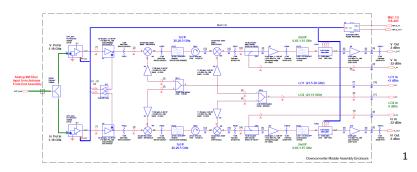
Polyphase Filtering: A Physicist's Understanding

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Introduction



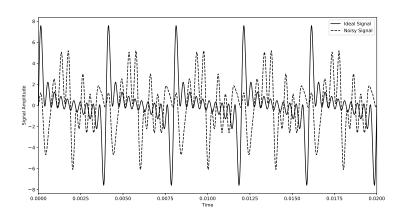
The digital revolution has changed many aspects of modern life. Scientific instrumentation has been no exception.

Et Tu, Science? The Fall Analog.

In the EOVSA array, the signal is digitized at the receiver, then sent to the control room. Why?

Digital vs. Analog: A Phase Fight

In analog systems, the gain to phase balance of a signal cannot be maintained to better than 1% over a range of temperatures (Harris, 2005).²





Signals, Nyquist Theorem, and Frequency Resolution

How do we digitize signals?

Nyquist Theorem

$$f_{crit} = \frac{f_{samp}}{2} \tag{1}$$

In radio astronomy, to measure a 10 GHz signal, we would need to process 20 billion samples, or around 160 Gigabytes of data, a second. Seem unreasonable? It is.

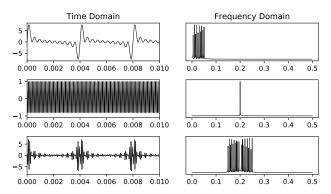
Along with Nyquist, there is a limit to how much resolution there is between frequencies when using Fast Fourier Transform(FFT), which is given by

$$f_{res} = f_{samp}/N$$
 (2)

where N is the number of sample points given to the FFT.

Downconversion: The Hero Gotham Deserves

Downconversion allows us to get around the absurd data requirement above. But how?



Downconversion: The Hero Gotham Deserves

Side Lobes: A Pain in the Power Spectra

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Windowing Functions: The Good, the Bad, and the Unresolved

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Filter Banks

The Polyphase Implementation: An Example

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When Windows Break: Channelizers and Polyphase Implementation

Complicate the Theory, Simplify the Hardware?

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The Universe Talks in Channels?

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