# Week 8 Maria Chiara Cigarini

Task 1 Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickenss to be 13 mm)

**Answer** 

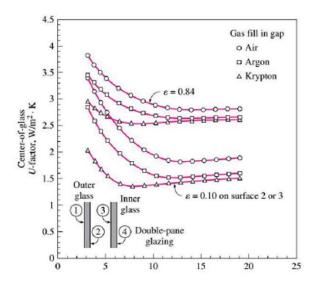
To calcolate the U value of the window

$$U_{window} = \frac{U_{center} A_{center} + U_{edge} A_{edge} + U_{fram} A_{fram}}{A_{window}}$$

If it's a double pane window, we can ignore the thermal resistance of glass layers

$$\frac{1}{U_{double}-pane} \cong \frac{1}{h_i} + \frac{1}{h_{space}} + \frac{1}{h_0} \; h_{space} = h_{rad,space} + h_{conv,space}$$

- The U<sub>center</sub> of the h<sub>space</sub> changes if we change the gas that fills the gap.
   From the diagram we can see that when the gap thickenss is 13 mm by changing the gas from air to argon, the U value of the centre of the gas decreases from 2.8 to 2.65 (5%); instead by changing the gas from air to krypton the U value decrease from 2.8 to 2.6 (7%)
- At the same time the  $U_{center}$  changes also by adding an extra pane. From the diagram we can see that when the gap thickenss is 13 mm and the gas is air, by adding an extra pain the U value decreases from 2.8 to 1.8 (35%).
- Otherwise we can change the U<sub>center</sub> coating the glass surfaces whit a low emissivity film.
  From the diagram we can see that when the gap thikenss is 13 mm and the gas is air, by
  coating the glass surfaces with a film that has 0.1 emissivity, the U value of the centre
  decreases from 2.8 to 1.8, which means the U value decreases 35%.



Task 2 Consider the house that we analysed in the last two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m2 on the west, fixed 3.6 m2 on the south and an operable 3.6 m2 on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium? The net area of walls (excluding doors and windows) of a building located in Piacenza is 105.8 m2, the calculated U value is 0.438 W/mq K for the winter and 0.435 w/mq K for the summer. Find the corresponding heating and cooling load.

						P	IACENZ	A, Italy						WMO#:	160840
Lat:	44.92N	Long:	9.73E	Elev:	138	StdP:	99.68		Time Zone: 1.00 (EUW)			Period: 89-10		WBAN:	99999
Annual He	eating and Hu	umidification	on Design C	onditions											
Coldest	Heating DB		Humidification DP/MCDB and HR						Coldest month WS/MCDB			MCWS/PCWD			
Month			99.6%			99%			0.4%		1% to 99.6		6% DB		
Month	99.6%	99%	DP	HR	MCDB	DP	HR	MCDB	WS	MCDB	WS	MCDB	MCWS	PCWD	
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(1)	(m)	(n)	(0)	
1	-6.2	-4.8	-11.6	1.4	3.1	-8.8	1.8	1.8	8.8	5.6	7.7	6.2	2.1	250	
nnual Co	ooling, Dehu	midificatio	n, and Entha	alpy Design	Conditions	k .									
Hottest	Hottest	Cooling DB/MCWB								Evaporation WB/MCDB				MCWS/	PCWD
Month	Month		0.4% 1%			2%	6	0	0.4%		% 2		% to 0.49		% DB
WIGHT	DB Range	DB	MCWB	DB	MCWB	DB	MCWB	WB	MCDB	WB	MCDB	WB	MCDB	MCWS	PCWD
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(1)	(m)	(n)	(0)	(P)
8	11.9	33.1	22.7	31.9	22.4	30.3	21.8	24.6	30.2	23.7	29.2	22.9	28.3	2.4	90

$$\Delta T_{cooling} = 31.9 - 24 = 7.9 \,^{\circ}\text{C}$$
  
 $\Delta T_{heating} = 20 - (-4.8) = 24.8 \,^{\circ}\text{C}$   
DR = 11.9  $^{\circ}\text{C}$ 

• Calculating the cooling load of the fixed window of the west:

Cooling Load: Wooden Frame

$$\dot{q}_{windowwest} = A \times CF_{windowwest}$$
 $A = 14.4 \text{ m}^2$ 

$$\begin{array}{l} CF_{windowwest} = CF_{windowwest\_heattransfer} + CF_{windowwest\_irridiation} \\ CF_{windowwest} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s \\ CF_{windowwest} + eattransfer = U(\Delta T - 0.46DR) \end{array}$$

The window has a fixed heat that absorb double layer grass with a wooden frame

$$U = 2.84$$

$$\begin{split} & \text{CF}_{windowwest\_heattransfer} = 2.84 \; (7.9 \text{ - } (0.46)(11.9)) = 6.89 \, \frac{\text{W}}{\text{m}^2} \\ & \text{CF}_{windowwest\_irridiation} = \text{PXI x SHGC x IAC x FF}_s \\ & \text{PXI} = E_D \; - \; E_d = \; 559 \; + \; 188 \; = \; 747 \\ & \text{SHGC} = 0.54 \end{split}$$

No internal shading so  $\rightarrow$  IAC = 1

$$\begin{split} FF_s &= 0.56 \\ CF_{windowwest\_irridiation} &= 747 \times 0.54 \times 1 \times 0.56 = 232.78 \, \frac{W}{m^2} \\ CF_{windowwest} &= CF_{windowwest\_heattransfer} \, + \, CF_{windowwest\_irridiation} \\ CF_{windowwest} &= 6.89 \, + \, 225.89 = 232.78 \, \frac{W}{m^2} \\ \dot{q}_{windowwest} &= \, A \times CF_{windowwest} = 14.4 \times 232.78 = 3352.07 \, \, W \end{split}$$

Calcoulating the heating load of the fixed window on the west

## Cooling Load: aluminium frame

$$\begin{aligned} \dot{q}_{windowwest} &= \text{A x CF}_{windowwest} \\ \text{A = 14.4 m}^2 \\ \text{CF}_{windowwest} &= \text{CF}_{windowwest\_heattransfer} + \text{CF}_{windowwest\_irridiation} \\ \text{CF}_{windowwest} &= \text{U}(\Delta \text{T - 0.46DR}) + \text{PXI x SHGC x IAC x FF}_s \\ \text{CF}_{windowwest\_heattransfer} &= \text{U}(\Delta \text{T - 0.46DR}) \\ \text{U = 3.61} \\ \text{CF}_{windowwest\_heattransfer} &= 3.61 \ (7.9 - (0.46)(11.9)) = 8.76 \ \frac{W}{m^2} \\ \text{CF}_{windowwest\_irridiation} &= \text{PXI x SHGC x IAC x FF}_s \\ \text{PXI = E}_D &- \text{E}_d = 559 + 188 = 747 \\ \text{SHGC = 0.56} \\ \text{IAC = 1} \\ \text{FF}_s &= 0.56 \\ \text{CF}_{windowwest\_irridiation} &= 747 \times 0.56 \times 1 \times 0.56 = 234.26 \ \frac{W}{m^2} \\ \text{CF}_{windowwest} &= 8.76 + 234.26 = 243.02 \ \frac{W}{m^2} \\ \dot{q}_{windowwest} &= \text{A x CF}_{windowwest} = 14.4 \times 243.02 = 3499.47 \ W \end{aligned}$$

### Heating Load: wooden frame

$$\dot{q}_{windowwest} = A \times HF_{windowwest}$$
 $A = 14.4 \text{ m}^2$ 
 $HF_{windowwest} = U_{windowwest} \times \Delta T_{heating}$ 
 $U = 2.84$ 
 $HF_{windowwest} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$ 

$$\dot{q}_{windowwest} = 2.84 \text{ x } 24.8 = 70.43 \frac{1}{\text{m}^2}$$
  
 $\dot{q}_{windowwest} = A \text{ x HF}_{windowwest} = 14.4 \text{ x } 70.43 = 1014.22 \text{ W}$ 

# Heating Load: aluminium frame

$$\dot{q}_{windowwest} = A \times HF_{windowwest}$$
 $A = 14.4 \text{ m}^2$ 
 $HF_{windowwest} = U_{windowwest} \times \Delta T_{heating}$ 
 $U = 3.61$ 

$$HF_{windowwest} = 3.61 \times 24.8 = 89.53 \frac{W}{m^2}$$
  
 $\dot{q}_{windowwest} = A \times HF_{windowwest} = 14.4 \times 89.53 = 1289.20 W$ 

#### Difference:

 Calcoulating the cooling load of the fixed window on the south Cooling load: wooden frame

$$\begin{array}{l} \dot{q}_{windowsouth} \ = \ A \ x \ CF_{windowsouth} \\ A = 3.6 \ m^2 \\ CF_{windowsouth} \ = \ CF_{windowsouth\_heattransfer} \ + \ CF_{windowsouth\_irridiation} \\ CF_{windowsouth} \ = \ U(\Delta T \ - \ 0.46DR) \ + \ PXI \ x \ SHGC \ x \ IAC \ x \ FF_s \\ CF_{windowsouth\_heattransfer} \ = \ U(\Delta T \ - \ 0.46DR) \\ \end{array}$$

$$U = 2.84$$

$$CF_{windowsouth\_heattransfer} = 2.84 (7.9 - (0.46)(11.9)) = 6.89 \frac{W}{m^2}$$

$$CF_{windowsouth\_irridiation} = PXI x SHGC x IAC x FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{windowsouth\_irridiation} = 557 \times 0.54 \times 1 \times 0.47 = 141.37 \frac{W}{m^2}$$

$$CF_{windowsouth} = CF_{windowsouth\_heattransfer} + CF_{windowsouth\_irridiation}$$

$$CF_{\text{windowsouth}} = 6.89 + 141.37 = 148.26 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 148.26 = 533.74 \text{ W}$$

## Cooling Load: aluminium frame

$$\dot{q}_{windowsouth} = A x CF_{windowsouth}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{windowsouth} = CF_{windowsouth\_heattransfer} + CF_{windowsouth\_irridiation}$$

$$CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{windowsouth\_heattransfer} = U(\Delta T - 0.46DR)$$

$$U = 3.61$$

$$CF_{windowsouth\_heattransfer} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{W}{m^2}$$

$$CF_{windowsouth\_irridiation} = PXI \ x \ SHGC \ x \ IAC \ x \ FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{windowsouth\_irridiation} = 557 \times 0.56 \times 1 \times 0.47 = 146.60 \frac{W}{m^2}$$

$$CF_{\text{windowsouth}} = 8.76 + 146.60 = 155.36 \frac{W}{m^2}$$

$$\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 155.36 = 559.30 \text{ W}$$

## Heating Load: wooden frame

$$\dot{q}_{windowsouth} = A \times HF_{windowsouth}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{windowsouth} = U_{windowsouth} \times \Delta T_{heating}$$

$$U = 2.84$$

$$HF_{windowsouth} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$$

$$\dot{q}_{windowsouth} = A \times HF_{windowsouth} = 3.6 \times 70.43 = 253.08 \text{ W}$$

# Heating Load: aluminium frame

$$\dot{q}_{windowsouth} = A x HF_{windowsouth}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{windowsouth} = U_{windowsouth} \ \textbf{x} \ \Delta T_{heating}$$

$$U = 3.61$$

$$HF_{windowsouth} = 3.61 \text{ x } 24.8 = 89.53 \frac{W}{m^2}$$

$$\dot{q}_{windowsouth} = A \times HF_{windowsouth} = 3.6 \times 89.53 = 322.31 \text{ W}$$

#### Difference:

• Calcoulating the cooling load of the operable window on the south

# Cooling Load: wooden frame $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$ $A = 3.6 \text{ m}^2$ $CF_{windowsouth} = CF_{windowsouth\_heattransfer} + CF_{windowsouth\_irridiation}$ $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_{s}$ $CF_{windowsouth\_heattransfer} = U(\Delta T - 0.46DR)$ U = 2.87 $CF_{windowsouth\_heattransfer} = 2.87 (7.9 - (0.46)(11.9)) = 6.96 \frac{W}{m^2}$ $CF_{windowsouth\_irridiation} = PXI \times SHGC \times IAC \times FF_s$ $PXI = E_D - E_d = 348 + 209 = 557$ SHGC = 0.46IAC = 1 $FF_s = 0.47$ $CF_{windowsouth\_irridiation} = 557 \times 0.46 \times 1 \times 0.47 = 120.42 \frac{W}{m^2}$ $CF_{windowsouth} = CF_{windowsouth\_heattransfer} + CF_{windowsouth\_irridiation}$ $CF_{windowsouth} = 6.96 + 120.42 = 127.38 \frac{W}{m^2}$ $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 127.38 = 458.57 \text{ W}$ Cooling load: aluminium frame $\dot{q}_{windowsouth} = A \times CF_{windowsouth}$ $A = 3.6 \text{ m}^2$ $CF_{windowsouth} = CF_{windowsouth\_heattransfer} \ + \ CF_{windowsouth\_irridiation}$ $CF_{windowsouth} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_{s}$ $CF_{windowsouth\_heattransfer} = U(\Delta T - 0.46DR)$ U = 4.62 $CF_{windowsouth\_heattransfer} = 4.62 (7.9 - (0.46)(11.9)) = 11.21 \frac{W}{m^2}$ $CF_{windowsouth\_irridiation} = PXI \times SHGC \times IAC \times FF_s$ $PXI = E_D - E_d = 348 + 209 = 557$ SHGC = 0.55IAC = 1 $FF_s = 0.47$ $CF_{windowsouth\_irridiation} = 557 \times 0.55 \times 1 \times 0.47 = 143.98 \frac{W}{m^2}$ $CF_{windowsouth} = 11.21 + 143.98 = 155.19 \frac{W}{m^2}$ $\dot{q}_{windowsouth} = A \times CF_{windowsouth} = 3.6 \times 155.19 = 558.68 \text{ W}$ Heating Load: wooden frame $\dot{q}_{windowsouth} = A \times HF_{windowsouth}$ $A = 3.6 \text{ m}^2$ $HF_{windowsouth} = U_{windowsouth} \times \Delta T_{heating}$ U = 2.87 $HF_{windowsouth} = 2.87 \times 24.8 = 71.18 \frac{W}{m^2}$

 $\dot{q}_{windowsouth} = A x HF_{windowsouth} = 3.6 x 71.18 = 256.23 W$ 

Heating Load: aluminium frame

 $\dot{q}_{windowsouth} = A x HF_{windowsouth}$   $A = 3.6 \text{ m}^2$ 

 $HF_{windowsouth} = U_{windowsouth} \; x \; \Delta T_{heating}$ 

U = 4.62

$$HF_{windowsouth} = 4.62 \text{ x } 24.8 = 114.58 \frac{W}{m^2}$$

$$\dot{q}_{windowsouth} = A \times HF_{windowsouth} = 3.6 \times 114.58 = 412.47 \text{ W}$$

#### Difference:

Cooling Load = 100.11 W

Heating Load = 156.24 W