

Math 425: Abstract Algebra I  
L<sup>A</sup>T<sub>E</sub>X Examples

- First note that I made some vertical space above this using the command `\vksip .25in`. Use this command liberally to help make your document readable.
- Math mode is generated with dollar signs. For example  $a^2 + b^2 = c^2$ . There is a difference between a and  $a$ .
- Centered equations can be made in many ways. Here are a few:

1. Double dollar signs

$$a_1 + a_2 + \cdots + a_n = 1$$

2. Square brackets

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

3. Equation environment - numbered (only use this if you're going to refer to this equation again)

$$x^2 - 2 = (x - \sqrt{2})(x + \sqrt{2}) \tag{1}$$

4. Equation environment - unnumbered

$$2435 \equiv 11 \pmod{24}$$

5. Multiple lines with lined up equations

$$\begin{aligned} 1 + 2 + \cdots + n + n + 1 &= \frac{n(n+1)}{2} + (n+1) \\ &= \frac{n(n+1)}{2} + \frac{2(n+1)}{2} \\ &= \frac{(n+1)(n+2)}{2} \end{aligned}$$

6. Multiple lines with explanations

$$\begin{aligned} (n+1)! &= n!(n+1) && \text{definition of factorial} \\ &\geq 2^n(n+1) && \text{inductive hypothesis} \\ &\geq 2^n \cdot 2 && \text{assumption of } n \geq 3 \\ &= 2^{n+1} && \text{exponent laws} \end{aligned}$$

- To write a proof use `\begin{proof}` and `\end{proof}`, and you will get something like this:

*Proof.* Let  $S$  be a set with binary operation  $*$ . Assume there is an identity element of  $*$  in  $S$ . Let  $e_1, e_2 \in S$  be identity elements of  $S$  with respect to  $*$ . We want to show  $e_1 = e_2$ . Since  $e_1$  is an identity element, we have

$$e_1 * e_2 = e_2.$$

Similarly since  $e_2$  is an identity element,

$$e_1 * e_2 = e_1.$$

Combining these two equations, we see

$$e_2 = e_1 * e_2 = e_1.$$

We conclude that if an identity exists with respect to a binary operation, then that identity is unique.  $\square$

- There are also examples in homework assignments. Please let me know if you have further questions.