Final Project

Objectvies:

In this project you will investigate the exponential distribution in R and compare it with the Central Limit Theorem. The exponential distribution can be simulated in R with exp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda. Set lambda = 0.2 for all of the simulations. You will investigate the distribution of averages of 40 exponentials. Note that you will need to do a thousand simulations.

Illustrate via simulation and associated explanatory text the properties of the distribution of the mean of 40 exponentials. You should

- 1. Show the sample mean and compare it to the theoretical mean of the distribution.
- 2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.
- 3. Show that the distribution is approximately normal.

Preparations

sample_mean <- mean(mean_si)</pre>

```
#Settings
set.seed(123)
lambda<- 0.2
n <- 40
simulations <- 1000

#Simulate
simulated_exp <- replicate(simulations,rexp(n,lambda))

#Calculate the mean
mean_si <- apply(simulated_exp,2,mean)</pre>
```

Q1. Show the sample mean and compare it to the theoretical mean of the distribution.

```
sample_mean

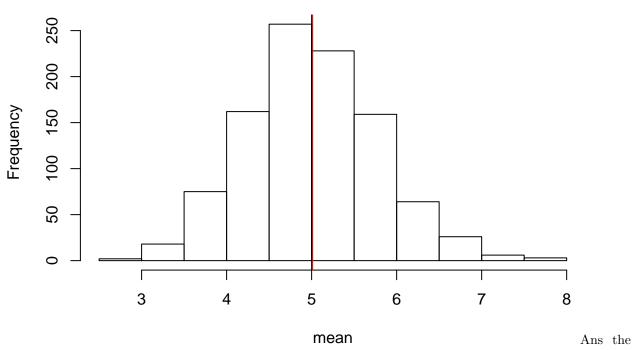
## [1] 5.011911

theory_mean <- 1/lambda
theory_mean

## [1] 5</pre>
```

```
#Visual
hist(mean_si, xlab= "mean", main= "Exponential Simulation")
abline(v= sample_mean, col="red")
abline(v= theory_mean, col="black")
```

Exponential Simulation



sample mean is close to the theoretical mean.

x <- seq(min(mean_si), max(mean_si), length=100) y <- dnorm(x, mean=1/lambda, sd=(1/lambda/sqrt(n)))

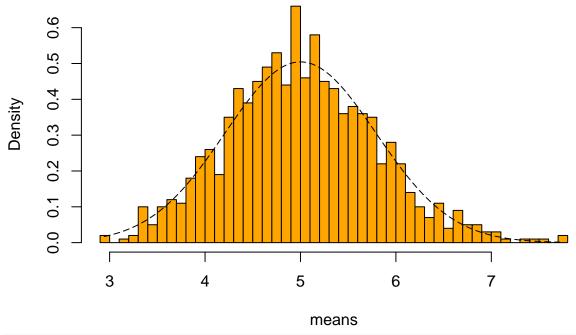
lines(x, y, pch=22, col="black", lty=5)

Q2. Show how variable it is and compare it to the theoretical variance of the distribution

```
#std of distribution
std_dist <- sd(mean_si)</pre>
std_dist
## [1] 0.7749147
#std from theory
std_theory <- (1/lambda)/(sqrt(n))</pre>
std_theory
## [1] 0.7905694
#Variance of distribution
var_dist <- (std_dist)^2</pre>
var_dist
## [1] 0.6004928
#variance from theory
var_theory <- ((1/lambda)*(1/sqrt(n)))^2</pre>
var_theory
## [1] 0.625
Q3 Show that the distribution is approximately normal.
```

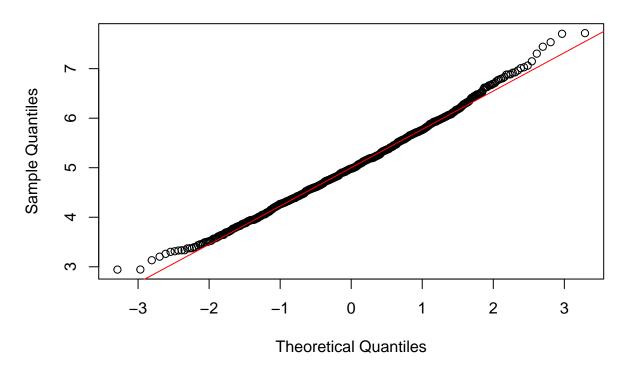
hist(mean_si,breaks=n,prob=T,col="orange",xlab = "means",main="Density of means")

Density of means



compare the distribution of averages of 40 exponentials to a normal distribution
qqnorm(mean_si)
qqline(mean_si, col = 2)

Normal Q-Q Plot



According to CLT, the distribution of avg of 40 exponentials is close to normal distribution.