## Computational Methods for Macroeconomics

Hanbaek Lee University of Cambridge Michaelmas 2024

## Assignment 1

A household consumes and supplies labor in the following way:

$$R(a, z) = \max\{W(a, z), N(a, z)\}$$

$$W(a, z) = \max_{c, n, a'} log(c) - \eta \frac{1}{1 + \frac{1}{\chi}} n^{1 + \frac{1}{\chi}} + \beta v(a')$$
s.t.  $c + a' = zw(1 - \tau)n + a(1 + r(1 - \tau)) + T$ 

$$N(a, z) = \max_{c, a'} log(c) + \beta v(a')$$
s.t.  $c + a' = b + a(1 + r(1 - \tau)) + T$ 

The idiosyncratic productivity z satisfies  $log(z) \sim_{iid} N(0, \sigma_z)$ . The production sector operates as follows:

$$Y = \max_{L} AK^{\alpha}L^{1-\alpha} - wL - rK$$

The government budget balance condition is as follows:

$$\underbrace{\int (wzh + ar)\tau d\Phi}_{\text{Revenue}} = \underbrace{\int_{\{\mathcal{NW}\}} bd\Phi + T}_{\text{Spending}}$$

Wage is determined in the following competitive effective labor market:

$$L^* = \int z n^*(z) d\Phi$$

- 1. Label and interpret the model ingredients properly.
- 2. Characterize the individual labor supply curve.
- 3. Characterize the aggregate labor supply curve.
- 4. Characterize the aggregate labor demand curve.
- 5. Suppose the following parameter levels:

$$a=1, \quad \alpha=0.3, \quad \tau=0.15, \quad \overline{z}=1, \quad A=1, \quad r=0.04, \quad \beta=0.96$$

Define and characterize the stationary recursive competitive equilibrium.

- 6. Visualize the aggregate supply and demand curves in the labor market.
- 7. Visualize the comparative statics of the wage with respect to the change in A (horizontal axis: A, vertical: w).
- 8. (Method of simulated moments) Estimate the parameters  $(\eta, b, \chi, \sigma_z)$  to match the following hypothetical moments in general equilibrium:
  - Total working hours: 0.33.
  - Unemployment rate: 0.06 (Assume unemployed = non-working).
  - Unemployment benefit: 25% of average wage income.
  - STD/Mean ratio of income: 0.70.
- 9. Counterfactual exercise: How does an increase in tax rate from 0.15 to 0.16 affects the total income inequality? (including non-working households). Check the various inequality measures.
- 10. Counterfactual exercise: Suppose  $\eta$  increases instantaneously by 20% (Say, Covid 19). How does it affects the total income inequality? (including non-working households). Check the various inequality measures.