

The menu

Today

- 1. Search
- 2. Optimization
- 3. CSP

Tomorrow

- 4. CSP continued
- 5. Games
- 6. Logic
  - a. Propositional
  - b. FOL

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Search

- 1. The flavours
  - a. Breadth first search
  - b. Uniform cost search
  - c. Depth first search
  - d. Uninformed searches
- 2. Formulating searches
  - a. Heuristics for searches

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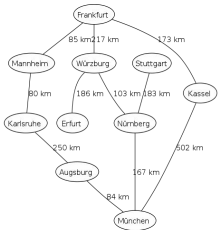
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BFS

Here is a graph of locations in Germany

If we perform BFS on this, what question are we answering?



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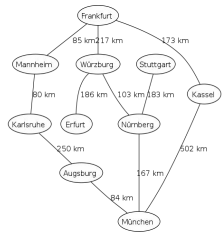
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Uniform cost search

Here is the graph of locations in Germany from before

If we perform UCS on this, what question are we answering?



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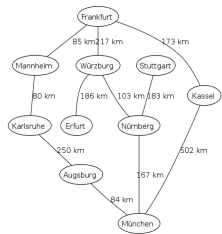
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DFS

Here is that thing again

If we perform DFS on this, what question are we answering?



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Question for you

What are the potential problems in using DFS for searches?

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## Think Uninformed searches → Think heuristics

1. Greedy best first
2. A\*

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## Greedy best first

- This is feels like DFS but implementation-wise it is like UCS
- When heuristic of a child node  $c$  is better than its parent  $p$  then
  - $c$ 's children are explored before  $c$ 's siblings
  - So, if the heuristic keeps returning better and better values it will behave like a DFS
- Greedy best first is implemented with a special priority queue
  - When  $h(c) > h(p)$ ,  $c$  is put in the front of the queue and  $p$  is inserted right behind it
  - Otherwise,  $c$  will bubble up the priority queue

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## A\*

- This is essentially UCS
- UCS prioritizes nodes based on the accumulative cost to the a node  $n$ ,  $g(n)$ 
  - For the rest of the presentation I will use  $s \rightarrow n$  to designate the path from  $s$  to  $n$
  - i.e. accumulative cost is denoted as  $g(s \rightarrow n)$
- A\* prioritizes nodes based on
  - $g(s \rightarrow n) +$
  - $h(n \rightarrow t)$



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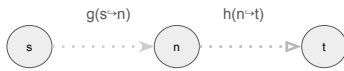
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## A\*

- $h$  is admissible  $\rightarrow$  solution is optimal on a tree
- $h$  is consistent  $\rightarrow$  solution is optimal on a graph




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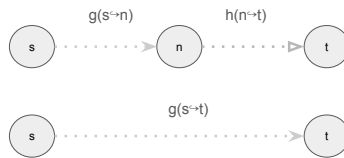
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## A\*

- Recall: UCS returns the first path to  $t$




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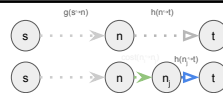
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## A\*

- $h(n_i \rightarrow t) \leq \text{cost}(n_i \rightarrow n_j) + h(n_j \rightarrow t)$  if  $h$  is consistent
- Say  $n_i$  precedes  $t$ 
  - $f(s \rightarrow t) = g(s \rightarrow t) + h(t \rightarrow t) =$   
 $= g(s \rightarrow n_i) + \text{cost}(n_i \rightarrow t) + h(t \rightarrow t)$   
 $\geq g(s \rightarrow n_i) + h(n_i \rightarrow t) = f(s \rightarrow n_i)$
- Because we use priority queue all paths so far with cost ie  $f(n_i \rightarrow t)$  less than  $g(s \rightarrow t)$  will be explored before examining  $s \rightarrow t$ 
  - ie  $f$  value along a path is never decreasing
- When  $s \rightarrow t$  is examined, all subsequent nodes in queue must be at least as expensive as  $g(s \rightarrow t)$




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A\*

- Say  $n_1$  precedes  $t$

$s \rightarrow n_2$	217km + $h(s \rightarrow n_2)$
$s \rightarrow t$	173km
$s \rightarrow n_1$	165km + $h(s \rightarrow n_1)$

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### Sidenote on heuristics

Dominance:

Say that  $h_1$  is admissible and  $h_2$  is also admissible then

if  $h_1$  does not dominate  $h_2$  does that mean  $h_2$  dominate  $h_1$ ?

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### Sidenote on heuristics

Dominance:

Say that  $h_1$  is admissible and  $h_2$  is also admissible then

if  $h_1$  does not dominate  $h_2$  does that mean  $h_2$  dominate  $h_1$ ?

Can we make  $h_3$  that dominates  $h_1$  and  $h_2$ ?

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Formulating searches

- Use formal notations
- Describe:
  - What we are looking at; state space
  - How different states are related to each other; graph connections, costs
  - What we are looking for; goal

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Example

Paraphrasing question from textbook:

- There is a map of different cities
  - Cities have distances between them
  - Two friends starting in different cities, want to meet up in a city (any city)
- At each iteration, the two friends will move to a neighbouring city
  - The faster friend will wait for the slower one before they communicate and relocate

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Fill this out

State space:

Relations:

Successor function:

Cost function:

Goal:

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Heuristics

Let  $D(i,j)$  be straight line distance between cities  $i$  and  $j$ .

Which of the following are admissible?

- 1.  $D(i,j)$
- 2.  $2 D(i,j)$
- 3.  $\frac{1}{2} D(i,j)$

For this we can examine the best case scenario

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Formulation

Paraphrasing question from textbook:

- There's a 3-foot tall monkey in an 8-foot tall room
- Banana is at the ceiling
- Room has 2 3-foot tall crates the monkey can:
  - Stack or
  - Move or
  - Climb

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Do the same thing

State space:

Relations:

Successor function:

Cost function:

Goal:

Paraphrasing question from textbook:

- There's a 3-foot tall monkey in an 8-foot tall room
- Banana is at the ceiling
- Room has 2 3-foot tall crates the monkey can:
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More exercises from textbook

Consider a state space where the start state is number 1 and each state  $k$  has two successors:  $2k$  and  $2k+1$

- What does the state space look like

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Continued

Let's say goal state is 11.

What is the ordering of nodes explored if we use:

- BFS
- Limited DFS of 3 levels
- Iterative deepening

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Continued

Bidirectional search.

What is it?

Does it help in this problem?

What are the branching factors of the 2 directions

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## Optimization

- Local searches
- Searching under partial observations

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## Local searches

- Hill climbing
  - Look at neighbours and take the *best* one
- Stochastic hill climbing
  - Look at neighbours and take a random one weighted by how *good* they are
- Random restart hill climbing
  - Hill climb from different starting points
- Simulated annealing
  - Greedily accept good neighbours and probabilistically accept bad ones; with the probability of accepting bad ones decreasing over time
- Local beam search
  - Start with  $k$  random states
  - Each iteration takes the best  $k$  neighbours of the previous states

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## Local beam search vs Random restart

Are they just essentially the same thing?

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Exercise from textbook

What are the equivalent algorithms to the following:

- Local beam search with  $k=1$
- Local beam search with 1 initial state and no limit on the number of states retained
- Simulated annealing with constant  $T=0$  and no termination test
- Simulated annealing with constant  $T=\infty$

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Exercise from textbook

What are the equivalent algorithms to the following:

- Local beam search with  $k=1$

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Exercise from textbook

What are the equivalent algorithms to the following:

- Local beam search with  $k=1$
  
- Hill Climbing

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### Exercise from textbook

What are the equivalent algorithms to the following:

- Local beam search with 1 initial state and no limit on the number of states retained

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### Exercise from textbook

What are the equivalent algorithms to the following:

- Local beam search with 1 initial state and no limit on the number of states retained
- BFS

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### Exercise from textbook

What are the equivalent algorithms to the following:

- Simulated annealing with constant  $T=0$  and no termination test
- Simulated annealing with constant  $T=\infty$

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## Exercise from textbook

What are the equivalent algorithms to the following:

- Simulated annealing with constant  $T=0$  and no termination test
- Simulated annealing with constant  $T=\infty$
  
- Hill Climbing
- Random Walk

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## Searching under no observations

- Conformant problem
  - We want to coerce an agent towards a particular state disregarding its initial state

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## Example

Given a set of recruits with unknown initial states

How do we turn them into real soldiers

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Formulations

- Belief states: every possible set of actual states
- Initial states: the state of every agent initially
- Actions: functions an agent can perform
- Transition model: mapping from <state , action> → state
- Path cost: mapping from <state, action> → cost
- Goal Test: set of states that we want to reach

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Try it with this

- Belief states: every possible set of actual states
- Initial states: the state of every agent initially
- Actions: functions an agent can perform
- Transition model: mapping from <state , action> → state
- Path cost: mapping from <state, action> → cost
- Goal Test: set of states that we want to reach

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