March Madness Analysis

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March Madness is an annual NCAA Division I Basketball tournament. The tournament occurs in the month of March, thereby earning its name. There are 64 teams in the tournament each year, seeded into four regions that each contain 16 teams. This report will look at how far each team makes it into the tournament, based on their regular season data and prior tournament success.

Introduction

In this report we work with data that was obtained from kaggle.com. We were interested to see what factors most affect a team's success in the March Madness tournament, so we compare teams to each other for every year that we have data. In doing so, we narrow down our predictors to find the best model of a team's success in the tournament for each year.

We were motivated to look into this data in part because the tournament is so hard to predict from year to year. We wondered what statistics and data from a team's season and history could be used to estimate how far the team would make it in the tournament. It is not uncommon for there to be many upsets over the course of the tournament, which can throw off any model, so we had to consider this uncertainty when choosing the best model.

Data Summary

From Kaggle's website, we downloaded a data set that gave us a look at all Division I teams who did or did not qualify for the March Madness tournament in the past 30 or so years. Each team is assigned a four digit code that is consistent from season to season and data set to data set. This allows us to manipulate and analyze the data across the different files.

We had data that was collected during the regular season and data that was collected during the tournament, but in the long run choose to focus our model on regular season data so as to be able to predict the current season's tournament success if need be.

For the years 1985 to 2003, we have data in regards to the wins and losses of each involved team. For the years 2003 to 2016, we have more in depth data that includes each team's statistics from each game all season and throughout the tournament.

We began by looking at the data that has been collected season to season and follow up by looking at the data from previous tournaments and regional and past seed data to see which factors effect a team's chances of winning games in the tournament.

Because this tournament occurs each year, and because our data spans many years, we also saw it fitting to analyze how well teams had performed in the past when trying to predict their success in the future. The expectations and reputation of a team surely have an impact on how well they perform during the season and tournament, so temporal data about past success was essential to our model.

Throughout this report, let the following be universally true:

Field Goals: defined as any shot that is made in the game and is worth 2 points (within the 3 point line, not a free throw)

Three Pointers: defined as any shot that is made in the game and is worth 3 points (outside the 3 point line, from any place)

Free Throws: defined as any shot that is made in the game and is worth 1 point (shot after being fouled in any form, from the free throw line)

Assist: defined as a pass to another player who then immediately scores

Rebound: defined as a play in which a player grabs the ball, which bounced off of either the rim or backboard on an attempted shot. For this paper, we include offensive and defensive rebounds

Turnovers: defined as any action that results in the loss of basketball. (an action that gives the basketball to the other team not including a failed shot attempt)

Steals: defined as a defensive play in which a player steals the basketball from an opposing player

Block: defined as a defensive play in which a player deflects an opposing shot attempt before it reaches the basket

Personal Fouls: defined as an action that results in either a loss of possession or free throws for the other team

Pre-Analysis

We began by looking at our data from a lens that based winning teams against losing teams. This was based on who won and lost each game of each season, so it is important to note that it is likely that teams would fall into both categories on occasion. We hoped to find what factors and variables in a season could predict a team's overall success in the tournament and moving forward.

We already had easy access to data that was parsed based on which team had won and which team had lost, so this seemed like a logical first step. We chose to keep regular season data apart from tournament data because the game play is so different in the tournament. In general, it is expected that the involved teams are among the best in the country, and the games have much higher stakes, so statistics may look different.

Regular Season Data

In working with the regular season data, we first looked at some larger scale averages, comparing winning teams to losing teams on a very basic level.

We compared the average statistics of winning teams to the average statistics of losing teams and found what many would expect: on average, winning teams perform better in areas that are considered "good"

statistics, whereas losing teams have higher rates of "bad" statistics.

Per Game Averages

Per Game Averages
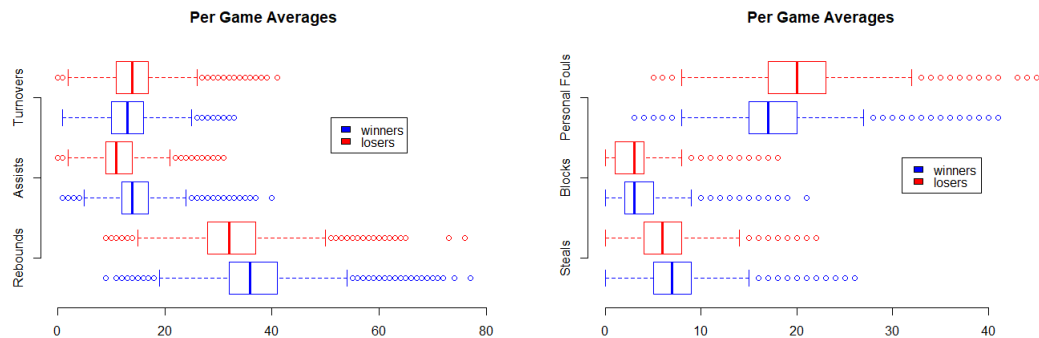
The above figures show the distribution of the winning and losing teams' averages throughout the years. They illustrate the above point that winning teams have higher averages in more beneficial statistics such as Rebounds, Assists, and Steals. This is a trend that we take note of when moving forward.

We then looked at winning and losing teams' average shooting percentages for the regular season. We were hoping to find which shots hold the most weight in the game. For example, three point shots are worth more points than any other shots, but free throws offer up an easy opportunity for a point or two and may be necessary late in the game.
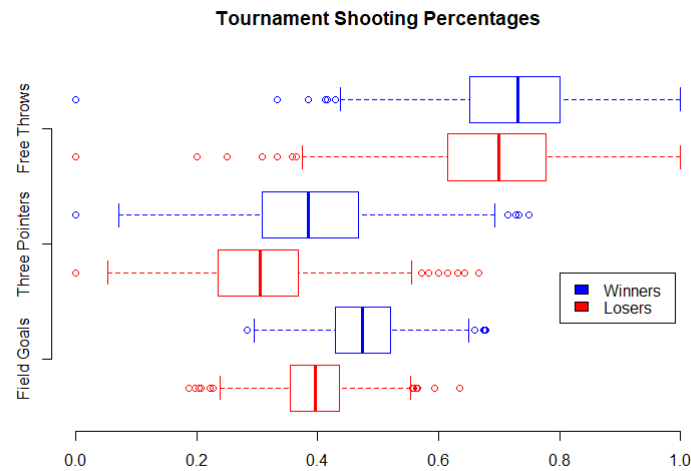
Season Shooting Percentages
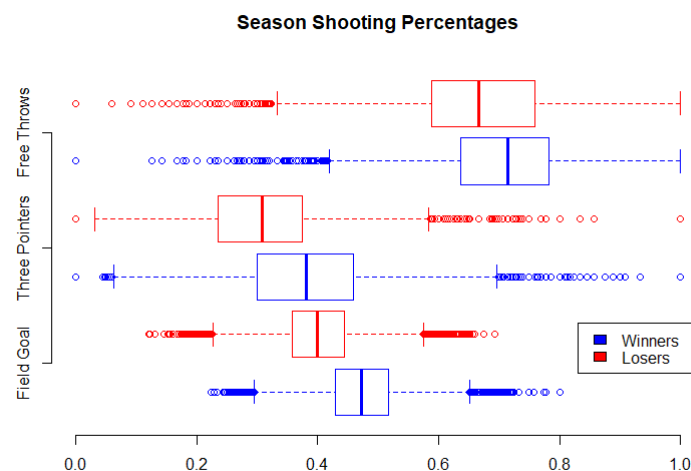
This figure visualizes the differences that exist, on average, in winning and losing teams' shot percentages. There are a large number of outliers in this plot, which should be noted for future analysis. It is also hard to tell which shots look to be more influential in the winning of a game because the data is so wide-spread.

Tournament Data

Much the same as when we worked with the regular season data, we analyzed the tournament data at first on a more basic level of winning teams versus losing teams. Much of the data that we had

for tournaments was centered on the teams' abilities to score. We analyzed their shooting percentages during the tournaments and compared average winning teams to average losing teams.

Tournament Shooting Percentages

As the above figure illustrates, winning teams, on average, have higher shooting percentages in all categories. It is essential to note how large the differences may be. From this data we can start to decide which types of shots are the most important to tournament success.

History of Success

As a result of looking at our data, and through our own personal knowledge of the sport, we decided it was fitting to look into each team's history of success in the tournament and how often they had been seeded near the top.

Overall Leaders (1985–2015)
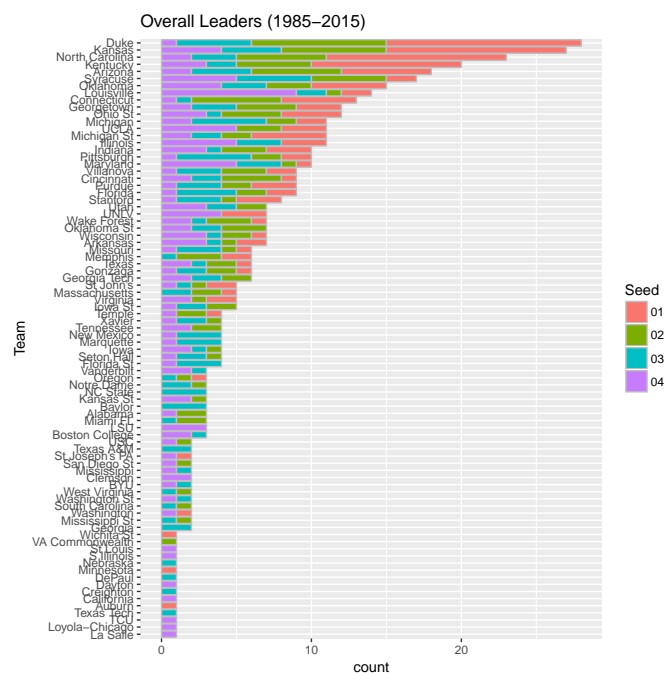
The above figure maps how often teams have been seeded among the top four, for any region in the tournament. Teams that have been successful in the past are more likely to be seeded near the top again in the future, as is pictured above. The teams near the top of this chart are those that are commonly discussed amongst basketball fans. They are teams that come from schools that are known for basketball, and they likely draw in more talented players as a result of their reputation, helping them further develop their program.

We continue this analysis of History of Success by looking at teams that are all-around leaders in past tournaments. We look at each team's past appearances in the tournament to compare them to each other.

History of Success(1985–2015)
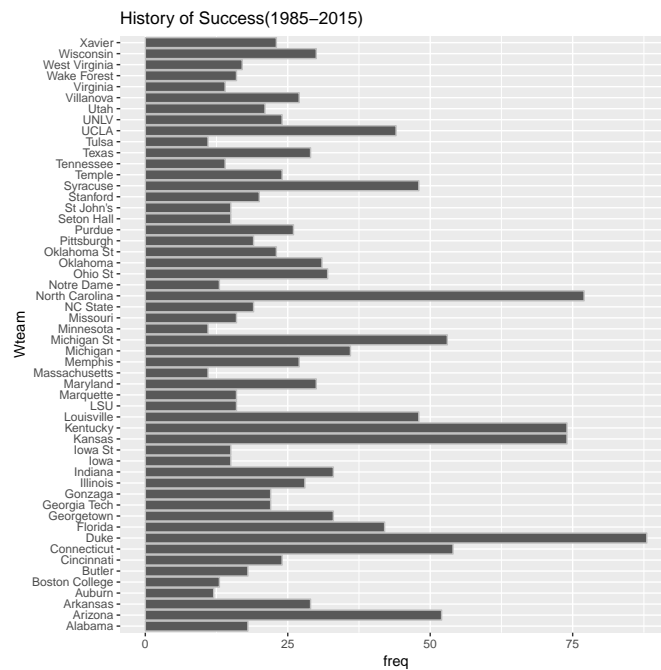
The figure above shows some of the teams with the most appearances in the March Madness tournament. Higher frequency logically relates to a better team, and this data allows us to see which teams are consistently present and performing in the tournament.

Initial Model

$$Y_{daynum} = \beta_0 + \beta_{conf} + \beta_{fgp} + \beta_{tpp} + \beta_{ass} + \beta_{rb} + \beta_{app} + \epsilon$$

Our original model contained all of the predictors that we felt would be the most important moving forward. These predictors and subscripts are outlined below:

- The response variable, *daynum*, signifies what day of the year the last game is played for each team. This is a good measure of two things: If a team makes the tournament and how far that team advances.

- *conf:* the conference the team plays in - different conferences have vastly different quality of teams

- *fgp:* refers to field goal percentage

- *tpp:* three point shooting percentage

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- *ass:* assists

- *rb:* rebounds

- *app:* prior tournament success - indicated by number of previous appearances in the tournament

Seed is not included because seeding is almost entirely determined by conference and record. Record is left out because it is in large part determined by a teams statistics, which we have included in the model.

Processing

In working with our data to develop a model, we realized that there may be a better way to interpret it. We also ran into problems with some predictors and variables because they were quite difficult to quantify or compare.

We found that *daynum* may not be the best measure of a team's success in the tournament because the respective games of a tournament are played on slightly different days each year. This means that the team who won the tournament in 2003 could have a higher daynum than the team who won the tournament in 2004, automatically ranking the 2003 team higher, although they played and won the same number of games.

We also found that *conf* was difficult to quantify because while some conferences are undoubtedly better than others, it is not up to our judgment as to decide how much better they are and which conferences deserve to be credited as the best.

Data Plumbing

Data Reconstruction

Full Model

$$Y_{GP_{year}} = \beta_0 + \beta_{avgScore} + \beta_{avgASS} + \beta_{avgFT} + \beta_{avgPF} + \beta_{avgTP} + \beta_{avgRB} + \beta_{avgTO}$$

$$+\beta_{avgSTL} + \beta_{avgBL} + \beta_{GP_{year-1}} + \epsilon$$

We fit a full model with all of the possible predictors that we pulled from the data. The full list of predictors includes:

- GP_{year}: number of games the team plays in the tournament in a given year

- *avgScore:* average score per team per game in regular season

- *avgASS:* average assists per team per game in regular season

- *avgFT:* average free throws per team per game in regular season

- *avgPF:* average personal fouls per team per game in regular season

- *avgTP:* average three point shots made per team per game in regular season

- *avgRB:* average total rebounds per team per game in regular season

- *avgTO:* average turnovers per team per game in regular season

- *avgSTL:* average steals per team per game in regular season

- *avgBL:* average blocks per team per game in regular season

- GP_{year-1}: number of games the team plays in the tournament in the prior year

We formed this model for each year from 2004 to 2015 because those are the years that we have the most data for, and we seek out the model with the highest R^2 value because it accounts for the most variation in the response. The coefficients and summary of some of the models are shown below:

```
> prev4 = addPriorYear(2,avgsZ,TRUE)
> fit04 = lm(GP04~.,prev4[,-1])
> summary(fit04)

Call:
lm(formula = GP04 ~ ., data = prev4[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.7484 -0.6289 -0.1841  0.5283  3.5693

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.476693    2.445436  -1.013   0.3157
avgScore04  -0.003557    0.084844  -0.042   0.9667
avgFG04      0.208241    0.238282   0.874   0.3860
avgTP04      0.111249    0.147521   0.754   0.4541
avgFT04            NA          NA      NA       NA
avgRB04      0.011671    0.018473   0.632   0.5302
avgASS04    -0.128551    0.119710  -1.074   0.2877
avgTO04     -0.239030    0.112035  -2.134   0.0374 *
avgSTL04    -0.124997    0.123520  -1.012   0.3161
avgBL04      0.328675    0.133100   2.469   0.0167 *
avgPF04      0.162716    0.105641   1.540   0.1293
GP03         0.076130    0.112047   0.679   0.4998
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.125 on 54 degrees of freedom
Multiple R-squared:  0.3546,Adjusted R-squared:  0.2351
F-statistic: 2.967 on 10 and 54 DF,  p-value: 0.004799

>
> prev9 = addPriorYear(7,avgsZ,TRUE)
> fit09 = lm(GP09~.,prev9[,-1])
> summary(fit09)

Call:
lm(formula = GP09 ~ ., data = prev9[, -1])
```

```
Residuals:
    Min      1Q  Median      3Q     Max
-1.6153 -0.6350 -0.1082  0.5441  2.6755


Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.17350    2.63262  -0.066 0.947699
avgScore09   0.22102    0.06561   3.369 0.001400 **
avgFG09     -0.59909    0.19117  -3.134 0.002789 **
avgTP09     -0.39458    0.12390  -3.185 0.002407 **
avgFT09          NA         NA      NA       NA
avgRB09      0.01778    0.01539   1.155 0.253025
avgASS09     0.34903    0.10525   3.316 0.001636 **
avgTO09     -0.03090    0.10399  -0.297 0.767497
avgSTL09     0.19539    0.12018   1.626 0.109797
avgBL09     -0.08933    0.11806  -0.757 0.452553
avgPF09     -0.15114    0.10048  -1.504 0.138351
GP08         0.28387    0.07955   3.568 0.000763 ***
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1


Residual standard error: 0.9419 on 54 degrees of freedom
Multiple R-squared:  0.5478,Adjusted R-squared:  0.4641
F-statistic: 6.542 on 10 and 54 DF,  p-value: 1.58e-06


>
> prev15 = addPriorYear(13,avgsZ,TRUE)
> fit15 = lm(GP15~.,prev15[,-1])
> summary(fit15)

Call:
lm(formula = GP15 ~ ., data = prev15[, -1])

Residuals:
    Min      1Q   Median      3Q     Max
-2.13475 -0.74144 -0.07461  0.59031  2.93999


Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.137942    2.505740  -0.454  0.65146
avgScore15   0.009128    0.087329   0.105  0.91712
avgFG15      0.222098    0.204176   1.088  0.28127
avgTP15     -0.161144    0.132683  -1.215  0.22956
avgFT15           NA          NA      NA       NA
avgRB15      0.018762    0.013055   1.437  0.15615
avgASS15    -0.062710    0.100166  -0.626  0.53378
avgTO15     -0.156939    0.122918  -1.277  0.20686
avgSTL15     0.055784    0.118423   0.471  0.63940
avgBL15     -0.035234    0.118800  -0.297  0.76787
avgPF15     -0.042033    0.082793  -0.508  0.61363
GP14         0.372234    0.099741   3.732  0.00044 ***
```

```
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.011 on 57 degrees of freedom
Multiple R-squared:  0.4606,Adjusted R-squared:  0.366
F-statistic: 4.868 on 10 and 57 DF,  p-value: 4.65e-05
```

The above code output shows the coefficients for three models, from years 2004, 2009, and 2015. Clearly, the R^2 values vary from model to model, but we found that the model from 2009 had the highest R^2 value and the most significant figures when compared to the other full models.

Full Model Analysis

Final Model

$$Y_{GP_{year}}^{-0.5} = \beta_0 + \beta_{avgASS} + \beta_{avgFT} + \beta_{avgPF} + \beta_{avgFG} + \beta_{avgTO} + \beta_{GP_{year-1}} + \epsilon$$

Final Model Analysis

Predictions

Further Research

Appendix

Summary output for full model:

```
> prev14 = addPriorYear(12,avgsZ,TRUE)
> fit14 = lm(GP14˜.,prev14[,-1])
> summary(fit14)

Call:
lm(formula = GP14 ˜ ., data = prev14[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.6535 -0.6375 -0.1490  0.3945  3.7843

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.301180   2.745766   1.931   0.0585 .
avgScore14  -0.104674   0.083860  -1.248   0.2171
avgFG14      0.309636   0.239501   1.293   0.2013
```

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```
avgTP14      0.156841   0.153644   1.021   0.3117
avgFT14           NA         NA      NA       NA
avgRB14      0.009232   0.018780   0.492   0.6249
avgASS14    -0.053165   0.107422  -0.495   0.6226
avgTO14     -0.209756   0.127291  -1.648   0.1049
avgSTL14    -0.145048   0.133040  -1.090   0.2802
avgBL14      0.275043   0.145680   1.888   0.0641 .
avgPF14     -0.106358   0.110073  -0.966   0.3380
GP13         0.082681   0.126693   0.653   0.5166
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.208 on 57 degrees of freedom
Multiple R-squared:  0.2437,Adjusted R-squared:  0.1111
F-statistic: 1.837 on 10 and 57 DF,  p-value: 0.07443


>
> prev13 = addPriorYear(11,avgsZ,TRUE)
> fit13 = lm(GP13~.,prev13[,-1])
> summary(fit13)

Call:
lm(formula = GP13 ~ ., data = prev13[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.8786 -0.6606 -0.1628  0.5599  3.1439

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept)  3.30169    3.04878   1.083   0.2834
avgScore13  -0.06515    0.09446  -0.690   0.4932
avgFG13      0.20597    0.23302   0.884   0.3805
avgTP13      0.08966    0.15024   0.597   0.5530
avgFT13           NA         NA      NA       NA
avgRB13      0.01222    0.02041   0.599   0.5516
avgASS13    -0.14487    0.11411  -1.270   0.2094
avgTO13     -0.04789    0.12670  -0.378   0.7068
avgSTL13     0.29211    0.13630   2.143   0.0364 *
avgBL13      0.01784    0.14977   0.119   0.9056
avgPF13     -0.16485    0.12234  -1.347   0.1832
GP12         0.25061    0.11103   2.257   0.0279 *
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.154 on 57 degrees of freedom
Multiple R-squared:  0.3101,Adjusted R-squared:  0.1891
F-statistic: 2.562 on 10 and 57 DF,  p-value: 0.01243


>
> prev12 = addPriorYear(10,avgsZ,TRUE)
```

```
> fit12 = lm(GP12~.,prev12[,-1])
> summary(fit12)

Call:
lm(formula = GP12 ~ ., data = prev12[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-2.3717 -0.6724 -0.1912  0.4705  2.8825

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept)  3.58332    2.81280   1.274  0.20786
avgScore12  -0.17995    0.08624  -2.087  0.04141 *
avgFG12      0.36211    0.25401   1.426  0.15945
avgTP12      0.01410    0.13270   0.106  0.91576
avgFT12           NA         NA      NA       NA
avgRB12      0.06054    0.02019   2.999  0.00402 **
avgASS12    -0.06248    0.13882  -0.450  0.65437
avgTO12     -0.01225    0.11686  -0.105  0.91686
avgSTL12     0.10954    0.12354   0.887  0.37899
avgBL12      0.07202    0.15598   0.462  0.64602
avgPF12     -0.04097    0.10304  -0.398  0.69239
GP11         0.22083    0.10731   2.058  0.04419 *
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.075 on 57 degrees of freedom
Multiple R-squared:  0.3898,Adjusted R-squared:  0.2827
F-statistic: 3.641 on 10 and 57 DF,  p-value: 0.0008516

>
> prev11 = addPriorYear(9,avgsZ,TRUE)
> fit11 = lm(GP11~.,prev11[,-1])
> summary(fit11)

Call:
lm(formula = GP11 ~ ., data = prev11[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.5599 -0.7117 -0.3055  0.4825  4.0113

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept)  2.261465   2.888834   0.783   0.4370
avgScore11  -0.007744   0.092958  -0.083   0.9339
avgFG11      0.256092   0.263395   0.972   0.3350
avgTP11      0.162204   0.166759   0.973   0.3348
avgFT11           NA         NA      NA       NA
avgRB11      0.013038   0.018242   0.715   0.4777
```

```
avgASS11   -0.293256   0.135765   -2.160   0.0350 *
avgTO11    -0.046868   0.145977   -0.321   0.7493
avgSTL11    0.108027   0.140027    0.771   0.4436
avgBL11     0.014608   0.162108    0.090   0.9285
avgPF11    -0.223840   0.124075   -1.804   0.0765 .
GP10        0.151927   0.102938    1.476   0.1455
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.201 on 57 degrees of freedom
Multiple R-squared:  0.2788,Adjusted R-squared:  0.1523
F-statistic: 2.204 on 10 and 57 DF,  p-value: 0.03038

>
> prev10 = addPriorYear(8,avgsZ,TRUE)
> fit10 = lm(GP10~.,prev10[,-1])
> summary(fit10)

Call:
lm(formula = GP10 ~ ., data = prev10[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.6940 -0.7676 -0.3351  0.5501  3.7452

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.40279    3.22112    0.435   0.6649
avgScore10  0.07318    0.09513    0.769   0.4451
avgFG10    -0.26524    0.25676   -1.033   0.3062
avgTP10     0.01756    0.19928    0.088   0.9301
avgFT10          NA         NA       NA       NA
avgRB10     0.01787    0.01944    0.919   0.3620
avgASS10    0.05366    0.12805    0.419   0.6768
avgTO10    -0.07381    0.14292   -0.516   0.6077
avgSTL10   -0.10435    0.13868   -0.752   0.4551
avgBL10     0.28555    0.17057    1.674   0.0999 .
avgPF10     0.03564    0.11033    0.323   0.7479
GP09        0.26721    0.11937    2.239   0.0293 *
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.257 on 54 degrees of freedom
Multiple R-squared:  0.1949,Adjusted R-squared:  0.04579
F-statistic: 1.307 on 10 and 54 DF,  p-value: 0.2504

>
> prev8 = addPriorYear(6,avgsZ,TRUE)
> fit08 = lm(GP08~.,prev8[,-1])
> summary(fit08)
```

```
Call:
lm(formula = GP08 ~ ., data = prev8[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.42411 -0.62107 -0.08825  0.63471  1.95409

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.38585    2.00584  -0.691  0.49258
avgScore08  -0.02949    0.07537  -0.391  0.69716
avgFG08      0.16887    0.18739   0.901  0.37152
avgTP08     -0.24737    0.12896  -1.918  0.06039 .
avgFT08           NA         NA      NA       NA
avgRB08      0.03838    0.01563   2.456  0.01730 *
avgASS08     0.03256    0.09736   0.334  0.73936
avgTO08     -0.23483    0.09382  -2.503  0.01537 *
avgSTL08     0.09159    0.10375   0.883  0.38123
avgBL08      0.06124    0.10269   0.596  0.55342
avgPF08      0.14675    0.09236   1.589  0.11792
GP07         0.33183    0.08974   3.698  0.00051 ***
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 0.9184 on 54 degrees of freedom
Multiple R-squared:  0.5701, Adjusted R-squared:  0.4905
F-statistic:  7.16 on 10 and 54 DF,  p-value: 4.689e-07


>
> prev7 = addPriorYear(5,avgsZ,TRUE)
> fit07 = lm(GP07~.,prev7[,-1])
> summary(fit07)

Call:
lm(formula = GP07 ~ ., data = prev7[, -1])

Residuals:
    Min      1Q  Median      3Q     Max
-1.7748 -0.7216 -0.2807  0.6634  2.4802

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept)  2.6029631  2.4564810   1.060  0.29403
avgScore07  -0.0651920  0.0718252  -0.908  0.36810
avgFG07      0.2446843  0.1938464   1.262  0.21228
avgTP07      0.1423438  0.1418684   1.003  0.32017
avgFT07             NA         NA      NA       NA
avgRB07     -0.0005477  0.0172239  -0.032  0.97475
avgASS07     0.0260457  0.1167849   0.223  0.82436
avgTO07     -0.2402723  0.0966838  -2.485  0.01608 *
avgSTL07    -0.0466975  0.1167059  -0.400  0.69064
```

```
avgBL07      0.1657333  0.1212501   1.367   0.17733
avgPF07     -0.0462716  0.0882245  -0.524   0.60209
GP06         0.3212087  0.1051509   3.055   0.00349 **
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.056 on 54 degrees of freedom
Multiple R-squared:  0.4317, Adjusted R-squared:  0.3265
F-statistic: 4.102 on 10 and 54 DF,  p-value: 0.0003138


>
> prev6 = addPriorYear(4,avgsZ,TRUE)
> fit06 = lm(GP06~.,prev6[,-1])
> summary(fit06)

Call:
lm(formula = GP06 ~ ., data = prev6[, -1])

Residuals:
    Min     1Q  Median     3Q     Max
-1.6347 -0.8841 -0.2856  0.5480  4.1550

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept)  0.205358  2.752568   0.075   0.9408
avgScore06   0.076930  0.095801   0.803   0.4255
avgFG06      0.017233  0.261605   0.066   0.9477
avgTP06     -0.005185  0.164894  -0.031   0.9750
avgFT06            NA        NA      NA        NA
avgRB06     -0.014477  0.017667  -0.819   0.4161
avgASS06    -0.055950  0.131938  -0.424   0.6732
avgTO06      0.030397  0.141820   0.214   0.8311
avgSTL06     0.046671  0.123428   0.378   0.7068
avgBL06      0.133624  0.139198   0.960   0.3414
avgPF06     -0.232631  0.114706  -2.028   0.0475 *
GP05         0.017416  0.106412   0.164   0.8706
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.235 on 54 degrees of freedom
Multiple R-squared:  0.2222, Adjusted R-squared:  0.07813
F-statistic: 1.542 on 10 and 54 DF,  p-value: 0.15


>
> prev5 = addPriorYear(3,avgsZ,TRUE)
> fit05 = lm(GP05~.,prev5[,-1])
> summary(fit05)

Call:
lm(formula = GP05 ~ ., data = prev5[, -1])
```

```
Residuals:
    Min      1Q  Median      3Q     Max
-1.6795 -0.7748 -0.1379  0.6690  2.4834

Coefficients: (1 not defined because of singularities)
Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.66958    2.56583  -0.651   0.5180
avgScore05  -0.05241    0.08522  -0.615   0.5412
avgFG05      0.06125    0.23014   0.266   0.7911
avgTP05      0.29683    0.14053   2.112   0.0393 *
avgFT05           NA         NA      NA       NA
avgRB05      0.02712    0.01794   1.512   0.1364
avgASS05     0.23750    0.12278   1.934   0.0583 .
avgTO05     -0.01358    0.11565  -0.117   0.9070
avgSTL05     0.24432    0.10904   2.241   0.0292 *
avgBL05     -0.14186    0.12764  -1.111   0.2713
avgPF05     -0.12144    0.10890  -1.115   0.2697
GP04         0.17571    0.10590   1.659   0.1029
---
Signif. codes:  0 *** 0.001 ** 0.01 * 0.05 . 0.1   1

Residual standard error: 1.09 on 54 degrees of freedom
Multiple R-squared:  0.3948,Adjusted R-squared:  0.2827
F-statistic: 3.523 on 10 and 54 DF,  p-value: 0.001242
```