

Week 8 Maria Chiara Cigarini

Task 1 Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? (keep the gap thickness to be 13 mm)

Answer

To calculate the U value of the window

$$U_{window} = \frac{U_{center}A_{center} + U_{edge}A_{edge} + U_{fram}A_{fram}}{A_{window}}$$

If it's a double pane window, we can ignore the thermal resistance of glass layers

$$\frac{1}{U_{double - pane}} \cong \frac{1}{h_i} + \frac{1}{h_{space}} + \frac{1}{h_o} \quad h_{space} = h_{rad,space} + h_{conv,space}$$

- The U_{center} of the h_{space} changes if we change the gas that fills the gap.
From the diagram we can see that when the gap thickness is 13 mm by changing the gas from air to argon, the U value of the centre of the gas decreases from 2.8 to 2.65 (5%); instead by changing the gas from air to krypton the U value decrease from 2.8 to 2.6 (7%)
- At the same time the U_{center} changes also by adding an extra pane.
From the diagram we can see that when the gap thickness is 13 mm and the gas is air, by adding an extra pane the U value decreases from 2.8 to 1.8 (35%).
- Otherwise we can change the U_{center} coating the glass surfaces with a low emissivity film.
From the diagram we can see that when the gap thickness is 13 mm and the gas is air, by coating the glass surfaces with a film that has 0.1 emissivity, the U value of the centre decreases from 2.8 to 1.8, which means the U value decreases 35%.

Cooling Load: Aluminum Frame

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}}$$

$$A = 14.4 \text{ m}^2$$

$$CF_{\text{windowwest}} = CF_{\text{windowwest_heattransfer}} + CF_{\text{windowwest_irradiation}}$$

$$CF_{\text{windowwest}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowwest_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 3.61$$

$$CF_{\text{windowwest_heattransfer}} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowwest_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 559 + 188 = 747$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_s = 0.56$$

$$CF_{\text{windowwest_irradiation}} = 747 \times 0.56 \times 1 \times 0.56 = 234.26 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowwest}} = 8.76 + 234.26 = 243.02 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times CF_{\text{windowwest}} = 14.4 \times 243.02 = 3499.47 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}}$$

$$A = 14.4 \text{ m}^2$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}}$$

$$U = 2.84$$

$$HF_{\text{windowwest}} = 2.84 \times 24.8 = 70.43 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 70.43 = 1014.22 \text{ W}$$

Heating Load: Aluminum Frame

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}}$$

$$A = 14.4 \text{ m}^2$$

$$HF_{\text{windowwest}} = U_{\text{windowwest}} \times \Delta T_{\text{heating}}$$

$$U = 3.61$$

$$HF_{\text{windowwest}} = 3.61 \times 24.8 = 89.53 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowwest}} = A \times HF_{\text{windowwest}} = 14.4 \times 89.53 = 1289.20 \text{ W}$$

Difference:

$$\text{Cooling Load} = 147.4 \text{ W}$$

$$\text{Heating Load} = 274.98 \text{ W}$$

- Calculating the cooling load of the fixed window on the south

Cooling Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 2.84$$

$$CF_{\text{windowsouth_heattransfer}} = 2.84 (7.9 - (0.46)(11.9)) = 6.89 \frac{W}{m^2}$$

$$CF_{\text{windowsouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.54$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowsouth_irradiation}} = 557 \times 0.54 \times 1 \times 0.47 = 141.37 \frac{W}{m^2}$$

$$CF_{\text{windowsouth}} = CF_{\text{windowsouth_heattransfer}} + CF_{\text{windowsouth_irradiation}}$$

$$CF_{\text{windowsouth}} = 6.89 + 141.37 = 148.26 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times CF_{\text{windowsouth}} = 3.6 \times 148.26 = 533.74 \text{ W}$$

Cooling Load: Aluminum Frame

$$\dot{q}_{\text{windowsouth}} = A \times CF_{\text{windowsouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowsouth}} = CF_{\text{windowsouth_heattransfer}} + CF_{\text{windowsouth_irradiation}}$$

$$CF_{\text{windowsouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowsouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 3.61$$

$$CF_{\text{windowsouth_heattransfer}} = 3.61 (7.9 - (0.46)(11.9)) = 8.76 \frac{W}{m^2}$$

$$CF_{\text{windowsouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.56$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowsouth_irradiation}} = 557 \times 0.56 \times 1 \times 0.47 = 146.60 \frac{W}{m^2}$$

$$CF_{\text{windowsouth}} = 8.76 + 146.60 = 155.36 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times CF_{\text{windowsouth}} = 3.6 \times 155.36 = 559.30 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}}$$

$$U = 2.84$$

$$HF_{\text{windowsouth}} = 2.84 \times 24.8 = 70.43 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}} = 3.6 \times 70.43 = 253.08 \text{ W}$$

Heating Load: Aluminum Frame

$$\dot{q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}}$$

$$U = 3.61$$

$$HF_{\text{windowsouth}} = 3.61 \times 24.8 = 89.53 \frac{W}{m^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times HF_{\text{windowsouth}} = 3.6 \times 89.53 = 322.31 \text{ W}$$

Difference:

$$\text{Cooling Load} = 25.56 \text{ W}$$

Heating Load = 69.23 W

SOUTH WINDOW (OPERABLE)

Cooling Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 2.87$$

$$CF_{\text{windowssouth_heattransfer}} = 2.87 (7.9 - (0.46)(11.9)) = 6.96 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.46$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.46 \times 1 \times 0.47 = 120.42 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = 6.96 + 120.42 = 127.38 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 127.38 = 458.57 \text{ W}$$

Cooling Load: Aluminum Frame

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$CF_{\text{windowssouth}} = CF_{\text{windowssouth_heattransfer}} + CF_{\text{windowssouth_irradiation}}$$

$$CF_{\text{windowssouth}} = U(\Delta T - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

$$CF_{\text{windowssouth_heattransfer}} = U(\Delta T - 0.46DR)$$

$$U = 4.62$$

$$CF_{\text{windowssouth_heattransfer}} = 4.62 (7.9 - (0.46)(11.9)) = 11.21 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth_irradiation}} = PXI \times SHGC \times IAC \times FF_s$$

$$PXI = E_D - E_d = 348 + 209 = 557$$

$$SHGC = 0.55$$

$$IAC = 1$$

$$FF_s = 0.47$$

$$CF_{\text{windowssouth_irradiation}} = 557 \times 0.55 \times 1 \times 0.47 = 143.98 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{windowssouth}} = 11.21 + 143.98 = 155.19 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times CF_{\text{windowssouth}} = 3.6 \times 155.19 = 558.68 \text{ W}$$

Heating Load: Wooden Frame

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}}$$

$$A = 3.6 \text{ m}^2$$

$$HF_{\text{windowssouth}} = U_{\text{windowssouth}} \times \Delta T_{\text{heating}}$$

$$U = 2.87$$

$$HF_{\text{windowssouth}} = 2.87 \times 24.8 = 71.18 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowssouth}} = A \times HF_{\text{windowssouth}} = 3.6 \times 71.18 = 256.23 \text{ W}$$

Heating Load: Aluminum Frame

$$\dot{q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}}$$

$$A = 3.6 \text{ m}^2$$

$$\text{HF}_{\text{windowsouth}} = U_{\text{windowsouth}} \times \Delta T_{\text{heating}}$$

$$U = 4.62$$

$$\text{HF}_{\text{windowsouth}} = 4.62 \times 24.8 = 114.58 \frac{\text{W}}{\text{m}^2}$$

$$\dot{q}_{\text{windowsouth}} = A \times \text{HF}_{\text{windowsouth}} = 3.6 \times 114.58 = 412.47 \text{ W}$$

Difference:

$$\text{Cooling Load} = 100.11 \text{ W}$$

$$\text{Heating Load} = 156.24 \text{ W}$$
