

自然語言處理與應用 Natural Language Processing and Applications

Statistical Language Models and Basic Word Representations

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生成式AI融合教學

- 以組為單位
 - ChatGPT Plus
 - Google Colab Pro 雲端運算付費服務
 - OpenAl API 呼叫大型語言模型進行生成式服務



自然語言處理基本功 (如何表達字詞)

- Week 1 Week 3
 - 自然語言處理介紹
 - 統計語言模型與基本詞向量方法
 - 詞嵌入模型





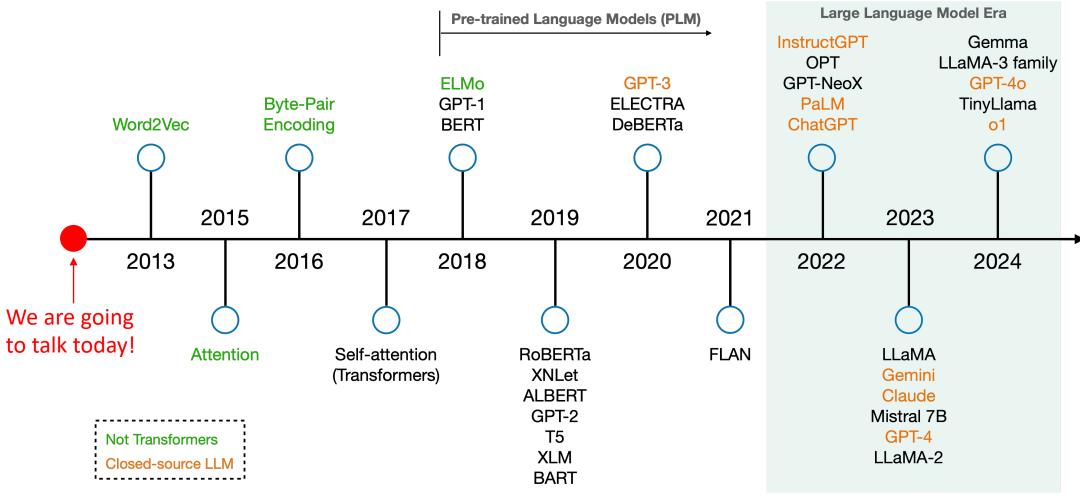
Outline

- Basic Word Representations
 - One-hot encodings
 - PMI
 - LSA
 - Bag-of-words (document representations)
 - TF-IDF (document representations)
- Language Models



Basic Word Representations

Language Model Evolution Path





Word Representations with One-hot Encodings



Basic Approach

Corpus

I like to eat apple

You like to watch TV

Vocabulary

apple [1, 0, 0, 0, 0, 0, 0, 0]

eat [0, 1, 0, 0, 0, 0, 0, 0]

l [0, 0, 1, 0, 0, 0, 0, 0]

like [0, 0, 0, 1, 0, 0, 0, 0]

watch [0, 0, 0, 0, 1, 0, 0, 0]

to [0, 0, 0, 0, 0, 1, 0, 0]

One hot encodings with each vector size equal to the vocab size (8 in this case)

Pros: handy, training-free **Cons**: sparse matrix which occupies much memory



- "A word is characterized by the company it keeps" was popularized by Firth (1957).
- In other words, semantically similar words may appear in similar contexts.

I drink <u>beer</u>. The <u>cat</u> licked its fur.

We drink wine. The Persian cat licked its fur.



Co-occurrence Matrices (共現矩陣)

Corpus

I love deep learning.

I love NLP.

I do programming.

Here the context size is set to 1.

	ı	love	do	deep	learning	NLP	progra mming
1	0	2	1	0	0	0	0
love	2	0	0	1	0	1	0
do	1	0	0	0	0	0	1
deep	0	1	0	0	1	0	0
learning	0	0	0	1	0	0	0
NLP	0	1	0	0	0	0	0
progra mming	0	0	1	0	0	0	0



Problem of Co-occurrence Matrices

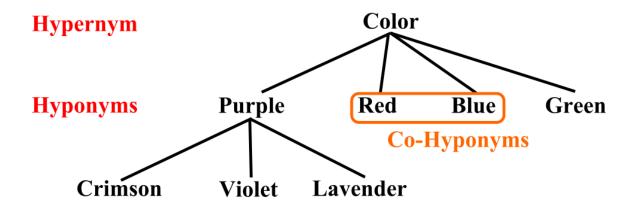
- High-frequency words impact the representations.
 - Such as "the", "a", "an"
- High-frequency words that do not significantly affect the semantics are stopwords.
- You can check common stopwords via:

from nltk.corpus import stopwords
stop_words = list(stopwords.words('english'))



NLTK (Natural Language Toolkit)

- Preprocessing functions: tokenization, removing stopwords
- WordNet
- ...





PMI (Pointwise Mutual Information)

 To fix the problem of co-occurrence matrix, we can discard the counting-based approach.

Given words w_i and w_j , their PMI score is:

$$PMI(w_i, w_j) = \log_2 \frac{P(w_i, w_j)}{P(w_i)P(w_j)}$$



The PMI Matrix

Corpus

I love deep learning.

I love NLP.

I do programming.

Here the context size is set to 1.

	ı	love	do	deep	learning	NLP	progra mming
1	-inf	1.222	1.222	-inf	-inf	-inf	-inf
love	1.222	-inf	-inf	0.807	-inf	1.807	-inf
do	1.222	-inf	-inf	-inf	-inf	-inf	2.807
deep	-inf	0.807	-inf	-inf	2.807	-inf	-inf
learning	-inf	-inf	-inf	2.807	-inf	-inf	-inf
NLP	-inf	1.807	-inf	-inf	-inf	-inf	-inf
progra mming	-inf	-inf	2.807	-inf	-inf	-inf	-inf



PPMI (Positive Pointwise Mutual Information)

$$PPMI(w_i, w_j) = \max \left(0, PMI(w_i, w_j)\right)$$
$$= \max \left(0, \log_2 \frac{p(w_i, w_j)}{p(w_i)p(w_i)}\right)$$

Or
$$PPMI(w_i, w_j) = PMI(w_i, w_j) + \epsilon$$

where ϵ is a small positive number.



The PPMI Matrix

Corpus

I love deep learning.

I love NLP.

I do programming.

Here the context size is set to 1.

	ı	love	do	deep	learning	NLP	progra mming
1	0	1.222	1.222	0	0	0	0
love	1.222	0	0	0.807	0	1.807	0
do	1.222	0	0	0	0	0	2.807
deep	0	0.807	0	0	2.807	0	0
learning	0	0	0	2.807	0	0	0
NLP	0	1.807	0	0	0	0	0
progra mming	0	0	2.807	0	0	0	0



Latent Semantic Analysis (LSA)

- latent (adj.)潛在的; Latent Semantic Analysis:潛在語義分析
- Current problems:
 - 1. 資料問題
 - 有出現不見得是相關
 - 沒出現不見得是無關
 - 2. 維度問題
 - The vector size is equal to the vocab size, which takes much memory.



Singular Value Decomposition (SVD)

Formula of SVD:

$$A = U\Sigma V^{\mathsf{T}}$$

where:

A: data matrix from PMI/PPMI or cooccurrence matrix.

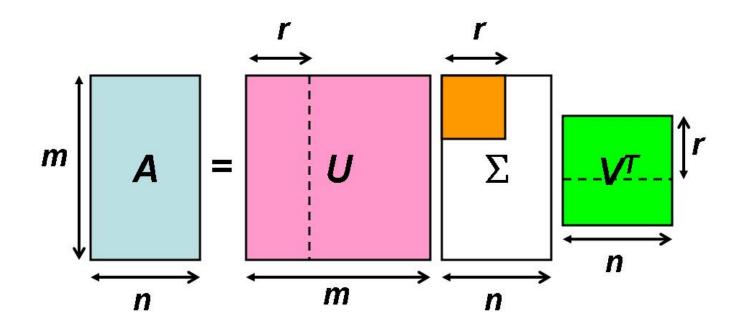
U: Left orthogonal matrix

Σ: diagonal matrix,對角線上的值為奇異值

V: Right orthogonal matrix



Singular Value Decomposition (SVD)



- 我們關注的是column space的
 降維 (以保留vocab維度)
- 因此我們可以取*U*的前r個向量 作為我們降維後的目標

Dimensionality Reduction (降維)!



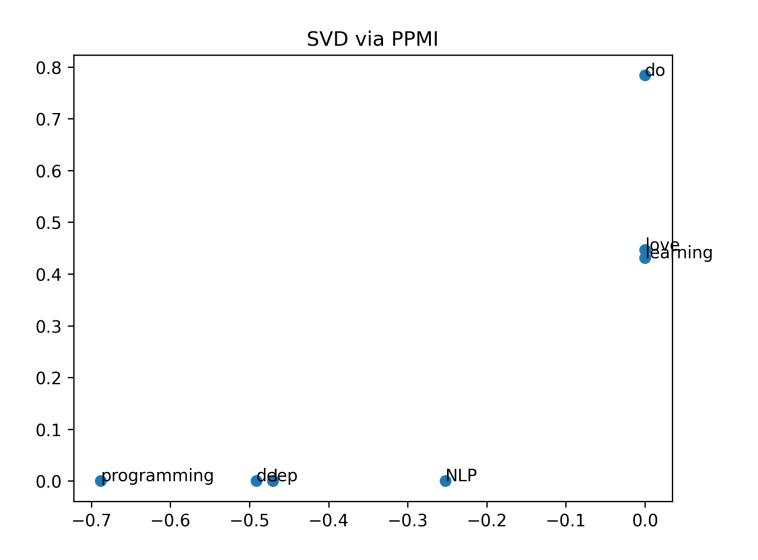
Results after SVD from the PPMI Matrix

Vocab	Dimension 1	Dimension 2
1	-0.47030617476956654	-4.440892098500626e-16
love	-8.326672684688674e-16	0.4464710977801294
do	8.881784197001252e-16	0.7838949952895327
deep	-0.4915010045415975	-1.3016463110087907e-16
learning	-1.582067810090848e-15	0.4314767609119055
NLP	-0.2523320838384413	-2.1837832516159107e-16
programming	-0.6881623238553303	-1.914220234434739e-16

原本一個字需要7個維度才能表示,但現在經過SVD之後只需要2個維度



Visualization of the SVD Results





Problems of SVD

- We can perform Singular Value Decomposition (SVD) for dimensionality reduction, however at a quadratic $(O(n^2))$ computational cost.
- In other words, SVD is slow for a big matrix.
- Adding a new word changes the entire matrix.



Summary

Methods	Туре	Word Order?	Semantics?	Dimensionality Reduction
One-hot Encodings		×	×	×
Co-occurrence / PMI /PPMI matrix	Word Embeddings	×	✓ (Co-occurrence)	×
LSA		×		(Computationally Expensive)



Embedding Lookup

Index	Vocab	Dimension 1	Dimension 2
0	I	-0.47030617476956654	-4.440892098500626e-16
1	love	-8.326672684688674e-16	0.4464710977801294
2	do	8.881784197001252e-16	0.7838949952895327
3	deep	-0.4915010045415975	-1.3016463110087907e-16
4	learning	-1.582067810090848e-15	0.4314767609119055
5	NLP	-0.2523320838384413	-2.1837832516159107e-16
6	programming	-0.6881623238553303	-1.914220234434739e-16



Basic Document Representations

Bag-of-words Model

Meaning: Each document (sentence) carries a bag of words.

Bag of words (BoW)

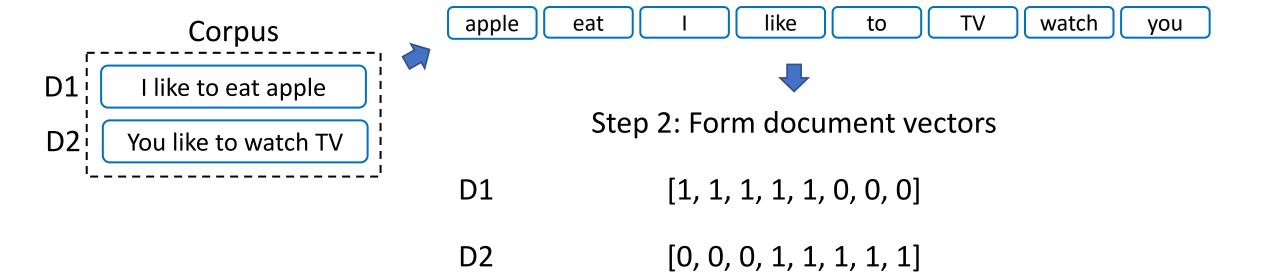
Very good drama although it appeared to have a few blank areas leaving the viewers to fill in the action for themselves. I can imagine life being this way for someone who can neither read nor write. This film simply smacked of the real world: the wife who is suddenly the sole supporter, the live-in relatives and their quarrels, the troubled child who gets knocked up and then, typically, drops out of school, a jackass husband who takes the nest egg and buys beer with it. 2 thumbs up... very very very good movie.



```
('the', 8),
(',', 5),
('very', 4),
('.', 4),
('who', 4),
('and', 3),
('good', 2),
('it', 2),
('to', 2),
('a', 2),
('for', 2),
('can', 2),
('this', 2),
('of', 2),
('drama', 1),
('although', 1),
('appeared', 1),
('have', 1),
('few', 1),
('blank', 1)
```



Bag-of-words Model (Example 1)



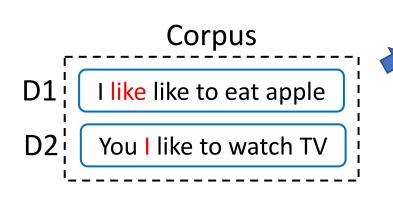
Notes:

- The vector size is equal to the vocab size.
 - Each position of a vector is corresponding to the position in the vocab.

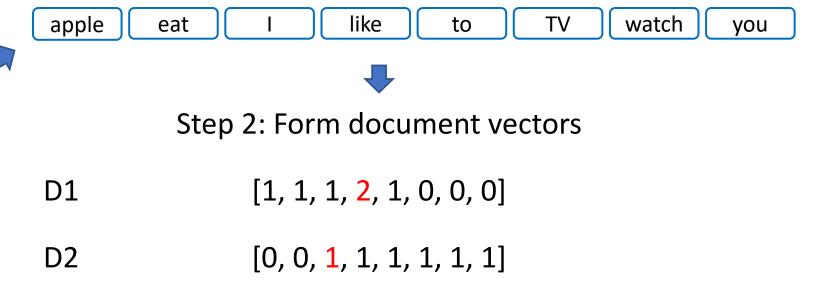
Step 1: Find unique words (vocab)



Bag-of-words Model (Example 2)



Step 1: Find unique words (vocab)



Notes:

- The vector size is equal to the vocab size.
- Each position of a vector is corresponding to the position in the vocab.



TF-IDF

> The mathematical representation of TF-IDF:

$$TF-IDF = TF \times IDF$$

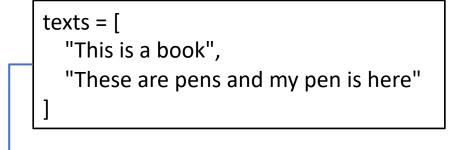
where
$$\mathrm{TF}_{i,j} = \frac{n_{i,j}}{\sum_k n_{k,j}} \qquad \mathrm{IDF_i} = \log \frac{|D|}{|\{j: t_i \in d_i\}|}$$

- \circ Where $n_{i,j}$ is the i-th word in the j-th document in the dataset.
- > TF (Term Frequency)
 - Represents the "frequency" of a term appearing in a text.
- IDF (Inverse Document Frequency)
 - Aims for terms to have higher specificity, meaning the fewer texts in the dataset contain the term, the better.

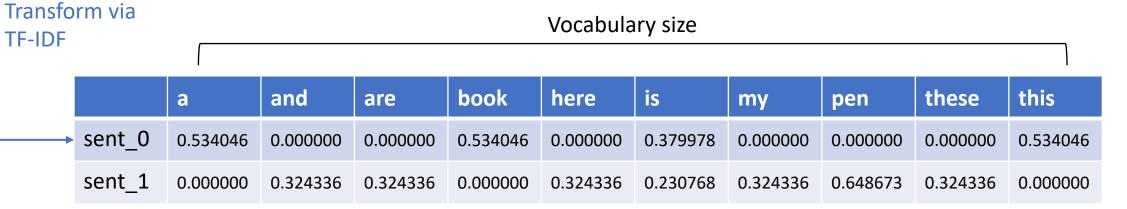


Sparse Embeddings: TF-IDF

- TF (Term Frequency)
- IDF (Inverse Document Frequency)



- The **TF-IDF** approach creates document embeddings.
- The embedding size is equal to the vocabulary size.
- Each value of an embedding is based on **TF x IDF**.

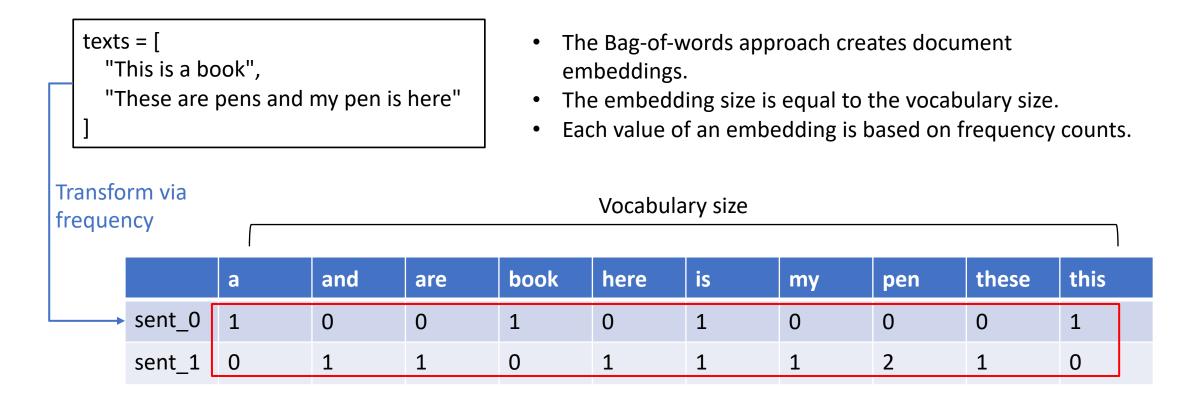


Since the outputs contain many zeros, this approach is called a sparse embedding method.

https://github.com/tsmatz/nlp-tutorials/blob/master/01_sparse_vector.ipynb



Sparse Embeddings: Bag-of-words



Since the outputs contain many zeros, this approach is called a sparse embedding method.



Preprocessing steps before creating vectors

Preprocessing text (optional)

- Stemming
 - By removing the suffixes from words (e.g. "cats," "catlike," "catty" all have "cat" as their base), we can revert the words back to their root forms.
- Feature Selection
 - ☐ Filter and select which parts of speech to retain, such as verbs or nouns.
 - ☐ Adjust the frequency of the terms (hyperparameter) using statistical methods or algorithms like TF-IDF.



Sparse Vectors

Sparse vector embeddings represent words as high-dimensional vectors with mostly zero values.

Each dimension corresponds to a unique feature (word), measure by some well-designed methods.

- ❖ TF-IDF, Bag-of-words
- ❖ PPMI



Dense Vectors

Dense vector embeddings represent words in a continuous vector space Semantically similar words are closer together.

- Word2Vec
- Contextualized Embeddings



Common NLP tasks

Text Classification

Text Generation

Sequence Tagging Text Matching

Sentiment Analysis

Machine Translation Part-of-speech tagging

Semantic Textual
Similarity

Natural Language Inference (NLI)

Summarization

Named Entity Recognition (NER)

Retrieval

Dialogue Generation Word Segmentation

BoW and TF-IDF can be used!



Semantic Textual Similarity

https://huggingface.co/datasets/sentence-transformers/stsb

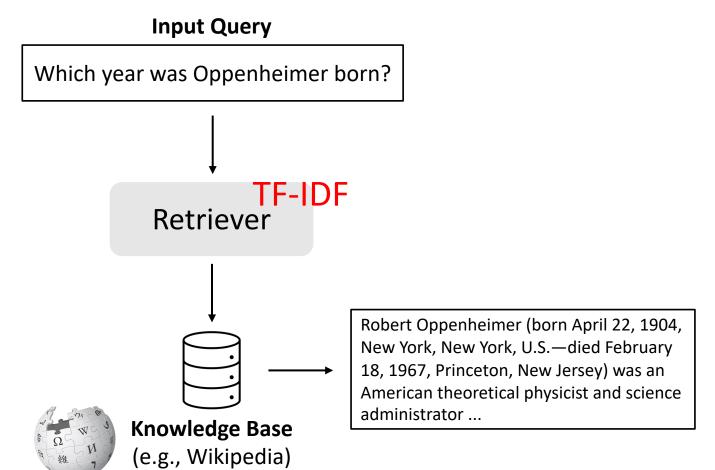
STS-B dataset

```
{
  'sentence1': 'A man is playing a large flute.',
  'sentence2': 'A man is playing a flute.',
  'score': 0.76,
}
```

```
{
    'sentence1': 'Two boys are driving.',
    'sentence2': 'Two bays are dancing.',
    'score': 0.12,
}
```



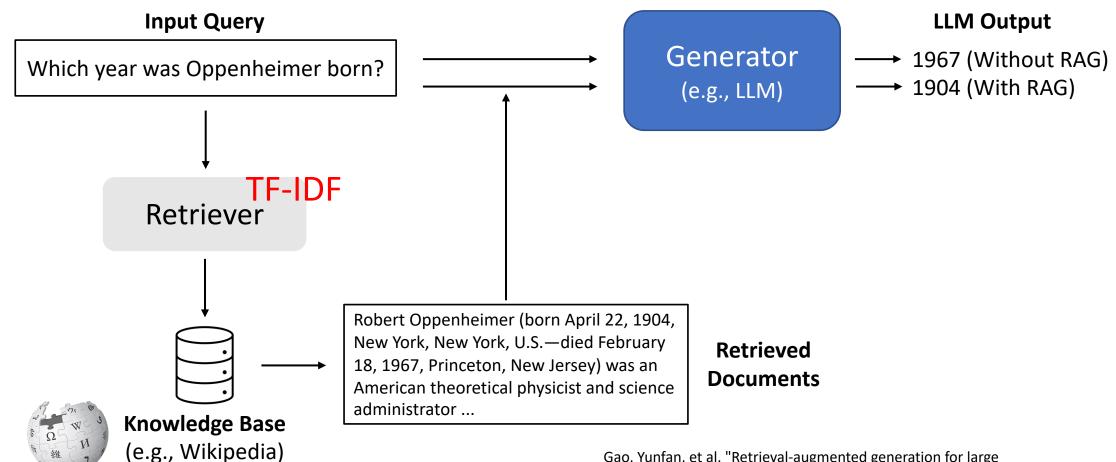
Retrieval



Retrieved Documents



Retrieval-Augmented Generation (RAG)



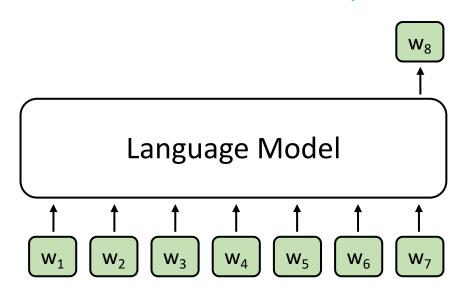


Gao, Yunfan, et al. "Retrieval-augmented generation for large language models: A survey." *arXiv preprint arXiv:2312.10997* (2023).

Language Models

What is a language model?

(The next word)



$$P(w_t|w_1, w_2, ..., w_{t-1})$$

- A model that assigns probabilities to upcoming words is called a language model.
- The task involving predictions of upcoming words is language modeling.



N-gram Language Modeling

Let's begin with the task of computing the probability (also called relative frequency)

$$P(w|h) = rac{C(w,h)}{C(h)}$$
 with his solution $C(t)$

w: the word to be generated

h: some history

C: the times the pattern show up in the dataset

 For example: Compute the probability of the word "the" given the history "its water is so transparent that".

$$P(the|its\ water\ is\ so\ transparent\ that) = rac{C(its\ water\ is\ so\ transparent\ that\ the)}{C(its\ water\ is\ so\ transparent\ that)}$$

For an N-gram LM, N=7 here



LM vs. n-gram LM

Language Model

Full history: P(Parliament | I declare resumed the session of the

European)

N-gram Language Model (only n-1 previous words are considered)

(example) Trigram: P(Parliament | the European)



Training and Evaluations

Training Set (訓練資料集)



Training Set (訓練資料集) Validation Set (驗證資料集)





Test Set (測試資料集)





Perplexity

Perplexity (PPL) is a quantitative criterion used to evaluate the capacities of language modeling models.

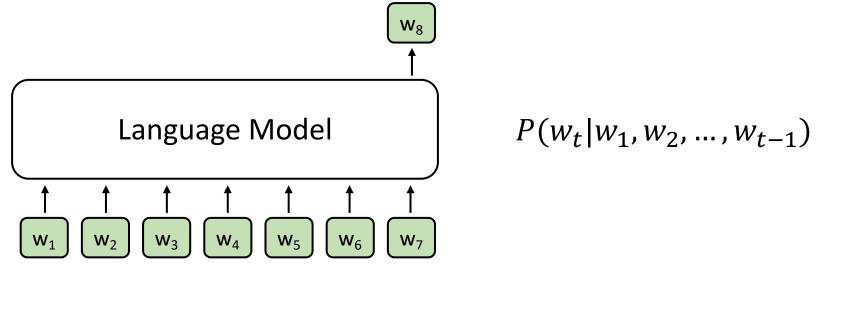
• Given the sequence of words $W=w_1,w_2,\ldots,w_N$ and an n-gram language model. The PPL of the model was computed by:

Perplexity(W) =
$$P(w_1, w_2, ..., w_N)^{-\frac{1}{N}} = \sqrt[N]{\prod_{t=1}^{N} \frac{1}{P(w_t | w_{t-n+1}, ..., w_{t-1})}}$$

The lower the value of perplexity, the better the language modeling capability of the model.



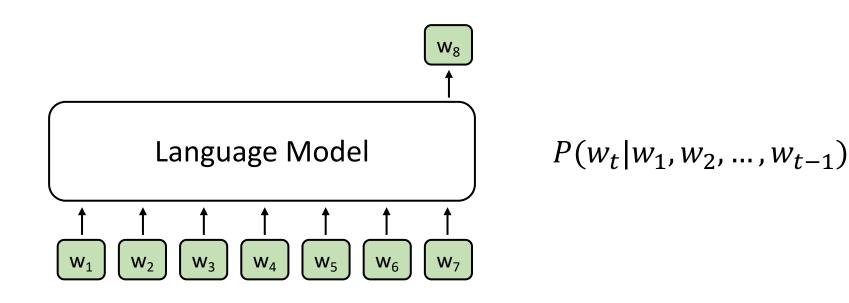
Language Modeling (the whole sentence)



$$P(w_{1:n}) = P(w_1) \cdot P(w_2|w_1) \cdot P(w_3|w_{1:2}) \cdot \dots \cdot P(w_n|w_{1:n-1})$$
$$= \prod_{t=1}^{n} P(w_t|w_{1:t-1})$$



Language Modeling (the whole sentence)



$$P(w_{1:n}) = P(w_1) \cdot P(w_2|w_1) \cdot P(w_3|w_{1:2}) \cdot \dots \cdot P(w_n|w_{1:n-1})$$



Statistical Language Models

$$P(w_{1:n}) = P(w_1) \cdot P(w_2|w_1) \cdot P(w_3|w_{1:2}) \cdot \dots \cdot P(w_n|w_{1:n-1})$$

For Bi-grams:

For Tri-grams:

$$P(w_t|w_{t-2},w_{t-1}) = \frac{\text{Count}(w_{t-2},w_{t-1},w_t)}{\text{Count}(w_{t-2},w_{t-1})} \quad \frac{w_{t-2},w_{t-1}}{\text{ \mathbb{R} \mathbb{R} \mathbb{R} \mathbb{R} \mathbb{R} } \mathbb{M}} \quad \text{\mathbb{R} \mathbb{R} $\mathbb{R}$$



Problems of Statistical Representations

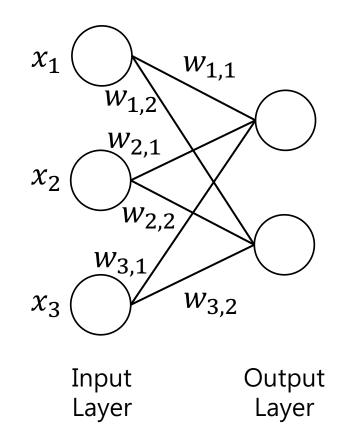
Lack of Long-Range Context

- 對於一個10個字的句子, n-gram 模型需要 V¹⁰ 次計算, 在V很大的情況下極為不可行, 因此通常只能考慮 1 或 2 個詞的上下文
- Lack of Word Similarity Awareness
 - One-hot encoding 是高維稀疏表示,導致詞之間無關聯
- The curse of dimensionality



Distributed Representations

The natural expression of distributed representations in a neural net is to make each concept be a single unit and to use the connections between units to encode the relationships between concepts.



Hinton, Geoffrey E. "Learning distributed representations of concepts." Proceedings of the Annual Meeting of the Cognitive Science Society. Vol. 8. 1986.



After Training Word Embeddings

• The outputs are dense vectors with a fixed dimension size:

```
Dimension size (e.g., 300)

apple -0.110960 0.016115 -0.004809 0.033589 0.121455 ...
banana -0.027713 -0.015676 0.003314 0.077602 0.159718 ...
...
...
```



Word Embeddings 視覺化



- Word embedding model: glove-wiki-gigaword-100
- Dimension reduction: t-SNE
- **Dataset**: Mikolov et al., 2013



Additional Resource

- (Textbook) Chapter 3: N-gram Language Models
 - https://web.stanford.edu/~jurafsky/slp3/3.pdf
- Statistical Language Models
 - https://aclanthology.org/www.mt-archive.info/MTMarathon-2010-Bertoldi-1ppt.pdf



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