Photoproduction of π^0 on Hydrogen using $e^+e^-(\gamma)$ detection mode with CLAS

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Abstract

We report the first high precision measurement of the exclusive π^0 photoproduction cross section via Dalitz decay and e^+e^- pair conversion mode on a hydrogen target in a wide kinematic range with the CLAS setup at Thomas Jefferson National Accelerator Facility. The measurement was performed in the reaction $\gamma p \to p e^+ e^- X(\gamma)$ using a tagged photon beam spanning an energy interval from the "resonance" to the "Regge" regimes, i.e photon energies E=1.25-5.55 GeV. The final state particles $p; e^+; e^-$ were detected where as the photon was inferred from energy and momentum conservation. This new data sample quadrupled the world bremsstrahlung database above E=2 GeV. Our data appear to favor the Regge pole model and the constituent counting rule while disfavoring the Handbag model.

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of-mass (c.m.) energies up to 2.5 GeV provides insights and challenges concerning the workings of the strong interaction through partial wave expansions, exchange potentials, non-relativistic quark models and QCD. Photoproduction of π^0 and η mesons has always enabled omplementary investigations, constrained various models, and led to further insights. At the interface between the crowded low energy resonance production and the smooth higher energy, small angle behavior, traditionally described by Regge poles [1], lies a region in which hadronic duality interpolates the different excitation function behavior. Exclusive π photoproduction and π nucleon elastic scattering show this duality in a semilocal sense through Finite Energy Sum Rules (FESR) [2]. The connection to QCD is more tenuous for on-shell photoproduction of pions at small scattering angles, but the quark content can become manifest through large fixed angle dimensional counting rules [3] as well as being evident in semi-inclusive or exclusive electroproduction of pions, described through Transverse Momentum Distributions (TMDs) and Generalized Parton Distributions (GPDs). 31

The Regge pole description of photoproduction amplitudes has a long and varied history. For π^0 and η photoproduction, all applications rely on a set of known meson Regge poles. There are two allowed t-channel J^{PC} quantum numbers, the odd-signature (odd spin) 1^{--} (ρ^0 , μ) and the μ -(μ) Reggeons. Regge cut amplitudes are incorporated into some models and are interpreted as rescattering of on-shell meson-nucleon amplitudes. The phases between the different poles and cuts can be critical

The rich pion-nucleon resonance spectrum for center41 in determining the polarizations and the constructive or
42 destructive interferences that can appear. Four distinct
43 Regge models are considered here.

The oldest model developed by Goldstein and 45 Owens [4] has the exchange of leading Regge trajectories 46 with appropriate t-channel quantum numbers along with 47 Regge cuts generated via final state rescattering through 48 Pomeron exchange. The Regge couplings to the nucleon ⁴⁹ were fixed by reference to electromagnetic form factors. $_{50}$ SU(3)_{flavor}, and low energy nucleon-nucleon meson ex-51 change potentials. At the time, the range of applica-52 bility was taken to be above the resonance region and ₅₃ | $t \leq 1.2 \,\mathrm{GeV}^2$, where t is the squared four-momentum ₅₄ transfer. Here we will let the |t| range extend to large |t| in order to see the predicted cross section dips from 56 the zeroes in Regge residues. Because even signature 57 partners $(A_2, \text{ etc.})$ of the odd spin poles $(\rho, \text{ etc.})$ lie on 58 the same trajectories, the Regge residues are required to 59 have zeroes to cancel the even (wrong) signature poles 60 in the physical region - nonsense wrong signature zeroes ₆₁ (NWSZ). While the dip near $t \approx -0.5 \text{ GeV}^2$ is present $_{62}$ in π^0 data, it is not in the recent beam asymmetry data $_{63}$ on η photoproduction [5]. This is not explained by the 64 standard form of the NWSZ Regge residues.

Quite recently, Mathieu et al. [6] (JPAC) (see also [7]), used the same set of Regge poles, but a simplified form of only ω -Pomeron cuts. They show that daughter trajectories are not significant as an alternative to the Regge cuts. However, to explain the lack of $t\approx -0.5~{\rm GeV^2}$ dip in η photoproduction, they remove the standard wrong signature zero, ad hoc. Donnachie and Kalashnikova [8] have included t-channel ρ^0 , ω , and the b_1^0 , but not the have included the hard different parameterizations from Ref. [4]. They include ω , ρ × Pomeron cuts, as well as ω , ρ × f₂ lower lying cuts, which help to fill in the wrong signature zeroes of the ω , ρ Regge pole residues.

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77 The model of Laget and collaborators [9] included u- 135 "Regge", and wide angle QCD regimes of phenomenolso called "saturating" the Regge trajectories at $\alpha(t) \to -1$ 138 both Regge and QCD-based models of the nucleon [20]. for $t < -1.5 \text{ GeV}^2$, thereby describing the full angular 139 In this work, we provide a large set of differential cross $_{82}$ range ($\theta=0-2\pi$), while the other models are good $_{140}$ section values from E=1.275 to 5.425 MeV in labofor more limited ranges of t [4, 6, 8]. Here, we examine 141 ratory photon energy, corresponding to a range of c.m. ₈₄ how Regge phenomenology works for the energy range of $_{142}$ energies, W=1.81-3.33 GeV. We have compared the $2.8 \text{ GeV} < E_{\gamma} < 5.5 \text{ GeV}.$

the incoming and one from the outgoing nucleon par- 149 well with a previous CLAS measurement [19]. of the productions cross section.

Binary reactions in QCD, with large momentum trans- 165 due to trigger and data acquisition restrictions. 108 fer occur via gluon and quark exchanges between collid- 166 115 As has been observed, first of all at SLAC by Ander- 176 cuts [21] and timing cuts were applied in the analysis. son et al., the reaction $\gamma p \to \pi^+ n$ shows agreement with 175 Different kinematic fittings were employed to cleanly 117 constituent counting rules that predict the cross section 176 identify the $\gamma p \to p e^+ e^-(\gamma)$ reaction. They were aprule is for $\gamma p \to \pi^0 p$ up to $s = 10 \text{ GeV}^2$.

certainties and do not have sufficient accuracy to perform 184 signal/background ratio. comprehensive phenomenological analyses. A previous 185 vided 164 data points of $d\sigma/dt(|t|)$ s [19].

The results described here are the first to allow a de- 189 ration [23]. tailed analysis, bridging the nucleon resonance and high 191 energy regions over a wide angular range, of exclusive $_{192}$ $\pi^+\pi^-$ events. To reduce the background further, a

channel baryon exchange. That model also connected 136 ogy. The broad range of c.m. energy, \sqrt{s} , is particularly the small and large t-channel regimes by a mechanism 137 helpful in sorting out the phenomenology associated with

143 Regge pole, the handbag, and the constituent counting In addition to Regge pole models, the introduction of 144 rule phenomenology with the new CLAS experimental inthe handbag mechanism, developed by Kroll et al. [10], 145 formation on $d\sigma/dt(|t|)$ for the $\gamma p \to \pi^0 p$ reaction above has provided complimentary possibilities for the inter- 146 the "resonance" regime. As will be seen, this data set pretation of hard exclusive reactions. In this approach, 147 quadruples the world bremsstrahlung database above E the reaction is factorized into two parts, one quark from 148 = 2 GeV and constrains the high energy phenomenology

ticipate in the hard sub-process, which is calculable us- 150 The experiment was performed during March-June, 93 ing pQCD. The soft part consists of all the other par- 151 2008 with the CLAS setup at TJNAF using a tagged tons that are spectators and can be described in terms of 152 photon beam produced by bremsstrahlung from the GPDs [11]. The HERMES measurement of beam asym- 153 5.72 GeV electron beam provided by the CEBAF ac-₉₆ metry in DVCS was the first to confirm the azimuthal ₁₅₄ celerator, which impinged upon a liquid hydrogen tardependence expected from the GPD interpretation [12]. 155 get, and was designated with the name "g12". The The handbag model applicability requires a hard scale, 156 experimental details are given in Ref. [21]. The reacwhich, for meson photoproduction, is only provided by 157 tion of interest is the photoproduction of neutral pions large transverse momentum. That corresponds to large 158 on a hydrogen target $\gamma p \to p\pi^0$, where the neutral piangle production, roughly for $-0.6 \le \cos\theta \le 0.6$. Here, 159 ons decay into a $e^+e^-\gamma$ final state either due to exterwe examined how the handbag model may extend for the 160 nal conversion, $\pi^0 \to \gamma \gamma \to e^+e^-\gamma$ or via Dalitz decay $\gamma p \to p \pi^0$ case as Kroll et al. proposed. The distribu- $_{161} \pi^0 \to \gamma^* \gamma \to e^+ e^- \gamma$. Running the experiment at high tion amplitude for the quark+antiquark to π^0 is fixed by 162 beam current was possible due to the final state containother phenomenology and leads to the strong suppression 163 ing three charged tracks, $p; e^+; e^-$, as opposed to single prong charged track detection, which impose limitations

Particle identification for the experiment was based ing particles. The constituent counting rules of Brod- 167 on β vs. momentum×charge. Lepton identification was $_{110}$ sky and Farrar [3] has a simple recipe to predict the $_{168}$ based on a kinematic constraint to the π^0 mass. Once energy dependence of the differential cross sections of 169 the data was skimmed for p, π^+ , π^- , all particles that two-body reactions at large angles when t/s is finite and 170 were π^+ , π^- were tentatively assigned to be electrons or is kept constant. The lightest meson photoproduction 171 positrons based on their charge (for details, see Ref. [22]). was examined in terms of the counting rules [13–17]. 172 After particle selection, standard g12 calibration, fiducial

should vary as s^{-7} [13]. The agreement extends down plied to filter background from misidentified double pion to $s=6~{\rm GeV^2}$ where baryon resonances are still playing production to the single π^0 production, to constrain the a role. Here, we examined how applicable the counting 179 missing mass of entire final state to a missing photon 180 and to ensure that the fit to the missing photon con-Previous bremsstrahlung measurements of $\gamma p \to p \pi^0$, 181 strained the squared invariant mass of $e^+e^-(\gamma)=m_{\pi^0}^2$. for $2 \le E \le 18$ GeV (1964 – 1979) provided 451 data 182 The values of the confidence levels cuts employed was points of $d\sigma/dt(|t|)$ s [18], have very large systematic un- 183 determined using statistical significance to get the best

The confidence levels for each constraint were con-CLAS measurement of $\gamma p \to p \pi^0$, for $2.0 \le E \le 2.9 \text{ GeV}$ 186 sistent between g12 data and Monte-Carlo simulations. as an overall systematic uncertainty of 5% but only pro- 187 tions. Monte-Carlo generation was performed using the 188 PLUTO++ package developed for the HADES Collabo-

The remainder of the background was attributed to pion photoproduction. By significantly extending the database they facilitate the examination of the resonance, 194 $M_x^2(p) = (P_\gamma + P_p - P_p')^2$, where P's are four-momenta

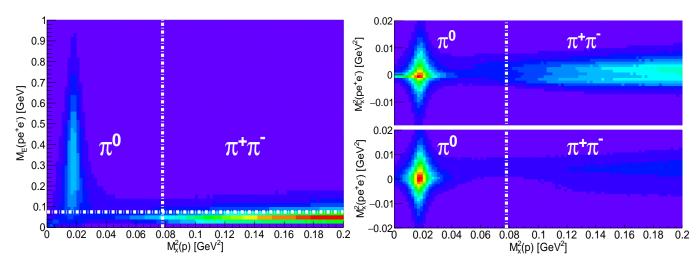


FIG. 1: (Color online)(left panel) $M_x^2(p)$ vs. $M_E(pe^+e^-)$. (Right panel) $M_x^2(p)$ vs. $M_x^2(pe^+e^-)$;(right-top panel) before applying the $M_E(pe^+e^-) < 75 \text{ MeV}$ condition, (right-bottom panel) after applying the $M_E(pe^+e^-) < 75 \text{ MeV}$ condition. The horizontal white dashed-dotted line depicted on the left panel illustrates the 75 MeV threshold used in this analysis. The vertical white dashed-dotted line depicts the kinematic threshold for $\pi^+\pi^-$ production.

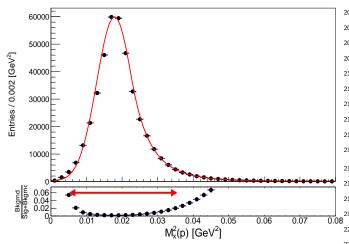


FIG. 2: (Color online) (top-panel) Peak of π^0 in the missing mass of proton for events with $pe^+e^-(\gamma)$ in the final state. The red-solid line depicts the fit function (signal+background). (bottom-panel) Relative contributions of Background Signal+Background. The red arrow indicates the cut placed on the $M_x^2(p)$ distribution to select π^0 events.

195 of the incoming photon, target proton and final state 231 (CEA), and SLAC, and Electron Synchrotron at Cornell 196 proton, and the missing energy of detected system was 232 Univ. experiments [18] and lower c.m. energy MAMI performed, see Fig. 1. This comparison revealed that the 233 A2 measurements [26]. The overall agreement is good, ₁₉₈ majority of $\pi^+\pi^-$ background has missing energy less ₂₃₆ particularly with the previous CLAS data. than 75 MeV. To eliminate this background all events with a missing energy less than 75 MeV were removed.

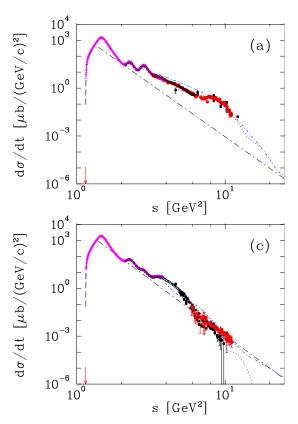
for events with $pe^+e^-(\gamma)$ in the final state is shown 239 counting rule [3]. The black dash-dotted line at 90° ₂₀₃ in Fig. 2. A fit was performed with the Crystal Ball ₂₄₀ (Fig. 3) is a result of the fit of new CLAS q12 data only, ₂₀₄ function [24, 25] for the signal, plus a 3rd order poly-₂₄₁ performed with a power function $\sim s^{-n}$, leading to n

206 nal+background fit is shown by a red solid line. The 207 fit resulted in $M_{\pi^0}^2 = 0.0179 \; {\rm GeV^2}$ and the Gaussian $\sigma = 0.0049 \text{ GeV}^2$. To select π^0 events, an asymmetric cut, 209 from the measured mean value, was placed in the range $_{210} 0.0056 \le M_x^2(p) \le 0.035$. This cut range can be seen 211 as the arrow in the bottom panel of Fig. 2 along with 212 the ratio of background events to the total number of 213 events. As shown in Fig. 2, the event selection strategy 214 for this analysis led to a negligible integrated background estimated to be no more than 1.05%.

Overall the systematic uncertainty varied between 9% and 12% as a function of energy. The individual contri-218 butions came from particle efficiency, sector-to-sector efficiency, flux determination, missing energy cut, the kinematic fitting probabilities, target length, branching ratio, fiducial cut, and the z-vertex cut. The largest contribu-222 tions to the systematic uncertainties were the sector-tosector (4.4 - 7.1%), flux determination (5.7%), and the 224 cut on the 1-C pull probability (1.6-6.1%). All system-225 atic uncertainties and their determinations are described 226 in Ref. [22].

The new CLAS high statistics cross sections, presented 228 here, for $\gamma p \rightarrow \pi^0 p$ are compared in Figs. 3 and 4 229 with data from previous CLAS measurements [19], and 230 bremsstrahlung DESY, Cambridge Electron Accelerator

At higher energies (above $s \sim 6 \text{ GeV}^2$) and large c.m. angles ($\theta \geq 90^{\circ}$), the results are consistent with the s^{-7} The distribution of the proton missing mass squared 238 scaling, at fixed t/s, as expected from the constituent ₂₀₅ nomial function for the background. The total sig-₂₄₂ = 6.89±0.26. Structures observed at 50° and 70° up to



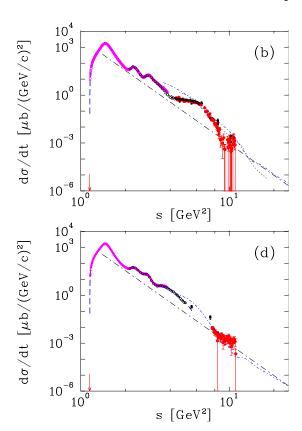


FIG. 3: (Color online) Differential cross section of $\gamma p \to \pi^0 p \, d\sigma/dt(s)$ at polar angles of (a) 50° , (b) 70° , (c) 90° , and (d) 110° in the c.m. frame as a function of c.m. energy squared, s. The red filled circles are the current g12 CLAS data. The recent tagged data are from previous CLAS Collaboration measurements [19] (black open circles) and the A2 Collaboration at MAMI [26] (magenta open diamonds with crosses). While black open filled squares are data from old bremsstrahlung measurements above E = 2 GeV [18]. Plotted uncertainties are statistical. The blue dashed line corresponds to the SAID PWA PR15 solution (no new CLAS g12 data are used for the fit) [26]. Black dot-dashed lines are plotted as the best fit result of the power function s^{-n} , with $n = 6.89 \pm 0.26$, for the spectrum at 90° . Pion production threshold is shown as a vertical red arrow. Regge results [4, 9] are given by black dotted and blue dash-dotted, respectively.

²⁴³ s∼10 GeV² indicate that the constituent counting rule ²⁶⁴ ries cross negative even integers. For the dominant vector vide a complete description.

247 els and the handbag [10] model.

Below $|t| \sim 0.6 \text{ GeV}^2$ there is a small difference be- 270 (Fig. 4). Note that some small dips start to appear 278 line). around $|t| = 0.6 \text{ GeV}^2$ $(\cos \theta = 0.6 - 0.8)$ where 275 when continued down to the "resonance" region. Our 280 of 1.81 $\leq W \leq$ 3.33 GeV. data show another visible dip above E = 3.6 GeV at 281 In this experiment a novel approach was employed

requires higher energies and higher |t| before it can pro- 265 meson Regge poles, these dips should appear at approx- $_{266}$ imately $-t=0.6, 3.0, 5.0 \text{ GeV}^2$, which agrees with the In Figs. 4 and 5, the $d\sigma/dt(|t|)$ results are shown along 267 data. The description of the π^0 photoproduction cross with predictions from Regge pole and cut [4, 6, 8, 9] mod- 268 sections at largest |t| requires improving the Regge model 269 by including additional exchange mechanisms.

Fig. 5 shows that the new CLAS data are orders of tween different Regge approaches. Overall, the Regge 271 magnitude higher than the handbag model prediction [10] approximation becomes less applicable below $E=3~{\rm GeV}^2$ for π^0 photoproduction below $s=11~{\rm GeV}^2$ (double solid

Through the experiments described above, an extenthe Regge models predict a dip. The dip at about 276 sive and precise data set (2030 data points) on the dif- $|t| \sim 5 \text{ GeV}^2$ is best modeled by [6]. Prior to this mea- 277 ferential cross section for π^0 photoproduction from the surement there was no indication of these dips Note that 278 proton has been obtained for the first time, except for a the Regge amplitudes impose non-negligible constraints 279 few points from previous measurements, over the range

around $|t| \sim 2.6 \text{ GeV}^2$ and possible manifestation of an- 282 based on Dalitz decay mode. Although this decay mode 261 other "possible new structure" around $|t| \sim 5 \text{ GeV}^2$ for 283 has a branching fraction of only about 1%, the en-262 E > 4.1 GeV, where the Regge models [4, 8, 9] predict 284 hanced event trigger selectivity enabled the figure of 263 wrong signature zeroes, this is where the Regge trajecto- 285 merit to be sufficiently high in order to extend the exist-

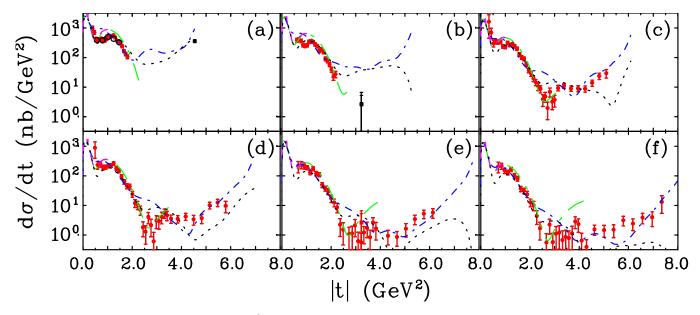


FIG. 4: (Color online) Samples of the π^0 photoproduction cross section, $d\sigma/dt(|t|)$, off the proton versus |t| above "resonance" regime. (a) E = 2825 MeV and W = 2490 MeV, (b) E = 3225 MeV and W = 2635 MeV, (c) E = 3675 MeVand W = 2790 MeV, (d) E = 4125 MeV and W = 2940 MeV, (e) E = 4575 MeV and W = 3080 MeV, and (f) E = 4125 MeV4875 MeV and W = 3170 MeV. Tagged experimental data are from the current CLAS q12 (red filled circles) and a previous CLAS measurement [19] (black open circles). The plotted points from previously published bremsstrahlung experimental data above E = 2 GeV [18] (black filled squares) are those data points within $\Delta E = \pm 3$ MeV of the photon energy in the laboratory system indicated on each panel. The uncertainties plotted are only statistical. Regge results [4, 6, 8, 9] are given by black dotted, blue short dash-dotted, green long dash-dotted, and magenta long dashed lines, respectively.

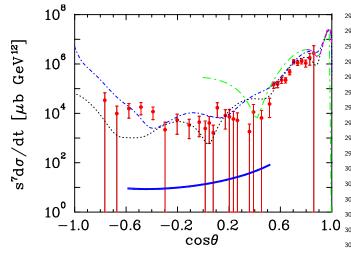


FIG. 5: (Color online) Differential cross section of π^0 photoproduction. The CLAS experimental data at $s = 11 \text{ GeV}^2$ are from the current experiment (red filled circles). The theoretical curves for the Regge fits are the same as in Fig. 4 and the handbag model by Kroll et al. [10] (blue double solid line).

286 ing world measurements into an essentially unmeasured 314 Science and Engineering Foundation. The Southeastern terra incognita domain.

 $_{289}$ $pe^+e^-X(\gamma)$ using a tagged photon beam spanning the $_{317}$ US DOE under contract DEAC05-84ER40150.

290 energy interval covered by "resonance" and "Regge" ²⁹¹ regimes. The measurements obtained here have been 292 compared to existing data. The overall agreement is good, while the data provided here quadrupled the world bremsstrahlung database above E = 2 GeV and covered the previous reported energies with finer resolution. By comparing this new and greatly expanded data set to 297 the predictions of several phenomenological models, the present data were found to support the Regge pole model and the constituent counting rule while disfavoring the handbag approach.

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