

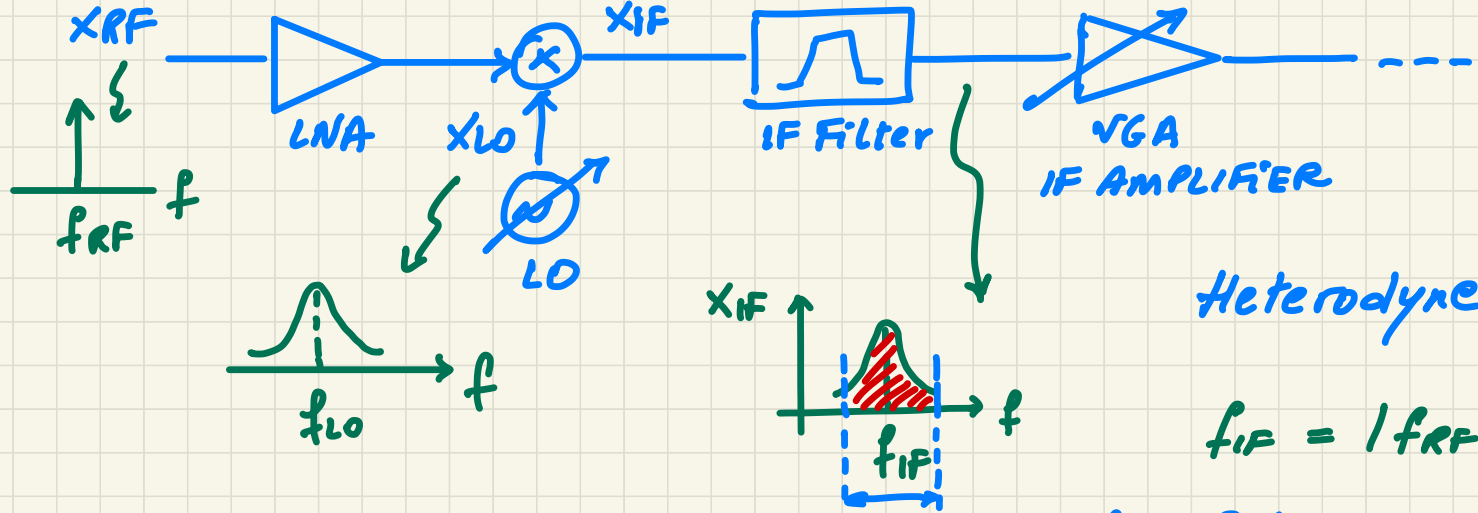
RF Circuit Design

L6



Impact of Phase Noise on RX performance

1. Direct impact



Heterodyne

$$f_{IF} = |f_{RF} - f_{LO}|$$

$$A \cdot x_{RF}(t) \cdot x_{LO}(t) = x_{IF}(t)$$

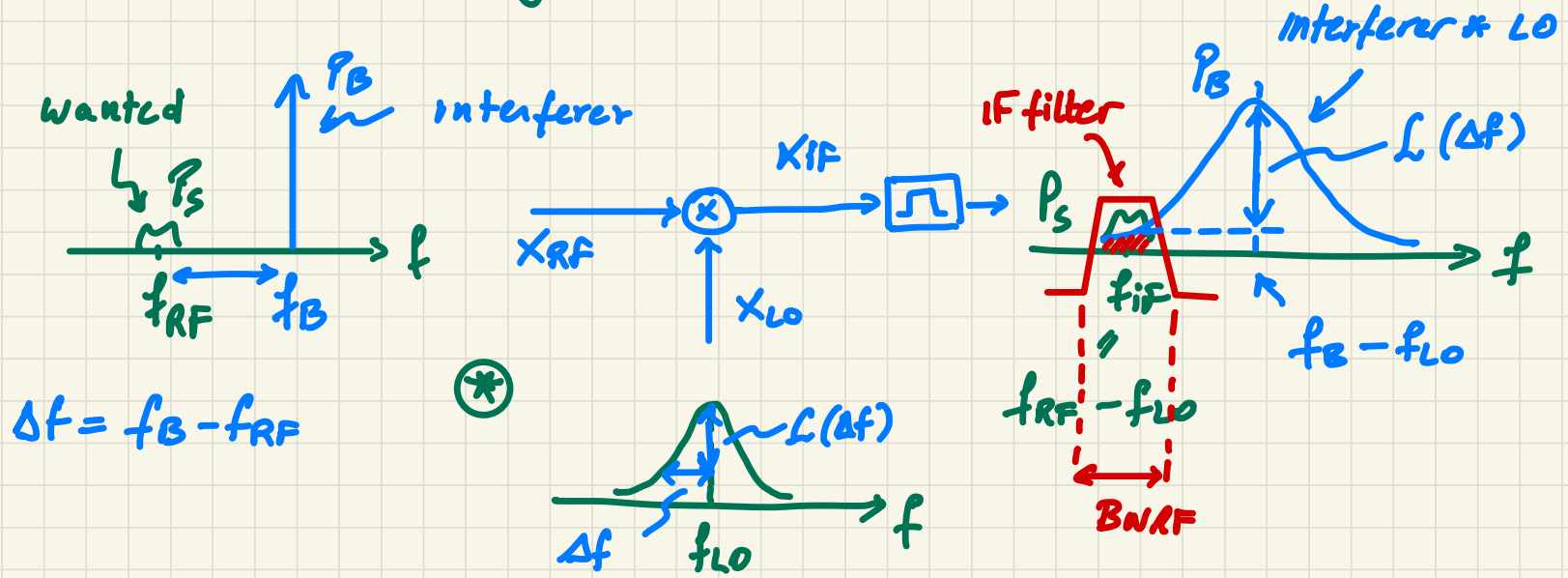
$$\Rightarrow A \cdot X_{RF}(f) * X_{LO}(f) = X_{IF}(f)$$

$$x_{LO}(t) = A_{LO} \cdot \cos[\omega_{LO}t + \varphi_n]$$

$$SNR \cong \frac{1}{\sigma_{\varphi_n}^2}$$

Phase noise degrades SNR of RX

2. Reciprocal mixing



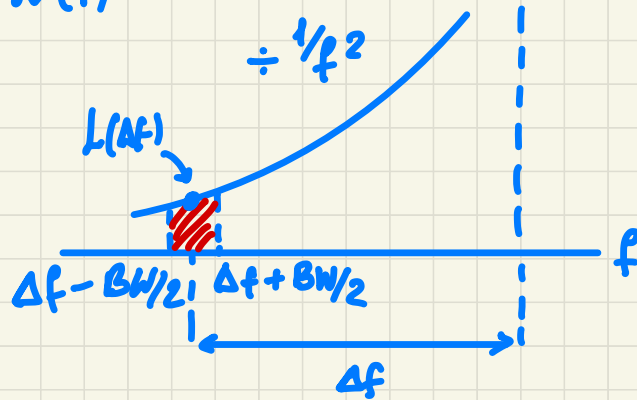
$$L(\Delta f) \triangleq \frac{P_n(f_{IF}) \text{ in 1Hz}}{P_B} ; \quad S_n(f_{in}) = \underbrace{L(\Delta f) \cdot P_B}$$

$$SNR = \frac{P_S}{P_n(f_{IF})} \approx \frac{P_S}{L(\Delta f) \cdot P_B \cdot B_{NRF}} \quad \Delta f \gg B_{NRF}$$

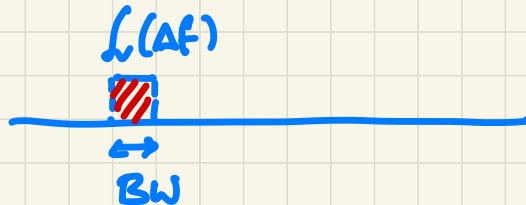
$$\Rightarrow \text{SNR} \text{ dB} = 10 \log_{10} \text{SNR} =$$

$$= \underset{(\text{dBm})}{P_s} - \underset{(\text{dBm})}{P_B} - \underset{(\text{dBc/Hz})}{L(\Delta f)} - \underline{\underline{10 \cdot \log_{10} (BW_{RF})}}$$

$L(f)$



$$\int_{\Delta f - BW/2}^{\Delta f + BW/2} L(\Delta f) d\Delta f$$



$$\approx L(\Delta f) \cdot BW$$

ex. GSM

• $P_s = -99 \text{ dBm}$

• $P_B = -40 \text{ dBm}$

(out-of-band interf.
at 0 dBm attenuated
by antenna filter by
 40 dB)

$f_{RF} = 2.01 \text{ GHz}$

$f_B = 2.03 \text{ GHz}$

$f_{LO} = 2.00 \text{ GHz}$

$BW_{RF} = 200 \text{ kHz}$

$SNR > 50 \text{ dB}$

$\mathcal{L} = ?$

$$\mathcal{L}(\Delta f) = P_s - P_B - SNR_{dB} - 10 \log_{10} BW_{RF} =$$

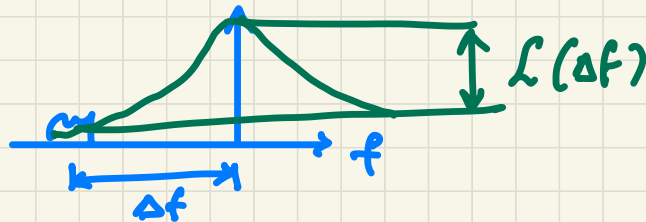
$$= -99 + 40 - 50 - 53 =$$

$$= -162 \text{ dBc/Hz at } 20 \text{ MHz}$$

$$10 \log_{10} BW_{RF} = 10 \log_{10} 2 \cdot 10^5 =$$

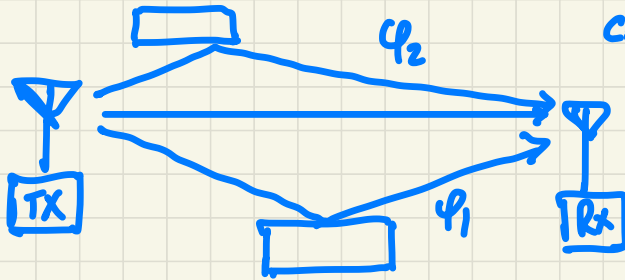
$$= 3 \text{ dB} + 50 \text{ dB} = 53 \text{ dB}$$

$$\Delta f = f_B - f_{RF} = 20 \text{ MHz}$$



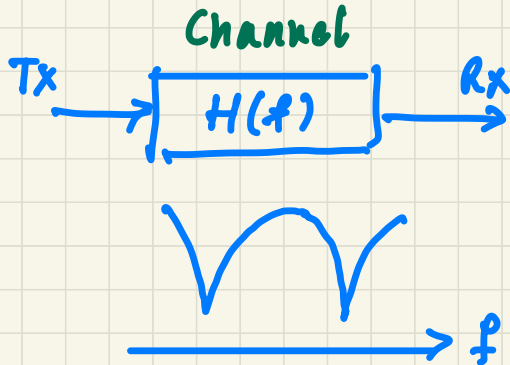
Fading

Multipath channel

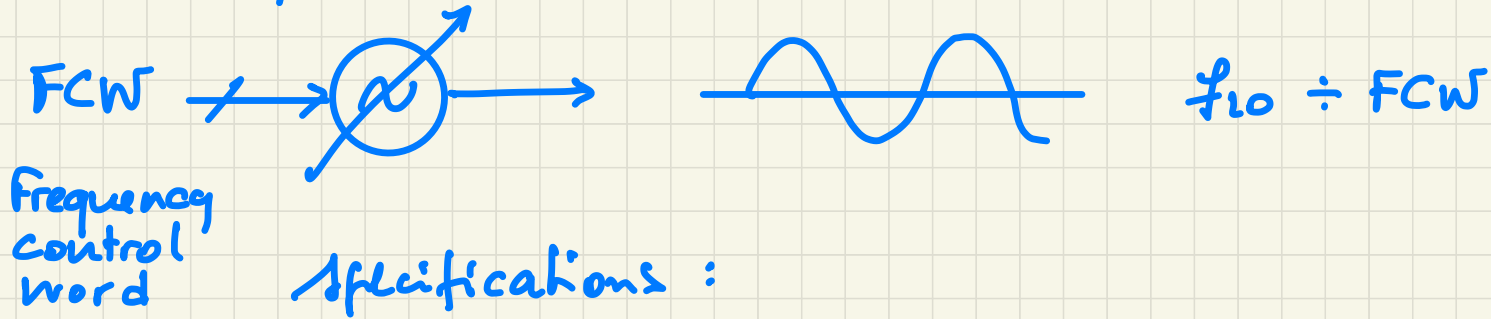


constructive/destructive interference :

$$A \cos \omega t + B \cos (\omega t + \phi_1) + C \cos (\omega t + \phi_2)$$



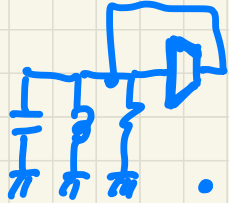
Frequency Synthesizers



- Accuracy $\frac{\Delta f_{LO}}{f_{LO}}$ (Aging + Drift)

e.g. GSM standard $\frac{\Delta f}{f} = 0.1 \text{ ppm} = 10^{-7}$

$f \approx 1 \text{ GHz} \Rightarrow \Delta f \approx 10^9 \cdot 10^{-7} = 100 \text{ Hz}$



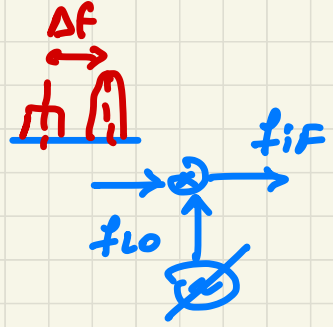
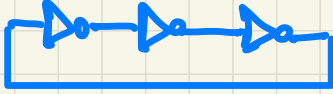
• LC oscillators

$$f = \frac{1}{2\pi\sqrt{LC}} \Rightarrow \frac{\Delta f}{f} \approx \frac{1}{2} \cdot \frac{\Delta C}{C} + \frac{1}{2} \cdot \frac{\Delta L}{L}$$

$1 \div 10\% \quad 1 \div 10\%$

- RC oscillator

$$f \div \frac{1}{RC} \Rightarrow \frac{\Delta f}{f} \cong \frac{\Delta R}{R} + \frac{\Delta C}{C}$$



- Resolution : minimum Δf of LO

- * for channel spacing $\sim 100 \text{ KHz}$

- * for temperature compensation $\sim \text{Hz}$

- Settling time : channel switching time

- * switch from one freq. to another at each frame
settling time $\sim 100 \mu\text{s}$ or even $\approx 10 \mu\text{s}$

- Spurious content : reciprocal mixing

- Phase Noise

- Pulling sensitivity of $\left(\frac{\Delta f_o}{\Delta V_{DD}}\right)$ frequency to V_{DD} , to load change

to improve accuracy : master/slave approach

Atomic
clock

10^{-9} s/day



Crystal
oscillators
(Quartz)

TCXO (temperature
compensated
crystal oscillator)



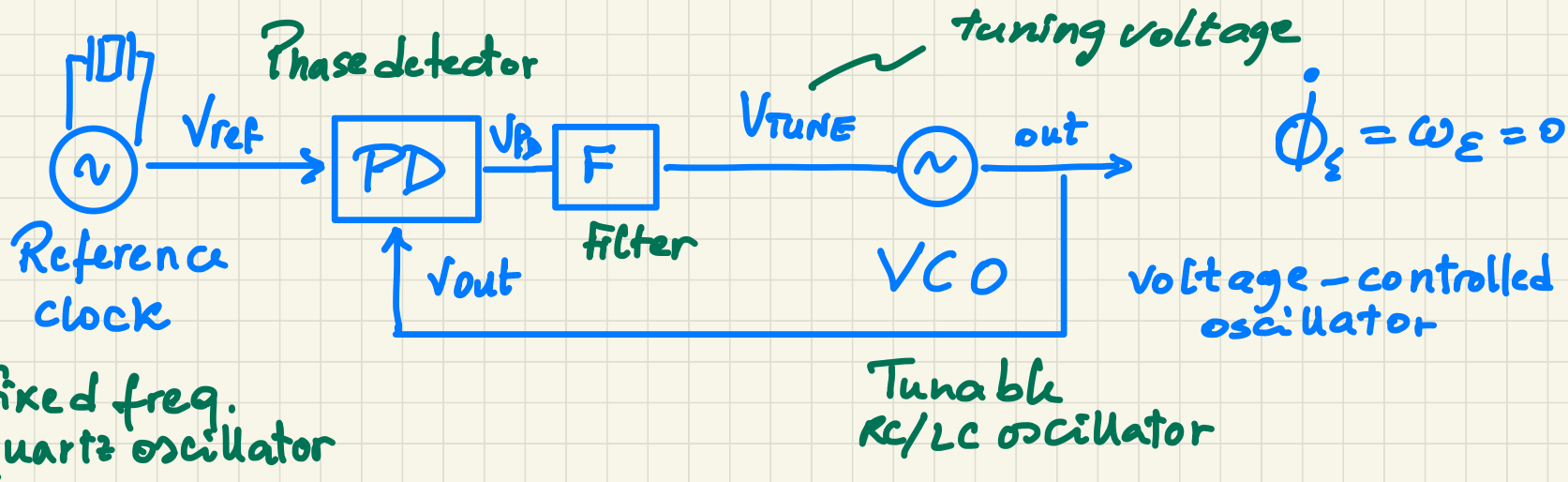
variable
RC / LC
oscillators

- good accuracy
- accuracy \approx 100 ppm
- aging \approx 0.5 ppm/year
- drift \approx 0.5 ppm $0-75^{\circ}\text{C}$

- not tunable (fixed frequency)
- low - frequency ($1 \div 10$ MHz)

- poor accuracy
- tunable
- can operate at
large frequency
100 GHz+

Phase-locked loop (PLL)



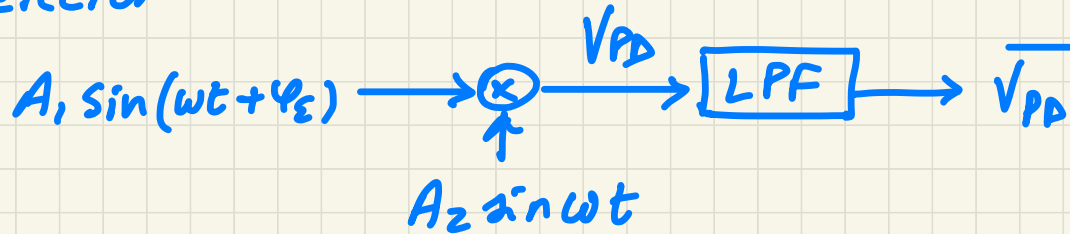
Hyp. linear tuning :

$$\omega_{out} = \omega_{FR} + K_{VCO} \cdot V_{TUNE}$$

ω_{out} : free-running (angular) frequency
 ω_{FR} : free-running (angular) frequency
 K_{VCO} : tuning sensitivity
 $[rad/s/V]$

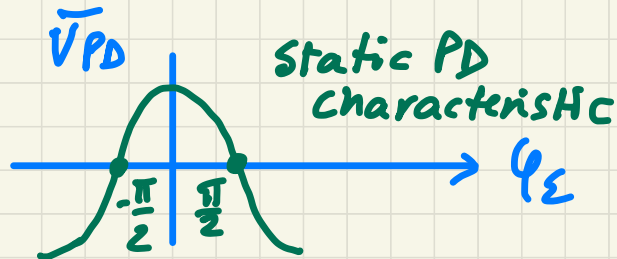
Phase detector

e.g.



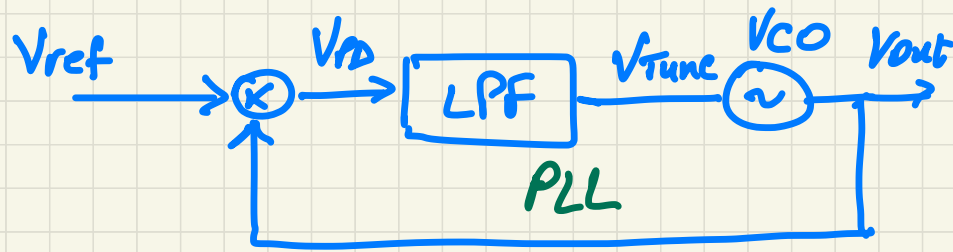
$$V_{PD} = \underbrace{-\frac{A_1 A_2}{2} \cos(2\omega t + \varphi_e)}_{\text{fast}} + \underbrace{\frac{A_1 A_2}{2} \cos(\varphi_e)}_{\text{DC}}$$

$$\bar{V}_{PD} \approx \frac{A_1 A_2}{2} \cos \varphi_e \quad \text{if } BW_{LPF} \ll 2\omega$$



$$\bar{V}_{PD} = 0 \quad \text{when} \quad \varphi_e = \pm \frac{\pi}{2}$$

Notation change



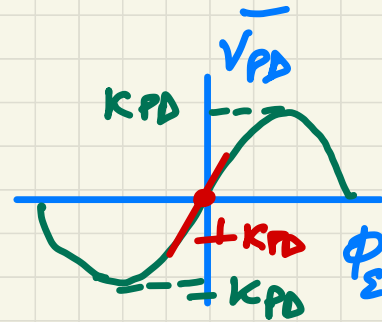
$$V_{ref} = A_r \cdot \sin \Phi_{ref}$$

absolute
phase

$$\hookrightarrow (\omega_{ref} t + \varphi_{ref})$$

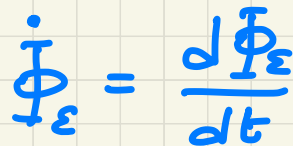
excess phase

$$V_{out} = A_o \cos \Phi_{out}$$



$$\Rightarrow \overline{V_{PD}} \cong \underbrace{G_c \cdot \frac{A_r \cdot A_o}{2}}_{\substack{K_{PD} (V) \\ PD \text{ gain}}} \cdot \underbrace{\sin [\Phi_{ref} - \Phi_{out}]}_{\substack{\Phi_{\epsilon} \\ \text{phase error}}}$$

$$= K_{PD} \cdot \sin \Phi_{\epsilon}$$



$$= \omega_{\text{ref}} - (\omega_{\text{AR}} + K_{\text{VCO}} V_{\text{TUNE}}) =$$

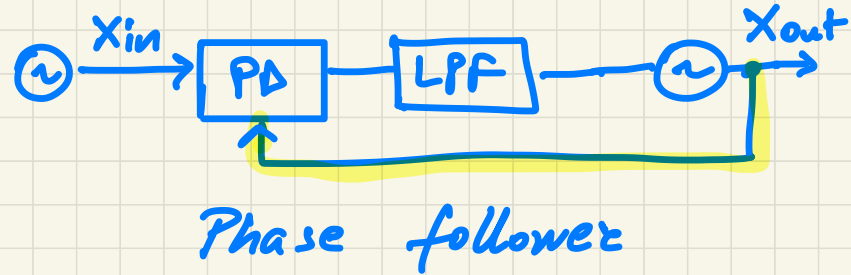
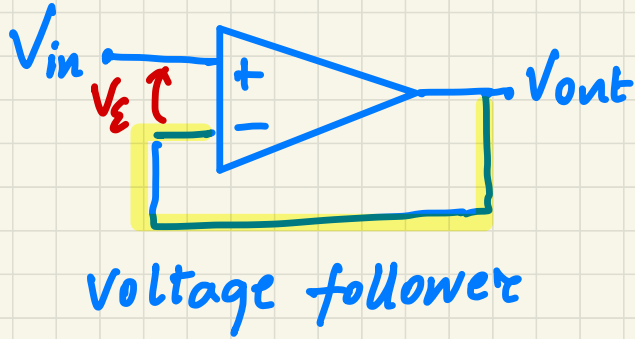
$$= \underbrace{\omega_{\text{ref}} - \omega_{\text{FR}}}_{\triangleq \Delta\omega \text{ (rad/s)}} - \underbrace{K_{\text{VCO}} \cdot K_{\text{PD}} \sin \Phi}_{\triangleq K \left(\frac{\text{rad}}{\text{s}} / \cancel{\psi} \cdot \cancel{\psi} \right)}$$

- $\omega_{out} = \omega_{FR} + K_{VCO} V_{TUNE}$

- $\overline{V_{PD}} = K_{PD} \cdot \sin \Phi_E$

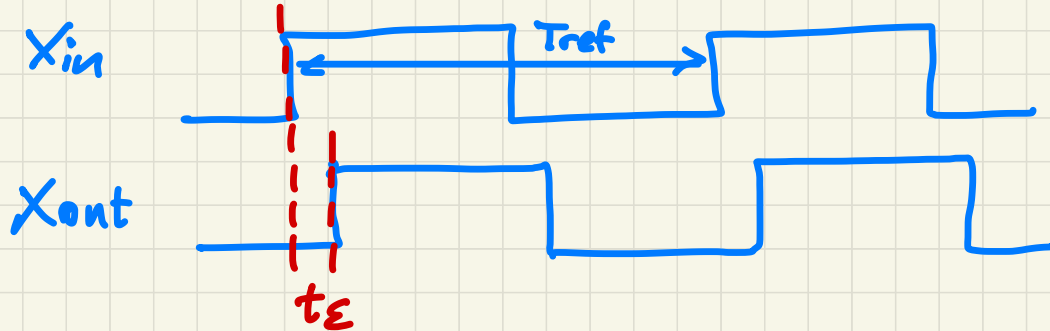
$$\Rightarrow \dot{\Phi}_\varepsilon = \Delta\omega - K \cdot \sin \Phi_\varepsilon$$

First-order differential eq. \rightarrow FIRST-ORDER PLL



$$\phi_\varepsilon = \omega_{ref} \cdot t_\varepsilon$$

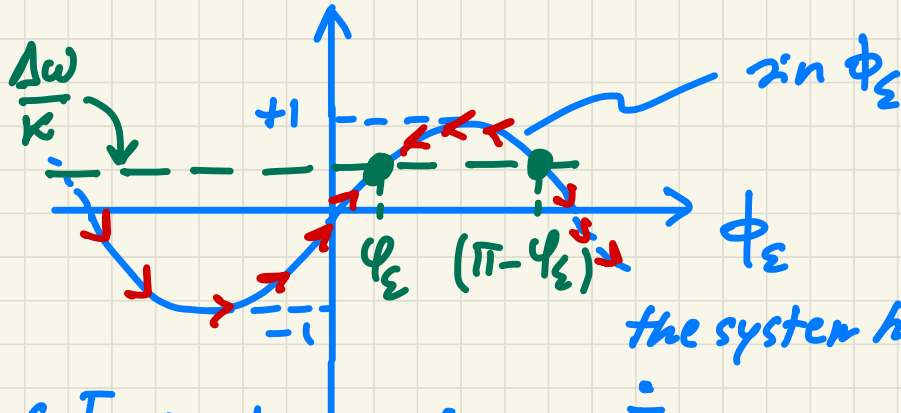
$$\omega_{ref} = 2\pi / T_{ref}$$



$$\dot{\Phi}_E = \Delta\omega - \kappa \cdot \sin \Phi_E$$

$$\Phi_E(t) \text{ unknown}$$

Equilibrium points : $\dot{\Phi}_E = 0 \Rightarrow \sin \Phi_E = \frac{\Delta\omega}{\kappa}$



IF $\left| \frac{\Delta\omega}{\kappa} \right| < 1$:

the system has 2 equilibrium points

(Φ_E is decreasing) $\dot{\Phi}_E < 0 \Leftrightarrow \Delta\omega - \kappa \sin \Phi_E < 0$

$$\sin \Phi_E > \frac{\Delta\omega}{\kappa}$$

(Φ_E is increasing) $\dot{\Phi}_E > 0 \Leftrightarrow \sin \Phi_E < \frac{\Delta\omega}{\kappa}$

$$\Phi_E(t) \rightarrow \varphi_E = \arcsin\left(\frac{\Delta\omega}{K}\right) \quad \text{is STABLE}$$

steady-state phase error depends on the frequency offset between ref. and the free-running freq. of the VCO

$(\pi - \varphi_E)$ is UNSTABLE eq. point

IF $\left| \frac{\Delta\omega}{K} \right| > 1$: no equilibrium point

$$\dot{\Phi}_E > 0$$

