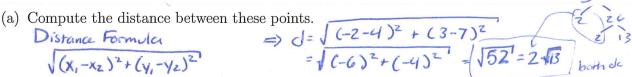
1. Given the points (-2,3) and (4,7).



(b) Find the midpoint of the line segment connecting them, $\Rightarrow \left(\frac{-2+4}{2}, \frac{3+7}{2}\right) = \left(1, 5\right)$ Midpoint Formula (c) Compute the slope of the line connecting the points.

Slope Formula $\Rightarrow m = \frac{7-3}{4-(-2)} = \frac{4}{6} = \frac{2}{3}$

(d) Write an equation for the line containing these two points. $y-7=\frac{3}{3}(x-4)$ or $|y-3-\frac{2}{3}(x+2)|$ or $|y-\frac{2}{3}x+\frac{13}{3}$

(e) Find the x- and y- intercepts of this line.

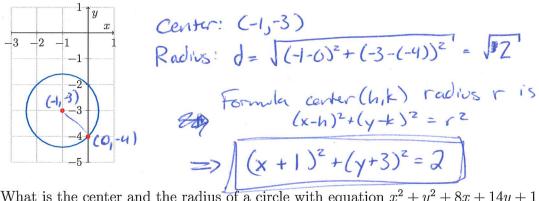
(e) Find the
$$x-$$
 and $y-$ intercepts of this line.
 $x-$ intercepts: when $y=0$

$$O=\frac{2}{3}x+\frac{13}{3} \Rightarrow x=-\frac{13}{2}$$
(f) Find the slope of a line perpendicular to this line.

(g) Write an equation for a line perpendicular to this line passing through the point (3,0).

$$y-0=\frac{-3}{2}(x-3) \rightarrow y=\frac{-3}{2}x+\frac{9}{2}$$

2. Write an equation for the circle graphed here.

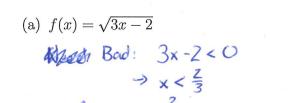


3. What is the center and the radius of a circle with equation $x^2 + y^2 + 8x + 14y + 1 = 0$? Complete the squeres

$$x^{2} + 8x + (\frac{8}{2})^{2} + y^{2} + |4y| + (\frac{14}{2})^{2} = -1 + (\frac{8}{2})^{2} + (\frac{14}{2})^{2} = -1 + 16 + 49$$

$$(x - 4)^{2} + (y - \frac{17}{7})^{2} = 64$$

$$(4,7) \quad \text{Radius: § 8}$$



Good
$$x \ge \frac{2}{3}$$

Thereal $\left[\frac{2}{3}, \infty\right)$ Set $\left\{x \in \mathbb{R} \mid x \ge \frac{2}{3}\right\}$

(b)
$$g(x) = \frac{2x+1}{x^2-9}$$

Bad: $x^2-9=0$
 $x^2-9=0$
 $x^2-9=0$
 $x^2-9=0$
 $x^2-3=0$
 $x^2-3=0$
 $x^2-3=0$

Interval $\left[\frac{2}{3}, \infty\right)$ Set $\left\{x \in \mathbb{R} \mid x \neq \frac{2}{3}\right\}$ $\left(-\infty, -3\right) \cup (3, 3) \cup (3, \infty)$ $\left\{x \in \mathbb{R} \mid x \neq \pm 3\right\}$

5. For each function compute the given items then determine if the function is even/odd/neither.

4. Find the domain of the function. Write your answer in interval and set builder notation.

(a)
$$f(x) = 3x^2 - 2$$

i. $f(0) = 3(0)^2 - 2 = [-3]$

ii.
$$f(4) = 3(4)^2 - 2 = 46$$

iii.
$$f(-2) = 3(-2)^2 - 2 = 10$$

iv.
$$f(a) = 3a^2 - 2$$

v.
$$f(x+h) = 3(x+h)^2 - 2$$
 better
vi. $f(t^2+1) = 3(t^2+1)^2 - 2$ better

vi.
$$f(t^2+1) = 3(t^2+1)^2 - 2$$

vii. x-intercepts

$$\sqrt{20}$$

$$0 = 3x^2 - 2 \rightarrow x^2 = \frac{2}{3} \rightarrow x = \pm \sqrt{\frac{2}{3}} \rightarrow \left(\pm \sqrt{\frac{2}{3}}, 0\right)$$

viii. y-intercepts

ix. the average value of y = f(x) from x = 1

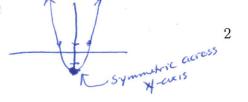
$$\frac{f(3)-f(1)}{3-1} = \frac{(3(3)^2-2)-(3(1)^2-2)}{2}$$

$$= \frac{24}{2} = 12$$

x. Is f even/odd/both/neither?

$$f(-x) = 3(-x)^2 - 2 = 3x^2 - 2 = f(x)$$

Graph:



(b)
$$g(x) = 2|x-1|-4$$

i. $g(0) = 2|0-1|-4 = 2|-1|-4$
 $= 2 \cdot 1-4 = [-2]$
ii. $g(4) = 2|4-1|-4 = 2|3|-4 = 2\cdot3-4 = [2]$

ii.
$$g(4) = 2|4-1|-4 = 2|3|-4 = 2.3-4 = 2$$

iii.
$$g(-2) = 2|-2-1|-4 = 2|-3|-4 = 2-3-4 = 2$$

v.
$$g(x+h) = 2 |x+h-1| - 4$$

vi.
$$g(r^2+1) = 2|r^2+1-1|-4 = 2|r^2|-4 = 2r^2-4$$

vii. x-intercepts 0 = 2|x-1| = -4 3 = |x-1| 3 = |x-1| (3,0), (-1,0)

viii. y-intercepts

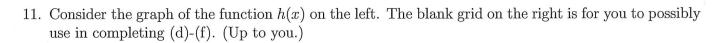
ix. the average value of
$$y = g(x)$$
 from $x = 1$ to $x = 3$

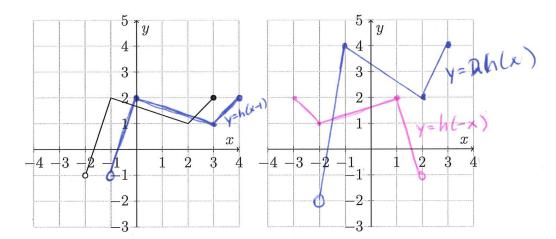
$$\frac{g(3) - g(1)}{3 - 1} = \frac{(2|3 - 1| - 4) - (2(|11 - 1|) - 4)}{2}$$

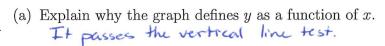
$$= \frac{0 - (-4)}{3} = \sqrt{2}$$

x. Is $g = \sqrt{\frac{d}{both}}$

	Is the relation $\{(2,3),(-1,3),(5,3)\}$ a function? What is the domain of the relation? What is the range of the relation?
	Yes this is a function - no two y's have the same x
	Domain: {2,-1,53} (Range: {33})
	If $H(t)$ describes the height of a tree that is t years old, then what does the average rate of change of H from $t = 1$ to $t = 5$ represent?
	The average rate of change represents the average number of feet the height of the true changes by each year.
r	A company that makes thing-a-ma-bobs has a start up cost of \$16936. It costs the company \$1.54 to make each thing-a-ma-bob and the company charges \$4.27 for each thing-a-ma-bob. Let x represent the number of thing-a-ma-bobs made.
	(a) Write a cost function for this company. $((x) = 1.54x + 16936)$
	(b) Write the revenue function for this company.
	(R(x)= 4.27x
	(c) Write the profit function for this company. P(x) = R(x) - R(x) = 4.27x - (1.54x + 16.936) = 2.73x - 16.936 = R(x)
	(d) What is the minimum number of thing-a-ma-bobs that the company must produce and sell to make a profit?
	$2.73 \times -16936 = 0 \rightarrow X = \frac{16936}{2.73} \approx 6203.663$
	=> Sell at least 6204 units
9. V	What does the graph of an even function look like? Sketch some examples. Symmetric across y-axis
	The American of the American o
10. V	What does the graph of an odd function look like? Sketch some examples.
	about origin
	1
	Name of the state







(m) Local Max Valves When x=-1, we have a local max it is/y=2

(b) Determine h(2). When x=2, y=1

(n) Local Min Values When x=2, we have a local min it is y= 1

(c) Determine h(-1).

- (d) Sketch a graph of y = h(x-1). on left graph (shift right lunit) (e) Sketch a graph of y = 2h(x). on right graph (double y vals)
- (f) Sketch a graph of y = h(-x). on right graph in sink reflect across y-axis

(g) What is the domain of h(x)?

(-2,3]

(h) What is the range of h(x)?

(i) What are the x- and y-intercepts of the graph?

(j) On what intervals is the function increasing?

(-2,-1) and (2,3)

(k) On what intervals is the function decreasing? (-1,2)

> descriptions of x-vals
where y-vals are going up Idown
to not include endpoints

to pool

(1) Write h(x) as a piecewise function by finding equations for each of the three linear portions of Line 1: $\frac{1}{3}$ slope $\frac{3}{3}$ $\frac{1}{3}$ $\frac{-2}{3}$ $\frac{2}{3}$ $\frac{-2}{3}$ $\frac{2}{3}$ $\frac{-2}{3}$ $\frac{2}{3}$ $\frac{-2}{3}$ $\frac{2}{3}$ $\frac{-2}{3}$ $\frac{-2}{3}$ the graph. This one

13 hard maybe -> don't spend tons of time

> maybe tocuson one line

and on piecewize

12. Given the piecwise function, evaluate the values.

$$g(x) = \begin{cases} x+2 & \text{if } x \le -5\\ |x+1|+2 & \text{if } -5 < x < 0\\ \frac{1}{3x+2} & \text{if } 0 \le x \le 2\\ x^2+x+1 & \text{if } x > 2 \end{cases}$$

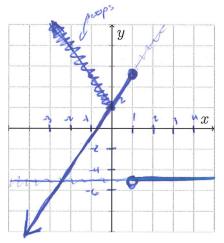
(a)
$$\frac{3}{2}(0) = \frac{1}{3 \cdot Or2} = \frac{1}{2}$$

(b)
$$\frac{3}{4}(-5) = -5+2 = |-3|$$

(c)
$$f(1) = \frac{1}{3-1+2} = \frac{1}{5}$$

13. Graph the piecewise function

$$r(x) = \begin{cases} 3x + 2 & \text{if } x \le 1\\ -5 & \text{if } x > 1 \end{cases}$$



14. Let $f(x) = x^2 + 1$, g(x) = |x - 2|, h(x) = 4x - 3.

(a) Compute
$$g(h(2))$$
.

$$h(2) = 4(2) - 3 = 5$$

(a) Compute
$$g(h(2))$$
. M

$$h(2) = 4(2) - 3 = 5$$
(b) Compute $f \circ g(-3) = f(g(-3))$.
$$g(-3) = |-3-2| = |-5| = 5$$
(c) Compute and simplify $f(h(x))$.
$$g(-3) = |-3-2| = |-5| = 5$$

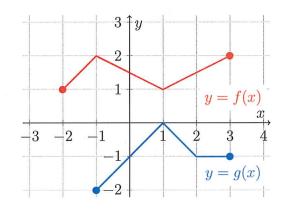
$$f(g(-3)) = f(5) = 5^2 + 1 = 26$$

$$f(h(x)) = f(4x-3) = (4x-3)^2 + 1 = |6x^2 - 24x + 9 + 1 = |6x^2 -$$

(d) Compute and simplify $h \circ h(x) = h(h(x))$.

$$h(h(x)) = h(4x-3) = 4(4x-3) - 3 = 16x - 12 - 3 = [16x-15]$$

15. Given the graphs below



(a) Compute
$$g(f(-2))$$
.
 $f(-2)=1 \rightarrow g(f(-2))=g(1)=0$

(b) Compute
$$f(g(2))$$
.
 $g(z) = -1 \rightarrow f(g(2)) = f(-1) = \boxed{2}$

(c) Compute
$$f \circ g(0)$$
.
 $f(g(0)) = f(-1) = 2$

(d) Compute
$$g \circ f(0)$$
.
 $g(f(0)) = g(1-5) = [-0.5]$

(e) Compute
$$f \circ f(-1)$$

$$f(f(-1)) = f(z) = 1.5$$

16. Let $H(x) = 4(x-2)^{10}$. Which of the following pairs of functions f(x) and g(x) will produce $f \circ g(x) = H(x)$? (There are two...) Can you find another decomposition?

•
$$f(x) = 4x - 2$$
 and $g(x) = x^{10}$
• $f(x) = x^{10}$ and $g(x) = 4x - 2$
• $f(x) = 4x^{10}$ and $g(x) = x - 2$
• $f(x) = x - 2$ and $g(x) = 4x^{10}$
• $f(x) = 4x$ and $g(x) = (x - 2)^{10}$
• $f(x) = (x - 2)^{10}$ and $g(x) = 4x$

$$f(x) = x^{2} \quad g(x) = 2(x-2)^{5}$$

$$f(x) = 4x^{5} \quad g(x) = (x-2)^{2}$$