

## Feedback — Priority Queues

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You submitted this quiz on **Sun 27 Sep 2015 1:59 PM EDT**. You got a score of **2.80** out of **3.00**. You can [attempt again](#), if you'd like.

To specify an array or sequence of values in an answer, separate the values in the sequence by whitespace. For example, if the question asks for the first ten powers of two (starting at 1), then the following answer is acceptable:

```
1 2 4 8 16 32 64 128 256 512
```

If you wish to discuss a particular question and answer in the forums, please post the entire question and answer, including the seed (which can be used by the course staff to uniquely identify the question) and the explanation (which contains the correct answer).

### Question 1

(seed = 467705)

Give the sequence of the keys in the array that results after inserting the sequence of 3 keys

```
95 57 80
```

into the following maximum-oriented binary heap of size 10:

```
81 77 75 43 36 30 67 19 24 15
```

Your answer should be a sequence of 13 integers, separated by whitespace.

**You entered:**

95 81 80 43 77 75 67 19 24 15 36 30 57

Your Answer	Score	Explanation
95 81 80 43 77 75 67 19 24 15 36 30 57	✓ 1.00	
Total	1.00 / 1.00	

**Question Explanation**

The correct answer is: 95 81 80 43 77 75 67 19 24 15 36 30 57

Here is the sequence of keys in the array after each insertion:

```

      81 77 75 43 36 30 67 19 24 15
95: 95 81 75 43 77 30 67 19 24 15 36
57: 95 81 75 43 77 57 67 19 24 15 36 30
80: 95 81 80 43 77 75 67 19 24 15 36 30 57

```

**Question 2**

(seed = 767245)

Give the sequence of keys in the array that results after performing 3 successive delete-the-max operations on the following maximum-oriented binary heap of size 10:

```
85 83 70 46 54 26 19 11 34 33
```

Your answer should be a sequence of 7 integers, separated by whitespace.

**You entered:**

54 46 34 11 33 26 19

Your Answer	Score	Explanation
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54 46 34 11 33 26 19



1.00

Total

1.00 / 1.00

**Question Explanation**

The correct answer is: 54 46 34 11 33 26 19

Here is the sequence of keys in the array after each deletion:

```

                85 83 70 46 54 26 19 11 34 33
[ 85 deleted ] 83 54 70 46 33 26 19 11 34
[ 83 deleted ] 70 54 34 46 33 26 19 11
[ 70 deleted ] 54 46 34 11 33 26 19

```

**Question 3**

(seed = 813697)

Which of the following statements about priority queues are true? Check all that apply. Unless otherwise specified, assume that the binary heap implementation is the one from lecture (e.g., max-oriented and using 1-based indexing).

**Your Answer****Score****Explanation**

0.20

Let  $a[]$  be a binary heap that contains the  $N$  distinct integers  $1, 2, \dots, N$ . Then, key  $N$  must be in  $a[1]$  and  $N-2$  must be in either  $a[2]$ ,  $a[3]$ ,  $a[4]$ ,  $a[5]$ ,  $a[6]$ , or  $a[7]$ .

Key  $N$  must be in root ( $a[1]$ ). Key  $N-1$  must be in either the left or right child of the root ( $a[2]$  or  $a[3]$ ). Key  $N-2$  must be in either a child of the root ( $a[2]$  or  $a[3]$ ) or a child of key  $N-1$  ( $a[4]$ ,  $a[5]$ ,  $a[6]$ , or  $a[7]$ ).



0.20

Unlike either mergesort or quicksort

Mergesort is not in-place; quicksort has only a probabilistic linearithmic guarantee.

rt, heapsort is a  
n in-place sortin  
g algorithm that  
has linearithmic  
worst-case perfor  
mance.

- 
- ☐ ✓ 0.20 This would violate the  $\sim N \lg N$  sorting lower bound since it would yield a  $\sim 2 N \lg (\lg N)$  compare-based sorting algorithm.
- It is possible to implement our priority queue API so that both insert() and delMax() take  $\sim \lg (\lg N)$  compares per operation (in the worst case), where  $N$  is the number of keys in the data structure.
- 
- ☒ ✓ 0.20 Bottom-up heap construction achieves this bound.
- Given an array of  $N$  comparable keys, it is possible to construct a binary heap containing those  $N$  keys using at most  $\sim 2 N$  compares.
- 
- ☐ ✗ 0.00 It can be done with 0 compares - a reverse-sorted array is a heap.
- Given a sorted array of  $N$  comparable keys, it is possible to build a binary heap containing those  $N$  keys using no more than  $\sim 1/2 N$  compares.
- 

Total 0.80 /  
1.00

**Question Explanation**