

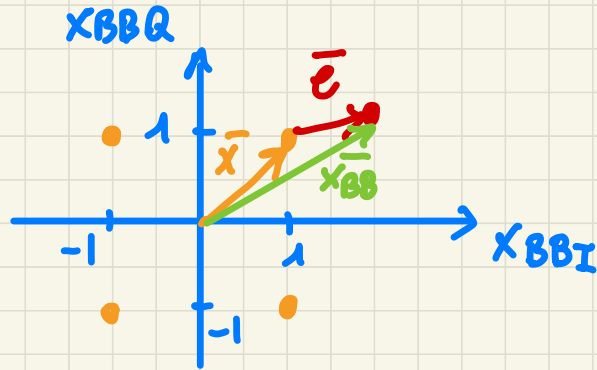
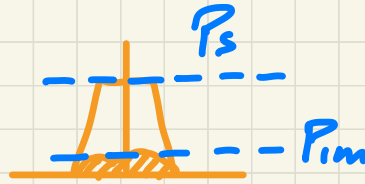
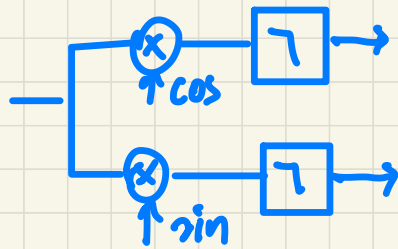
RF Circuit Design

L23



I/Q imbalances

$$IRR = \frac{P_S}{P_{Im}}$$



$$\begin{cases} x_{BBI} = x_I \left(1 + \frac{\epsilon}{2}\right) \cos \frac{\theta}{2} - x_Q \left(1 + \frac{\epsilon}{2}\right) \sin \frac{\theta}{2} \\ x_{BBQ} = x_Q \left(1 - \frac{\epsilon}{2}\right) \cos \frac{\theta}{2} - x_I \left(1 - \frac{\epsilon}{2}\right) \sin \frac{\theta}{2} \end{cases}$$

≈ 1
 $\approx \theta/2$

$$IRR = \frac{|\bar{x}|^2}{|\bar{e}|^2} = \frac{|\bar{x}|^2}{|\bar{x}_{BB} - \bar{x}|^2} = \frac{|x|^2}{(x_{BBI} - x_I)^2 + (x_{BBQ} - x_Q)^2}$$

$$\begin{aligned}
 \text{SNR} &= \frac{2}{\left[\left(1 + \frac{\varepsilon}{2}\right) \left(1 - \frac{\theta}{2}\right) - 1 \right]^2 + \left[\left(1 - \frac{\varepsilon}{2}\right) \left(1 - \frac{\theta}{2}\right) - 1 \right]^2} \\
 &\approx \frac{4}{\varepsilon^2 + \theta^2} = \frac{1}{\left(\frac{\varepsilon}{2}\right)^2 + \left(\frac{\theta}{2}\right)^2} = \text{IRR}
 \end{aligned}$$

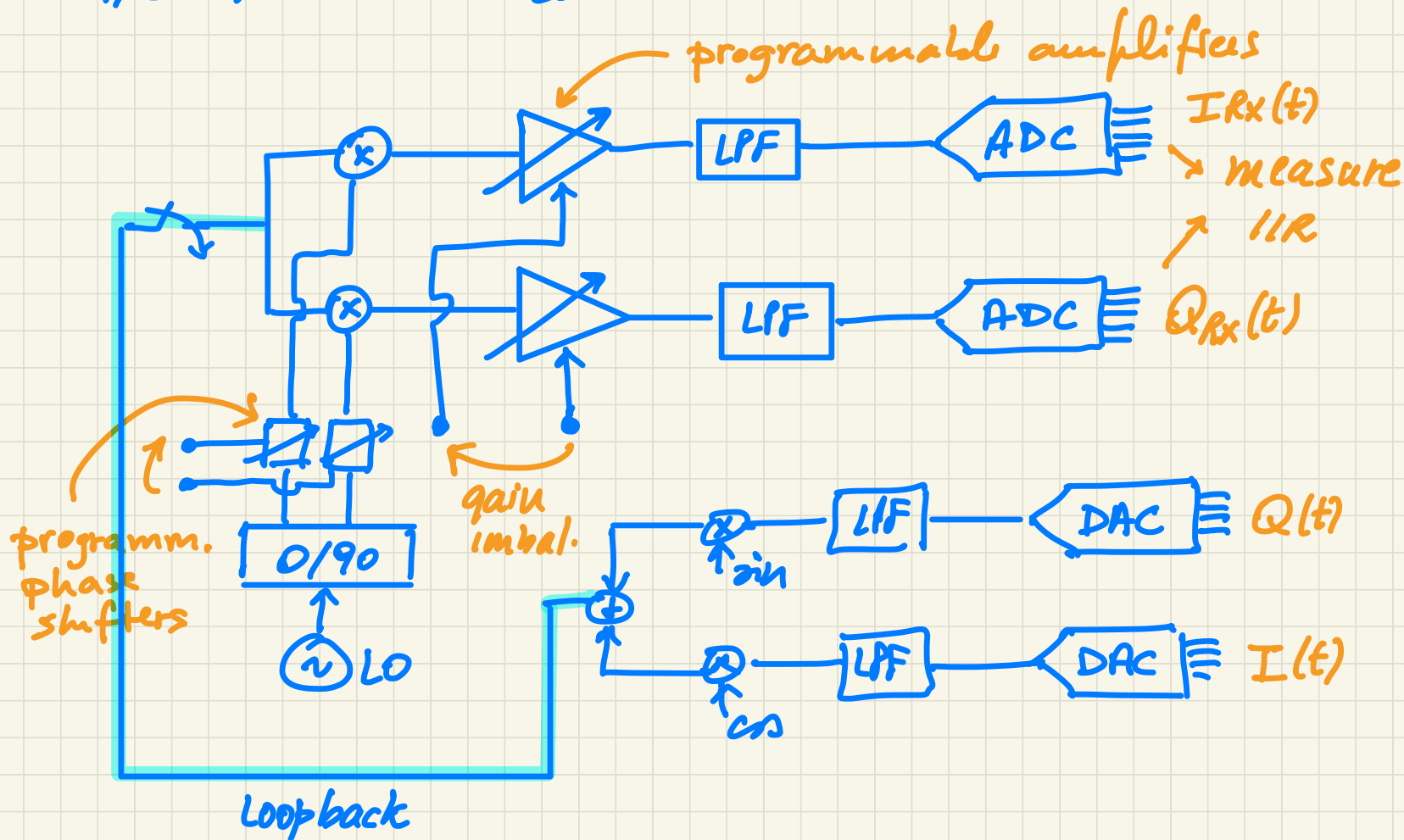
typically, an accurate design in GHz range
leads to $\text{IRR} \approx 30 \text{ dB}$

e.g. $\varepsilon = 0.1$ (10% matching)

$$\theta = 1^\circ = \frac{1^\circ}{180^\circ} \cdot \pi = 0.0174 \text{ rad} \quad (1 \text{ degree phase matching})$$

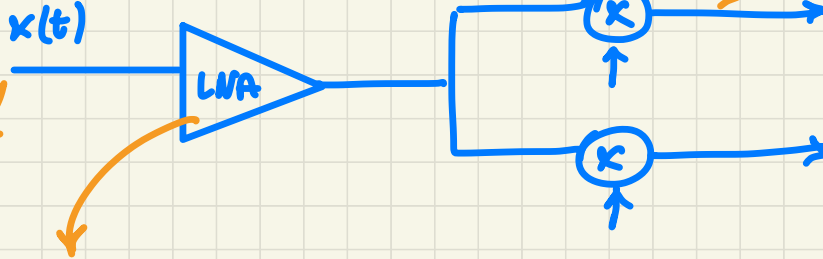
$$\Rightarrow \text{IRR} = 10 \log \frac{1}{0.00257} \approx 26 \text{ dB}$$

I/Q mismatch calibration

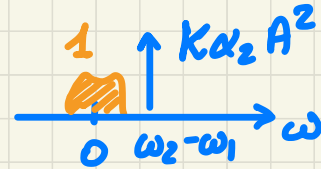


- Even - order distortion

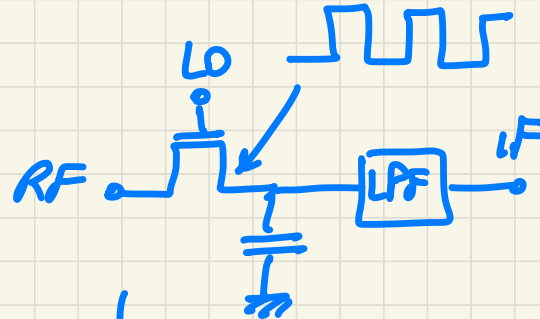
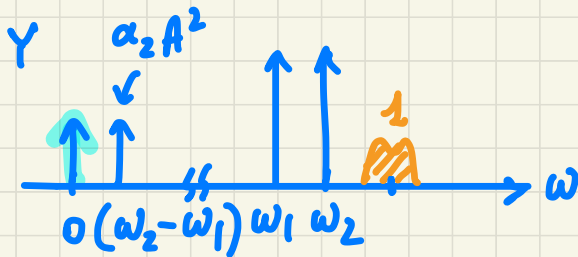
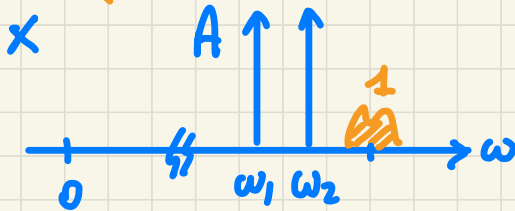
✓ sol.
use differential circuits



mixer RF-to-IF feedthrough



$$y(t) \approx \alpha_1 x(t) + \alpha_2 x^2(t)$$

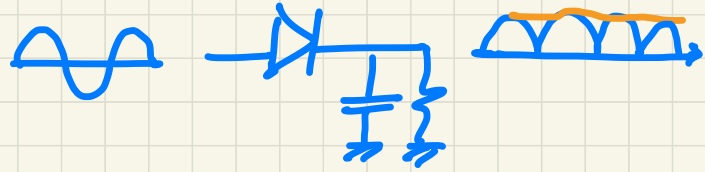
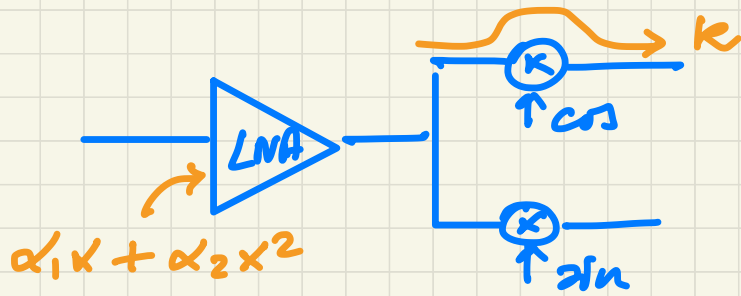


in single balanced mixer
 $K \approx -30 \text{ dB}$

$$V_{IF} = \left(\frac{1}{2}\right) V_{RF} + \text{o.t.} \Rightarrow K = \frac{1/2}{1/\pi} = \frac{\pi}{2}$$

$$A_V = \frac{V_{IF}(\omega_{IF})}{V_{RF}(\omega_{RF})} = \left(\frac{1}{\pi}\right)$$

Unwanted demodulation of AM interferers

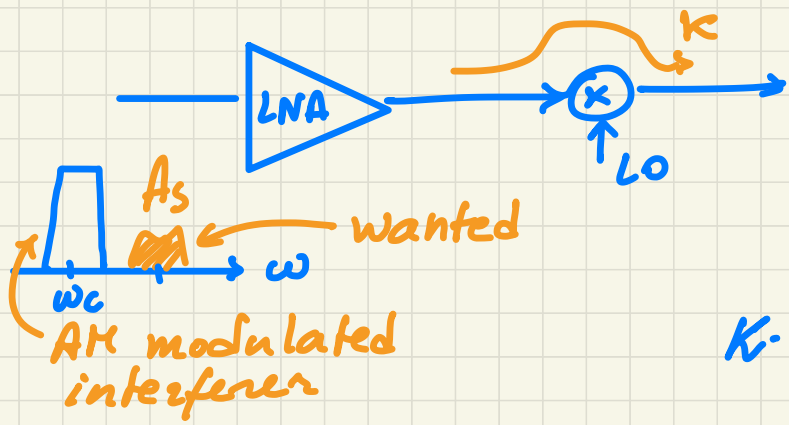


$$x(t) = \underbrace{[A_{int} + a(t)]}_{\text{AM modulation of an interferer}} \cdot \cos \omega_c t$$

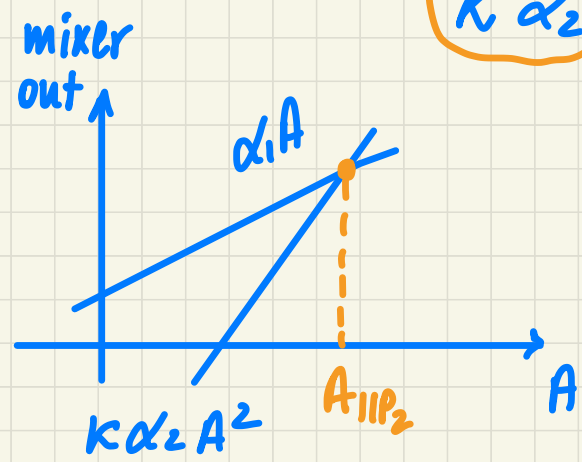
$$d_2 x^2(t) = \alpha_2 \cdot 2 \cdot A_{int} \cdot a(t) \cdot \cos^2 \omega_c t + o.t. =$$

$\frac{1 + \cos 2\omega_c t}{2}$

$$= \underbrace{\alpha_2 \cdot 2 \cdot A_{int} \cdot a(t) \cdot \frac{1}{2}}_{\text{Low-pass unwanted component}} + o.t. \rightarrow \underbrace{\alpha_2 A_{int}^2 \cdot \frac{1}{2}}_{\text{DC offset}}$$



$$\sqrt{SNR} = \frac{\alpha_1 \cdot A_{s,rms}}{K \alpha_2 \cdot A_{int} \cdot a_{rms}} = \frac{A_{1IP2} \cdot A_{s,rms}}{A_{int} \cdot a_{rms}}$$



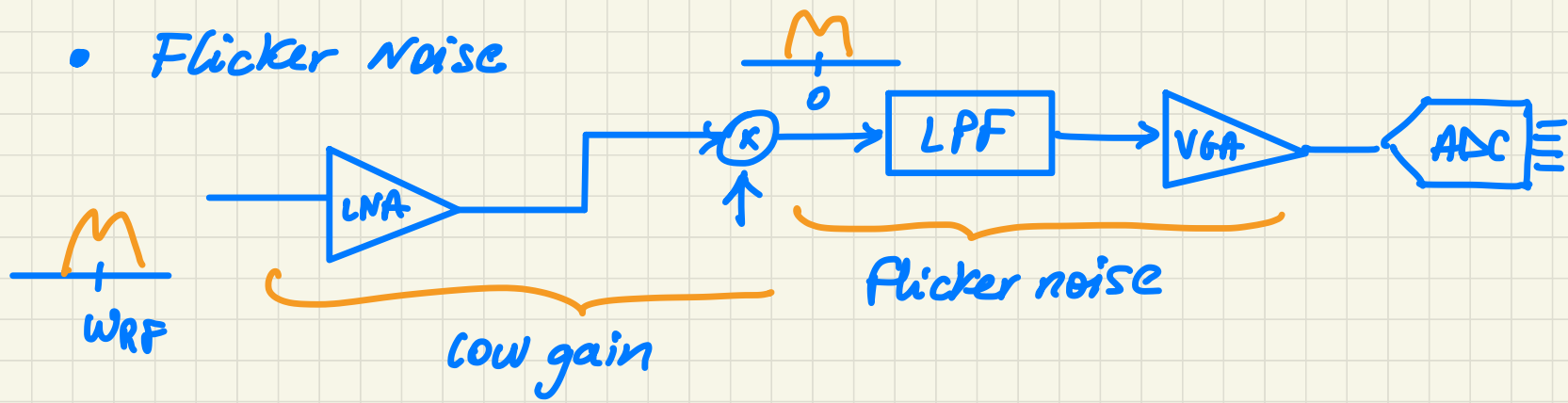
$$\alpha_1 A_{1IP2} = K \alpha_2 A_{1IP2}^2$$

$$\Downarrow$$

$$A_{1IP2} = \frac{\alpha_1}{K \alpha_2}$$

2nd nonlin.
demodulates
amplitude
modulations

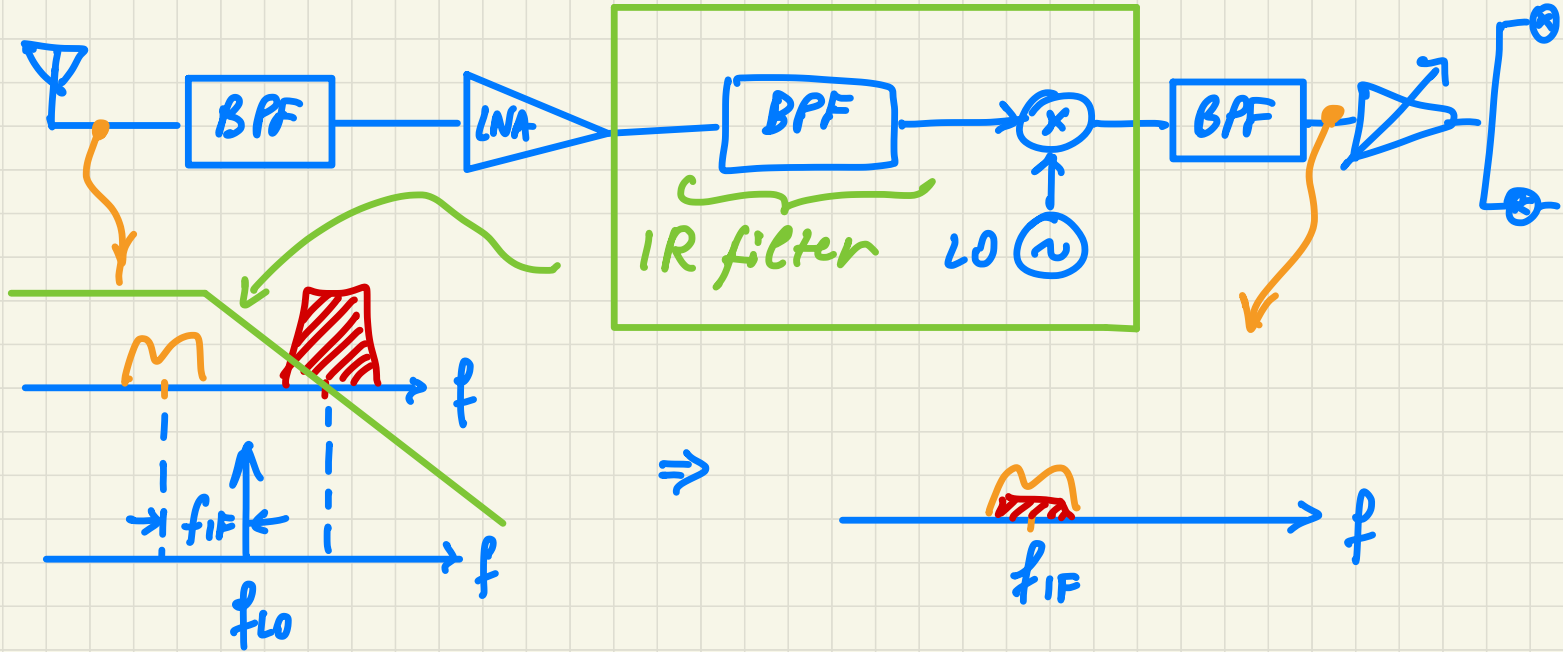
- Flicker noise



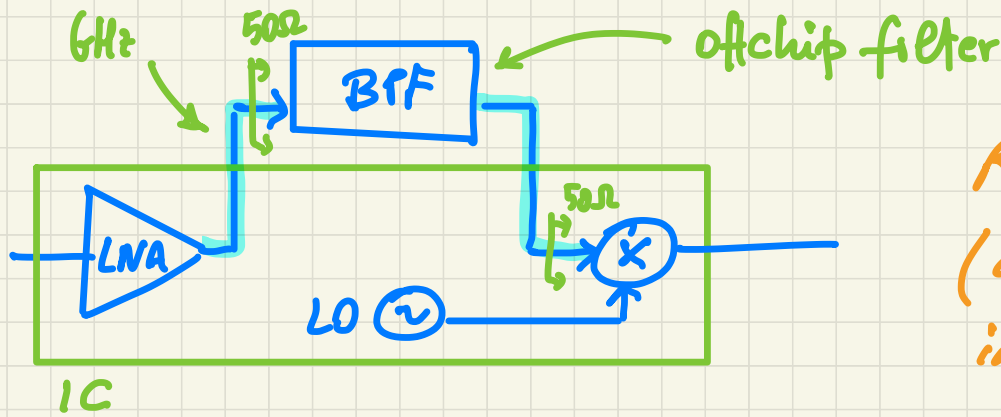
- Solutions:
- large devices in mixers and VGA/LPF
 - offset cancellation techniques

Image - Reject Receivers

image rejection
based on filtering



Variant : dual-IF architecture (to relax image problem)

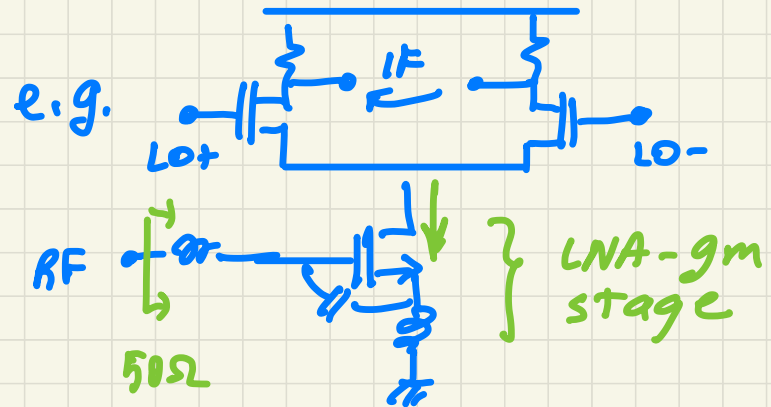
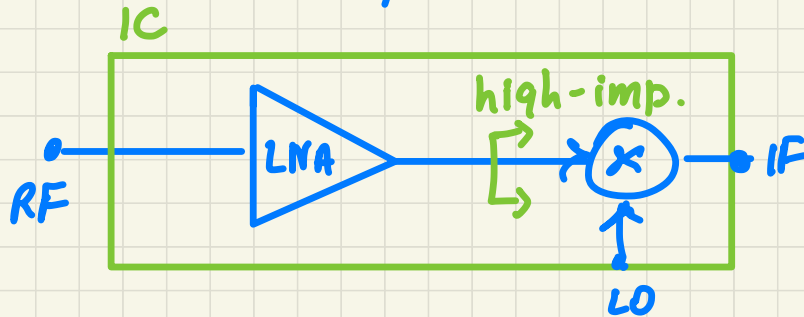


RF off-chip blocks (as filters) require impedance matching



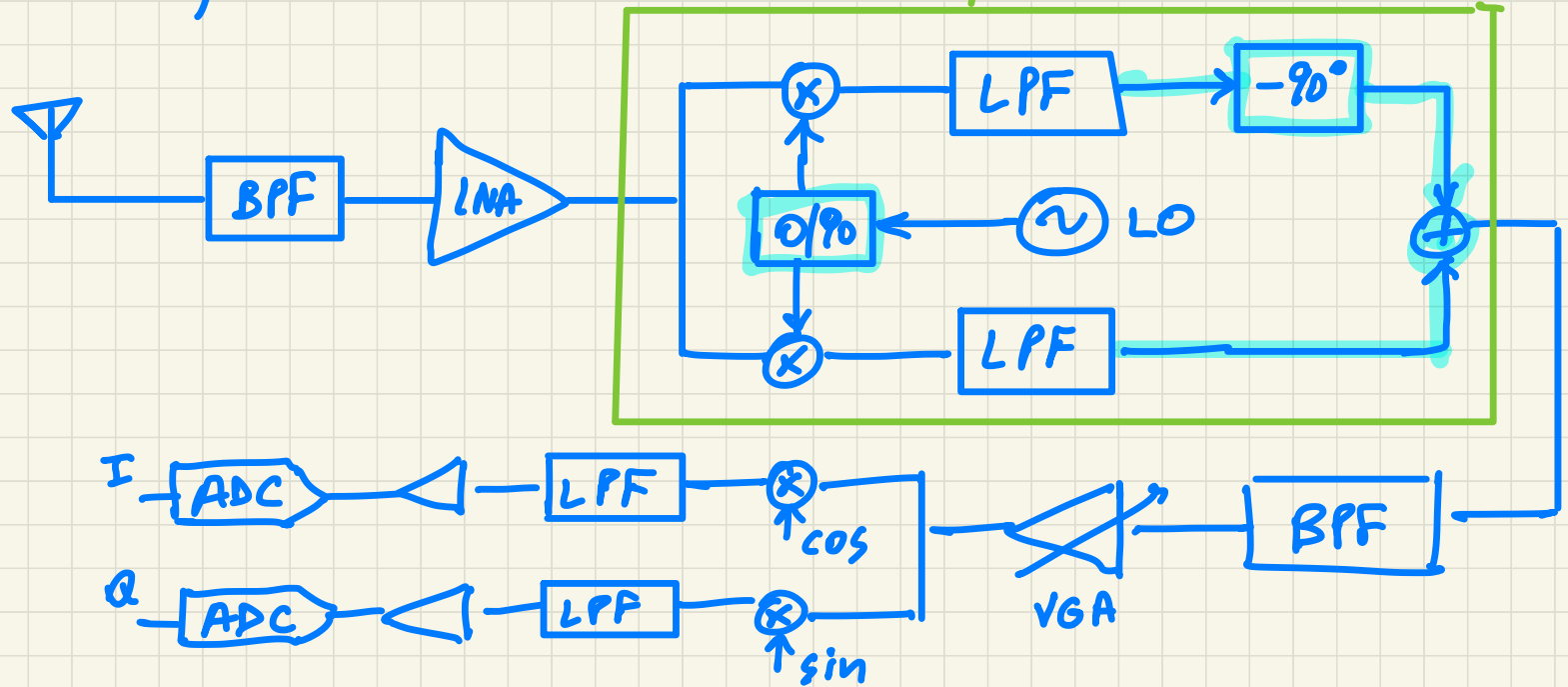
large power consumption

LNA : requires an output stage to drive 50Ω impedance

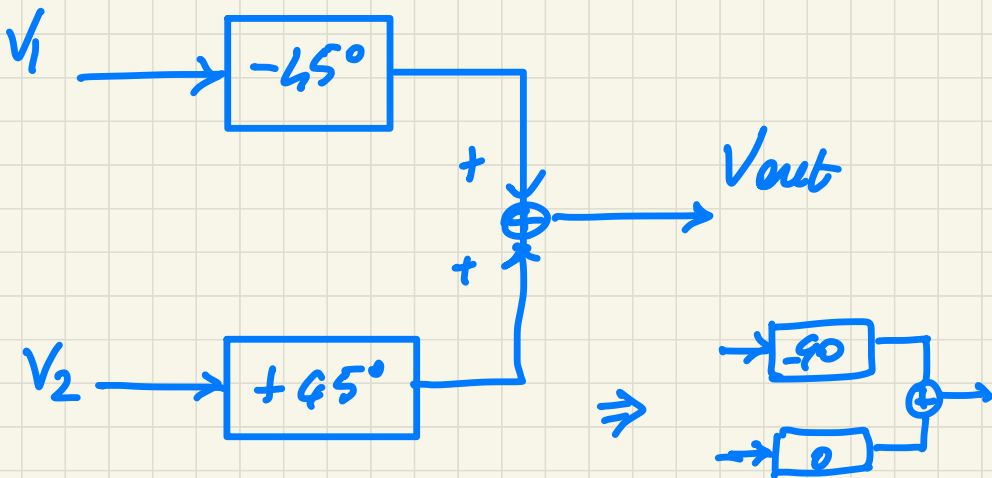
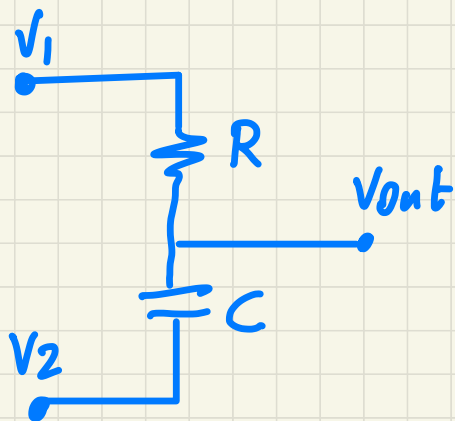
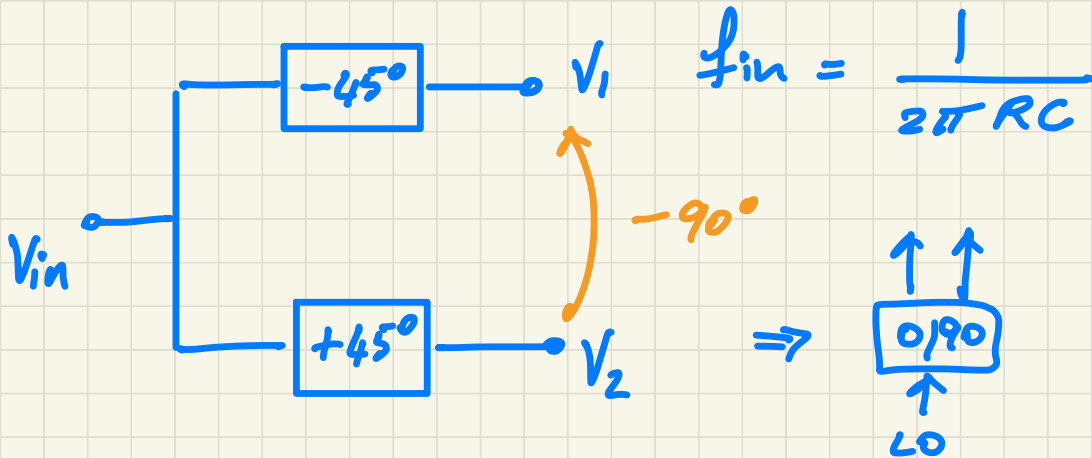
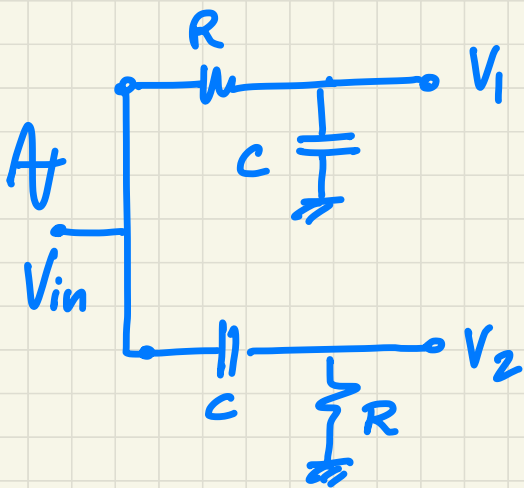


Hartley Image-reject RX

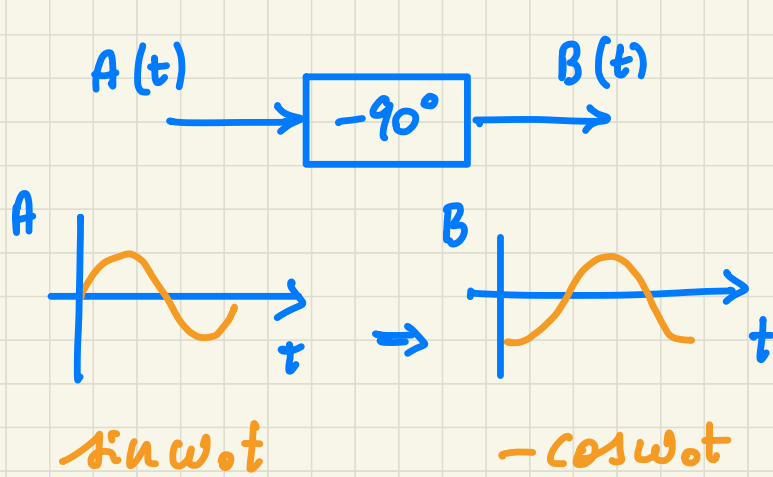
Replaces BPF + mixer



Avoids ext. BPF filter for image rejection
Requires two mixers, quadrature LO



Transfer function of phase shifter

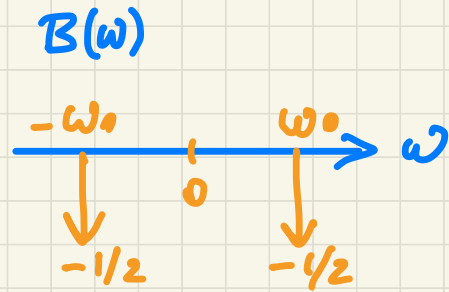
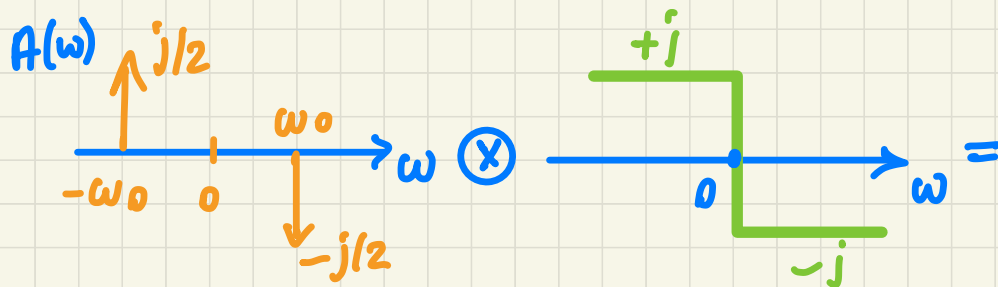


$$\sin \omega_0 t = j \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{-2j}$$

Fourier transform pairs for the input signal:

- $\sin \omega_0 t \xrightarrow{\mathcal{F}} j/2 \delta(\omega - \omega_0) - j/2 \delta(\omega + \omega_0)$

In Fourier domain:



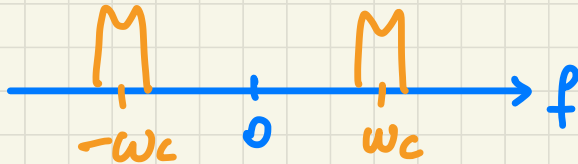
$$G(\omega) = -j \cdot \text{sign}(\omega)$$

transfer function

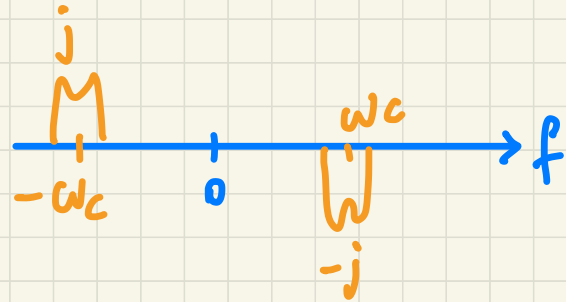
$$A(\omega)$$

$$B(\omega) = G(\omega) \cdot A(\omega)$$

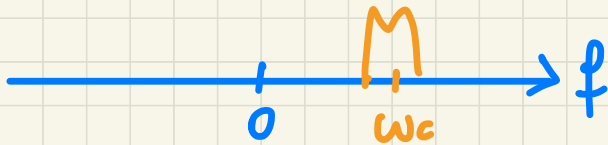
Hilbert transform



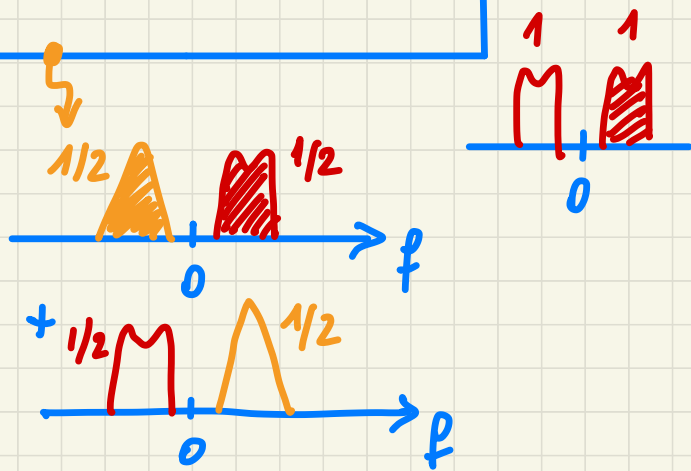
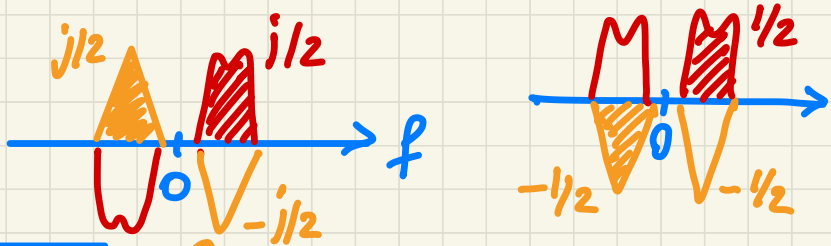
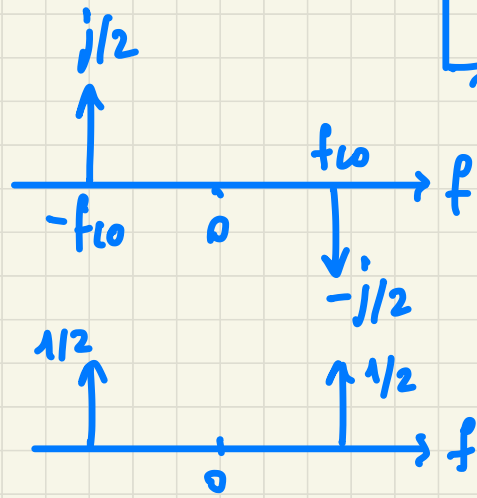
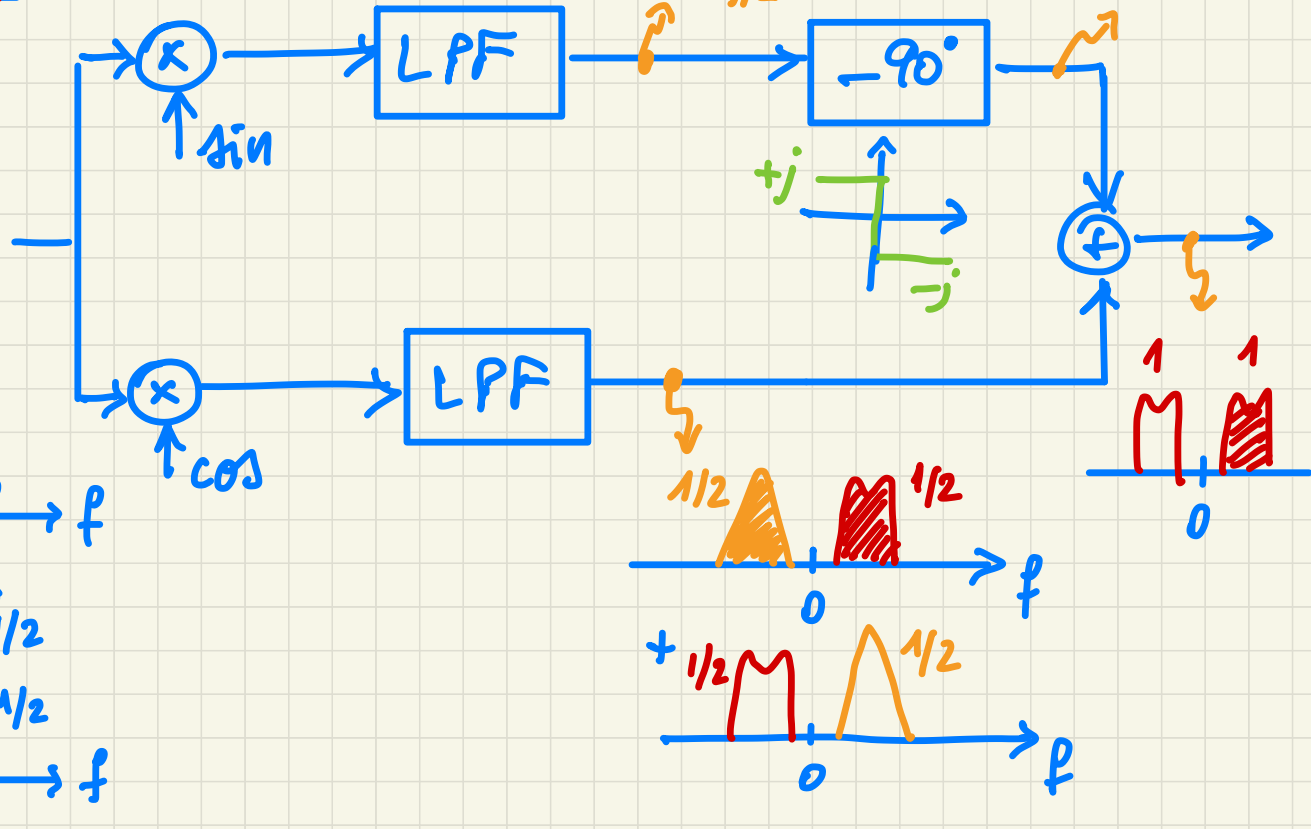
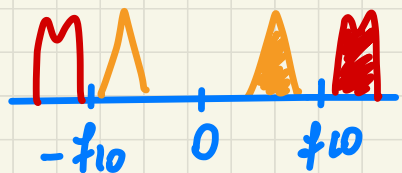
\Rightarrow

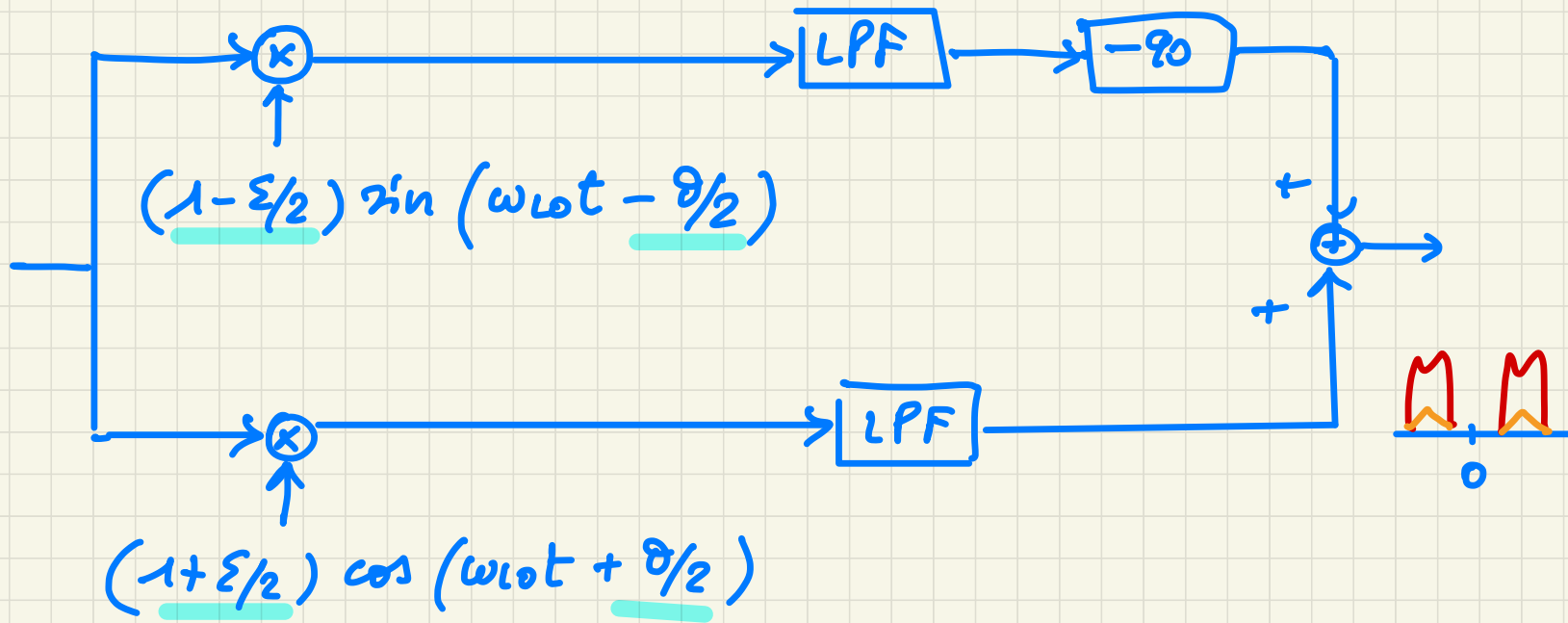


$$S(\omega) = \underbrace{A(\omega)} + j \cdot B(\omega) \quad \text{Analytical signal}$$



$$A(t) = \text{Re} \{ S(t) \}$$





$$IRR = \frac{P_s}{P_{im}} = \dots = \frac{4}{\epsilon^2 + \theta^2}$$