Support Vector Machines for Credit Default Prediction

Matthew Collins
Department of Computer Science
Clemson University
mbc3@clemson.edu

Abstract

This class project presents an analysis of support vector machines (SVMs) applied to the UCI Default of Credit Card Clients dataset. The project explores the impacts of different kernel functions and optimization techniques on classification performance. SVMs with linear, radial basis function (RBF), polynomial, and sigmoid kernels are evaluated. A grid search approach is used for hyperparameter optimization, and the decision boundary is visualized using Principal Component Analysis (PCA). The results are evaluated using accuracy, precision, recall, F1-score, and runtime, demonstrating the utility of SVMs for binary classification tasks on tabular data.

1 Introduction

Support vector machines are a powerful supervised machine learning approach that have demonstrated robust performance in a wide range of classification tasks. This project investigates the application of SVMs to the UCI Default of Credit Card Clients dataset, with a specific focus on assessing the impact of kernel functions and optimization techniques on model performance. The study also examines how hyperparameter tuning can enhance SVM efficiency and accuracy, while PCA is employed to visualize the decision boundary for improved interpretability. The primary objective of this study is to assess the efficacy of SVMs for predicting credit card default and to analyze the computational trade offs associated with various kernel functions and optimization strategies.

2 Dataset

The UCI Default of Credit Card Clients dataset is a multivariate dataset containing data from 30,000 credit card holders in Taiwan. The dataset is primarily designed for binary classification tasks, specifically predicting whether a client would default on their next month's payment. It includes 23 features, which consist of demographic variables such as age, sex, education, and marital status, along with financial metrics like credit limits, historical bill statements, and repayment amounts. The target variable is binary, indicating whether a client defaulted (1) or did not default (0) on their credit card payment.

The dataset includes a mix of categorical and numerical variables. Key variables include repayment statuses (`PAY_0` through `PAY_6`), historical bill amounts (`BILL_AMT1` through `BILL_AMT6`), and historical repayment amounts (`PAY_AMT1` through `PAY_AMT6`). Additionally, demographic variables such as `SEX`, `EDUCATION`, and `MARRIAGE` provide insights into customer profiles. Table 1 summarizes the features included in the dataset.

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Table 1: Summary of Key Features in the Dataset

Variable Name	Type	Description	Units
SEX	Categorical	Gender	1 = Male, 2 = Female
EDUCATION	Categorical	Education level	1 = Graduate, etc.
MARRIAGE	Categorical	Marital status	1 = Married, etc.
BILL_AMT1-6	Numerical	Monthly bill amounts (6 months)	NT Dollars
PAY_AMT1-6	Numerical	Historical repayment amounts (6 months)	NT Dollars
PAY_0-6	Categorical	Repayment status (-2: advance payment)	Discrete values
DEFAULT (Target)	Binary	Default status for the next month	0 = No, 1 = Yes

To prepare the dataset for modeling, extensive preprocessing was conducted. Several variables, such as `SEX`, `EDUCATION`, `MARRIAGE`, and repayment statuses (`PAY_0` through `PAY_6`), were categorical in nature. Since support vector machines require numerical input, these categorical variables were transformed into one hot encoded binary variables. This encoding ensured that each category was treated as an independent feature, avoiding implicit ordinal assumptions. Furthermore, the dataset exhibited significant class imbalance, with the majority of clients not defaulting on their payments. To address this imbalance, the majority class (non-default clients) was downsampled to create a balanced dataset, ensuring that the model learned patterns equally well from both defaulting and non-defaulting clients.

Another essential preprocessing step involved standardizing numerical features, such as bill amounts and repayment amounts. These features had varying scales, with some variables measured in monetary units and others as categorical values. Without standardization, features with larger magnitudes could disproportionately influence the model. Therefore, all continuous features were scaled to have a mean of zero and a standard deviation of one, ensuring fair contribution from each variable.

The preprocessing steps of one hot encoding, downsampling, and standardization were necessary to ensure that the dataset was compatible with support vector machines and capable of producing meaningful predictions. These transformations addressed the challenges posed by mixed feature types, class imbalance, and variable scaling, ultimately improving the efficiency and accuracy of the machine learning models applied in this study.

3 Methodology

The Support Vector Machine (SVM) algorithm aims to find an optimal hyperplane that maximizes the margin between two classes while minimizing classification errors. For a training dataset with n points $\{(\mathbf{x}_i, y_i)\}_{i=1}^n$ where $\mathbf{x}_i \in \mathbb{R}^d$ and $y_i \in \{-1, 1\}$, the primal optimization problem is formulated as:

$$\min_{\mathbf{w},b,\xi} \frac{1}{2}\|\mathbf{w}\|^2 + C\sum_{i=1}^{n} \xi_i$$

subject to the constraints:

$$y_i(\mathbf{w}^\top \mathbf{x}_i + b) \geq 1 - \xi_i, \quad \xi_i \geq 0, \quad i = 1, \dots, n$$

where $\mathbf{w}$ is the normal vector to the hyperplane, b is the bias term, ξ_i are slack variables allowing for soft margin violations, and C is the regularization parameter controlling the trade-off between margin maximization and error minimization.

The dual formulation of this optimization problem, derived using Lagrange multipliers, is:

$$\max_{\boldsymbol{\alpha}} \sum_{i=1}^{n} \alpha_i - \frac{1}{2}\sum_{i=1}^{n}\sum_{j=1}^{n} \alpha_i\alpha_j y_i y_j \mathbf{x}_i^\top \mathbf{x}_j$$

subject to:

$$0 \leq \alpha_i \leq C, \quad i = 1, \ldots, n \quad \text{and} \quad \sum_{i=1}^{n} \alpha_i y_i = 0$$

To handle nonlinear classification problems, kernel functions $K(\mathbf{x}_i, \mathbf{x}_j)$ are introduced to implicitly map the input features into a higher-dimensional space. The kernel trick transforms the dual optimization problem to:

$$\max_{\boldsymbol{\alpha}} \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j K(\mathbf{x}_i, \mathbf{x}_j)$$

In this project, four kernel functions were evaluated:

1. Linear: $K(\mathbf{x}_i, \mathbf{x}_j) = \mathbf{x}_i^\top \mathbf{x}_j$
2. Polynomial: $K(\mathbf{x}_i, \mathbf{x}_j) = (\gamma \mathbf{x}_i^\top \mathbf{x}_j + r)^d$
3. RBF (Gaussian): $K(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2)$
4. Sigmoid: $K(\mathbf{x}_i, \mathbf{x}_j) = \tanh(\gamma \mathbf{x}_i^\top \mathbf{x}_j + r)$

The decision function for classifying new points becomes:

$$f(\mathbf{x}) = \text{sign}\left(\sum_{i=1}^{n} \alpha_i y_i K(\mathbf{x}_i, \mathbf{x}) + b\right)$$

Grid search cross-validation was employed to optimize the hyperparameters C and γ for each kernel. The search space included:

- $C \in \{0.1, 1, 10, 100\}$
- $\gamma \in \{0.001, 0.01, 0.1, 1\}$

To facilitate visualization and interpretation, Principal Component Analysis (PCA) was applied to reduce the feature space to two dimensions. Given the centered data matrix $\mathbf{X} \in \mathbb{R}^{n \times d}$, where n is the number of samples and d is the number of features, PCA first computes the covariance matrix:

$$\boldsymbol{\Sigma} = \frac{1}{n} \mathbf{X}^\top \mathbf{X}$$

PCA then performs eigendecomposition of the covariance matrix:

$$\boldsymbol{\Sigma} = \mathbf{V} \boldsymbol{\Lambda} \mathbf{V}^\top$$

where $\mathbf{V} \in \mathbb{R}^{d \times d}$ contains the eigenvectors as columns (sorted by decreasing eigenvalues) and $\boldsymbol{\Lambda} = \text{diag}(\lambda_1, \ldots, \lambda_d)$ contains the corresponding eigenvalues. The transformed features are obtained by projecting the data onto the first two principal components:

$$\mathbf{X}_{\text{transformed}} = \mathbf{X} \mathbf{V}_{1:2}$$

where $\mathbf{V}_{1:2} \in \mathbb{R}^{d \times 2}$ contains the first two eigenvectors. This projection preserves the maximum possible variance in the data while reducing dimensionality to facilitate visualization of the decision boundaries.

4 Results

The comparative analysis of kernel functions yielded results, summarized in Table 2. The RBF kernel outperformed other kernels, achieving the highest accuracy (68.75%) and F1-score (0.65). The scree plot in Figure 3 highlights the explained variance by the principal components, providing insights into the dimensionality reduction process.

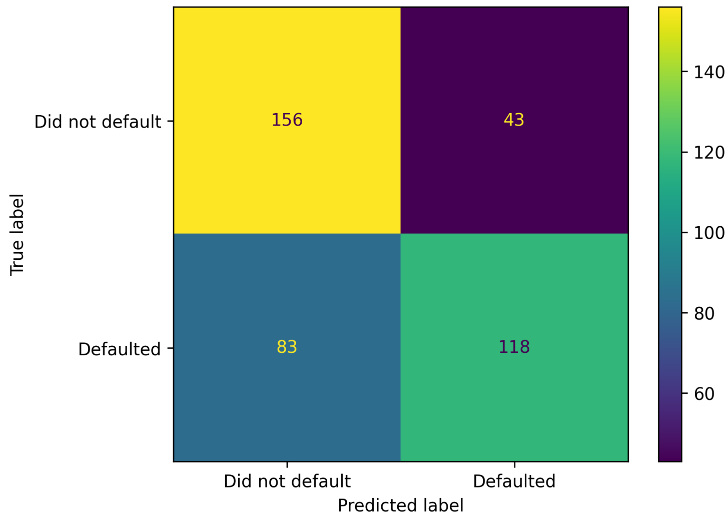

Figure 1: Confusion Matrix Before Grid Search.

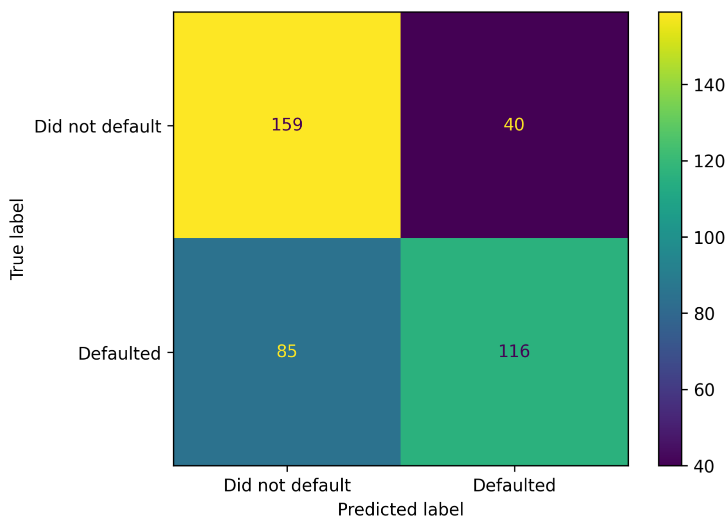

Figure 2: Confusion Matrix After Grid Search.

Table 2: Kernel Comparison Results

Kernel	**Accuracy**	**Precision**	**Recall**	**F1-Score**	**Runtime (s)**	**Best Hyperparameters (C, γ)**
Linear	0.6525	0.7095	0.5224	0.6017	0.2457	(1, Scale)
Polynomial	0.6700	0.7226	0.5572	0.6292	0.0629	(10, 0.01)
RBF	0.6875	0.7436	0.5771	0.6499	0.0634	(1, 0.01)
Sigmoid	0.6450	0.7007	0.5124	0.5920	0.0891	(100, 0.001)

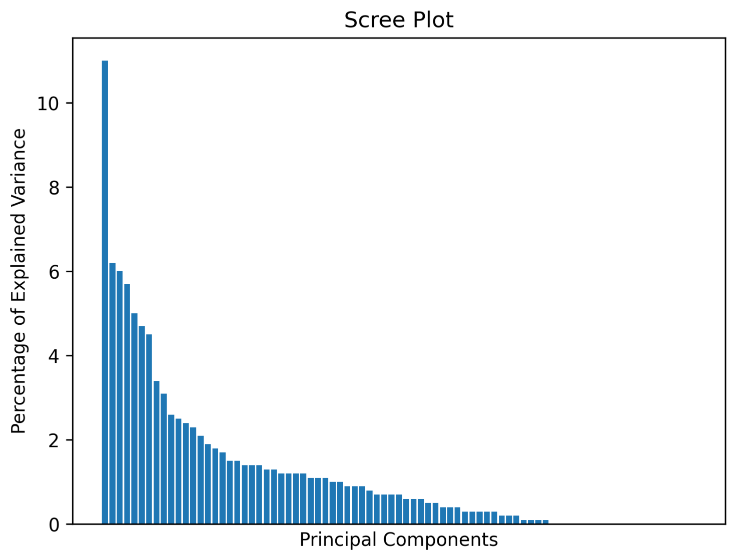

Figure 3: Scree Plot Showing Percentage of Explained Variance.

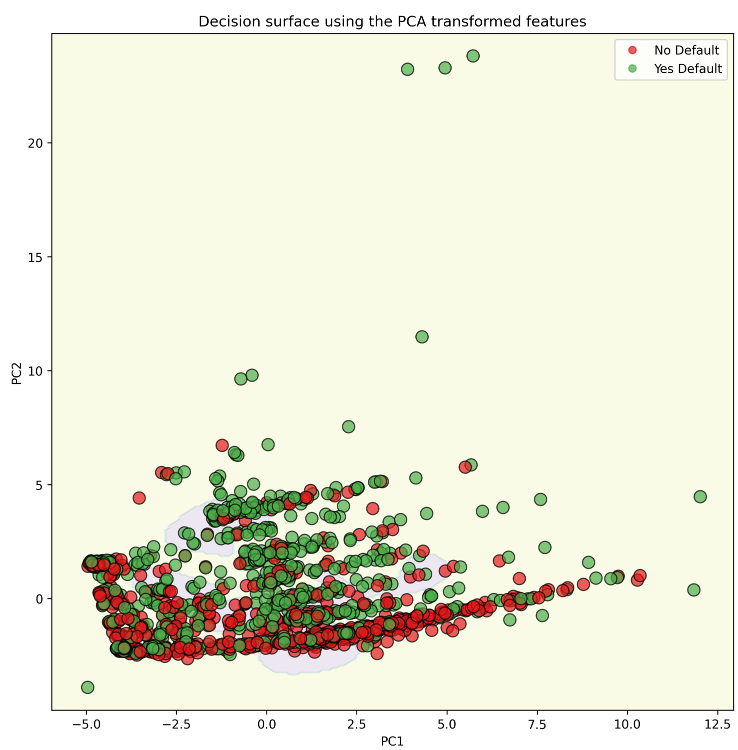

Figure 4: Decision Surface Using PCA Transformed Features.

5 Discussion

The results highlight the importance of kernel selection in Support Vector Machines (SVMs) for binary classification tasks. Among the evaluated kernels, the radial basis function (RBF) kernel emerged as the best performing option, achieving an accuracy of 68.75%. This performance underscores the RBF kernel's strength in mapping data into higher-dimensional spaces, enabling it to capture nonlinear decision boundaries. However, the achieved accuracy is relatively modest, raising questions about the suitability of SVMs for this particular dataset. While the polynomial kernel showed competitive performance with an accuracy of 67.00%, its sensitivity to parameter tuning limited its robustness. The linear kernel underperformed, achieving an accuracy of only 65.25%, which can be attributed to its inability to handle the nonlinear structure of the data. The sigmoid kernel, with its complex parameterization, struggled to converge effectively and yielded the lowest accuracy of 64.50%.

The relatively low accuracy across all kernels suggests that SVMs, while powerful, may not be the optimal model for this task. The imbalanced and high-dimensional nature of the dataset likely contributed to the suboptimal performance. Although hyperparameter tuning via grid search improved the models, as evidenced by the enhanced confusion matrix after optimization (Figure 2), the gains were incremental and insufficient to achieve high accuracy. This indicates that the inherent characteristics of the dataset—such as overlapping class distributions and complex relationships among features—pose challenges that SVMs alone may not effectively address.

The PCA visualization of the decision boundary (Figure 4) provided insights into the separability of the classes, but the limited explained variance from the first two principal components (Figure 3) suggests that the majority of the dataset's complexity lies in higher dimensions. This highlights a limitation of using PCA for interpretability and suggests that other dimensionality reduction techniques, could provide more nuanced insights into the data's structure.

6 Conclusion

This study demonstrates the effectiveness of support vector machines for credit card default prediction. The findings emphasize the importance of kernel selection, with the RBF kernel offering the best performance among the four kernels evaluated. Hyperparameter tuning further enhanced classification accuracy, though its impact was secondary to the choice of kernel. Future work could explore additional dimensionality reduction techniques, alternative kernel functions, and the application of SVMs to larger, more diverse datasets. In summary, while SVMs demonstrated some utility in this study, the results indicate that they may not be the most effective model for predicting credit card default. The modest accuracy, despite careful preprocessing and hyperparameter tuning, underscores the need for exploring alternative machine learning models and techniques to better address the complexity of the dataset and improve predictive performance.

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