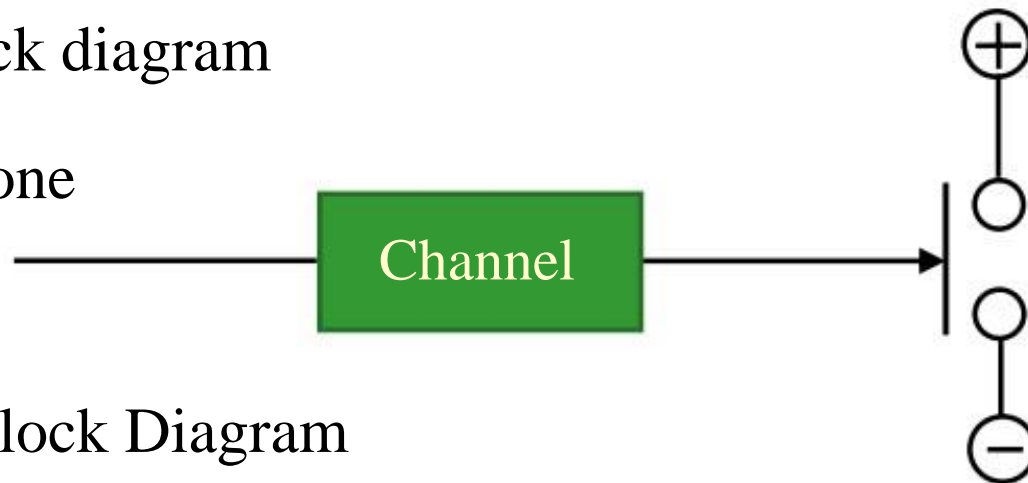


# 1001 System (fault tolerance=0)

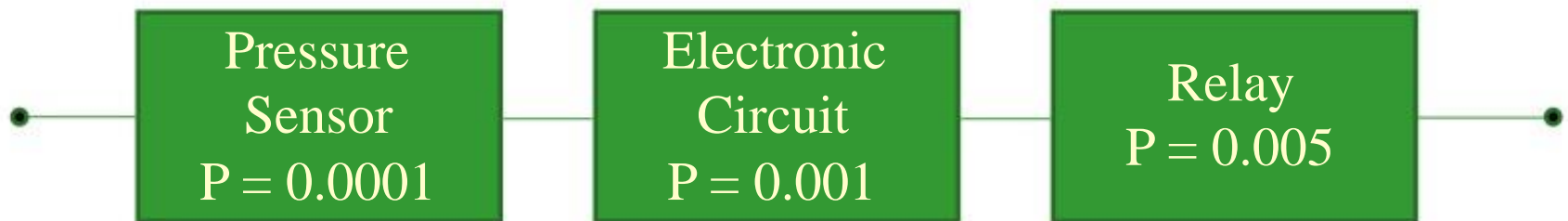
- A single channel where any dangerous failure leads to a failure of the safety function when a demand arises

- Physical block diagram

One-out-of-one



- Reliability Block Diagram



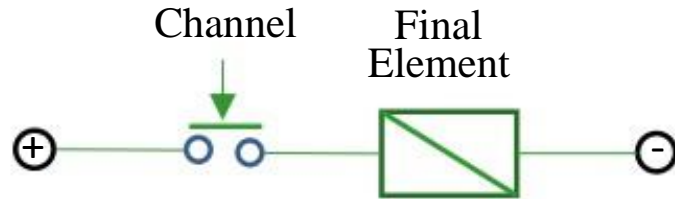
(P = Probability of dangerous failure)



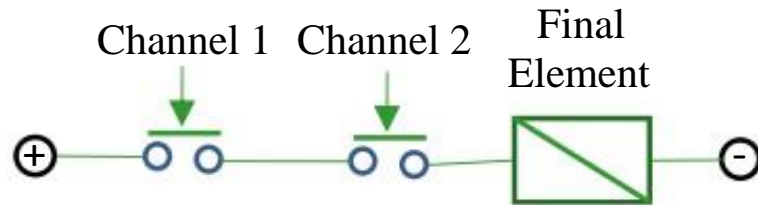
# Voting Techniques

Each subsystem can be represented as one or more following voting groups

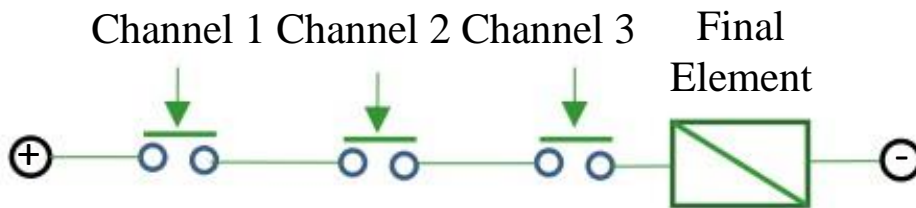
1001 system



1002 system

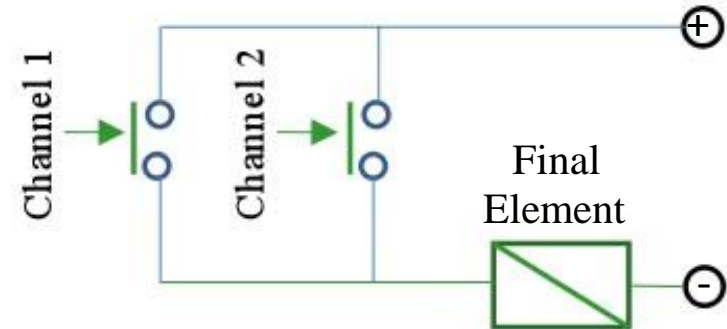


1003 system

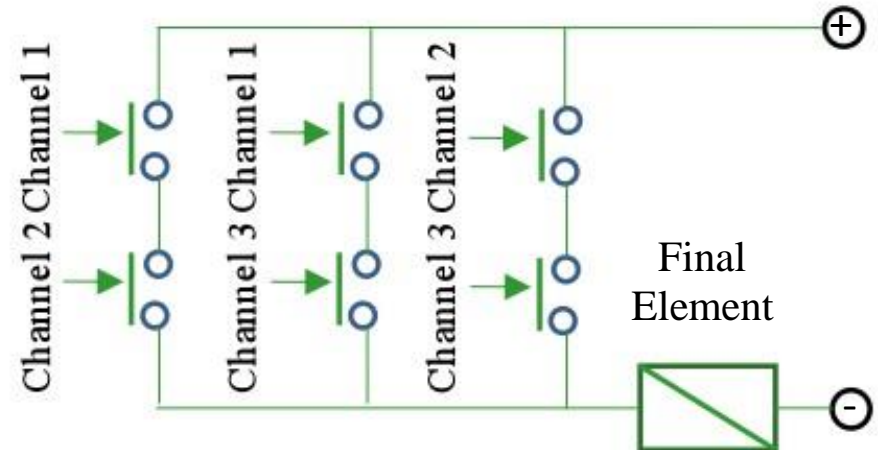


**If one channel asks off → output off**

2002 system



2003 system



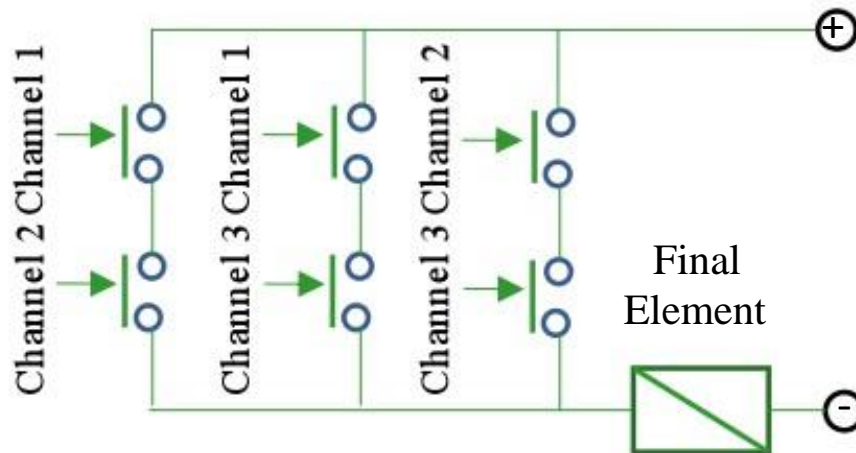
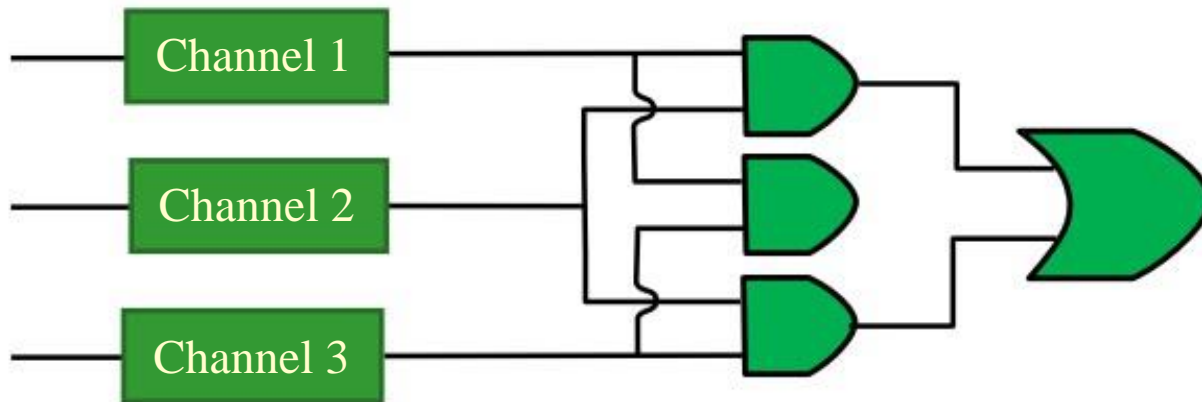
**If two channels asks off → output off**



# 2003 = two channels out of three must vote

The logic gate solution below gives one as the output for ones on two out of three channels .

It also gives zero for the output if two channels ask for zero.



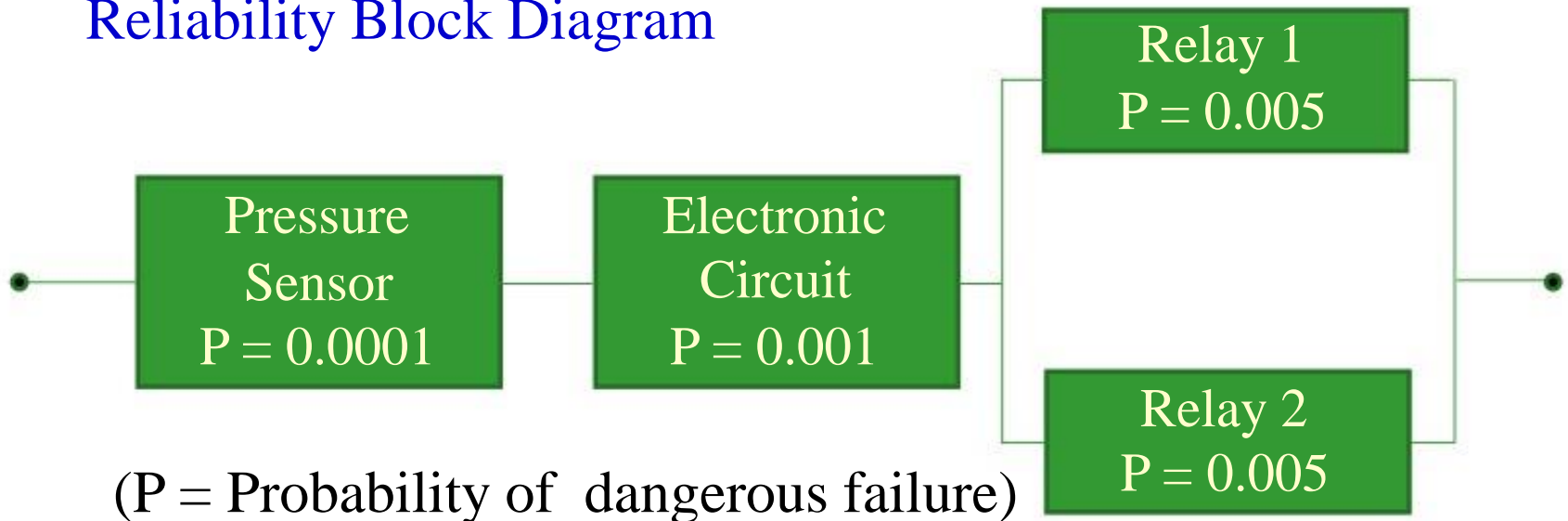
# Component redundancy

## Physical block diagram

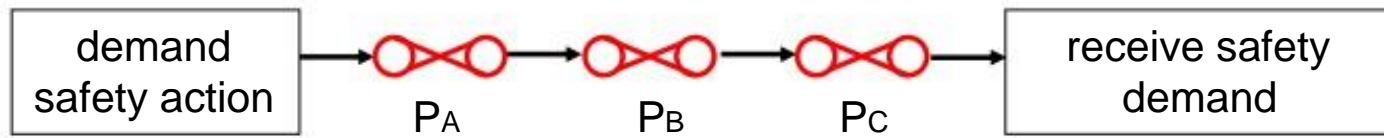
One-out-of-one



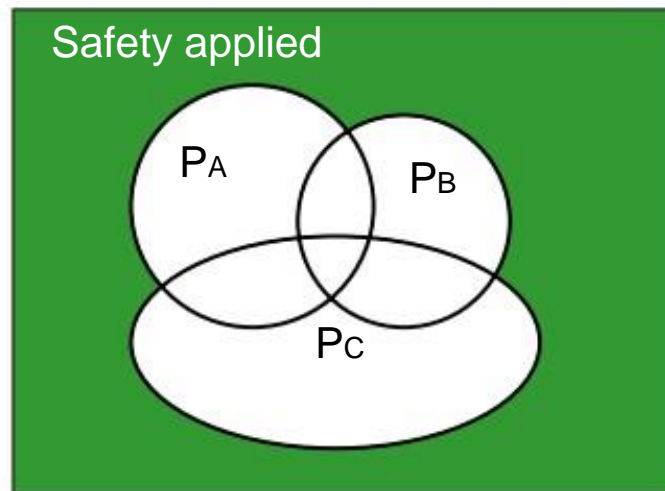
## Reliability Block Diagram



# Series Faults



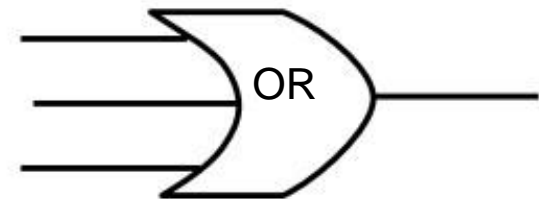
$P_x$  represents  
probability of failure



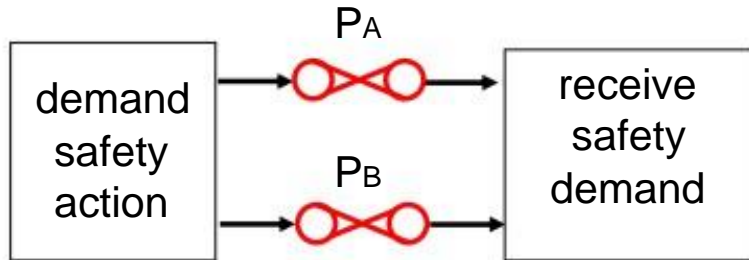
Full box represents  
signal sent

$$\text{Probability of Failure} = P_A + P_B + P_C - P_A.P_B - P_A.P_C - P_B.P_C + 2P_A.P_B.P_C$$

$$\text{Worst Case Probability of Failure} = P_A + P_B + P_C$$

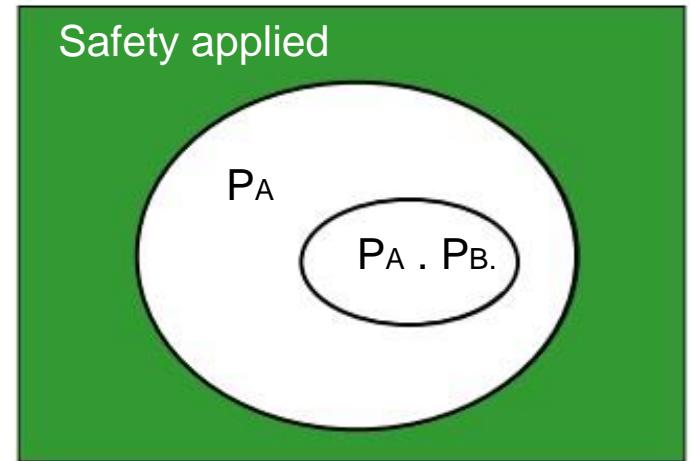


# Parallel Redundancy Faults



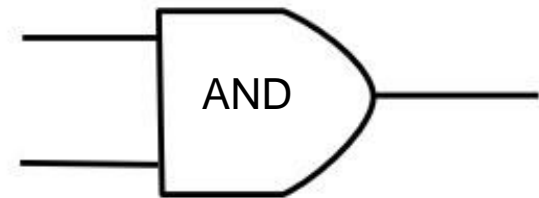
$P_x$  represents probability of failure

We now worry if B fails once A has failed



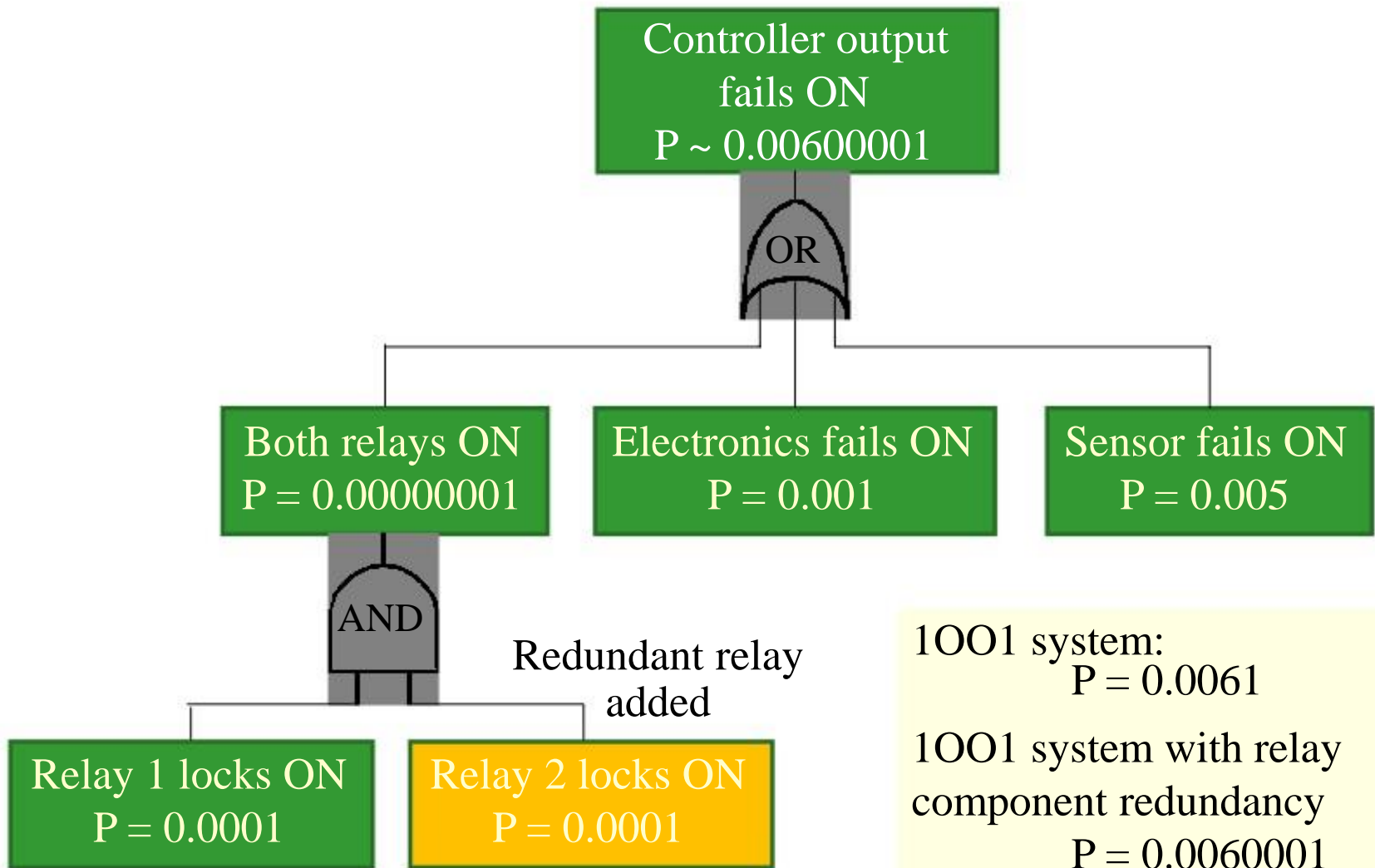
Full box represents signal sent

$$\text{Probability of Failure} = P_A . P_B = P_B . P_A$$





# Fault tree analysis of 1001 system



1001 system:  
 $P = 0.0061$

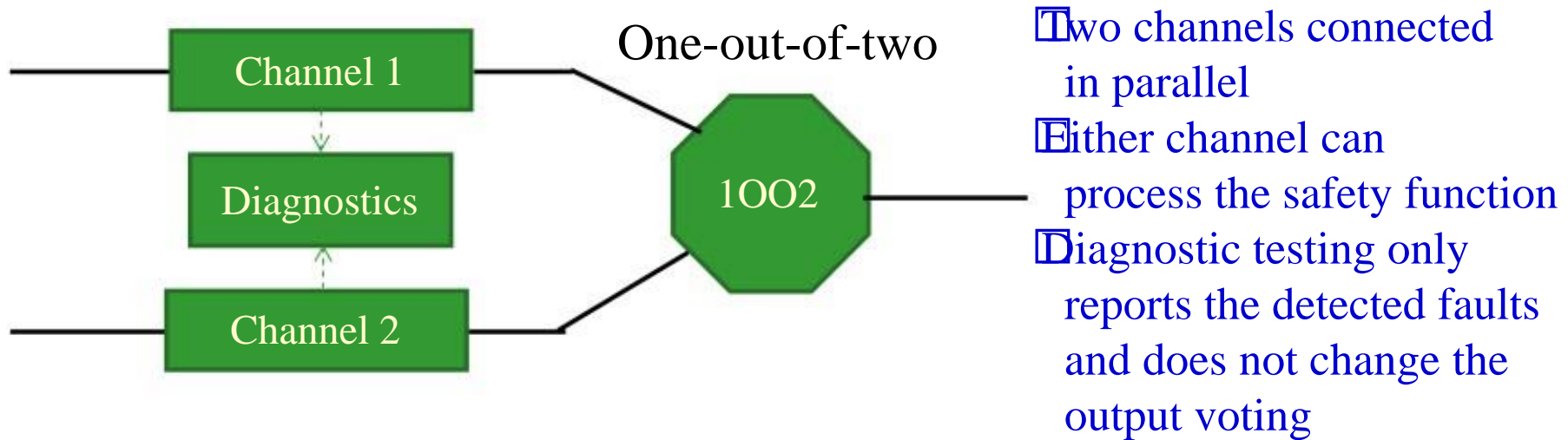
1001 system with relay  
component redundancy  
 $P = 0.0060001$

Only minor improvement

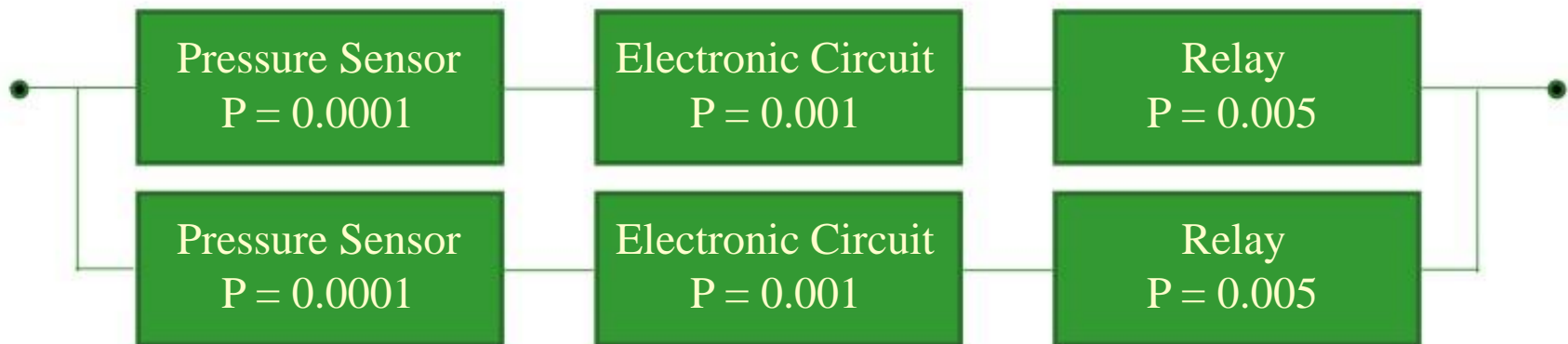


# 1002 redundant system

- Physical block diagram

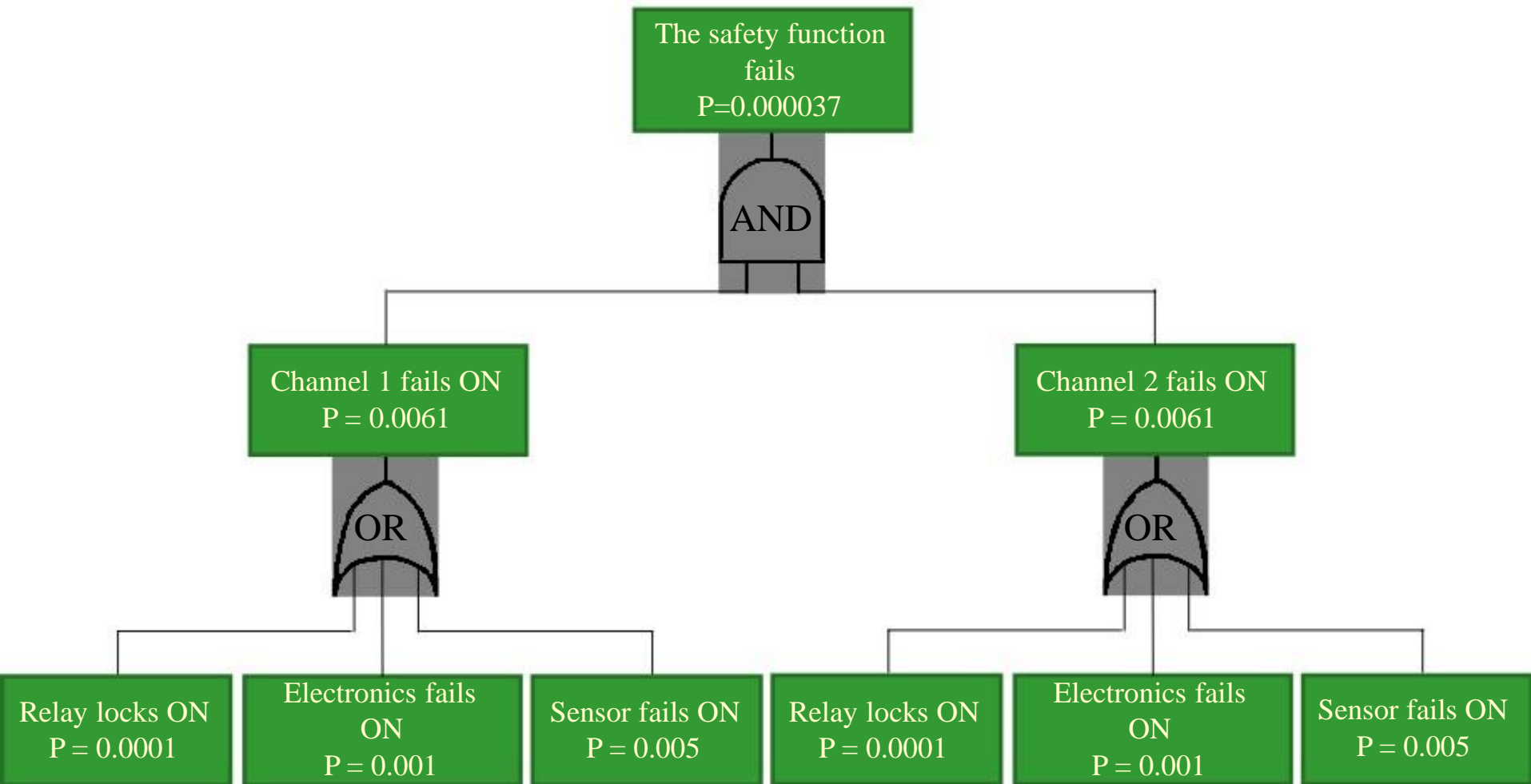


- Reliability Block Diagram



(P = Probability of dangerous failure)

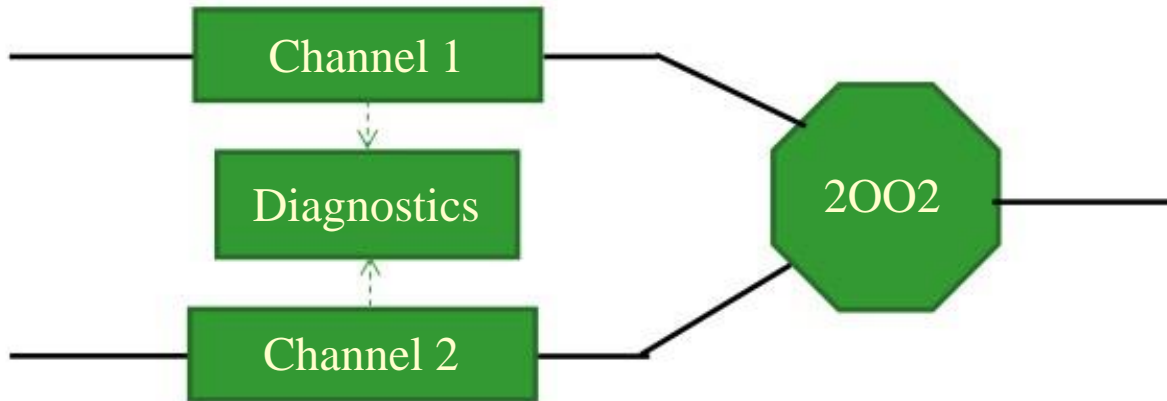
# Fault tree analysis of 1OO2 redundant system



Great improvement in 1OO2 redundant control system

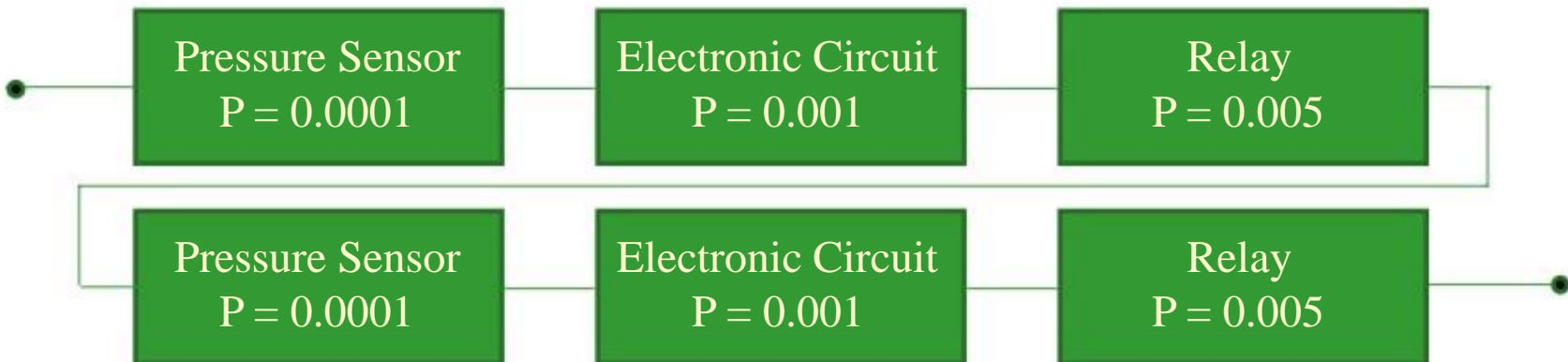
# 2002 redundant system

- Physical block diagram



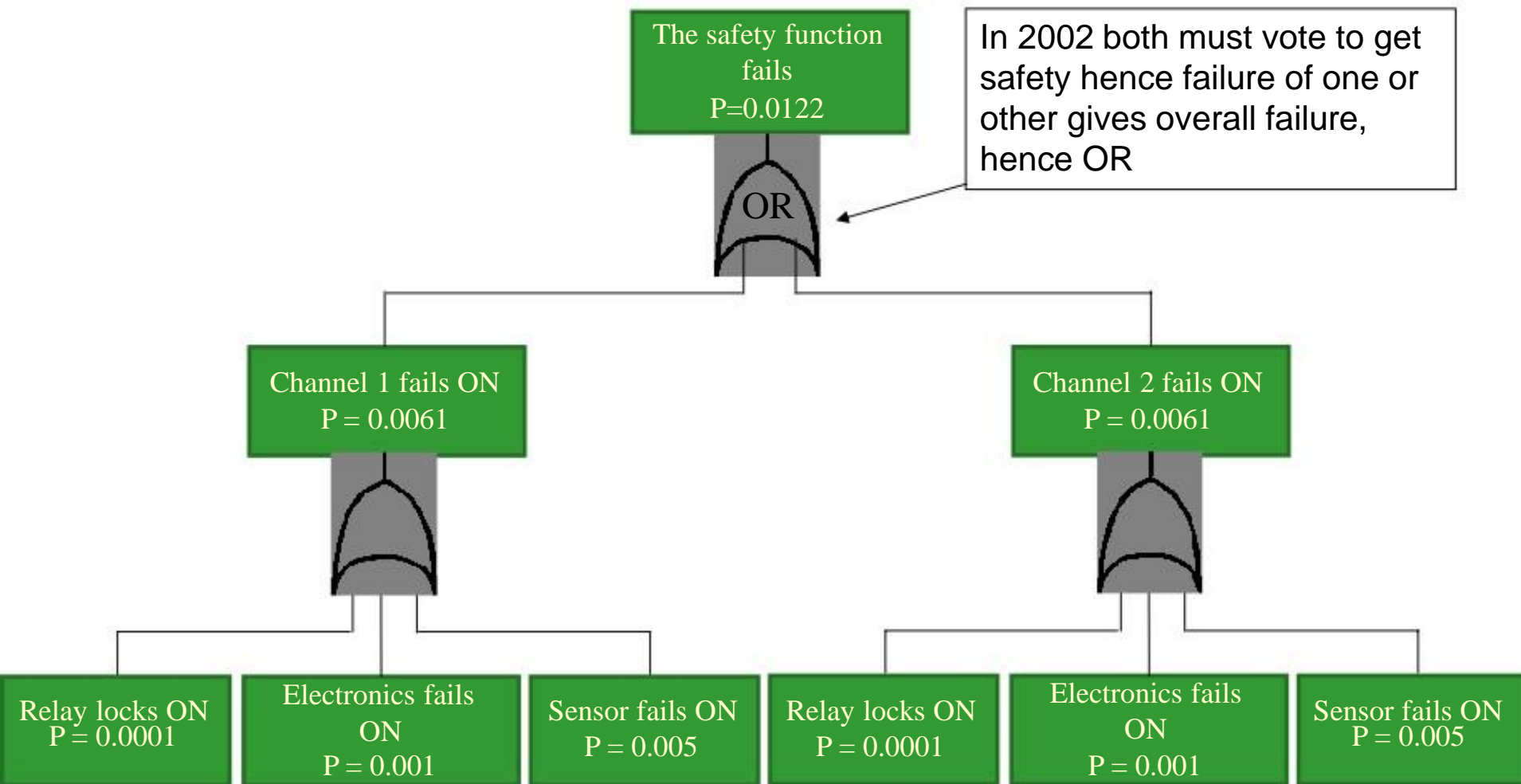
- Two channels connected in parallel
- Both channels need to demand the safety function before it can take place
- Diagnostic testing only reports the detected faults and does not change the output voting

- Reliability Block Diagram



(P = Probability of dangerous failure)

# Fault tree analysis of 2002 redundant system

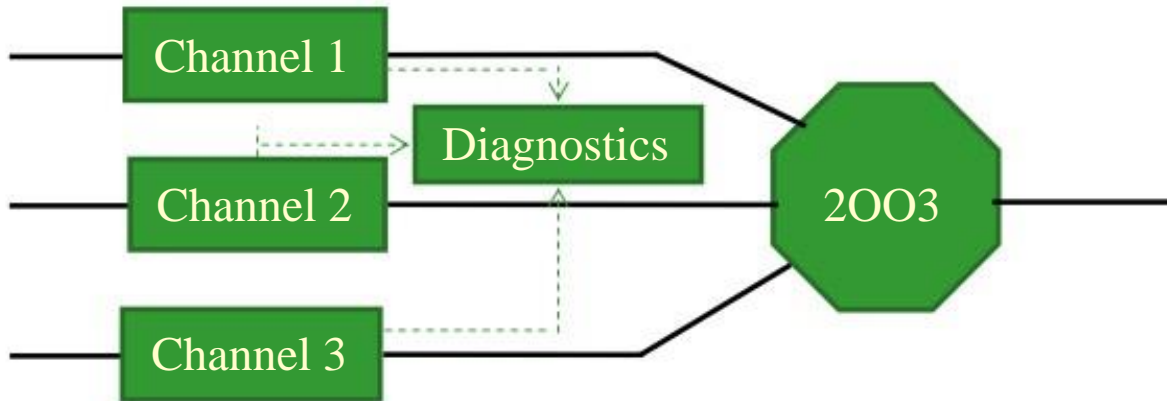


Poor safety performance in 2002 redundant control system



# 2003 redundant system

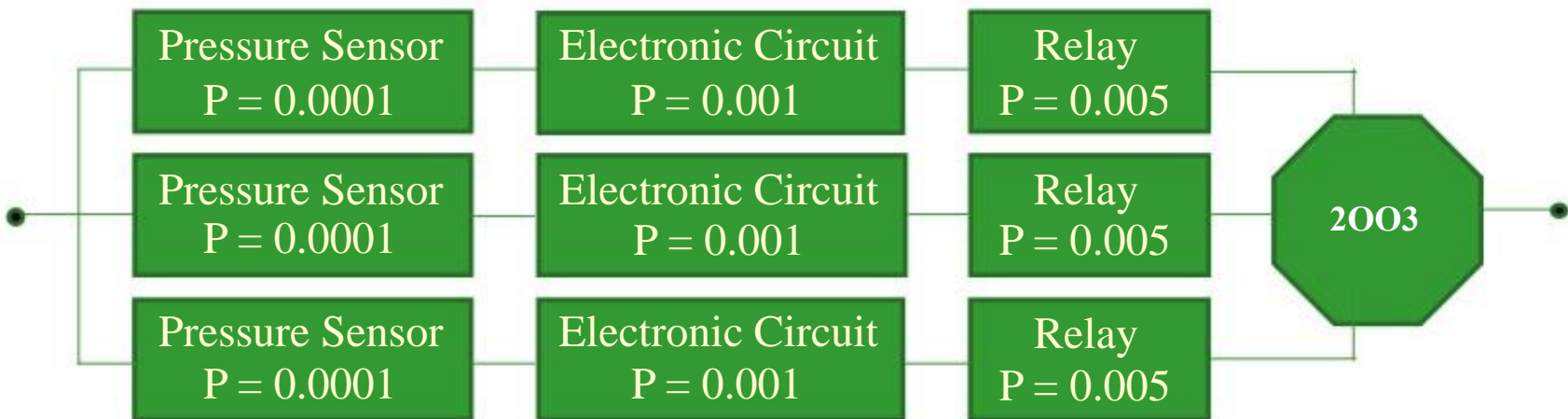
- Physical block diagram



Three channels connected in parallel with a majority voting arrangement for the output signals

The output state is not changed if only one channel gives a different result which disagrees with the other two channels

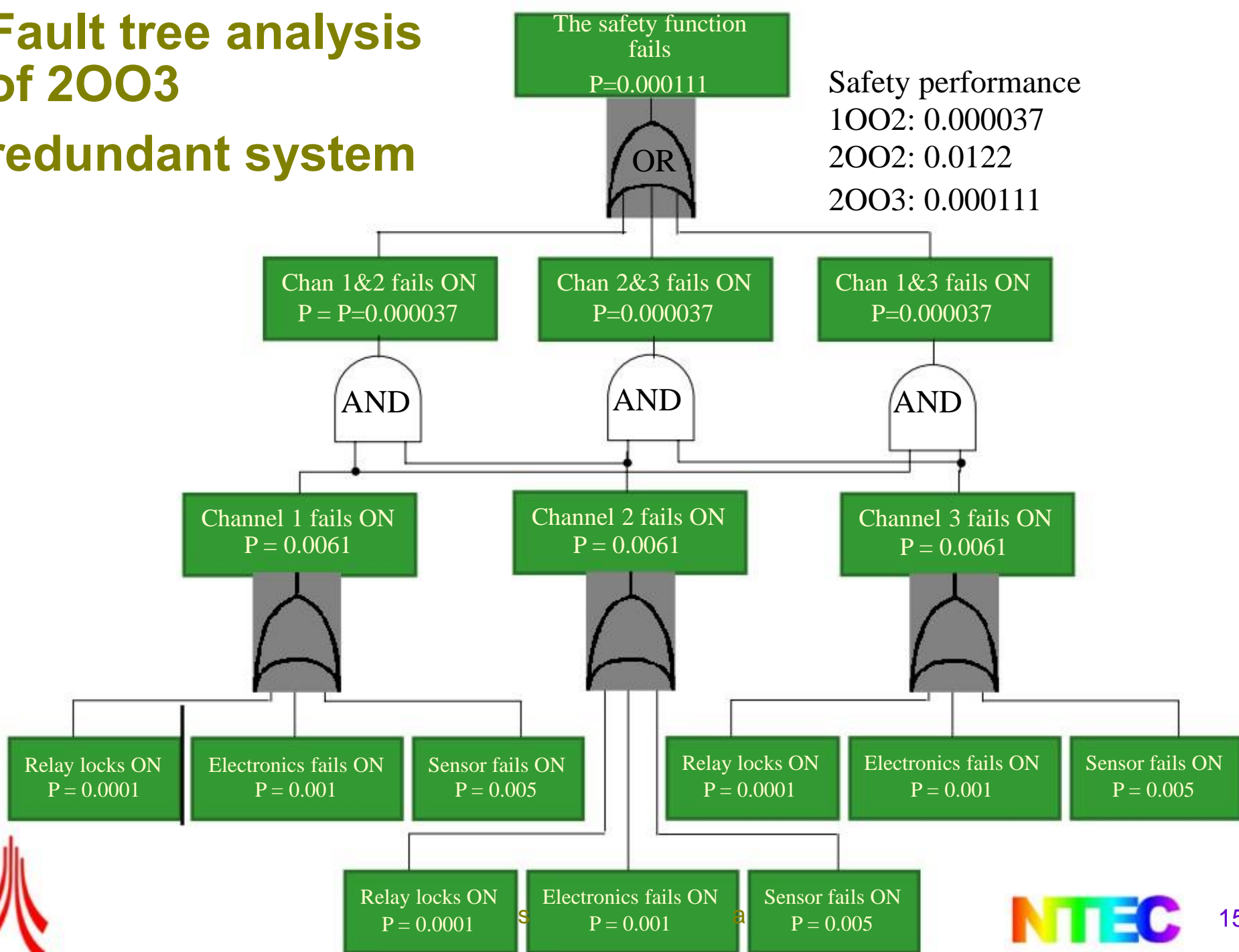
- Reliability Block Diagram



(P = Probability of dangerous failure)

The Design of Safety Critical Systems

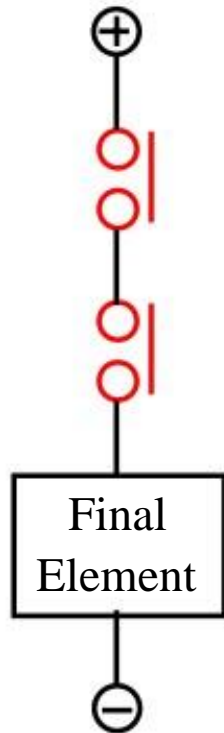
# Fault tree analysis of 2003 redundant system



# Safety versus availability

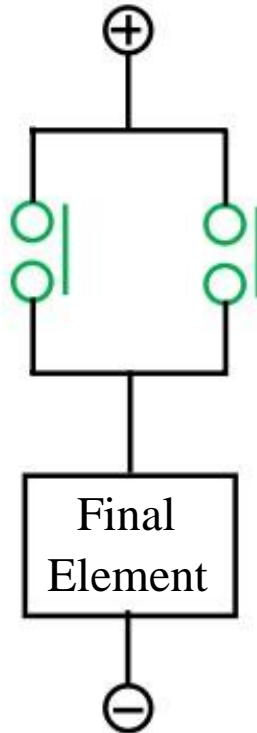
A flaw with this type diagram is that it is not clear whether safe is on or off

1002



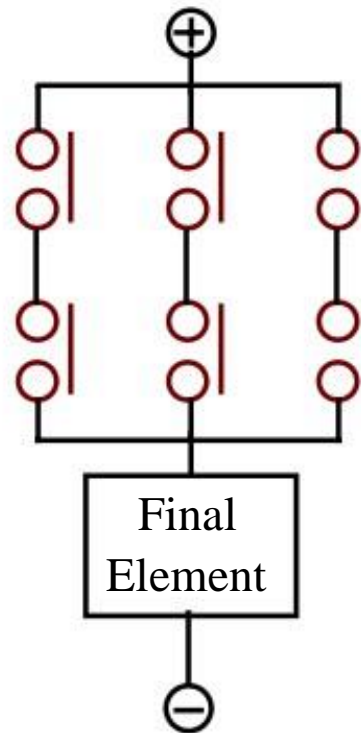
$P=0.000037$

2002



$P=0.0122$

2003



$P=0.000111$

Assume loop normally energised, (i.e., de-energise to trip)

- Consider “stuck at 1 failures” (i.e. contacts welded)
- Consider “stuck at 0 failures” (i.e. high resistance build-up on contacts)

**Safety Only**

**Availability Only**

**Safety & Availability**

Either ask off

Both ask off

Two of three ask off

