Cheat Sheet

python库

二分

```
import bisect
a = [1, 2, 4, 4, 8]
print(bisect.bisect_left(a, 4)) # 输出: 2
print(bisect.bisect_right(a, 4)) # 输出: 4
print(bisect.bisect(a, 4)) # 输出: 4
```

优先队列

即该队列自动的保证顺序

```
import heapq

data = [1, 3, 5, 7, 9, 2, 4, 6, 8, 0]
heapq.heapify(data)
print(data) # 输出: [0, 1, 2, 3, 9, 5, 4, 6, 8, 7]

heapq.heappush(data, -5)
print(data) # 输出: [-5, 0, 2, 3, 1, 5, 4, 6, 8, 7, 9]

print(heapq.heappop(data)) # 输出: -5
```

日期与时间

```
import calendar, datetime

print(calendar.isleap(2020)) # 输出: True

print(datetime.datetime(2023, 10, 5).weekday()) # 输出: 3 (星期四)
```

数据结构

```
import collections
# deque
dq = collections.deque([1, 2, 3])
dq.append(4)
print(dq) # 输出: deque([1, 2, 3, 4])
dq.appendleft(0)
print(dq) # 输出: deque([0, 1, 2, 3, 4])
dq.pop()
print(dq) # 输出: deque([0, 1, 2, 3])
dq.popleft()
print(dq) # 输出: deque([1, 2, 3])
dd = collections.defaultdict(int)
dd['a'] += 1
print(dd) # 输出: defaultdict(<class 'int'>, {'a': 1})
od = collections.OrderedDict()
od['a'] = 1
od['b'] = 2
od['c'] = 3
print(od) # 输出: OrderedDict([('a', 1), ('b', 2), ('c', 3)])
Point = collections.namedtuple('Point', ['x', 'y'])
p = Point(11, 22)
print(p) # 输出: Point(x=11, y=22)
print(p.x, p.y) # 输出: 11 22
```

遍历

```
import itertools

for item in itertools.product('AB', repeat=2):
    print(item) # 输出: ('A', 'A'), ('A', 'B'), ('B', 'A'), ('B', 'B')
```

函数

```
import functools
print(functools.reduce(lambda x, y: x + y, [1, 2, 3, 4])) # 输出: 10
```

分数与有理数

```
import fractions, decimal
frac = fractions.Fraction(1, 3)
print(frac) # 输出: 1/3

dec = decimal.Decimal('0.1')
print(dec) # 输出: 0.1
```

数学

```
import math
print(math.ceil(4.2)) # 输出: 5
print(math.floor(4.2)) # 输出: 4
```

拷贝

```
import copy

original = [1, 2, [3, 4]]

copied = copy.deepcopy(original)
print(copied) # 输出: [1, 2, [3, 4]]
```

数组操作

```
squared = list(map(lambda x: x**2, [1, 2, 3, 4]))
print(squared) # 输出: [1, 4, 9, 16]

a = [1, 2, 3]
b = ['a', 'b', 'c']
zipped = list(zip(a, b))
print(zipped) # 输出: [(1, 'a'), (2, 'b'), (3, 'c')]

filtered = list(filter(lambda x: x > 2, [1, 2, 3, 4]))
print(filtered) # 输出: [3, 4]

enumerated = list(enumerate(['a', 'b', 'c']))
print(enumerated) # 输出: [(0, 'a'), (1, 'b'), (2, 'c')]
```

算法

dfs模板

连通域染色

水淹七军

bfs模板

螃蟹采蘑菇

```
def bfs(n, grid):
    start, end = find_start_end(n, grid)
    q = deque([start])
    visited = set()
    visited.add(tuple(start))
    flag = False
    while q:
        if flag:
            break
        current = q.popleft()
        if end in current:
            flag = True
            break
        for dx, dy in directions:
            nx1, ny1 = current[0][0]+dx, current[0][1]+dy
            nx2, ny2 = current[1][0]+dx, current[1][1]+dy
            if 0 \le nx1 \le n and 0 \le ny1 \le n and 0 \le nx2 \le n and 0 \le ny2 \le n:
                if grid[nx1][ny1] != 1 and grid[nx2][ny2] != 1:
                    next_state = [(nx1, ny1), (nx2, ny2)]
                    if tuple(next_state) not in visited:
                         visited.add(tuple(next_state))
                         q.append(next_state)
    return flag
```

筛法

```
def euler_sieve(n):
    is_prime = [True] * (n + 1)
    primes = []
    for i in range(2, n + 1):
        if is_prime[i]:
            primes.append(i)
        for p in primes:
            if i * p > n:
                break
        is_prime[i * p] = False
        if i % p == 0:
                break
    return primes

n = 50
print(euler_sieve(n)) # 输出: [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47]
```

dp

01背包

完全背包

```
def knapsack_complete(weights, values, capacity):
    dp = [0] * (capacity + 1)
    for i in range(len(weights)):
        for w in range(weights[i], capacity + 1):
            dp[w] = max(dp[w], dp[w - weights[i]] + values[i])
    return dp[capacity]

weights = [1, 2, 3, 4]
values = [10, 20, 30, 40]
capacity = 5
print(knapsack_complete(weights, values, capacity)) # 输出: 50
```

必须装满的完全背包

```
def knapsack_complete_fill(weights, values, capacity):
    dp = [-float('inf')] * (capacity + 1)
    dp[0] = 0
    for i in range(len(weights)):
        for w in range(weights[i], capacity + 1):
            dp[w] = max(dp[w], dp[w - weights[i]] + values[i])
    return dp[capacity] if dp[capacity] != -float('inf') else 0

weights = [1, 2, 3, 4]
values = [10, 20, 30, 40]
capacity = 5
print(knapsack_complete_fill(weights, values, capacity)) # 输出: 50
```

多重背包 (二进制优化)

```
def binary_optimized_multi_knapsack(weights, values, quantities, capacity):
   n = len(weights)
   items = []
   # 将每个物品拆分成若干子物品
   for i in range(n):
       w, v, q = weights[i], values[i], quantities[i]
       k = 1
       while k < q:
           items.append((k * w, k * v))
           q -= k
           k <<= 1
       if q > 0:
           items.append((q * w, q * v))
   # 动态规划求解01背包问题
   dp = [0] * (capacity + 1)
   for w, v in items:
       for j in range(capacity, w - 1, -1):
           dp[j] = max(dp[j], dp[j - w] + v)
   return dp[capacity]
weights = [1, 2, 3]
values = [6, 10, 12]
quantities = [10, 5, 3]
capacity = 15
print(binary_optimized_multi_knapsack(weights, values, quantities, capacity)) # 输出: 120
```

Dijkstra

```
import heapq
def dijkstra(graph, start):
    n = len(graph)
    distances = {node: float('inf') for node in range(n)}
    distances[start] = 0
    priority_queue = [(0, start)]
    while priority_queue:
        current_distance, current_node = heapq.heappop(priority_queue)
        if current_distance > distances[current_node]:
            continue
        for neighbor, weight in graph[current_node]:
            distance = current_distance + weight
            if distance < distances[neighbor]:</pre>
                distances[neighbor] = distance
                heapq.heappush(priority_queue, (distance, neighbor))
    return distances
graph = {
    0: [(1, 4), (2, 1)],
    1: [(3, 1)],
    2: [(1, 2), (3, 5)],
    3: []
}
start_node = 0
print(dijkstra(graph, start_node)) # 输出: {0: 0, 1: 3, 2: 1, 3: 4}
```

走山路(高度差为距离)

```
from heapq import heappop, heappush
directions = ((1, 0), (-1, 0), (0, 1), (0, -1))
INF = float("inf")
def dijkstra(start_x, start_y, end_x, end_y):
    global m, n, terrian
    if terrian[start_x][start_y] == "#" or terrian[end_x][end_y] == "#":
        return "NO"
    pq = [(0, start_x, start_y)]
    distance = [[INF]*n for _ in range(m)]
    distance[start_x][start_y] = 0
    while pq:
        d, x, y = heappop(pq)
        if x == end_x and y == end_y:
            return d
        for dx, dy in directions:
            nx, ny = x+dx, y+dy
            if 0 <= nx < m and 0 <= ny < n and terrian[nx][ny] != "#":</pre>
                nd = d+abs(terrian[nx][ny]-terrian[x][y])
                if nd < distance[nx][ny]:</pre>
                    distance[nx][ny] = nd
                    heappush(pq, (nd, nx, ny))
    return "NO"
```

Kadane算法

最大子序列

```
def max_subarray_sum(nums):
    max_sum = current_sum = nums[0]
    for num in nums[1:]:
        current_sum = max(num, current_sum + num)
        max_sum = max(max_sum, current_sum)
    return max_sum

nums = [-2, 1, -3, 4, -1, 2, 1, -5, 4]
print(max_subarray_sum(nums)) # 输出: 6
```

最大子矩阵

枚举 1~r 列的子式,按行求和后,求这些和的最大子序列即可。

最长上升子序列

dp方法

二分法

```
import bisect

def length_of_lis_binary(nums):
    if not nums:
        return 0

    tails = []
    for num in nums:
        pos = bisect.bisect_left(tails, num)
        if pos == len(tails):
            tails.append(num)
        else:
            tails[pos] = num
        return len(tails)

nums = [10, 9, 2, 5, 3, 7, 101, 18]
print(length_of_lis_binary(nums)) # 输出: 4
```

其它

下一个全排列

```
def next_permutation(nums):
    i = len(nums) - 2
    while i >= 0 and nums[i] >= nums[i + 1]:
        i -= 1
    if i >= 0:
        j = len(nums) - 1
        while nums[j] <= nums[i]:
            j -= 1
        nums[i], nums[j] = nums[j], nums[i]
        nums[i + 1:] = reversed(nums[i + 1:])
    return nums

nums = [1, 2, 3]
print(next_permutation(nums)) # 输出: [1, 3, 2]</pre>
```

Manacher算法

```
def manacher(s):
    s = '#' + '#'.join(s) + '#'
    n = len(s)
    p = [0] * n
    c = r = 0
    for i in range(n):
       mirr = 2 * c - i
       if i < r:
            p[i] = min(r - i, p[mirr])
       while i + p[i] + 1 < n and i - p[i] - 1 >= 0 and s[i + p[i] + 1] == s[i - p[i] - 1]:
           p[i] += 1
       if i + p[i] > r:
           c, r = i, i + p[i]
    max_len, center_index = max((n, i) for i, n in enumerate(p))
    return s[center_index - max_len:center_index + max_len].replace('#', '')
s = "babad"
print(manacher(s)) # 输出: "bab" 或 "aba"
```