

Compliance classes

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| randomized to control condition $A^0 = A^1$ | randomized to treatment condition $A^{z=0} = A^1$ | Label |
|--|--|-------------------------|
| 0 (no treatment) | 0 (no treatment) | Never-takers |
| 0 | 1 | Compliers |
| 1 (yes treatment) | 0 | Defiers (Non-compliers) |
| 1 | 1 (yes treatment) | Always-takers |

↳ if $A=0$: no treatment received; if $A=1$: yes treatment received.

think of these as subpopulations of people

Never-takers subpopulation: (no variability in treatment in this group)

- they don't take the treatment, regardless of randomization

↳ encouragement doesn't work on these subjects

⇒ we would not learn anything about the effect of treatment in this subpopulation, as there is no variation in treatment received (both, A^0 & A^1 are 1).

Compliers subpopulation:

- take treatment if encouraged to, and don't otherwise.

↳ treatment received (A) in this group is always equal to treatment assigned (Z).

⇒ in this group, treatment received is randomized. So we can learn about the causal effect of treatment.

Defiers: - do the opposite of what they are encouraged to do

↳ in this group, treatment received is also randomized BUT in the opposite way.

Always-takers: - no variation in treatment received → no way to learn about causal effects.

Causal Effect:

- motivation for using IV: general concern about unmeasured confounding

↳ when there is unmeasured confounding, we cannot average/marginalize over all confounders (via matching, IPTW, etc.)

IV methods do not focus on population average causal effects

↳ focus with IV methods is on local average treatment effect

Local average treatment effect:

- the target of inference is: $E(Y^{z=1} | A^0=0, A^1=1) - E(Y^{z=0} | A^0=0, A^1=1)$

↳ difference in means of potential outcomes

↳ b/c we look at the same subpopulation of subjects (i.e. $A^0=0, A^1=1 \Rightarrow$ compliers), we can compute a valid causal effect of treatment.

note that: $E(Y^{z=1} | A^0=0, A^1=1) - E(Y^{z=0} | A^0=0, A^1=1) =$

$E(Y^{z=1} - Y^{z=0} | \text{Compliers}) \quad \text{Why can we claim this?}$

$E(Y^{A=1} - Y^{A=0} | \text{Compliers}) \quad \text{B/c for compliers when } z=1 \Rightarrow A=1 \text{ and o.w. } z=0 \Rightarrow A=0$

↳ this is a local average treatment effect b/c we look at a

subpopulation being compliers

- this is a valid causal effect b/c it contrasts counterfactuals in a common population.

⇒ a.k.a. Complier average causal effect (CACE)

↳ this is a causal effect in a subpopulation ⇒ thus "local".

↳ no inference about: defiers, always-takers, never-takers.

Observed data:

- for each person, we observe an A and a Z , not (A^0, A^1)

treatment assigned \swarrow treatment received \downarrow potential treatment if assigned to treatment

Z A A^0 A^1 Class (compliance)

| Z | A | A^0 | A^1 | Class (compliance) |
|-----|-----|-------|-------|---------------------------|
| 0 | 0 | 0 | ? | Complier OR never-taker. |
| 0 | 1 | 1 | ? | Defier OR always-taker. |
| 1 | 0 | ? | 0 | Defier OR never-taker. |
| 1 | 1 | ? | 1 | Complier OR always-taker. |

we don't know for sure what

they are; we can only narrow

down the label to 2 options.

Identifiability:

- compliance classes a.k.a. principal strata, and they are latent (i.e. not directly observable)

→ so how can we then estimate the complier average causal effect (CACE)?

→ next lectures/videos provides necessary assumptions.