Photoproduction of π^0 on Hydrogen using $e^+e^-(\gamma)$ detection mode with CLAS

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Abstract

We report the first high precision measurement of the exclusive π^0 photoproduction cross section via Dalitz decay and e^+e^- pair conversion mode on a hydrogen target in a wide kinematic range with the CLAS setup at Thomas Jefferson National Accelerator Facility. The measurement was performed in the reaction $\gamma p \to p e^+ e^- X(\gamma)$ using a tagged photon beam spanning an energy interval from the "resonance" to the "Regge" regimes, i.e photon energies E = 1.25 - 5.55 GeV. The final state particles $p; e^+; e^-$ were detected while the photon was not detected. This new data sample quadrupled the world bremsstrahlung database above E = 2 GeV. Our data appear to favor the Regge pole model and the constituent counting rule while disfavoring the Handbag model.

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The rich $\pi + N$ resonance spectrum for center-of-mass 41 constructive or destructive interferences that can appear. (c.m.) energies up to 2.5 GeV provides insights and 42 Four models are considered here. challenges concerning the workings of the strong inter-12 action through partial wave expansions, exchange potentials, non-relativistic quark models and QCD. The π^0 and η photoproduction have always been complementary tools to investigate and constrain the various models and to lead to further insights. At the interface between the crowded low energy resonance cross section and the smooth higher energy, small angle behavior, traditionally described by Regge poles [1], lies a region in which hadronic duality interpolates the varying cross section behavior. Exclusive π photoproduction and π nucleon elastic scattering show this duality in a semi-local sense through Finite Energy Sum Rules (FESR) [2]. The connection to QCD is more tenuous for on-shell photoproduction of pions at small scattering angles, but the quark content can become manifest through large fixed angle dimensional counting rules [3] as well as being evident in semi-inclusive or exclusive electroproduction of pions, described through Transverse Momentum Distributions (TMDs) and Generalized Parton Distributions (GPDs).

The Regge pole description of photoproduction amplitudes has a long and varied history. For π^0 and η photoproduction, all applications rely on a set of known meson Regge poles. There are two allowed t-channel J^{PC} quantum numbers series, the odd-signature(odd spin) 1⁻⁻ (ρ^0, ω) and the 1⁺⁻ (b_1^0, h_1) Reggeons. Regge cut ampli-37 tudes are incorporated into some models and are inter-38 preted as rescattering of on-shell meson-nucleon ampli-39 tudes. The phases between the different poles and cuts 40 can be critical in determining the polarizations and the

The oldest model developed by Goldstein and 44 Owens [5] has the exchange of leading Regge trajectories ⁴⁵ with appropriate t-channel quantum numbers along with 46 Regge cuts generated via final state rescattering through ⁴⁷ Pomeron exchange. The Regge couplings to the nucleon 48 were fixed by reference to electromagnetic form factors, ⁴⁹ $SU(3)_{flavor}$, and low energy nucleon-nucleon meson ex-50 change potentials. At the time, the range of applicabil- $_{51}$ ity was taken to be s above the resonance region and $_{52} \mid t \mid \leq 1.2 \,\mathrm{GeV^2}$, where t is the squared four-momentum transfer. Here we will let the t range extend to large $_{54}$ | t | in order to see the predicted cross section dips from 55 the zeroes in Regge residues. Because even signature 56 partners $(A_2, \text{ etc.})$ of the odd spin poles $(\rho, \text{ etc.})$ lie on 57 the same trajectories, the Regge residues are required to 58 have zeroes to cancel the even (wrong) signature poles 59 in the physical region - nonsense wrong signature zeroes 60 (NWSZ). While the dip near $t \approx -0.5 \text{ GeV}^2$ is present $_{61}$ in π^0 data, it is not in the recent beam asymmetry data ₆₂ on η photoproduction [6]. This is not explained by the 63 standard form of the NWSZ Regge residues.

Quite recently, Mathieu et al. [7] (JPAC) (see also [8]), 65 used the same set of Regge poles, but a simplified form of ₆₆ only ω -Pomeron cuts. They show that daughter trajec-67 tories are not significant as an alternative to the Regge 68 cuts. However, to explain the lack of $t \approx -0.5 \text{ GeV}^2 \text{ dip}$ $_{69}$ in η photoproduction, they remove the standard wrong 70 signature zero, ad hoc. Donnachie and Kalashnikova [9] ₇₁ have included t-channel ρ^0 , ω , and the b_1^0 , but not the n_1 Reggeon, all with different parameterizations from 73 Ref. [5]. They include $\omega, \rho \times \text{Pomeron cuts}$, as well 74 as $\omega, \rho \times f_2$ lower lying cuts, which help to fill in the vrong signature zeroes of the ω, ρ Regge pole residues. 76 The model of Laget and collaborators [10] included u-77 channel baryon exchange. That model also connected

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78 the small and large t-channel regimes by a mechanism 136 helpful in sorting out the phenomenology associated with ₇₉ called "saturating" the Regge trajectories at $\alpha(t) \to -1$ ₁₃₇ both Regge and QCD-based models of the nucleon [4]. so for $t < -1.5 \text{ GeV}^2$, thereby describing the full angular 138 In this work, we provide a large set of differential cross 81 range ($\theta=0-2\pi$), while the other models are good 139 section values from E=1.275-5.425 MeV in labora-82 for different ranges of the forward direction, i.e., from 140 tory photon energy, corresponding to a range of c.m. en- $_{83}$ $|t|=-t_{min}$ at $\theta=0$ to $\theta=\pi/2$ [5, 7, 9]. Here, we ex- $_{141}$ ergies, W=1.81-3.33 GeV. We have compared the amine how Regge phenomenology works for the energy 142 Regge pole, the handbag, and the constituent counting range of 2.8 GeV < E $_{\gamma}$ < 5.5 GeV.

two parts, one quark from the incoming and one from 148 well with a previous CLAS measurement [20]. and contributes to orders of magnitude short-fall.

reactions at large angles when t/s is finite and is kept 169 due to trigger and data acquisition restrictions. constant. The lightest meson photoproduction was ex- 170 Lepton identification was based on a kinematic con-116 counting rules that predict the cross section should vary 174 their charge (for details, see Ref. [22]). After particle seas s^{-7} [14]. The agreement extends down to $s = 6 \text{ GeV}^2$ lection, standard g12 calibration, fiducial cuts [21] and where baryon resonances are still playing a role. Here, 176 timing cuts were applied in the analysis. we examined how the counting rule is applicable to the $_{178}$ $\gamma p \to \pi^0 p$ up to s = 10 GeV².

vided 164 data points of $d\sigma/dt(|t|)$ s [20].

"Regge", and wide angle QCD regimes of phenomenol- 193 package developed for the HADES Collaboration [23]. ₁₃₅ ogy. The broad range of c.m. energy, \sqrt{s} , is particularly ₁₉₅ The remainder of the background was attributed to

143 rule phenomenology with the new CLAS experimental in-The introduction of the handbag mechanism, devel- 144 formation on $d\sigma/dt(|t|)$ for the $\gamma p \to \pi^0 p$ reaction above oped by Kroll et al. [11], has provided complimentary 145 the "resonance" regime. As will be seen, this data set possibilities for the interpretation of hard exclusive re- 146 quadruples the world bremsstrahlung database above E actions. In this approach, the reaction is factorized into 147 = 2 GeV and constrains the high energy phenomenology

the outgoing nucleon participate in the hard sub-process, 149 The experiment was performed during March-June, which is calculable using pQCD. The soft part consists 150 2008 with the CLAS setup at TJNAF using a tagged of all the other partons that are spectators and can be $_{151}$ photon beam produced by bremsstrahlung from the 94 described in terms of GPDs [12]. The HERMES mea- 152 5.72 GeV electron beam provided by the CEBAF ac-95 surement of beam asymmetry in DVCS was the first 153 celerator, which impinged upon a liquid hydrogen tar-96 to confirm the azimuthal dependence expected from the 154 get. The experiment as a whole was a set of different GPD interpretation [13]. The handbag model applica- 155 experiments running at the same time with the same exbility requires a hard scale, which, for meson photopro- 156 perimental conguration (cryogenic target, tagger, trigduction, is only provided by large transverse momentum. 157 ger conguration, and CLAS) and was designated with That corresponds to large angle production, roughly for 158 the name "g12". Particle identication for the exper- $-0.6 \le \cos \theta \le 0.6$. Here, we examined how the hand- 159 iment was based on β vs. momentum×charge. The bag model may extend for the $\gamma p \to p\pi^0$ case as Kroll 160 experimental details are given in Ref. [21]. The reacet al. proposed. The distribution amplitude for the 161 tion of interest is the photoproduction of neutral pions quark+antiquark to π^0 is fixed by other phenomenology 162 on a hydrogen target $\gamma p \to p\pi^0$, where the neutral pions decay into a $e^+e^-\gamma$ final state either due to exter-Binary reactions in QCD, with large momentum trans- 164 nal conversion, $\pi^0 \to \gamma \gamma \to e^+ e^- \gamma$ or via Dalitz decay 107 fer occur via gluon and quark exchanges between collid- 165 $\pi^0 \to \gamma^* \gamma \to e^+ e^- \gamma$. Running the experiment at high ing particles. The constituent counting rules of Brodsky 166 beam current was possible due to the final state containand Farrar [3] has a simple recipe to predict the energy 167 ing three charged tracks, $p; e^+; e^-$, as opposed to single dependence of the differential cross sections of two-body 168 prong charged track detection, which impose limitations

amined in terms of the counting rules [14–18]. As has $_{171}$ straint to the π^0 mass. Once the data was skimmed been observed, first of all at SLAC by Anderson et al., $_{172}$ for p, π^+ , π^- , all particles that were π^+ , π^- were tenthe reaction $\gamma p \to \pi^+ n$ shows agreement with constituent 173 tatively assigned to be electrons or positrons based on

The analysis employed three separate kinematic fitting 179 hypotheses, 4-C, 1-C, and 2-C, as well as a cut on the Previous bremsstrahlung measurements of $\gamma p \to p\pi^0$, 180 missing energy of the detected system. The 4-C fit used for $2 \le E \le 18$ GeV (1964 – 1979) provided 451 data 181 the $\gamma p \to p \pi^+ \pi^-$ channel to filter background from doupoints of $d\sigma/dt(|t|)$ s [19], have very large systematic uncertainties and do not have sufficient accuracy to perform 183 The 1-C fit was used for the topology of $\gamma p \to p e^+ e^- (\gamma)$ comprehensive phenomenological analyses. A previous 184 to fit to a missing final state photon. The 2-C fit was used CLAS measurement of $\gamma p \to p\pi^0$, for 2.0 $\leq E \leq$ 2.9 GeV 185 for the topology of $\gamma p \to p e^+ e^-(\gamma)$ to fit to a missing final has an overall systematic uncertainty of 5% but only pro- 186 state photon but also to constrain the squared invariant mass of $e^+e^-(\gamma)=m_{\pi^0}^2$. The values of the "confidence" The new measurement, presented here, currently is the 188 levels" cuts employed was determined using statistical only measurement that bridges resonance and high en- 189 significance to get the best signal/background ratio. The ergy, both narrow and wide angles, regions of exclusive π^0 190 "confidence levels" for each constraint were consistent photoproduction. This significantly extends the available 191 between g12 data and Monte-Carlo simulations. Montedatabase, facilitating the examination of the resonance, 192 Carlo generation was performed using the PLUTO++

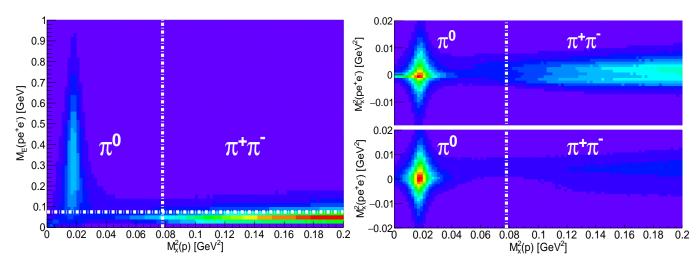


FIG. 1: (Color online)(left panel) $M_x^2(p)$ vs. $M_E(pe^+e^-)$. (Right panel) $M_x^2(p)$ vs. $M_x^2(pe^+e^-)$;(right-top panel) before applying the $M_E(pe^+e^-) < 75 \text{ MeV}$ condition, (right-bottom panel) after applying the $M_E(pe^+e^-) < 75 \text{ MeV}$ condition. The horizontal white dashed-dotted line depicted on the left panel illustrates the 75 MeV threshold used in this analysis. The vertical white dashed-dotted line depicts the kinematic threshold for $\pi^+\pi^-$ production.

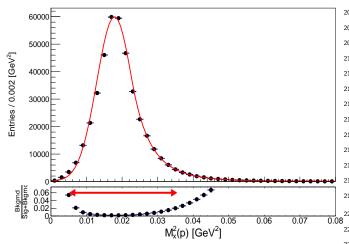


FIG. 2: (Color online) (top-panel) Peak of π^0 in the missing mass of proton for events with $pe^+e^-(\gamma)$ in the final state. The red-solid line depicts the fit function (signal+background). (bottom-panel) Relative contributions of Background Signal+Background. The red arrow indicates the cut placed on the $M_x^2(p)$ distribution to select π^0 events.

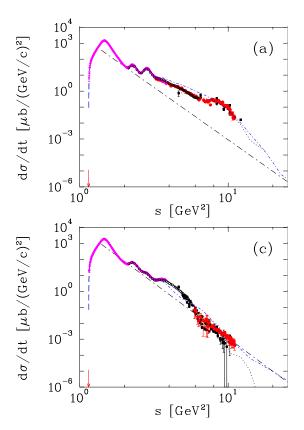
197 comparison of the missing mass squared off the proton, 233 with data from previous CLAS measurements [20], and $_{198}$ $M_x^2(p) = (P_\gamma + P_p - P_p')^2$, where P's are four-momenta $_{234}$ bremsstrahlung DESY, Cambridge Electron Accelerator 199 of the incoming photon, target proton and final state 235 (CEA), and SLAC, and Electron Synchrotron at Cornell 200 proton, and the missing energy of detected system was 236 Univ. experiments [19]. The overall agreement is good, 201 preformed, see Fig. 1. This comparison revealed that the 238 particularly with the previous CLAS data. 202 majority of $\pi^+\pi^-$ background has missing energy less than 75 MeV. To eliminate this background all events $\frac{1}{240}$ angles ($\theta \ge 90^{\circ}$) in c.m., the results are consistent with with a missing energy less than 75 MeV were removed.

207 in Fig. 2. A fit is performed with the Crystal Ball 208 function [24, 25] for the signal, plus a 3rd order poly-209 nomial function for the background. The total sig-210 nal+background fit is shown by a red solid line. The $_{211}$ fit results in $M_{\pi^0}^2=0.0179~{\rm GeV^2}$ and the Gaussian $_{212}$ $\sigma{=}0.0049~{\rm GeV^2}.$ To select π^0 events, an asymmetric cut, 213 from the measured mean value, was placed in the range $_{214} 0.0056 \le M_x^2(p) \le 0.035$. This cut range can be seen 215 as the arrow in the bottom panel of Fig. 2 along with 216 the ratio of background events to the total number of 217 events. As shown in Fig. 2, the event selection strategy for this analysis allowed to have a negligible integrated background of no more than $\sim 1.05\%$.

Overall the systematic uncertainty varies between 9% and 12% as a function of energy. The individual con-222 tributions came from particle efficiency, sector-to-sector 223 efficiency, flux determination, missing energy cut, 4-C, 2-224 C, and 1-C probabilities, target length, branching ratio, 225 fiducial cut, and the z-vertex cut. The largest contribu-226 tions to the systematic uncertainties were the sector-tosector (4.4 - 7.1%), flux determination (5.7%), and the 228 cut on the 1-C pull probability (1.6-6.1%). All system-229 atic uncertainties and their determinations are described 230 in Ref. [22].

The new CLAS high statistics cross sections, presented 231 $_{196}$ $\pi^+\pi^-$ events. To reduce the background further, a $_{232}$ here, for $\gamma p \to \pi^0 p$ are compared in Figs. 3 and 4

At higher energies (above $s \sim 6 \text{ GeV}^2$) and large c.m. the s^{-7} scaling, at fixed t/s, as expected from the con-The distribution of the proton missing mass squared 242 stituent counting rule [3]. The black dash-dotted line at ₂₀₆ for events with $pe^+e^-(\gamma)$ in the final state is shown ₂₄₃ 90° (Fig. 3) is a result of the fit of new CLAS g12 data



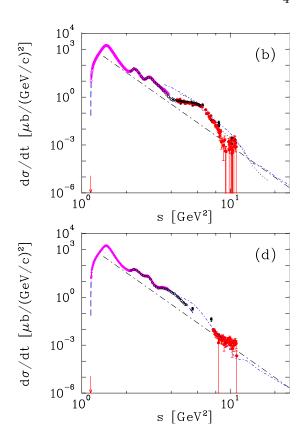


FIG. 3: (Color online) Differential cross section of $\gamma p \to \pi^0 p \, d\sigma/dt(s)$ at polar angles of (a) 50° , (b) 70° , (c) 90° , and (d) 110° in the c.m. frame as a function of c.m. energy squared, s. The red filled circles are the current g12 CLAS data. The recent tagged data are from previous CLAS Collaboration measurements [20] (black open circles) and the A2 Collaboration at MAMI [26] (magenta open diamonds with crosses). While black open filled squares are data from old bremsstrahlung measurements above E = 2 GeV [19]. Plotted uncertainties are statistical. The blue dashed line corresponds to the SAID PWA PR15 solution (no new CLAS g12 data are used for the fit) [26]. Black dot-dashed lines are plotted as the best fit result for the spectrum at 90°. Pion production threshold shown as a vertical red arrow. Regge results [5, 10] are given by black dotted and blue dash-dotted, respectively.

only, performed with a power function $\sim s^{-n}$, leading $_{266} > 4.1$ GeV, where the Regge models [5, 9, 10] predict provide a valid description.

249 models and the handbag [11] model.

Below $|t| \sim 0.6 \text{ GeV}^2$ there is a small difference between ²⁷⁴ mation becomes less relevant below E = 3 GeV (Fig. 4). 276 production below $s = 11 \text{ GeV}^2$ (double solid line). This CLAS data make this statement more apparent. 278 of this dip, in data, prior to this measurement. Note that $\,^{\,}_{283}$ of 1.81 $\,\leq W \leq$ 3.33 GeV. the Regge amplitudes impose non-negligible constraints 284 In this experiment a novel approach was employed $_{264}$ around $|t| \sim 2.6 \text{ GeV}^2$ and possible manifestation of an- $_{287}$ hanced event trigger selectivity enabled the figure of

to $n = 6.89 \pm 0.26$. Oscillations observed at 50° and 70° 267 wrong signature zeroes, this is where the Regge trajectoup to s~10 GeV² indicate that the constituent counting 268 ries cross negative even integers. For the dominant vector rule requires higher energies and higher |t| before it can 269 meson Regge poles, these dips should appear at approx-270 imately $-t = 0.6, 3.0, 5.0 \text{ GeV}^2$, which agrees with the In Figs. 4 and 5, the $d\sigma/dt(|t|)$ values are shown along 271 data. The description of the π^0 photoproduction cross with predictions from Regge pole and cut [5, 7, 9, 10] 272 sections at largest |t| requires some improvement of the 273 Regge model probably by including u-channel exchange.

Fig. 5 shows that the new CLAS data are orders of different Regge approaches. Overall, the Regge approxi- 275 magnitude higher than the handbag model for π^0 photo-

Through the experiments described above, an exten-Note that some small structures start to appear around 279 sive and precise data set (2030 data points) on the dif- $|t| = 0.3 - 0.6 \text{ GeV}^2 (\cos \theta = 0.6 - 0.8) \text{ below E} = 4 \text{ GeV}, \text{ 280 ferential cross section for } \pi^0 \text{ photoproduction from the}$ where, at higher energies, Regge models predict a dip. 281 proton has been obtained for the first time, except for a This is surprising since there was no previous indication 282 few points from previous measurements, over the range

when continued down to the "resonance" region. Our 285 based on Dalitz decay mode. Although this decay mode data show another visible dip above E = 3.6 GeV at 286 has a branching fraction of only about 1%, the enother "possible new structure" around $|t| \sim 5 \text{ GeV}^2$ for E 288 merit to be sufficiently high in order to extend the exist-

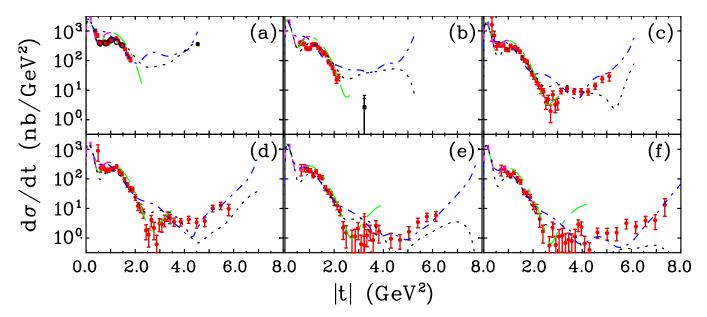


FIG. 4: (Color online) Samples of the π^0 photoproduction cross section, $d\sigma/dt(|t|)$, off the proton versus |t| above "resonance" regime. (a) E = 2825 MeV and W = 2490 MeV, (b) E = 3225 MeV and W = 2635 MeV, (c) E = 3675 MeVand W = 2790 MeV, (d) E = 4125 MeV and W = 2940 MeV, (e) E = 4575 MeV and W = 3080 MeV, and (f) E = 4125 MeV4875 MeV and W = 3170 MeV. Tagged experimental data are from the current CLAS q12 (red filled circles) and a previous CLAS measurement [20] (black open circles). The plotted points from previously published bremsstrahlung experimental data above E = 2 GeV [19] (black filled squares) are those data points within $\Delta E = \pm 3$ MeV of the photon energy in the laboratory system indicated on each panel. The uncertainties plotted are only statistical. Regge results [5, 7, 9, 10] are given by black dotted, blue short dash-dotted, green long dash-dotted, and magenta long dashed lines, respectively.

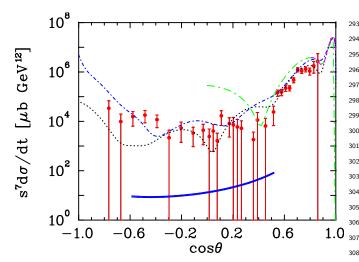


FIG. 5: (Color online) Differential cross section of π^0 photoproduction. The CLAS experimental data at $s = 11 \text{ GeV}^2$ are from the current experiment (red filled circles). The theoretical curves for the Regge fits are the same as in Fig. 4 and the handbag model by Kroll et al. [11] (blue double solid line).

289 ing world measurements into an essentially unmeasured 317 Science and Engineering Foundation. The Southeastern 290 terra incognita domain.

 $_{292}$ $pe^+e^-X(\gamma)$ using a tagged photon beam spanning the $_{320}$ US DOE under contract DEAC05-84ER40150.

293 energy interval covered by "resonance" and "Regge" ²⁹⁴ regimes. The measurements obtained here have been 295 compared to existing data. The overall agreement is good, while the data provided here quadrupled the world bremsstrahlung database above E = 2 GeV and covered the previous reported energies with finer resolution. By comparing this new and greatly expanded data set to 300 the predictions of several phenomenological models, the 301 present data were found to support the Regge pole model 302 and the constituent counting rule while disfavoring the handbag approach.

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