

# R Notebook

```
data <- read_csv("SAT_School_Participation_and_Performance__2012-2013.csv")
```

```
## Parsed with column specification:
## cols(
##   `District Number` = col_double(),
##   District = col_character(),
##   School = col_character(),
##   `Test-takers: 2012` = col_double(),
##   `Test-takers: 2013` = col_double(),
##   `Test-takers: Change%` = col_double(),
##   `Participation Rate (estimate): 2012` = col_double(),
##   `Participation Rate (estimate): 2013` = col_double(),
##   `Participation Rate (estimate): Change%` = col_double(),
##   `Percent Meeting Benchmark: 2012` = col_double(),
##   `Percent Meeting Benchmark: 2013` = col_double(),
##   `Percent Meeting Benchmark: Change%` = col_double()
## )
```

*#Alex's contribution: Tidying up the data*

```
df <- data %>% select(-1, -6, -9, -12) %>% rename(district = "District", school = "School", t_takes2012 = "t_takes2012", t_takes2013 = "t_takes2013", part_rate2012 = "part_rate2012", part_rate2013 = "part_rate2013")
df <- df %>% dplyr::filter(!is.na(t_takes2012) | is.na(t_takes2013) | is.na(part_rate2012) | is.na(part_rate2013))
df
```

```
## # A tibble: 187 x 8
##   district school t_takes2012 t_takes2013 part_rate2012 part_rate2013
##   <chr>    <chr>      <dbl>      <dbl>      <dbl>      <dbl>
## 1 Ansonia  Anson~        118        104         67         61
## 2 Avon     Avon ~        254        243         90         89
## 3 Berlin   Berli~        216        220         81         82
## 4 Bethel   Bethe~        200        190         86         82
## 5 Bloomfi~ Bloom~        116        130         79         89
## 6 Bloomfi~ Big P~         14         30        100        100
## 7 Bolton   Bolto~         62         70         85         96
## 8 Branford Branf~        196        213         77         84
## 9 Bridgep~ Bassi~        105        122         52         60
## 10 Bridgep~ Centr~        346        305         78         69
## # ... with 177 more rows, and 2 more variables: perc_mb2012 <dbl>,
## #   perc_mb2013 <dbl>
```

$\text{bmr} = \text{number of meeting Benchmark} / \text{number of total seniors} = (t\_takes / \text{perc\_mb}) / (t\_takes / \text{part\_rate})$   
 $= \text{perc\_mb} / \text{part\_rate}$   $\text{bmr} = \text{perc\_mb} / \text{part\_rate} \times 0.0001$

We use bmr because it's a better measurement for comparing how well schools do. If 2 schools have the same percentage meeting benchmark, but one of them has a higher participation rate then the one with the higher participation rate is the better school.

*#Alex's contribution: creating BMR formula*

*#df1 is for testtakers for each school+year*

```
df1 <- df %>%
```

```

select(1:4) %>%
rename(`2012` = t_takes2012, `2013` = t_takes2013) %>%
gather(3,4,key = "year", value = "t_takes") %>%
arrange(school)

#df2 is participation rate for each school+year
df2 <- df %>% select(1,2,5,6) %>%
  rename(`2012` = part_rate2012, `2013` = part_rate2013) %>%
  gather(3,4,key = "year", value = "part_rate")

#df3 is percentage meeting benchmark for each school+year
df3 <- df %>%
  select(1,2,7,8) %>%
  rename(`2012` = perc_mb2012, `2013` = perc_mb2013) %>%
  gather(3,4,key = "year", value = "perc_mb")

#df4 combines them all
df4 <- df1 %>%
  full_join(df2,by = c("district","school","year")) %>%
  full_join(df3,by = c("district","school","year"))
df4 <- df4 %>%
  mutate(bmr = perc_mb*part_rate*1e-4)

df4

```

```

## # A tibble: 374 x 7
##   district      school      year  t_takes part_rate perc_mb   bmr
##   <chr>         <chr>    <chr>   <dbl>    <dbl>   <dbl> <dbl>
## 1 Stamford      Academy of In~ 2012     133      82     47 0.385
## 2 Stamford      Academy of In~ 2013     142      88     51 0.449
## 3 Connecticut Techn~ Albert I Prin~ 2012      92     58      1 0.0058
## 4 Connecticut Techn~ Albert I Prin~ 2013      88     55      0 0
## 5 Amistad Academy D~ Amistad Acade~ 2012      34    100     32 0.32
## 6 Amistad Academy D~ Amistad Acade~ 2013      31    100     39 0.39
## 7 Regional 05      Amity Regiona~ 2012     381     87     61 0.531
## 8 Regional 05      Amity Regiona~ 2013     348     80     63 0.504
## 9 Ansonia          Ansonia High ~ 2012     118     67     18 0.121
## 10 Ansonia         Ansonia High ~ 2013     104     61     18 0.110
## # ... with 364 more rows

```

First we'll get the senior population for each school (denoted as pop)

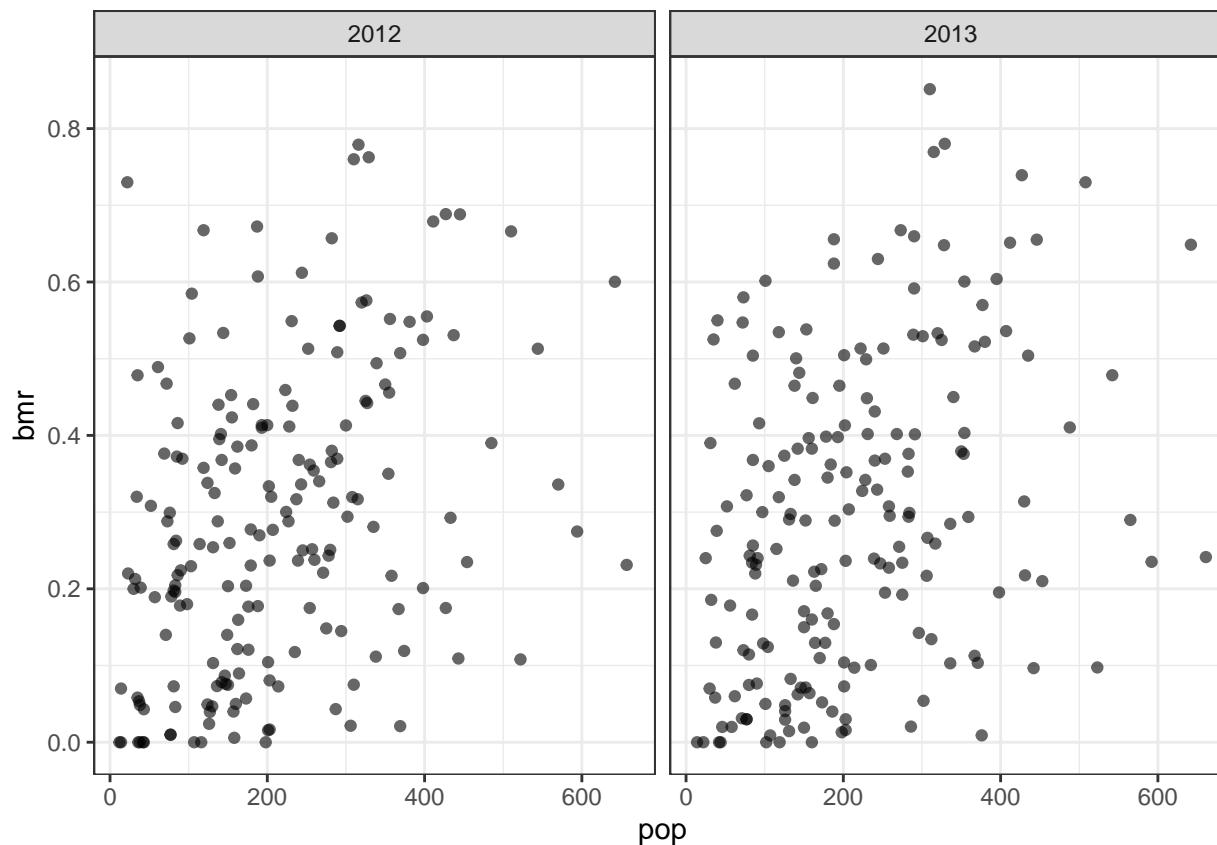
```
data <- df4 %>% mutate(pop = floor(1e2*t_takes / part_rate))
```

Now lets plot it

```

ggplot(data) +
  geom_point(aes(pop,bmr),alpha=3/5) +
  facet_wrap(~year) +
  theme_bw()

```



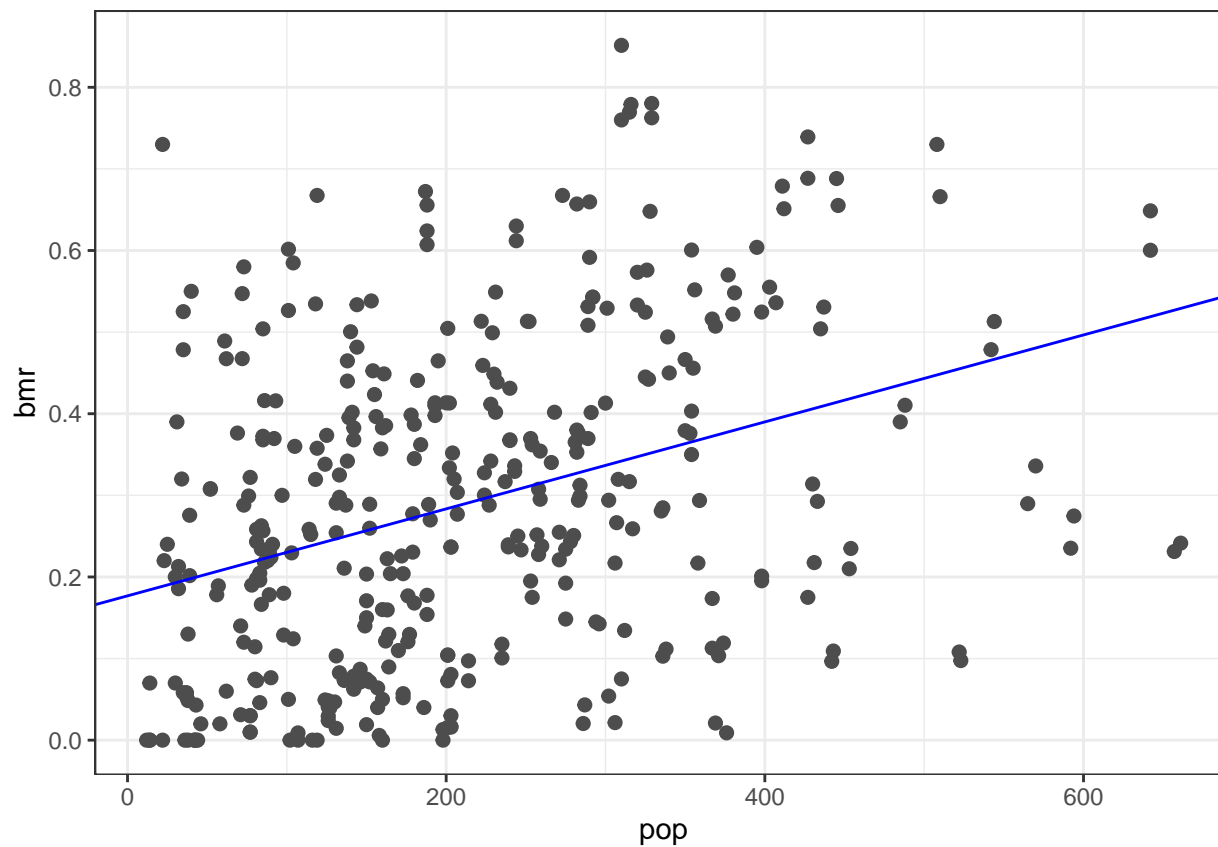
The data is relatively scattered, but we can see a weak positive linear trend.

Let's use mean-square residuals

```
#mean-square residuals
measure_distance <- function(mod,data){
  diff <- data$bmr - (mod[1] + data$pop*mod[2])
  sqrt(mean(diff^2))
}

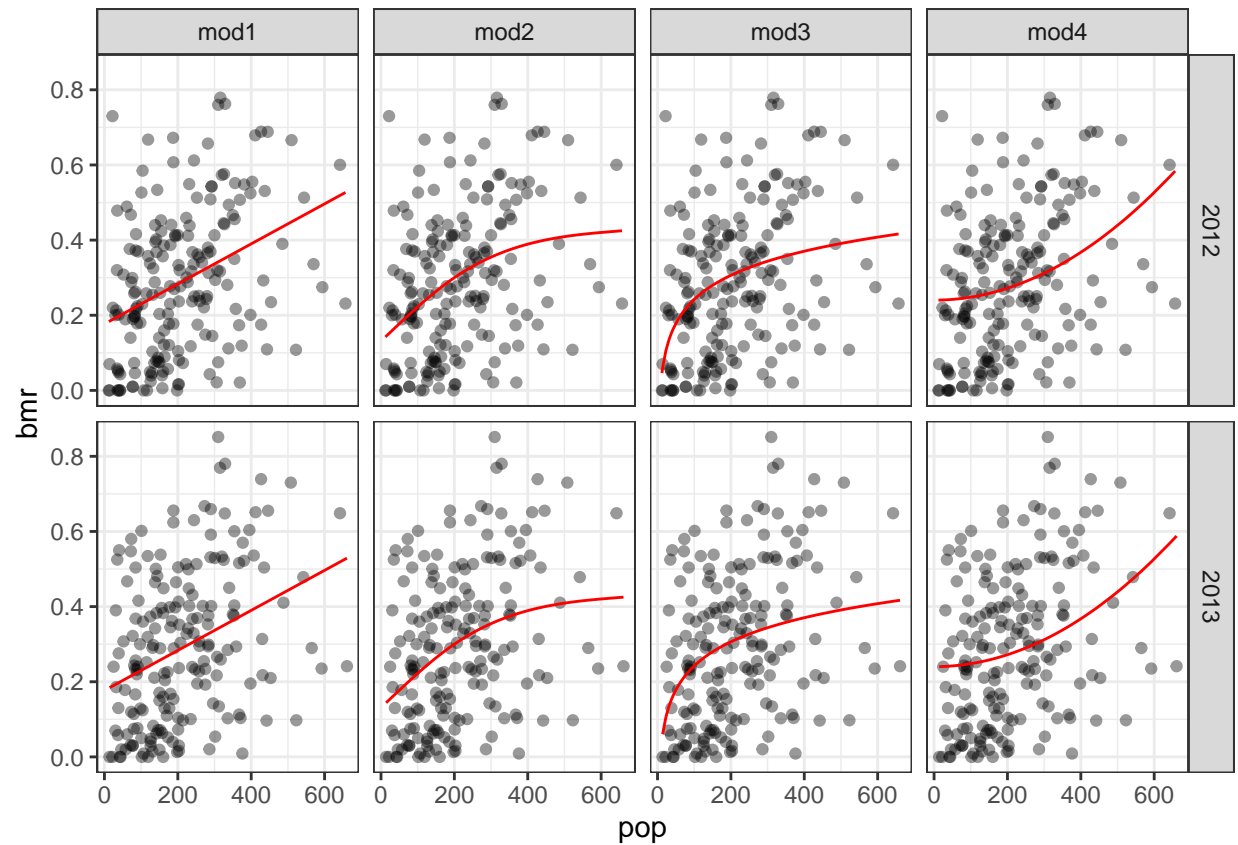
best <- optim(c(0, 0), measure_distance, data = data)

ggplot(data, aes(pop, bmr)) +
  geom_point(size = 2, colour = "grey30") +
  geom_abline(color="blue",intercept = best$par[1], slope = best$par[2]) +
  theme_bw()
```



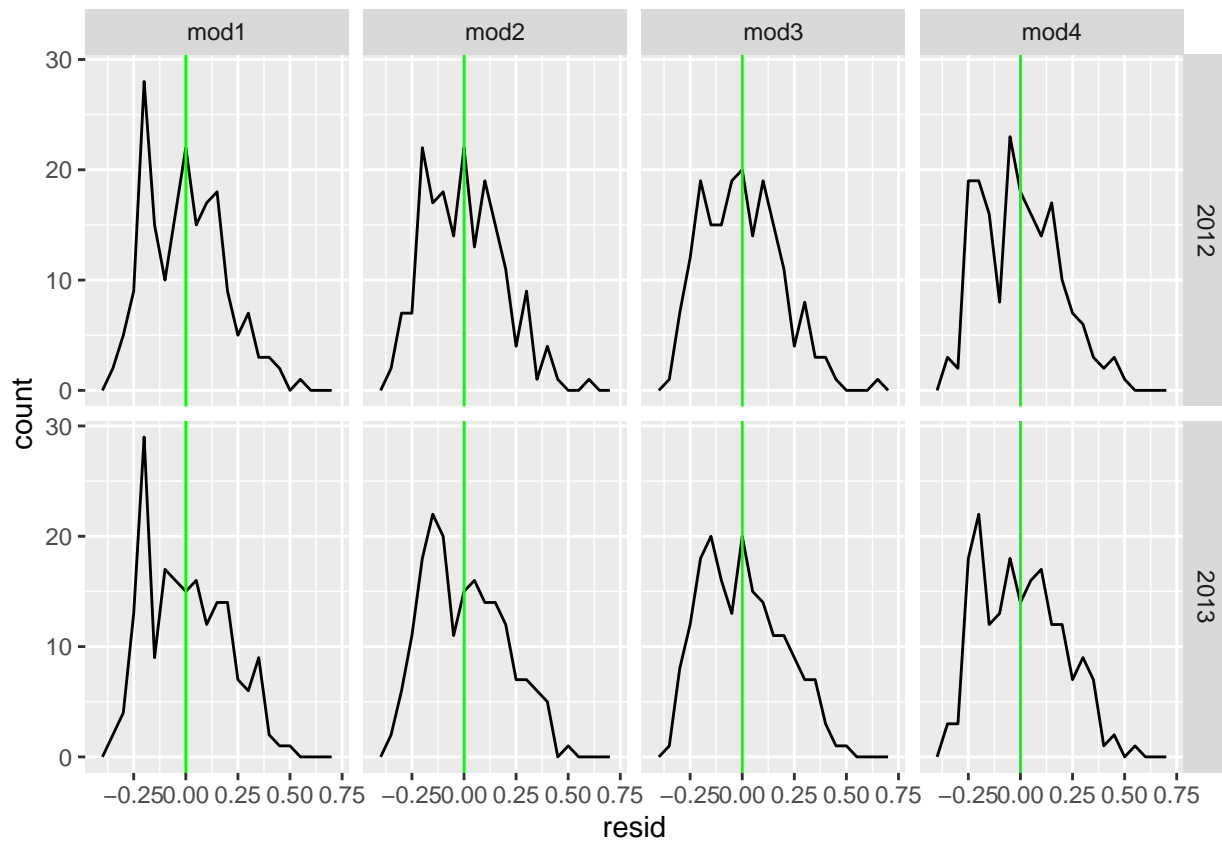
```
mod1 <- lm(bmr ~ ns(pop, 1), data = data)
mod2 <- lm(bmr ~ ns(pop, 2), data = data)
mod3 <- lm(bmr ~ log(pop, base = exp(1)), data = data)
mod4 <- lm(bmr ~ I(pop^2), data = data)
```

```
data %>%
  gather_predictions(mod1, mod2, mod3, mod4) %>%
  ggplot(aes(pop, bmr)) +
  geom_point(alpha=2/5) +
  geom_line(aes(pop, pred), colour = "red") +
  facet_grid(year ~ model) +
  theme_bw()
```



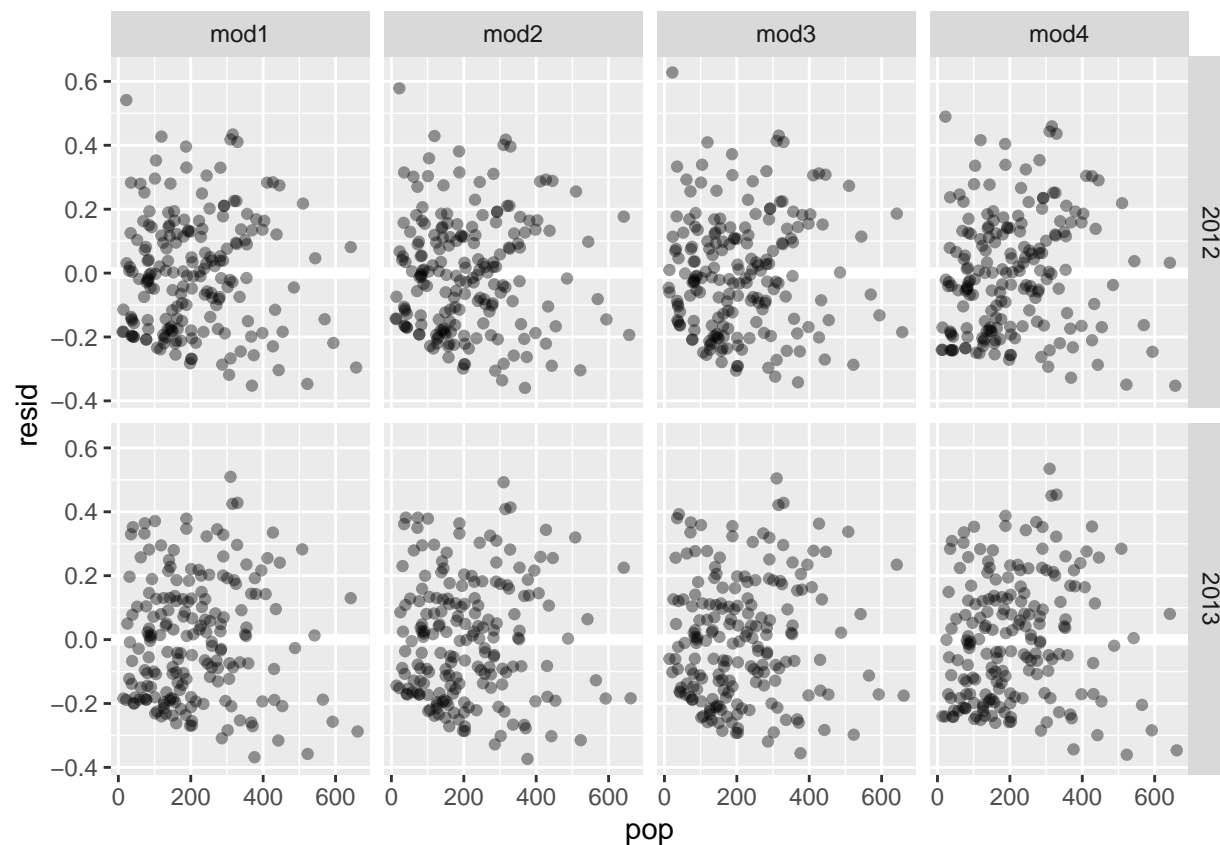
Let's check the residuals for any patterns

```
data %>%
  gather_residuals(mod1,mod2,mod3,mod4) %>%
  ggplot(aes(resid)) +
  geom_freqpoly(binwidth = 0.05) +
  geom_vline(xintercept = 0, colour = "Green", size=0.5) +
  facet_grid(year ~ model)
```



Looks approximately normal for all.

```
data %>%
  gather_residuals(mod1,mod2,mod3,mod4) %>%
  ggplot(aes(pop, resid)) +
  geom_hline(yintercept = 0, colour = "white", size = 2) +
  geom_point(alpha=2/5) +
  facet_grid(year ~ model)
```



Coefficient of Determination ( $r^2$ )

```
summary(mod1)$r.squared
```

```
## [1] 0.1260082
```

```
summary(mod2)$r.squared
```

```
## [1] 0.137638
```

```
summary(mod3)$r.squared
```

```
## [1] 0.1248974
```

```
summary(mod4)$r.squared
```

```
## [1] 0.09041305
```

These coefficients SUCK

What if I repeated something with districts that have more than 5 schools

```
popularDistrict <- data %>%
  group_by(district) %>%
  summarize(n=n()) %>%
  dplyr::filter(n>10) %>%
  left_join(data,by="district") %>%
  select(-n)
popularDistrict
```

```
## # A tibble: 78 x 8
##   district      school      year  t_takes part_rate perc_mb    bmr    pop
##   <chr>         <chr>      <chr>   <dbl>    <dbl>   <dbl> <dbl> <dbl>
## 1 Connecticut Te~ Albert I P~ 2012     92      58     1 0.0058  158
## 2 Connecticut Te~ Albert I P~ 2013     88      55     0 0      160
## 3 Connecticut Te~ Bullard Ha~ 2012    127      64     0 0      198
## 4 Connecticut Te~ Bullard Ha~ 2013    129      65     2 0.013  198
## 5 Connecticut Te~ E C Goodwi~ 2012     38      30     8 0.024  126
## 6 Connecticut Te~ E C Goodwi~ 2013     62      49     6 0.0294 126
## 7 Connecticut Te~ E. T. Gras~ 2012     59      40    19 0.076  147
## 8 Connecticut Te~ E. T. Gras~ 2013     57      38     5 0.019  150
## 9 Connecticut Te~ Eli Whitne~ 2012     76      65     0 0      116
## 10 Connecticut Te~ Eli Whitne~ 2013     31      26     0 0      119
## # ... with 68 more rows
```

```
ggplot(popularDistrict) +
  geom_point(aes(pop,bmr,color=district),alpha=3/5) +
  facet_grid(district~year) +
  theme_bw()
```



