

Q & A

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8/6/2021

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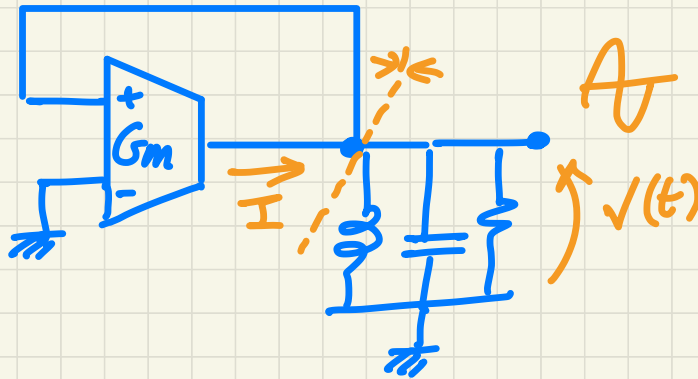
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# Gain margin in an oscillator



$G_m$  is real number

$$LG(s) = G_m \cdot Z(s)$$

$$G_m \cdot |Z(j\omega_0)| = 1$$

$$\angle Z(j\omega_0) = 0$$

Startup :

$$LG(j\omega_0) = EG$$

$$Z_a = -Z(j\omega_0) \quad \text{oscillation condition}$$

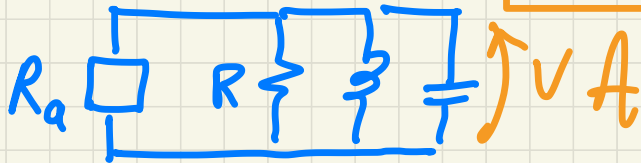
$$-\frac{1}{G_m} = -Z(j\omega_0)$$

$$G_m V^2 = \frac{V^2}{R}$$

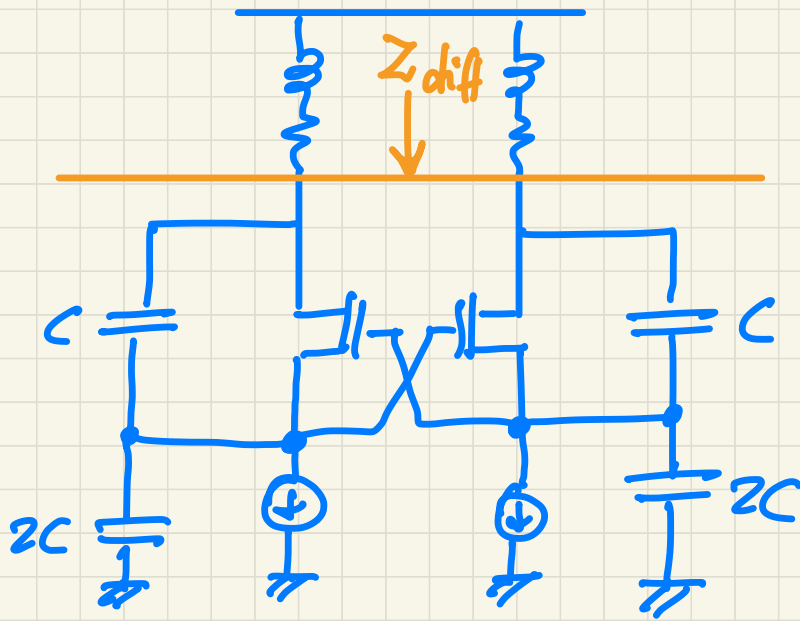
$$\begin{aligned} \text{active power} &= \\ &= \text{dissipated power} \end{aligned}$$

Startup :

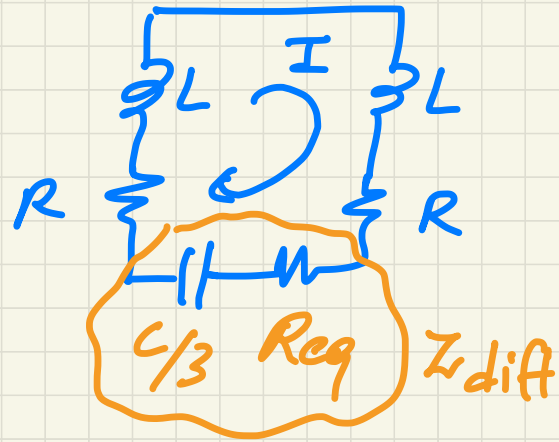
$$EG = \frac{\text{active power}}{\text{dissipated power}}$$



$$EG = \frac{V^2/|R_a|}{V^2/R} = \frac{R}{|R_a|} > 1$$



$$Z_{diff} = - \underbrace{\frac{2g_m}{\omega^2 C^2}}_{R_{eq}} + j\omega \underbrace{\left(\frac{3}{C}\right)}_{Z_{diff}}$$

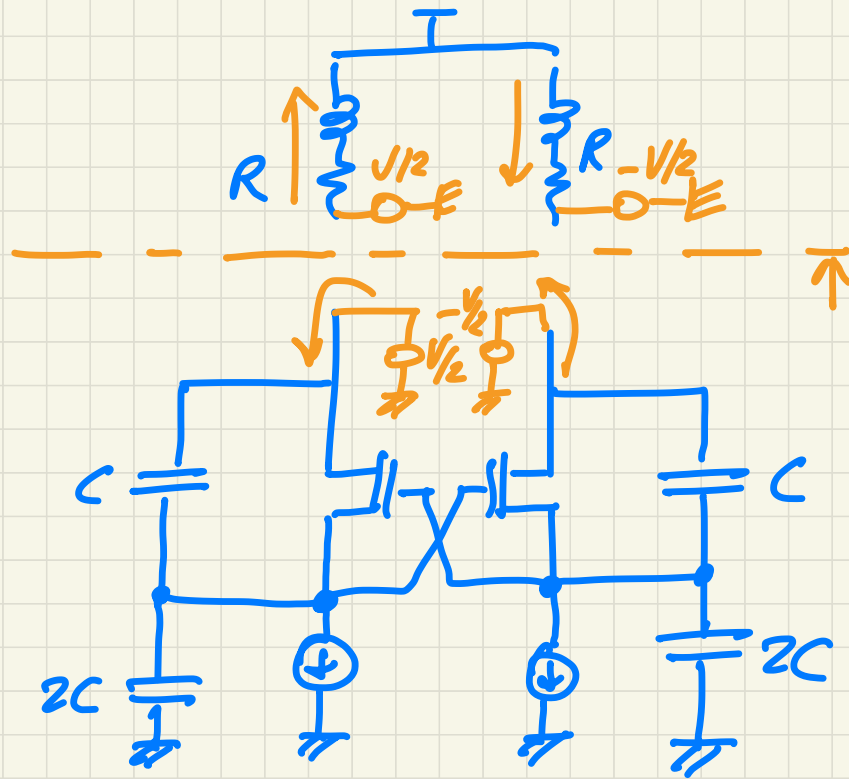


$$1) \quad 2R = R_{eq}$$

$$2) \quad \omega_0 = \frac{1}{\sqrt{2L \cdot C/3}}$$

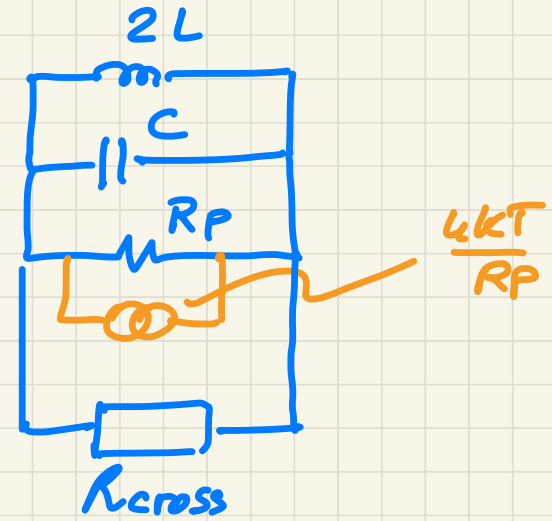
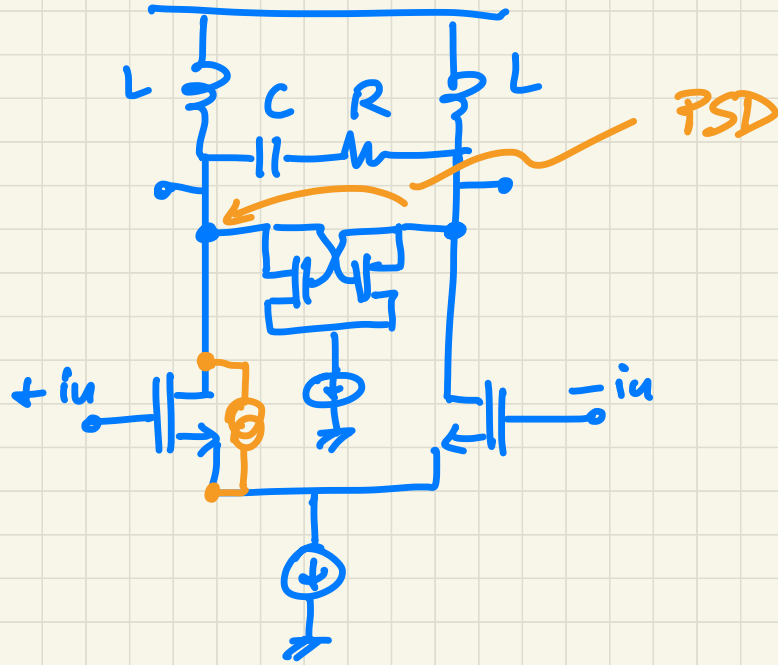
$$EG = \frac{|R_{eq}| I^2}{2R \cdot I^2} > 1 ;$$

$$\frac{2g_m}{\omega^2 C^2} = 2 \cdot R \cdot EG ; \quad g_m = \omega^2 C^2 \cdot EG$$

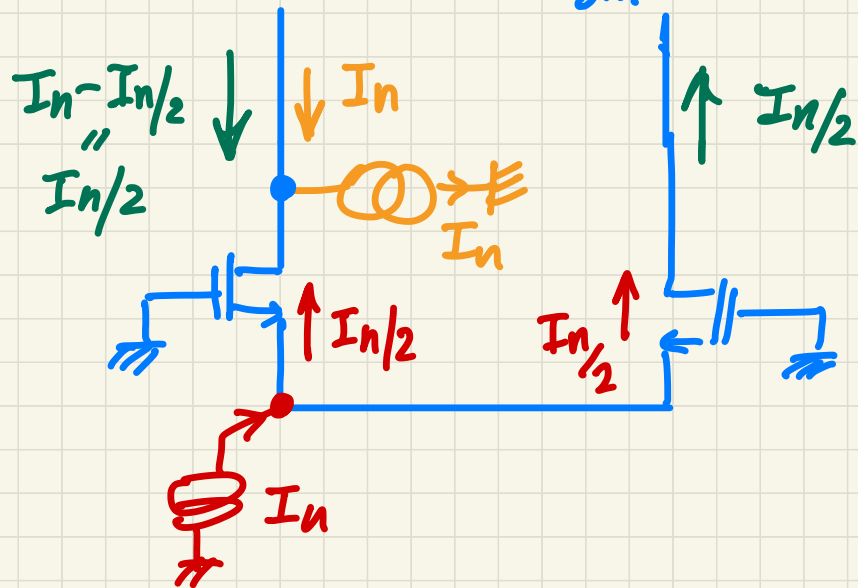
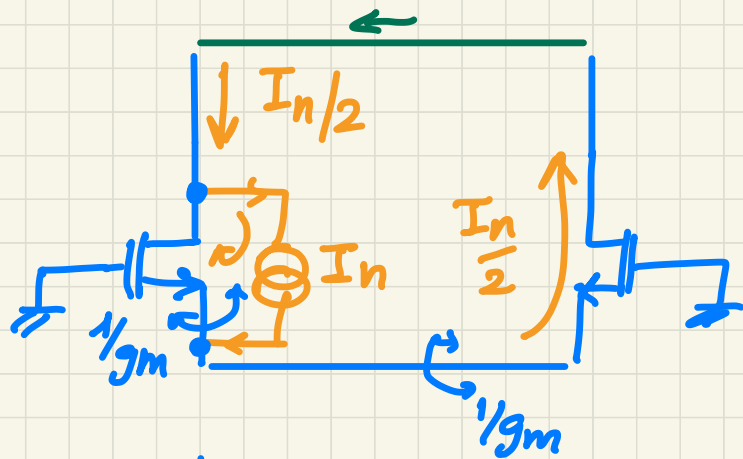


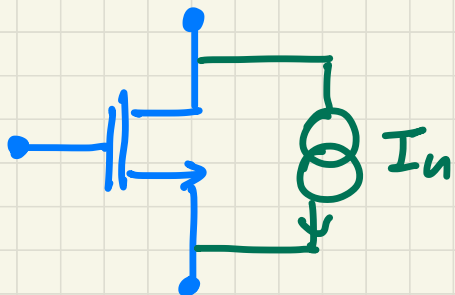
$$Z(s) = Z_L + Z_R$$

T7.3



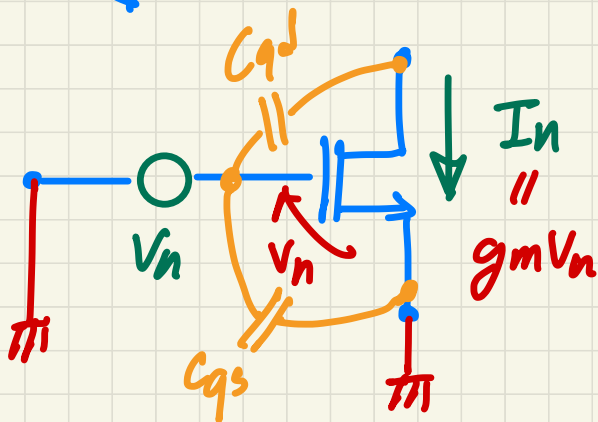
$$S_{V_{out}}(\omega_0) = \frac{4kT}{R_p} \cdot (R_p \parallel R_{cross})^2$$





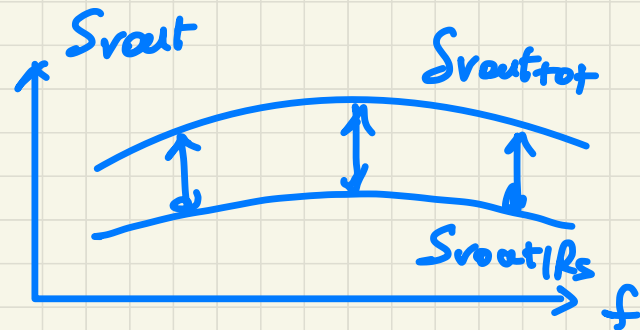
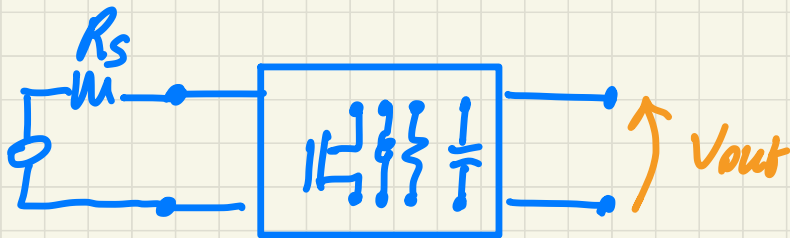
$$\frac{\langle I_n^2 \rangle}{\Delta f} = 4kT \frac{\gamma}{\alpha} g_m$$

input-referred

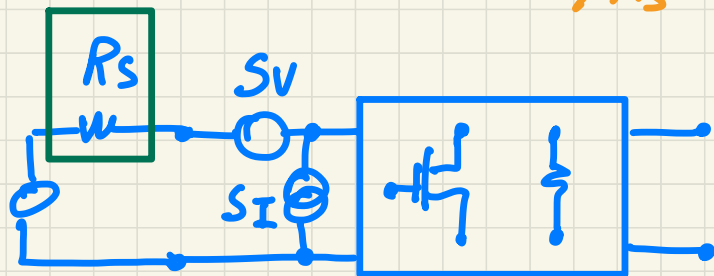


$$\begin{aligned} \frac{\langle V_n^2 \rangle}{\Delta f} &= \frac{\langle I_n^2 \rangle / g_m^2}{\Delta f} = \\ &= 4kT \frac{\gamma}{\alpha} \frac{1}{g_m} \end{aligned}$$

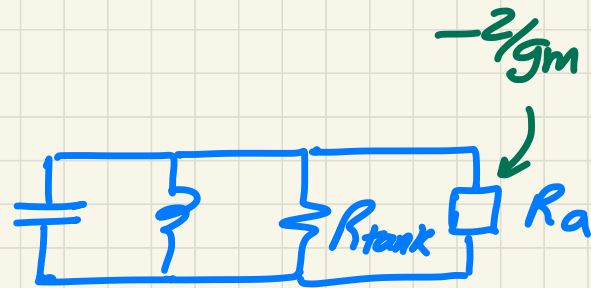
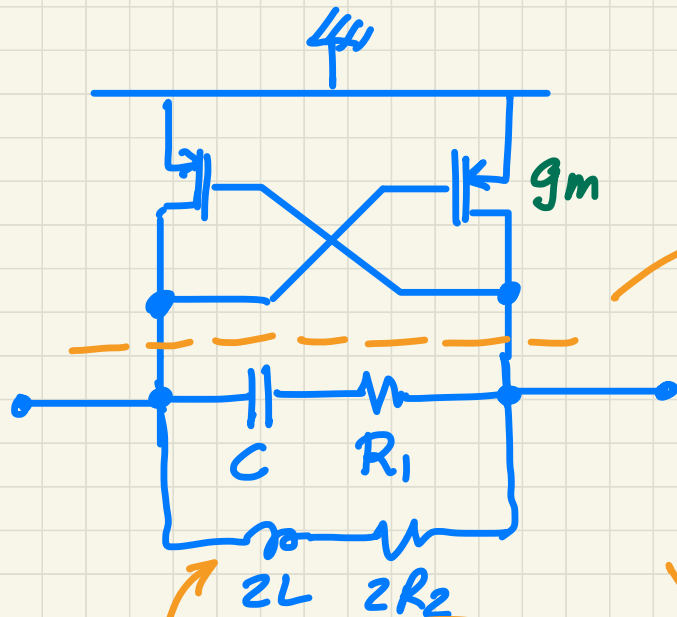




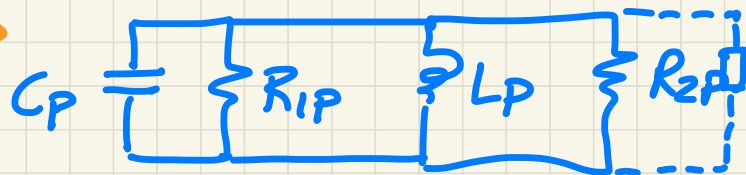
$$NF = \frac{S_{vout\ tot}}{S_{vout/R_s}}$$



input-referred  
noise source

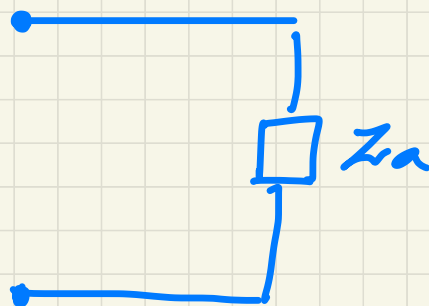
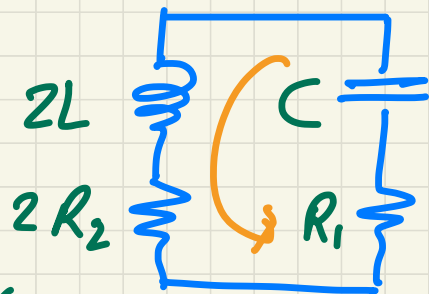


long method

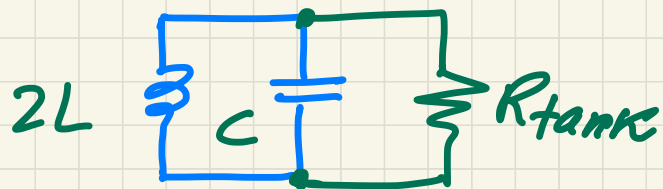


$$R_{\text{tank}} = R_{1p} \parallel R_{2p}$$

fast method



small losses

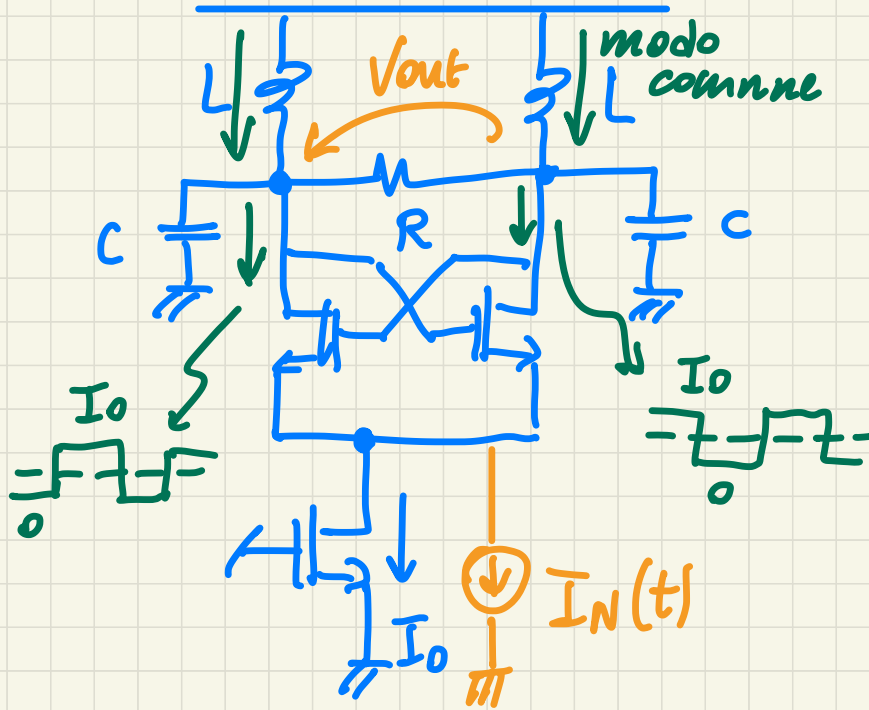


$$R_{\text{tank}} = \frac{Q}{\omega_0 C} = \frac{\omega_0 L}{Q}$$

Compute  $Q$  of a network :  $Q = \frac{2\omega_0 L}{R_1 + 2R_2}$

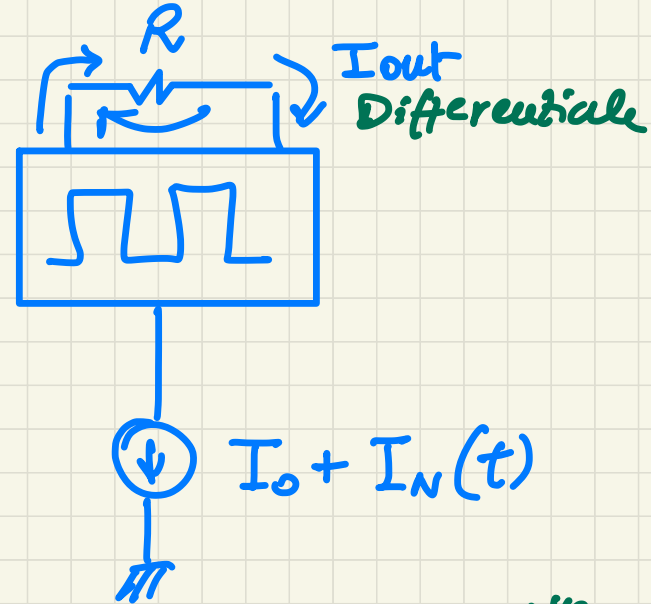
26.06.18

# Problem #2

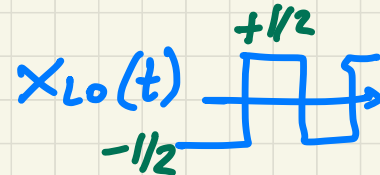


$$I_N = 0.5 \text{ mA} \cdot \cos 2\omega_0 t$$

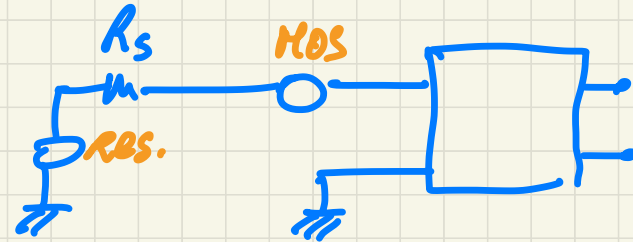
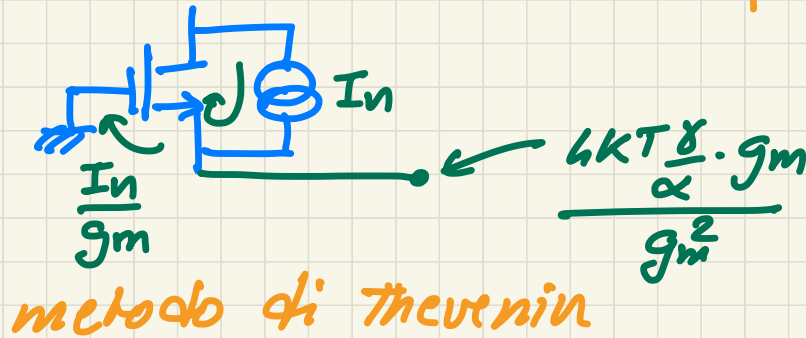
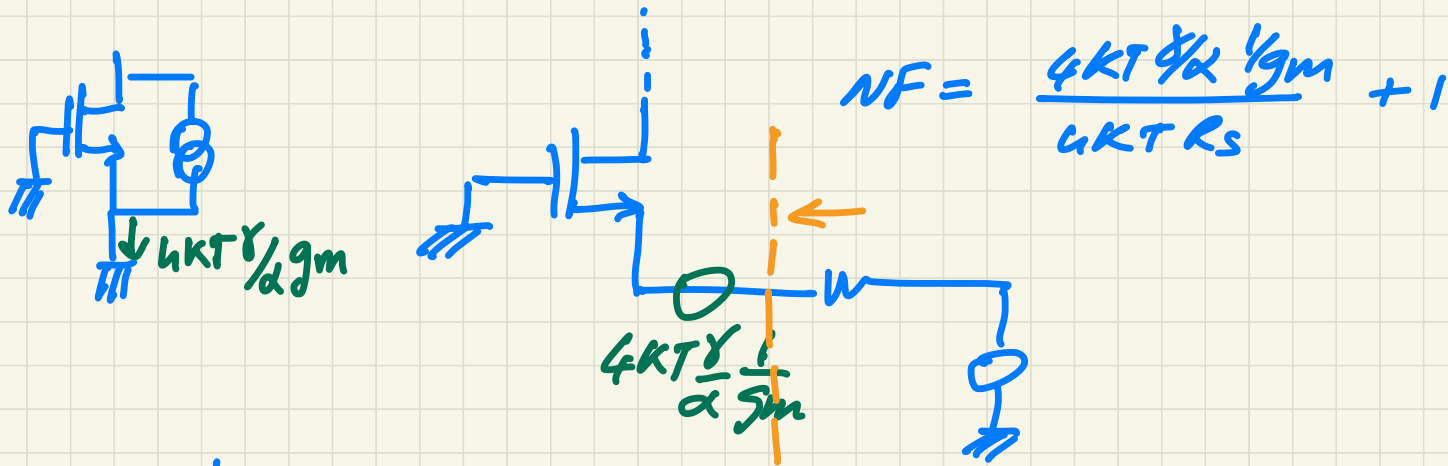
$$I_o = 1 \text{ mA}$$

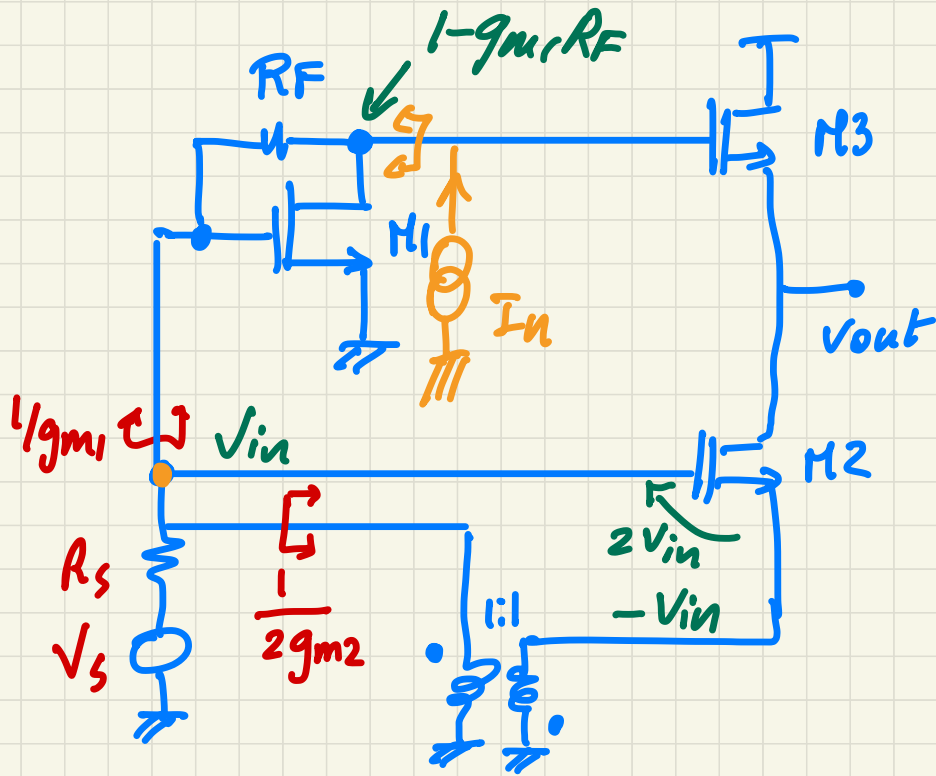


$$I_{out}(t) = [I_o + I_N(t)] \cdot X_{Lo}(t)$$



$$\begin{aligned}
 \Rightarrow I_{\text{out}}(t) &= [I_0 + \underline{I_2 \cos 2\omega_0 t}] \cdot \frac{1}{2} \left( \frac{4}{\pi} \cos \omega_0 t \right. \\
 &\quad \text{Differenziale} \\
 &\quad \left. - \frac{4}{3\pi} \cos 3\omega_0 t \right. \\
 &\quad \left. + \text{o.t.} \right) = \\
 &= \frac{2}{\pi} I_0 \cos \omega_0 t + \\
 &\quad + \frac{2}{\pi} \cdot \frac{I_2}{2} \cos \omega_0 t + \\
 &\quad - \frac{2}{3\pi} \cdot \frac{I_2}{2} \cos \omega_0 t + \text{o.t.}
 \end{aligned}$$





$$\frac{V_{out}}{I_{in}} = \text{path}_1 - \text{path}_2 = 0$$

$$Z_{in} = \frac{1}{g_{m1} + 2g_{m2}}$$

$$\frac{V_{out}}{V_{in}} = \underbrace{1 - g_{m1}R_F}_{\text{path A}} + \underbrace{\frac{2g_{m2}}{g_{m3}}}_{\text{path B}}$$

