Static Inference of Regular Grammars for Ad Hoc Parsers

MICHAEL SCHRÖDER, TU Wien, Austria JÜRGEN CITO, TU Wien, Austria

Parsing—the process of structuring a linear representation according to a given grammar—is a fundamental activity in software engineering. While formal language theory has provided theoretical foundations for parsing, the most common kind of parsers used in practice are written ad hoc. They use common string operations without explicitly defining an input grammar. These ad hoc parsers are often intertwined with application logic and can result in subtle semantic bugs. Grammars, which are complete formal descriptions of input languages, can enhance program comprehension, facilitate testing and debugging, and provide formal guarantees for parsing code. But writing grammars-e.g., in the form of regular expressions-can be tedious and error-prone. Inspired by the success of type inference in programming languages, we propose a general approach for static inference of regular input string grammars from unannotated ad hoc parser source code. We use refinement type inference to synthesize logical and string constraints that represent regular parsing operations, which we then interpret with an abstract semantics into regular expressions. Our contributions include a core calculus λ_{Σ} for representing ad hoc parsers, a formulation of (regular) grammar inference as refinement inference, an abstract interpretation framework for solving string refinement variables, and a set of abstract domains for efficiently representing the constraints encountered during regular ad hoc parsing. We implement our approach in the PANINI system and evaluate its efficacy on a benchmark of 204 Python ad hoc parsers. Compared with state-of-the-art approaches, PANINI produces better grammars (100 % precision, 93 % average recall) in less time $(0.82 \pm 2.85 \text{ s})$ without prior knowledge of the input space.

CCS Concepts: • Software and its engineering \rightarrow Automated static analysis; • Theory of computation \rightarrow Type theory; Abstraction; Regular languages.

Additional Key Words and Phrases: ad hoc parsers, grammars, refinement types, abstract interpretation

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1 Introduction

Parsing is one of the fundamental activities in software engineering. It is an activity so common that pretty much every program performs some kind of parsing at one point or another. Yet in every-day software engineering, only a small minority of programs, mainly compilers and some protocol implementations, make use of formal grammars to document their input languages or use formalized parsing techniques such as combinator frameworks [Leijen and Meijer 2001] or parser generators [Johnson and Sethi 1990; Parr and Quong 1995; Warth and Piumarta 2007]. The vast majority of parsing code in software today is *ad hoc*.

Ad hoc parsers are pieces of code that combine common string operations like indexing s[i], substring search s.find(t), or whitespace trimming s.strip() to effectively perform parsing. A programmer manipulating strings in an ad hoc fashion would probably not even think about the fact that they are actually writing a parser. These string-manipulating programs can be found in

Authors' Contact Information: Michael Schröder, TU Wien, Vienna, Austria, michael.schroeder@tuwien.ac.at; Jürgen Cito, TU Wien, Vienna, Austria, juergen.cito@tuwien.ac.at.



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functions handling command-line arguments, reading configuration files, or as part of any number of minor programming tasks involving strings, often deeply entangled with application logic—a phenomenon known as *shotgun parsing* [Momot et al. 2016]. They have also been shown to produce subtle and difficult to identify semantic bugs [Eghbali and Pradel 2020; Kapugama et al. 2022].

A grammar is a complete formal description of all values an input string may assume. It can elucidate the corresponding parsing code, revealing otherwise hidden features and potentially subtle bugs or security issues. By focusing on data rather than code, grammars provide a high-level perspective, allowing programmers to grasp an input language directly, without being distracted by the mechanics of the parsing process and the intricacies of imperative string manipulation. Augmenting regular documentation with formal grammars can increase program comprehension by providing alternative representations for a programming task [Fitter and Green 1979; Gilmore and Green 1984]. Because a grammar is also a generating device, it is possible to construct any sentence of its language in a finite number of steps—manually or in an automated fashion. Being able to reliably generate concrete examples of possible inputs is invaluable during testing and debugging. Grammar-based fuzzing is an automated testing method that uses input grammars to generate syntactically valid fuzz inputs that can penetrate into deep program states, passing through syntactic checks (i.e., ad hoc parsers) to uncover semantic bugs [Hodován et al. 2018; Holler et al. 2012; Zeller et al. 2024].

But despite providing all these benefits, hardly anyone ever bothers to write down a grammar, even for more complex ad hoc parsers. Grammars share the same fate as most other forms of specification: they are tedious to write, hard to get right, and seem hardly worth the trouble—especially for such small pieces of code like ad hoc parsers.

The only type of grammar that people actually routinely write down are *regular expressions* [Thompson 1968], probably the biggest and most widely known success story of applied formal language theory. However, in practical use they are often embedded within bigger pieces of ad hoc parsing code and thus usually only describe part of the actual input grammar of an ad hoc parser.

But there is another form of specification that we can draw inspiration from: *types*. Formal grammars are similar to types, in that an ad hoc parser without a grammar is very much like a function without a type signature—it might still work, but you will not have any guarantees about it before actually running the program. Types have one significant advantage over grammars, however: most type systems offer a form of *type inference*, allowing programmers to omit type annotations because they can be automatically recovered from the surrounding context. If we could infer grammars like we can infer types, we would reap all the rewards of having a complete specification of our program's input language, without burdening the programmer with the tedious task of writing a grammar by hand—we would have "grammars for free" [Schröder and Cito 2022].

Our Contribution. In this paper, we present a general approach for static inference of regular string grammars from unannotated ad hoc parser source code. We pose the problem of (regular) grammar inference as a sub-goal of refinement type inference. During type inference, we synthesize logical constraints that declaratively represent the parsing operations performed on the input string. We then interpret this complex first-order formula using an abstract semantics, in order to find a minimal sub-constraint to use as an input string refinement, rendered as a regular expression.

In brief, the contributions of our work are:

- A core calculus λ_{Σ} for representing ad hoc parsers.
- A formulation of (regular) grammar inference as refinement inference.
- An abstract interpretation framework for solving string refinement variables.
- A set of abstract domains related to regular ad hoc parsing.
- An implementation of our approach in the PANINI system.

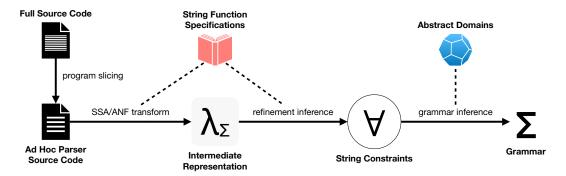


Fig. 1. The complete Panini system.

2 Overview

Figure 1 presents a schematic overview of Panini, our end-to-end grammar inference system. At the center of our approach is λ_{Σ} , a language-agnostic intermediate representation for ad hoc parsers. It is powerful enough to represent all relevant parsing operations and simple enough to enable straight-forward refinement type inference. The refinement type system of λ_{Σ} allows us to synthesize constraints over a parser's input string—i.e., it allows us to infer a parser's grammar.

The Panini system can be separated into a front end and a back end. In the front end, ad hoc parsers written in a general-purpose programming language, e.g., Python, are translated into λ_{Σ} programs. In the back end, those λ_{Σ} programs are statically analyzed and their input string constraints extracted. This paper is about the back end. In short order, we will describe the λ_{Σ} calculus, its refinement type system, our grammar inference algorithm, and the underlying abstract domains. To situate this work, we first want to briefly sketch the front-end process, and then step through a number of short examples that illustrate our approach.

2.1 The Front End: From Source to λ_{Σ}

After locating an ad hoc parser slice, it is first translated into static single assignment (SSA) form [Braun et al. 2013] and then, via an SSA-to-ANF transformation [Chakravarty et al. 2004], into a PANINI program. This requires a library of string function specifications that map the source language's string operations to equivalent λ_{Σ} functions. Note that it is not necessary to have actual λ_{Σ} implementations of these operations. We only need axiomatic specifications—in the form of type signatures—to capture those properties of the original functions that are necessary to synthesize string grammars. Table 1 gives (simplified) examples of such axioms for certain Python functions.

The front-end transformations (parser slicing, source-to- λ_{Σ} translation) and accompanying axiomatic string function specifications need to be defined and implemented (and proven correct) only once per source programming language. For the remainder of this paper, we will assume a Python-to- λ_{Σ} transformation and a library of Python string function specifications.

2.2 The Back End: From λ_{Σ} to Grammar

 λ_{Σ} is a simple λ -calculus with a refinement type system in the style of *Liquid Types* [Rondon et al. 2008; Vazou et al. 2014]. Refinement types allow us to extend base types with logical constraints. This is useful to precisely describe subsets of values, as well as track complex relationships between values, all on the type level. For example, the type of natural numbers can be defined as a subset of the integers, $\mathbb{N} = \{v : \mathbb{Z} \mid v \geq 0\}$, and we can give a precise definition of the length function on

¹Named in honor of the Sanskrit grammarian Pāṇini [Bhate and Kak 1991–1992], as well as the delicious Italian sandwiches.

Python	λ_{Σ} specification	
assert b	$assert: \{b: \mathbb{B} \mid b\} \to \mathbb{1}$	assertion
a == b	$eq: (a:\mathbb{Z}) \to (b:\mathbb{Z}) \to \{c:\mathbb{B} \mid c \Leftrightarrow a=b\}$	integer equality
len(s)	length : $(s:\mathbb{S}) \to \{n:\mathbb{N} \mid n = s \}$	string length
s[i]	$charAt: (s:\mathbb{S}) \to \{i:\mathbb{N} \mid i < s \} \to \{c:\mathbb{Ch} \mid c = s[i]\}$	character-at-index
s == t	$\operatorname{eqChar}: (s:\mathbb{Ch}) \to (t:\mathbb{Ch}) \to \{b:\mathbb{B} \mid b \Leftrightarrow s = t\}$	character equality

Table 1. Python operations as axiomatic λ_{Σ} specifications.

strings using a dependent function type and the string length operator $|\Box|$ of the refinement logic, $(s:\mathbb{S}) \to \{n:\mathbb{N} \mid n=|s|\}$. Checking a refinement type reduces to proving a so-called *verification condition* (VC), a first-order constraint in the refinement logic generated by the type system. The validity of the VC entails the correctness of the program's given and inferred types [Nelson 1980]. For example, in order to check whether $\{x:\mathbb{Z}\mid x>42\}$ (the type of all numbers greater than forty-two) is a subtype of \mathbb{N} , the VC constraint $\forall x.\ x>42\Rightarrow x\geq 0$ has to be verified. For verification to remain practical, the refinement logic is typically chosen to allow for decidable *satisfiability modulo theories* (SMT), which means VCs can be discharged using an off-the-shelf constraint solver such as Z3 [De Moura and Bjørner 2008].

Refinement Inference. To infer a refinement type for any given term, one must find a predicate that describes (at most) all possible values the term could have during any (successful) run of the program. To facilitate this, refinement type systems typically first infer the basic shapes of all types in the program, using standard type inference à la Hindley-Damas-Milner [Damas and Milner 1982; Hindley 1969], with placeholder variables standing in for as-yet-unknown refinement predicates. These placeholder variables—variously called " κ variables" [Cosman and Jhala 2017], "Horn variables" [Jhala and Vazou 2020], or "liquid type variables" [Rondon et al. 2008]—are also present in the VC at this point and prevent it from being discharged (since they are unknown). The type system then tries to find the strongest satisfying assignments for all refinement variables in the VC constraints, in order to both validate the VC and complete the inferred type.

Example 2.1. The simple λ_{Σ} program if true then 1 else 2 can be inferred to have an incomplete type of shape $\{v : \mathbb{Z} \mid \kappa(v)\}$, where κ is an unknown refinement variable, together with the VC

(true
$$\Rightarrow \forall v. \ v = 1 \Rightarrow \kappa(v)$$
) \land (false $\Rightarrow \forall v. \ v = 2 \Rightarrow \kappa(v)$).

In order to complete the type, we now have to find an assignment for κ . With such a simple constraint, the refinement solver can easily infer the correct assignment $\kappa(\nu) \mapsto \nu = 1$, which validates the VC and produces the final type $\{\nu : \mathbb{Z} \mid \nu = 1\}$.

Grammar Inference. If a κ variable stands for an input string refinement, we call this a *grammar variable*, because its solution must be some finite description of all strings that are accepted by the program, i.e., a grammar. To be practical, we would like this grammar to be as complete as possible.

Example 2.2. To illustrate, consider the Python expression **assert** $s[\emptyset] = "a"$. Assuming the function specifications from Table 1, we can transform this expression to an equivalent λ_{Σ} program (below left) with an inferred top-level refinement type of $\{s : \mathbb{S} \mid \kappa(s)\} \to \mathbb{I}$ and a VC (below right) that closely matches the program.

$$\lambda s: \mathbb{S}$$
. $\forall s. \kappa(s) \Rightarrow$ let $x = \text{charAt } s \text{ 0 in}$ $0 < |s| \land \forall x. \ x = s[0] \Rightarrow$ let $p = \text{eqChar } x \text{ 'a' in}$ $\forall p. \ (p \Leftrightarrow x = \text{ 'a'}) \Rightarrow$ assert p p

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In order to complete both the VC and the top-level type, we have to find an appropriate assignment for the grammar variable κ . The assignment must take the form of a single-argument function constraining the string s. It is clear that choosing $\kappa(s) \mapsto$ true is not a valid solution because allowing *any* string for s does not satisfy the VC. On the other hand, choosing $\kappa(s) \mapsto$ false trivially validates the VC, but it implies that the function could never actually be called, as no string satisfies the predicate false. One possible assignment could be $\kappa(s) \mapsto s = \text{`a''}$, which only allows exactly the string "a" as a value for s. While this validates the VC and produces a correct type in the sense that it ensures the program will never go wrong, it is much too strict: we are disallowing an infinite number of other strings that would just as well fulfill these criteria (e.g., "aa", "ab", and so on). The correct assignment is $\kappa(s) \mapsto s[0] = \text{`a'}$, which ensures that the first character of the string is 'a' but leaves the rest of the string unconstrained. This is equivalent to the regular language $a\Sigma^*$, where Σ is any letter from the input alphabet. Note that the solution is a minimized version of the top-level consequent in the VC.

The key insight that allows us to find suitable assignments for grammar variables in a general manner is that the top-level VC for a parser will always be of the form $\forall s.\ \kappa(s)\Rightarrow \varphi,$ where s is the input string and φ is a constraint that precisely captures all parsing operations the program performs on s. By simply taking $\kappa(s)\mapsto \varphi,$ the VC becomes a trivially valid tautology and the string refinement captures exactly those inputs that the parser accepts. But clearly this solution is practically useless: we want a succinct predicate in a grammar-like form, but the top-level VC consequent φ is a complex term in first-order logic that is basically identical to the program code itself; it does not lead to any further insight about the parser's actual input language.

However, we can use φ as a starting point and reduce it into a simpler predicate by performing an *abstract interpretation* of φ . Our approach utilizes an abstract semantics of first-order formulas over string constraints in order to soundly eliminate quantifiers and approximate the parser's input language. The precision of this approximation depends on the language complexity of the parser, the ability of the refinement inference system to synthesize program invariants, and the expressiveness of the underlying abstract value domains.

To give an idea of how grammar inference works in practice, we present a brief example.

Example 2.3. The program shown in Fig. 2a is a simple parser written in Python that checks if the first character of the input string is "a" and, if so, asserts that the length of the string must be one and thus the string must be exactly "a"; otherwise, if the first character is not "a", then the program asserts that the second character must be "b", with no further restrictions on the input string. Note that the Python string indexing operations s[0] and s[1] are themselves types of assertions, since they will cause the program to crash if the index is out of bounds. This behavior is captured in the λ_{Σ} equivalent of the source program via its function axioms (Table 1).

Figure 2b shows the parser's top-level typing derivation (§ 3). The refinement inference judgement, applied to the parser function and its axioms, results in an incomplete refinement type containing an unsolved κ variable, and a verification condition of the form $\forall s. \ \kappa(s) \Rightarrow \varphi$, which tells us that this κ variable is indeed a grammar variable. We can see that the VC's consequent φ captures all of the parsers explicit and implicit constraints over its program variables.

Finally, Fig. 2c shows a (possible) step-by-step reduction of φ into a simple quantifier-free predicate using abstract interpretation (see § 4). First, the innermost quantifiers $\forall v_1, \forall n, \forall v_2, \text{ and } \forall y$ are eliminated and their quantified variables replaced by semantically equivalent expressions. Then we eliminate $\forall p_1$, followed by $\forall x$. At this point, there are no more quantified variables and we can fully abstract each occurrence of the only free variable s. Finally, we normalize the quantifier-free predicate into a single abstract string relation $s \in (a + (\Sigma \setminus a)b\Sigma^*)$.

```
def parser(s):
                                                          parser = \lambda s : \mathbb{S}.
  if s[0] == "a":
                                                             \mathbf{let} \ x = \mathbf{charAt} \ s \ 0 \ \mathbf{in}
     assert len(s) == 1
                                                             let p_1 = \operatorname{eqChar} x 'a' in
  else:
                                                             if p_1 then
     assert s[1] == "b"
                                                                let n = \text{length } s in
                                                                let p_2 = eq n 1 in
                                                                assert p_2
>>> parser("")
                        # IndexError
                                                             else
>>> parser("a") # \sqrt{
                                                                let y = \text{charAt } s \text{ 1 in}
>>> parser("b") # IndexError
                                                                let p_3 = \operatorname{eqChar} y 'b' in
>>> parser("ab") # AssertionError
                                                                assert p_3
>>> parser("bb") # \sqrt{
```

(a) A Python program (left) and its λ_{Σ} equivalent (right).

axioms incomplete refinement verification condition
$$\widehat{\Gamma} \vdash \text{parser} \nearrow \overline{\{s : \mathbb{S} \mid \kappa(s)\} \to \mathbb{1}} = \overline{\forall s. \ \kappa(s) \Rightarrow \varphi}$$

$$\varphi \doteq (\forall v_1. \ v_1 = 0 \Rightarrow v_1 \ge 0 \land v_1 < |s|) \land \\
(\forall x. \ x = s[0] \Rightarrow (\forall p_1. \ p_1 = \text{true} \Leftrightarrow x = \text{`a'} \Rightarrow \\
(p_1 = \text{true} \Rightarrow (\forall n. \ n \ge 0 \land n = |s| \Rightarrow n = 1)) \land \\
(p_1 = \text{false} \Rightarrow (\forall v_2. \ v_2 = 1 \Rightarrow v_2 \ge 0 \land v_2 < |s|) \land \\
(\forall y. \ y = s[1] \Rightarrow y = \text{`b'}))))$$

(b) An incomplete refinement typing of the λ_{Σ} program above.

```
\varphi \stackrel{1}{\leadsto} |s| > 0 \quad \land (\forall x. \ x = s[0] \Rightarrow (\forall p_1. \ p_1 = \text{true} \Leftrightarrow x = \text{`a'} \Rightarrow (p_1 = \text{true} \Rightarrow |s| = 1) \land (p_1 = \text{false} \Rightarrow |s| > 1 \quad \land s[1] = \text{`b'})))
\stackrel{2}{\leadsto} |s| > 0 \land (\forall x. \ x = s[0] \Rightarrow (x = \text{`a'} \land |s| = 1) \lor (x \neq \text{`a'} \land |s| > 1 \land s[1] = \text{`b'}))
\stackrel{3}{\leadsto} |s| > 0 \land ((s[0] = \text{`a'} \land |s| = 1) \lor (s[0] \neq \text{`a'} \land |s| > 1 \land s[1] = \text{`b'}))
\stackrel{4}{\leadsto} s \in \Sigma^+ \land ((s \in a\Sigma^* \land s \in \Sigma) \lor (s \in (\Sigma \backslash a)\Sigma^* \land s \in \Sigma^2\Sigma^* \land s \in \Sigma b\Sigma^*))
\stackrel{5}{\leadsto} s \in (a + (\Sigma \backslash a)b\Sigma^*)
```

- (c) Possible steps in the abstract interpretation of φ : (1) eliminate $\forall v_1, \forall n, \forall v_2, \forall y$; (2) eliminate $\forall p_1$;
- (3) eliminate $\forall x$; (4) abstract s; (5) normalize. Highlights indicate changes relative to previous step.

Fig. 2. An example of grammar inference.

3 Refinement Inference

We now give a formalization of λ_{Σ} , our core abstraction for representing ad hoc parsers. The language and its type system were heavily inspired the Sprite tutorial language [Jhala and Vazou 2020], Liquid Haskell [Vazou et al. 2014], and the Fusion algorithm [Cosman and Jhala 2017]. Our main contribution in this area is an extended refinement variable solving procedure that synthesizes precise grammars for input string constraints (§§ 3.3 and 4).

3.1 Syntax

 λ_{Σ} is a small λ -calculus that exists solely for type synthesis and its programs are neither meant to be executed nor written by hand. Its syntax (Fig. 3) is thus minimal and has few affordances.

Values are either primitive constant literals or variables. **Terms** are comprised of values and the usual constructs: function applications, λ -abstractions, **let**-bindings and recursive **rec**-bindings, and branches. Applications are in A-normal form (ANF) [Bowman 2022; Flanagan et al. 1993], which means that functions can only be applied to atomic values and so all intermediate results need to be **let**-bound. ANF is a natural result of the SSA translation performed on the original source code (see § 2.1), but we also generally enforce this in the syntax to simplify the typing rules (see § 3.2, rule Syn/App) and to enable better type inference [cf. Rondon et al. 2008, § 4.4]. There are no type annotations, except on λ -binders and recursive **rec**-binders, whose (base) types we assume are inferred in a pre-processing phase or provided by the programmer.

The primitive **Base Types** are 1 (unit), \mathbb{B} (Boolean), \mathbb{Z} (integer), $\mathbb{C}\mathbb{h}$ (character), and \mathbb{S} (string). **Types** are formed by decorating base types with refinements, or by constructing (dependent) function types whose output types can refer to input types. **Refinements** are either fully known predicates or contain holes \star which are replaced with κ -applications during type synthesis (§ 3.2).

Predicates are terms in a Boolean logic and contain the usual Boolean constants and logical connectives, plus (in)equality relations and arithmetic comparisons between predicate expressions, as well as membership queries for regular expression matching. Predicates also contain applications of unknown κ variables and existential quantifiers, which arise during the Fusion phase of κ solving (see § 3.3). Both κ applications and existentials are not part of the user-visible surface syntax, which is limited to SMT-solvable predicates from quantifier-free linear arithmetic with uninterpreted functions (QF_UFLIA) extended with a theory of operations over strings [Barret et al. 2016]. **Expressions** are built from lifted values and functions, in particular linear integer arithmetic and operations over strings, such as length $|\Box|$, character-at-index $\Box[\Box]$, or substring $\Box[\Box...\Box]$. We assume the usual notational conveniences for functions and write a + b for +(a, b) or |s| for str.len(s) and so on. To simplify the presentation, predicate expressions are not further syntactically stratified, but are assumed to always occur well-typed (which is assured by the implementation).

VC generation (§ 3.2) results in **Constraints** that are Horn clauses [Bjørner, Gurfinkel, et al. 2015] in negation normal form (NNF), basically tree-like conjunctions of refinement predicates, where each root-to-leaf path is a constrained Horn clause (CHC). This representation of VCs is due to Cosman and Jhala [2017], who cleverly employ the constraints' nested scoping structure to make κ solving tractable. Note that constraints arise during type inference and provide the means to infer typing holes but are not themselves part of any inferred types, which can only contain quantifier-free predicates.

3.2 Type System

The main purpose of the type system of λ_{Σ} is to generate constraints, in particular input string constraints for parser functions. Thus, the type system is focused on inference/synthesis, rather than type checking. Terms need only be minimally annotated, at λ -abstractions and recursive

```
Values v ::= unit
                                                       unit
                                                       Booleans
                             true | false
                             \dots, -1, 0, 1, \dots
                                                       integers
                            'a', . . .
                                                       characters
                             "abc", . . .
                                                       strings
                             x, y, z, \ldots
                                                       variables
        Terms e := v
                                                       value
                                                       application
                            e v
                           \lambda x : b. e
                                                       abstraction
                            let x = e_1 in e_2
                                                       binding
                             \operatorname{rec} x : t = e_1 \ e_2
                                                       recursion
                             if v then e_1 else e_2
                                                       branch
 Base Types b := 1 \mid \mathbb{B} \mid \mathbb{Z} \mid \mathbb{Ch} \mid \mathbb{S}
        Types t := \{x : b \mid r\}
                                                       refined base
                       x:t_1\to t_2
                                                       dependent function
Refinements r :=
                                                       known predicate
                                                       refinement hole
                                                       Boolean constants
  Predicates p := \text{true} \mid \text{false}
                        | p_1 \wedge p_2 | p_1 \vee p_2 connectives
                            p_1 \Rightarrow p_2 \mid p_1 \Leftrightarrow p_2 implications
                            \neg p
                                                       negation
                            \exists x : b. p
                                                       existential quantification
                            \kappa(\overline{v})
                                                       \kappa application
                             w_1 = w_2 \mid w_1 \neq w_2
                                                       (in)equality
                                                       arithmetic comparison
                             w_1 < w_2 \mid w_1 \leq w_2
                             w \in RE
                                                       regular language membership
                                                       value
Expressions w :=
                            f(\overline{w})
                                                       function
 Constraints c :=
                                                       predicate
                             c_1 \wedge c_2
                                                       conjunction
                            \forall x: b. \ p \Rightarrow c
                                                       universal implication
```

Fig. 3. Syntax of λ_{Σ} terms, types, and refinements.

bindings. The types of applied functions need to be known, however, and be available in the typing context (see the discussion of axioms, § 2.1 and Table 1). We combine typing rules and VC generation into one syntax-driven declarative system of inference rules, shown in Fig. 4.

 $t_1 <: t_2 \dashv c$ **Subtyping.** A type t_1 is a subtype of t_2 , meaning the values denoted by t_1 are subsumed by t_2 , if the entailment constraint c is satisfied. In the SUB/BASE case, this means that t_1

$$\frac{t_1 <: t_2 \dashv c \quad \textbf{Subtyping} }{ \{v_1 : b \mid p_1\} <: \{v_2 : b \mid p_2\} \dashv \forall v_1 : b. p_1 \Rightarrow p_2[v_2 := v_1] }$$
 Sub/Base
$$\frac{s_2 <: s_1 \dashv c_1 \quad t_1[x_1 := x_2] <: t_2 \dashv c_0}{x_1 : s_1 \rightarrow t_1 <: x_2 : s_2 \rightarrow t_2 \dashv c_1 \land (x_2 :: s_2 \Rightarrow c_0) }$$
 Sub/Fun
$$\frac{s_2 <: s_1 \dashv c_1 \quad t_1[x_1 := x_2] <: t_2 \dashv c_0}{x_1 : s_1 \rightarrow t_1 <: x_2 : s_2 \rightarrow t_2 \dashv c_1 \land (x_2 :: s_2 \Rightarrow c_0) }$$
 Sub/Fun
$$\frac{\Gamma \vdash t \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Base
$$\frac{\Gamma}{\Gamma \vdash t \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Base
$$\frac{\Gamma}{\Gamma \vdash t \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Base
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash b \mid \mathbf{Template Generation}}$$
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 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash t_1 \vdash t_1 \vdash t_2 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash t_1 \vdash t_1 \vdash t_2 \vdash t_2 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash t_1 \vdash t_2 \vdash t_1 \vdash t_2 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash t_1 \vdash t_2 \vdash t_2 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t_1 \vdash b \mid \mathbf{Template Generation}}{\Gamma \vdash t \vdash t_1 \vdash b \mid \mathbf{Template Generation}}$$
 Kap/Fun
$$\frac{\Gamma \vdash t \vdash t_1 \vdash$$

Fig. 4. Typing rules for λ_{Σ} .

and t_2 must be of the same base type and the refinement predicate of t_1 must imply the predicate of t_2 , for all possible values the types can have. In the Sub/Fun case, where the contra-variant input constraint is joined with the co-variant output constraint, we add an additional implication to the output constraint, strengthening it with the supertype's input predicate. To ensure that only base types are bound to quantifiers, this is done using a *generalized implication* operation,

$$x :: t \Rightarrow c \stackrel{\text{def}}{=} \begin{cases} \forall x : b. \ p[v := x] \Rightarrow c & \text{if } t \equiv \{v : b \mid p\}, \\ c & \text{otherwise.} \end{cases}$$

<u>Γ + t > î</u> Template Generation. If the refinement of a type t is unknown (i.e., t contains a refinement hole \star), we can turn the type into a template \hat{t} , where the unknown refinement predicate is denoted by a placeholder variable whose resolution is deferred (see §§ 2.2, 3.3, and 4). The rule Kap/Base introduces a fresh κ variable for the hole, representing an n-ary relation between the type itself and all variables in the current environment Γ. In the function case Kap/Fun, templates are generated recursively while extending the output environment with the input binder. If t already has a concrete refinement (i.e., t does not contain a hole, although it might already contain a κ variable), then Kap/Conc simply leaves the type as-is. To enable complete type synthesis for all intermediate terms, it is sometimes necessary to turn a type into a template, even if it already has some known refinement (e.g., true). To facilitate this, the $\lfloor t \rfloor$ function returns the *shape* of a type t by erasing any refinements from t and returning the non-refined version of the type.

 $\Gamma \vdash e \nearrow t \dashv c$ **Type/Constraint Synthesis.** Given a typing context Γ mapping values to types, and a term e, we can synthesize a type t whose correctness is implied by the constraint c. The rule Syn/Var retrieves the type of a variable from the current context, using *selfification* [Ou et al. 2004] to produce the most precise possible type by lifting the variable into the refinement, allowing each occurrence of the variable in different branches of the program to be precisely typed.

$$self(x,t) \stackrel{\text{def}}{=} \begin{cases} \{v : b \mid p \land v = x\} & \text{if } t \equiv \{v : b \mid p\}, \\ t & \text{otherwise.} \end{cases}$$

Syn/Con synthesizes built-in primitive types for constant values, denoted by prim(v) in the obvious way, i.e., $prim(0) \stackrel{\text{def}}{=} \{ v : \mathbb{Z} \mid v = 0 \}$ and so on. Syn/App synthesizes the result type of a function application, where the given input can be a subtype of the function's declared input type. In the result type, the declared input variable is replaced by the given input, using standard capture-avoiding substitution. Note that because our terms are in ANF, no arbitrary expressions are introduced into the type during this substitution. The synthesized VC is simply a conjunction of the function's VC and the constraint created by the subtyping judgement. SYN/LAM produces a function type whose input refinement is yet unknown, with a base type according to the annotation on the λ -binder. Syn/Let first synthesizes the type t_1 for the bound term, then the type t_2 for the expression's body under an environment where x is bound to t_1 . To ensure that x does not escape its scope, the whole let-expression is given the templated type \hat{t}_2 , a supertype of t_2 with a κ variable in place of its refinement. Syn/Rec is similar to Syn/Let, with the addition that we first assume the bound term's type as a placeholder \hat{t}_1 based on the annotation \tilde{t}_1 on the binder, before synthesizing it as t_1 , allowing for recursion in the bound term. Note that we do not erase any pre-existing refinement of \tilde{t}_1 , if there is one. This enables us to manually direct constraint synthesis when necessary, for example to inject loop invariants. Syn/IF synthesizes the type of the whole conditional as a (templated) supertype of both branches. In the VC, we imply the then-branch's constraints if the condition is true, and the else-branch's constraints if the condition is false. The κ variable in the templated supertype \hat{t} allows this path-sensitive information to travel back upwards.

3.3 Variable Solving

Before the synthesized VCs can be sent off to an SMT solver to be proven valid, we have to replace all κ variables with concrete refinement predicates. Some of these variables represent input string refinements and this is the point where we need to find the grammars describing those strings.

Algorithm 1 gives a high-level overview of the VC solving procedure. We start with an incomplete VC constraint c that contains any number of κ variables. We use Fusion [Cosman and Jhala 2017] and predicate abstraction [Rondon et al. 2008] to deal with non-grammar κ variables. For grammar variables, we use our abstract interpretation approach, as detailed in § 4. If the complete VC, with all κ variables replaced by their solutions, is satisfiable, then the inferred type is valid and σ contains concrete assignments for all of the type's refinement variables, including grammar refinements for all string types. If no satisfying solution could be found, the program must be ill-typed.

Algorithm 1 Solve an incomplete VC and find all κ assignments

```
1: procedure Solve(c)
         c \leftarrow \text{Fusion}(c)
                                                  ▶ eliminate local acyclic κ variables [Cosman and Jhala 2017]
         \sigma \leftarrow \text{Liquid}(c)
                                                \triangleright solve residual non-grammar \kappa variables [Rondon et al. 2008]
3:
         for all constraints in \sigma(c) of the form \forall s : \mathbb{S}. \kappa(s) \Rightarrow \varphi do
4:
              \hat{\sigma} \leftarrow \llbracket \varphi \rrbracket^{\sharp}
                                                                  ▶ infer grammar using abstract interpretation [§ 4]
5:
              \sigma \leftarrow \sigma \cup \{\kappa(s) \mapsto s \in \hat{\sigma}(s)\}
6:
         end for
         if Satisfiable(\sigma(c)) then return Valid \sigma else return Invalid
8:
9: end procedure
```

4 Grammar Inference

Given a program P with a partially inferred refinement type $\{s: \mathbb{S} \mid \kappa(s)\} \to \mathbb{1}$ and an incomplete verification condition of the form $\forall s: \mathbb{S}$. $\kappa(s) \Rightarrow \varphi$, our goal is to find an assignment for κ that both validates the VC and meaningfully refines the type of s. Trivially, the assignment $\kappa(s) \mapsto$ false always validates the VC, but is hardly a meaningful refinement. Assuming that P is a parser, we ideally want an assignment for κ that constrains s in a way that

- (1) disallows any string rejected by P (soundness) and
- (2) allows all strings accepted by *P* (*completeness*).

In other words, we want a refinement for s that is a *grammar* for P, i.e., a finite description of the (possibly infinite) set of strings contained in the language L(P).

Luckily, the VC's consequent φ already appears to be what we are looking for: it is a first-order formula over a free string variable s that exactly captures the semantics of the parsing operations performed by P on s. Assuming that φ itself does not contain any other unsolved κ variables (these having been eliminated by prior inference and solving steps, e.g., Fusion and predicate abstraction), as well as the correctness of all involved axiomatic string function specifications, then, under some model $\mathfrak M$ of the refinement logic (e.g., QF_UFLIA plus basic string operations), by construction,

```
\mathfrak{M}, [s \mapsto t] \models \varphi \iff P \text{ successfully parses } t \iff t \in L(P)
```

The parser P represented by φ accepts some particular string t if and only if φ is true under an assignment of s to t. The set of all strings that satisfy φ is exactly the language L(P) accepted by P. Thus, φ is technically a complete grammar for P.

Practically, however, φ makes for a rather poor grammar. It is a first-order formula close in size and structure to the parsing program P itself. While $\kappa(s) \mapsto \varphi$ is an ideal assignment in the sense

that it is both sound and complete, it results in a rather impractical refinement that would puzzle a human programmer. The presence of quantifiers within φ complicates any further analysis.

In order to obtain a better grammar for L(P), we will use φ as a starting point to derive a quantifier-free predicate that is much simpler but semantically equivalent. Our approach comprises

- (1) an abstract interpretation of certain first-order string formulas as grammars (§ 4.1),
- (2) an extended constraint syntax that mixes symbolic and abstract representations (§ 4.2),
- (3) an abstract semantics of relations between predicate expressions (§ 5),
- (4) a procedure for eliminating quantified variables by abstract substitution (§ 5.1),
- (5) abstract value representations of all base types (§ 6).

4.1 Abstract Interpretation

Background. Abstract interpretation is a well-established framework for formalizing static program analyses [P. Cousot and R. Cousot 1977, 1979]. It involves the sound approximation of all possible states of a program, usually trading precision for efficiency. The concrete semantics of a program \mathcal{P} are defined by a semantic function $[\![\Box]\!]:\mathcal{P}\to\wp(C)$, which produces a power set of concrete values C. The concrete domain $\wp(C)$ can be approximated by an abstract domain \mathcal{A} , with an abstraction function $\alpha:\wp(C)\to\mathcal{A}$ and a concretization function $\gamma:\mathcal{A}\to\wp(C)$ mapping elements between the domains. Usually, \mathcal{A} is a complete lattice $(\mathcal{A},\sqsubseteq,\sqcap,\sqcup,\bot,\top)$ and the two domains form a Galois connection $(\wp(C),\subseteq) \xleftarrow{\gamma}_{\alpha} (\mathcal{A},\sqsubseteq)$, which intuitively means that relationships between elements of $\wp(C)$ also hold between the corresponding abstracted elements of \mathcal{A} . We can then define an abstract semantics $[\![\Box]\!]^{\sharp}:\mathcal{P}\to\mathcal{A}$ to abstractly interpret programs and directly produce abstract values. The abstract interpretation is *sound* iff $\alpha([\![\mathcal{P}]\!]) \sqsubseteq [\![\mathcal{P}]\!]^{\sharp}$ for all programs \mathcal{P} , and it is also *complete* iff $\alpha([\![\mathcal{P}]\!]) = [\![\mathcal{P}]\!]^{\sharp}$. Completeness in this context means that the abstract semantics incurs no loss of precision relative to the underlying abstract domain, i.e., the abstract semantics can take full advantage of the whole domain. Finally, an abstract interpretation is *exact* iff $[\![\mathcal{P}]\!] = \gamma([\![\mathcal{P}]\!]^{\sharp})$, meaning the abstraction loses no information and the abstract semantics exactly captures the concrete semantics of the program [P. Cousot 1997; Giacobazzi and Quintarelli 2001].

Parser Semantics. In our case, the kind of program we want to abstractly interpret is a parser P represented by a first-order formula φ . We take the concrete semantics $\llbracket \varphi \rrbracket$ to be an assignment σ of free variables to values, with the parser's input string denoted by the free variable s, such that

$$\mathfrak{M}, \sigma \models \varphi \iff \sigma \in \llbracket \varphi \rrbracket \iff \sigma(s) \in L(P).$$

Trying to compute $\llbracket \varphi \rrbracket$ directly will generally result in an infinite set of values. Hence our desire for an abstract semantics $\llbracket \varphi \rrbracket^{\sharp}$ that produces a finite approximation of this set such that

$$\mathfrak{M}, \hat{\sigma} \models \varphi \quad \Longleftrightarrow \quad \hat{\sigma} = \llbracket \varphi \rrbracket^{\sharp} \quad \Longrightarrow \quad \hat{\sigma}(s) \subseteq L(P),$$

where $\hat{\sigma}$ is an assignment of free variables to abstract values. In particular, $\hat{\sigma}(s)$ is now a grammar describing (a subset of) the strings in L(P).

The completeness of the approximation $\hat{\sigma}$ depends on the underlying abstract domains. Panini uses the following domains to abstract primitive values (complete definitions are given in § 6):

```
unit \wp(\mathbb{1}) = \hat{\mathbf{1}} the two-element lattice Booleans \wp(\mathbb{B}) = \hat{\mathbf{B}} Boolean subset lattice integers \wp(\mathbb{Z}) \supseteq \hat{\mathbf{Z}} open-ended interval lists characters \wp(\mathbb{C}\mathbb{h}) = \hat{\mathbf{C}} Unicode character sets strings \wp(\mathbb{S}) \supseteq \hat{\mathbf{S}} regular expressions over \hat{\mathbf{C}}
```

$$\llbracket \varphi \rrbracket^{\sharp} \doteq \left\{ x \mapsto \llbracket \varphi \rrbracket \right\}_{x} \mid x \in \operatorname{vars}(\varphi) \right\}$$

$$\llbracket \varphi_{1} \wedge \varphi_{2} \rrbracket \uparrow_{x} \doteq \llbracket \varphi_{1} \rrbracket \uparrow_{x} \sqcap \llbracket \varphi_{2} \rrbracket \uparrow_{x} \quad \text{if } \varphi_{1}, \varphi_{2} \text{ quantifier-free}$$

$$\llbracket \varphi_{1} \vee \varphi_{2} \rrbracket \uparrow_{x} \doteq \llbracket \varphi_{1} \rrbracket \uparrow_{x} \sqcup \llbracket \varphi_{2} \rrbracket \uparrow_{x} \quad \text{if } \varphi_{1}, \varphi_{2} \text{ quantifier-free}$$

$$\llbracket \neg \varphi \rrbracket \uparrow_{x} \doteq \neg \llbracket \varphi \rrbracket \uparrow_{x} \quad \text{if } \varphi \text{ quantifier-free}$$

$$\llbracket \varphi \rrbracket \uparrow_{x} \doteq \llbracket \operatorname{qelim}(\varphi) \rrbracket \uparrow_{x}$$

$$\llbracket \rho \rrbracket \uparrow_{x} \doteq \left\{ \omega, \quad \text{as defined by domain;} \right.$$

$$\left\{ \langle \rho[x := \bullet] \rangle, \quad \text{otherwise.} \right.$$

Fig. 5. Abstract semantics of λ_{Σ} constraints.

Note that our abstract string domain \hat{S} represents sets of strings with regular expressions. This means that we must under-approximate any L(P) above regular in the Chomsky hierarchy. For super-regular languages, we can only infer a partial grammar representing a regular subset, if one exists. However, if L(P) is (at most) regular, then we can infer a complete grammar for P.

Using our abstract interpretation, we can construct a finite but quantifier-free solution for the grammar refinement variable,

$$\kappa(s) \mapsto s \in \hat{\sigma}(s), \text{ where } \hat{\sigma} = \llbracket \varphi \rrbracket^{\sharp}.$$

The definition of the abstract semantics function $\llbracket \Box \rrbracket^{\sharp}$ is given in Fig. 5. It depends on a novel variable-focused relational semantics $\llbracket \Box \rrbracket \uparrow_{\Box}$ and a quantifier elimination procedure qelim(\Box). We describe these in the remainder of this section, after establishing some extensions to λ_{Σ} constraints.

4.2 Extended Constraint Syntax

We extend the formal syntax of predicates and constraints from Fig. 3 to include abstract values and relations. The extended syntax is given in Fig. 6.

Constraints φ , in addition to Boolean constants and the usual logical connectives, now include both universal and existential quantification, as well as generalized relations ρ between (potentially abstract) expressions. There are no κ applications at this point. The base types of all bound variables are known, but we elide them from the presentation to reduce clutter.

Expressions ω , in addition to concrete values (e.g., integers or string literals, as well as variables; see Fig. 3), now also include abstract values and abstract relations. **Abstract Values** \hat{v} are taken from the underlying abstract domains (see § 6) and are representations of potentially infinite sets of concrete values. For example, the abstract value $[1, \infty]$ represents an infinite set of integers $\{1, 2, 3, \ldots\}$ and the abstract string Σ^* a represents the set of all strings that end with the character a. If an abstract value appears in a function, it lifts the whole expression into the abstract realm; for example, $x + [1, \infty]$ represents the set of expressions $\{x + 1, x + 2, x + 3, \ldots\}$.

If a relation contains a hole \bullet , it is an **Abstract Relation** $\langle \rho \rangle$ that represents the maximum set of values that can be put into the hole to make the relation true. For example, the abstract relation $\langle \bullet > 5 \rangle$ represents "the set of all values that are greater than five" and $\langle s[\bullet] = c \rangle$ represents the set of all indexes at which the string in variable s contains the character in variable s.

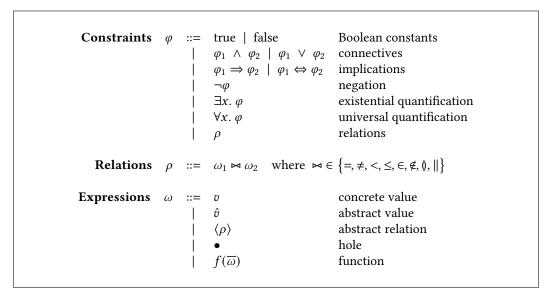


Fig. 6. Extended syntax of λ_{Σ} constraints.

In general, **Relations** ρ are comprised of the usual (in)equality and arithmetic comparisons, as well as set (non)inclusion (\in , \notin) and (non-)empty intersection (\emptyset , \parallel). The latter are simply abbreviations for common set operations, with

```
A \not A B \equiv A \cap B \neq \emptyset, meaning "A and B have at least one element in common," A \mid B \equiv A \cap B = \emptyset, meaning "A and B have no elements in common."
```

Since abstract values are essentially sets, relating them works the same way. Note the distinction between $x \in [0, \infty]$ (i.e., "x is a member of the set $\{0,1,\ldots\}$ "), $x = [0, \infty]$ (i.e., "x is the set $\{0,1,\ldots\}$ "), and $x \notin [0,\infty]$ (i.e., "x has at least one element in common with the set $\{0,1,\ldots\}$ ").

Normalization. Both expressions and relations can be normalized by partial evaluation. If abstract values are involved, the semantics of the particular abstract domains apply. If possible, relations are fully abstracted using their relational semantics (§ 5). In the remainder, we assume that expressions and relations are always fully normalized; some examples are given below.

$$1 + x - 2 \rightsquigarrow x - 1$$

$$\langle \bullet > 5 \rangle \rightsquigarrow [6, \infty]$$

$$x + 2 \leq 5 \rightsquigarrow x \leq 3 \rightsquigarrow x \in [-\infty, 3]$$

$$|s| + 1 > 2 \rightsquigarrow |s| > 1 \rightsquigarrow s \in \Sigma^{+}$$

$$s[i..i] = \text{`a'} \rightsquigarrow s[i] = \text{`a'}$$

$$[1, 2] \emptyset \langle s[\bullet] = \text{`a'} \rangle \rightsquigarrow s[[1, 2]] \ni \text{`a'} \rightsquigarrow s \in \Sigma\Sigma^{?} a\Sigma^{*}$$

5 Relational Semantics

The concrete semantics $[\![\rho]\!]$ of a single relation are all those assignments of the relation's free variables that make the relation true. For example,

$$[[x > 3]] \doteq \{x \mapsto 4, x \mapsto 5, \dots\},$$
$$[[|s| > 3]] \doteq \{\dots, s \mapsto \text{``abaa''}, s \mapsto \text{``abab''}, \dots\}$$
$$[[|s| > x]] \doteq \{\dots, \begin{pmatrix} s \mapsto \text{``ab''} \\ x \mapsto 0 \end{pmatrix}, \begin{pmatrix} s \mapsto \text{``ab''} \\ x \mapsto 1 \end{pmatrix}, \dots \}.$$

Unfortunately, constructing an abstract semantics even for such simple relations is decidedly non-trivial. It requires complex relational domains to capture just a limited set of constraints between multiple variables [P. Cousot and Halbwachs 1978; Logozzo and Fähndrich 2010; Simon et al. 2003].

Fortunately, we do not actually need a full abstract semantics that condenses relations over multiple variables into singular abstract values. For our purposes, it is sufficient to consider relational semantics on a per-variable basis. To this end, we introduce a variable-focused abstract semantics function $[\![\rho]\!]\uparrow_x$ that for a given variable x occurring free in ρ produces an abstract expression whose concrete values are exactly those that could be substituted for x to make ρ true,

$$\mathfrak{M}, [x \mapsto c] \models \rho \iff c \in \llbracket \rho \rrbracket \uparrow_x.$$

Abstract relations $\langle \rho \rangle$ provide a convenient "default" implementation,

$$\llbracket \rho \rrbracket \uparrow_x \doteq \langle \rho[x := \bullet] \rangle.$$

But we can often do better than this. Depending on the underlying abstract domains and domain-specific knowledge about the involved operations, more specific definitions of $\llbracket \Box \rrbracket \uparrow_{\Box}$ are possible (see § 6). For example, for the domains of regular strings and integers, we can define precise abstractions for simple string length relations,

$$[\![s] = \mathbf{n}]\!] \uparrow_s \doteq \Sigma^{\mathbf{n}}, \qquad [\![s] \geq \mathbf{n}]\!] \uparrow_s \doteq \Sigma^{\mathbf{n}} \Sigma^*, \qquad [\![s] \leq \mathbf{n}]\!] \uparrow_s \doteq \Sigma^0 + \Sigma^1 + \dots + \Sigma^n,$$

where n is a meta-variable denoting some concrete integer value. With these and other domain-specific semantics, we can construct variable-focused abstractions for the earlier examples. Note how in all cases the abstraction effectively eliminates the chosen variable:

$$[[x > 3]] \uparrow_x \doteq [4, \infty]$$

$$[[s > 3]] \uparrow_s \doteq \Sigma^4 \Sigma^*$$

$$[[s > x]] \uparrow_s \doteq \langle | \bullet | > x \rangle$$

$$[[s > x]] \uparrow_x \doteq |s| - [1, \infty]$$

5.1 Quantifier Elimination

Figure 7 presents our procedure for eliminating quantifiers by abstract substitution. The top-level function $\operatorname{qelim}(\varphi)$ traverses a given constraint φ to eliminate all of its quantifiers. During this traversal, we apply standard logical transformations to simplify the problem, such as DeMorgan's law and distributivity of \exists over \forall . The actual variable elimination happens in $\operatorname{qelim}(x, R)$, where we eliminate a single (existentially quantified) variable x from one conjunction of relations x, returning a conjunctive predicate that is logically equivalent to x0 but no longer contains x2, i.e.,

$$\mathfrak{M} \models \exists x. R \iff \mathfrak{M} \models \hat{R} \text{ where } \hat{R} = \operatorname{gelim} 1(x, R) \text{ and } x \notin \hat{R}.$$

To eliminate a particular variable x from the relations in R, we first compute the x-relative relational semantics $[\![\rho]\!]\uparrow_x$ for all relations that contain x as a free variable. We then form the (partial) meet closure of these expressions, resulting in a minimal set of x-less expressions E, whose members all represent some aspect of x in R. While the expressions in E do not contain x, they might contain other free variables. We now generate all unordered pairwise combinations of expressions in E and create a new non-empty intersection relation between each pair of expressions. The result is a set of relations \hat{R} that contain no reference to x yet preserve the semantics of the original conjunction of relations. Finally, we return \hat{R} together with those relations in R that did not contain x.

6 Abstract Domains

We now define abstract domains for each of the base types in our system. Each domain efficiently captures (possibly infinite) sets of concrete values of the corresponding type, lifts certain operations of the type to the abstract domain, and defines some abstract relational semantics $\llbracket \Box \rrbracket \uparrow_{\Box}$ for expression involving those operations. To simplify the definitions and avoid boilerplate repetition,

```
\begin{aligned} \operatorname{qelim}(\exists x.\ \varphi) &\doteq \bigvee \left\{ \operatorname{qelim}(x,R) \ \middle| \ R \in \operatorname{dnf}(\operatorname{qelim}(\varphi)) \right\} \\ \operatorname{qelim}(\forall x.\ \varphi) &\doteq \operatorname{qelim}(\neg \exists x.\ \neg \varphi) \\ \operatorname{qelim}(\varphi_1 \land \varphi_2) &\doteq \operatorname{qelim}(\varphi_1) \land \operatorname{qelim}(\varphi_2) \\ \operatorname{qelim}(\varphi_1 \lor \varphi_2) &\doteq \operatorname{qelim}(\varphi_1) \lor \operatorname{qelim}(\varphi_2) \\ \operatorname{qelim}(\neg \varphi) &\doteq \neg \operatorname{qelim}(\varphi) \\ \operatorname{qelim}(\varphi) &\doteq \varphi \\ \operatorname{qelim}(\operatorname{true}) &\doteq \operatorname{true} \\ \operatorname{qelim}(\operatorname{false}) &\doteq \operatorname{false} \end{aligned}
\operatorname{qelim}(x,R) &\doteq \hat{R} \land \left\{ \rho \in R \ \middle| \ x \notin \operatorname{vars}(\rho) \right\}
\operatorname{where}
\hat{R} &= \left\{ \omega_1 \not \otimes \omega_2 \ \middle| \ (\omega_1,\omega_2) \in \binom{E}{2} \right\}
E &= \bigcap \left\{ \llbracket \rho \rrbracket \uparrow_x \ \middle| \ \rho \in R, \ x \in \operatorname{vars}(\rho) \right\}
```

Fig. 7. Quantifier elimination

we generally assume that expressions have already been arranged in a uniform manner and are fully normalized (§ 4.2). We also forego subscripting domain-specific operations and elements if there is no ambiguity (e.g., we write \top instead of differentiating $\top_{\hat{\mathbf{i}}}$, $\top_{\hat{\mathbf{k}}}$, and so on).

6.1 Unit

The abstract unit type $\hat{1}$ simply adds a bottom element, forming the two-element lattice, with

$$\alpha = \gamma = \mathrm{id}, \quad [x = \mathrm{unit}] \uparrow_x \doteq \mathrm{unit}, \quad [x \neq \mathrm{unit}] \uparrow_x \doteq \bot.$$

6.2 Booleans

The Boolean subset lattice $\langle \wp(\mathbb{B}), \subseteq \rangle$ is a complete abstraction of the Boolean values, adding \emptyset and $\{\text{true}, \text{false}\}$ as bottom and top elements, respectively, and forming a complete complemented lattice via subset inclusion and set complement. For consistency with the other definitions, we call this abstraction $\hat{\mathbf{B}}$ and will use the notation $\langle \hat{\mathbf{B}}, \sqsubseteq, \bot, \top, \sqcup, \sqcap, \neg \rangle$ for the lattice elements and operations. The abstract semantics are defined by

$$\alpha = \gamma = \mathrm{id}, \qquad [\![x = \mathbf{b}]\!] \uparrow_x \doteq \{\mathbf{b}\}, \qquad [\![x \neq \mathbf{b}]\!] \uparrow_x \doteq \{\neg \mathbf{b}\}.$$

6.3 Integers

Any concrete set of contiguous integers $\{x \in \mathbb{Z} \mid a \le x \le b\}$ can be represented efficiently as an interval [a, b], even allowing for a or b to be $\pm \infty$. The domain of integer intervals

$$\mathbf{IZ} \stackrel{\mathrm{def}}{=} \left\{ [a, b] \mid a, b \in \mathbb{Z} \cup \{-\infty, \infty\}, \ a \le b \right\}$$

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forms a pseudo-semi-lattice $\langle IZ, \sqsubseteq, \top, \sqcup, \sqcap \rangle$ with a bounded meet but no \bot element:

We can also define some standard operations and convenient relations between intervals:2

$$[a,b] + [c,d] = [a+c,b+d]$$

$$[a,b] \text{ precedes } [c,d] \iff b < (c-1)$$

$$[a,b] - [c,d] = [a-d,b-c]$$

$$[a,b] \text{ is before } [c,d] \iff b < c$$

$$[a,b] \text{ contains } [c,d] \iff a \le c \land d \le b$$

$$[a,b] \text{ overlaps } [c,d] \iff a \le c \land c \le b \land b < d$$

While **IZ** can represent infinite contiguous sets, such as those defined by a single inequality relation like $\{x \in \mathbb{Z} \mid x > 5\}$, it cannot represent even finite non-contiguous sets like $\{1, 5, 7\}$ or inequalities like $\{x \in \mathbb{Z} \mid x \neq 2\}$. Thus the connection between \mathbb{Z} and **IZ** is only partial:

$$\alpha: \wp(\mathbb{Z}) \hookrightarrow \mathbf{IZ} \qquad \qquad \gamma: \mathbf{IZ} \to \wp(\mathbb{Z})$$

$$\alpha(\{x \in \mathbb{Z} \mid a \le x \le b\}) = [a, b] \qquad \qquad \gamma([a, b]) = \{x \in \mathbb{Z} \mid a \le x \le b\}$$

To completely represent *non*-contiguous sets of integers, we can use ordered lists of non-overlapping intervals; e.g., $\{1, 2, 3, 7, 8, \ldots\}$ can be represented as $[1, 3][7, \infty]$. As long as the number of gaps between intervals is bounded, $\wp(\mathbb{Z})$ can be efficiently abstracted by the domain

$$\hat{\mathbf{Z}} \stackrel{\text{def}}{=} \{ x_1 x_2 \cdots x_n \mid x_i \in \mathbf{IZ}, x_i \text{ is before } x_{i+1}, i \leq n \},$$

which forms a complete complemented lattice $\langle \hat{\mathbf{Z}}, \sqsubseteq, \bot, \top, \sqcup, \neg \rangle$, with $\bot = \emptyset$ and $\top = [-\infty, \infty]$ and the operations defined below. We use Haskell list notation (x : xs) to peel off (or add on) the first interval x in a list, with xs denoting the remaining intervals.

$$(x:xs) \sqsubseteq (y:ys) \iff (x \sqsubseteq_{\operatorname{IZ}} y \land xs \sqsubseteq (y:ys)) \lor (y \text{ is before } x \land (x:xs) \sqsubseteq ys)$$

$$(x:xs) \sqcup (y:ys) = \begin{cases} x:(xs \sqcup (y:ys)) & \text{if } x \text{ precedes } y \\ y:((x:xs) \sqcup ys) & \text{if } y \text{ precedes } x \\ ((x \sqcup_{\operatorname{IZ}} y) \sqcup xs) \sqcup ys & \text{otherwise} \end{cases}$$

$$(x:xs) \sqcap (y:ys) = \begin{cases} xs \sqcap (y:ys) & \text{if } x \text{ is before } y \\ (x:xs) \sqcap ys & \text{if } y \text{ is before } x \\ (x \sqcap_{\operatorname{IZ}} y):((x:xs) \sqcap ys) & \text{if } x \text{ contains } y \text{ or } y \text{ overlaps } x \\ (x \sqcap_{\operatorname{IZ}} y):(xs \sqcap (y:ys)) & \text{if } y \text{ contains } x \text{ or } x \text{ overlaps } y \\ (x \sqcap_{\operatorname{IZ}} y):(xs \sqcap ys) & \text{otherwise} \end{cases}$$

$$\neg [a_1,b_1] \cdots [a_n,b_n] = \begin{cases} [b_1+1,a_2-1] \cdots [b_{n-1}+1,a_n-1] & \text{if } a_1,b_n = -\infty, \infty \\ [b_1+1,a_2-1] \cdots [b_{n-1}+1,a_n-1][b_n+1,\infty] & \text{if } a_1 = -\infty \\ [-\infty,a_1-1][b_1+1,a_2-1] \cdots [b_{n-1}+1,a_n-1][b_n+1,\infty] & \text{if } b_n = \infty \\ [-\infty,a_1-1][b_1+1,a_2-1] \cdots [b_{n-1}+1,a_n-1][b_n+1,\infty] & \text{otherwise} \end{cases}$$

²These interval relations are reminiscent of the temporal interval algebra of Allen [1983]. Our definitions of "precedes" and "overlaps" are identical to Allen's, whereas "is before" corresponds to Allen's "precedes or meets," and our "contains" is equivalent to Allen's "contains or equals or is started by or is finished by."

The standard arithmetic operations are lifted into $\hat{\mathbf{Z}}$ via pointwise mapping of the equivalent operations on IZ. We assume a standard semantics for abstract integer expressions, allowing us to reduce and rewrite arithmetic expressions into a canonical form, e.g., $[3,5] + 1 \rightarrow [4,6]$.

We can construct the abstraction function $\alpha: \wp(\mathbb{Z}) \to \hat{\mathbf{Z}}$ for any finite subset of integers $X \in \wp(\mathbb{Z})$ by first sorting all elements of X in ascending order and then identifying all non-overlapping intervals of consecutive integers. This strategy does not work if X is infinite, and in any case is rather inefficient. Likewise, the concretization function $\gamma: \hat{\mathbf{Z}} \to \wp(\mathbb{Z})$, defined as

$$\gamma(x_1x_2\cdots x_n)=\bigcup_{i\leq n}\gamma_{\rm IZ}(x_i),$$

is not very practical. Fortunately, for our use case we only need to abstract and concretize sets of integers defined via relational predicates, which is easily tractable, even with infinite bounds. The corresponding semantic functions are defined below, with a standing for a concrete integer.

6.4 Characters

Abstract characters (i.e., sets of possible characters) are a common component of string grammars—whitespace, for example, is usually defined as a set of certain invisible characters. While the size of any string alphabet is always bounded and thus the maximum number of possibilities for a single character is finite, these bounds can be quite large—the Unicode standard currently defines 154 998 characters [Unicode 16.0]. Additionally, it is often desirable to define elements of a string by what characters are *not* allowed to be there. Thus the need for an efficient abstract representation of large sets of (im)possible characters.

Formally, we can define the domain of abstract characters \hat{C} via the alphabet subset lattice $\langle \wp(\Sigma), \subseteq \rangle$, with the usual operations and elements $\langle \hat{C}, \sqsubseteq, \bot, \top, \sqcup, \sqcap, \neg \rangle$ (cf. abstract Booleans \hat{B}). We use the familiar notation Σ interchangeably with \top , indicating the set of all characters of the alphabet. We use set difference to indicate exclusion, e.g., $\Sigma \setminus \{a,b\}$ means the set of all characters excluding 'a' and 'b'. For singleton sets like $\{a\}$ we will usually drop the braces and just write a. Note that $\bot = \emptyset$ is *not* equivalent to the empty string; rather, it is the empty set of characters, representing a space that is impossible to fill or a character that is impossible to produce. The abstract semantics of \hat{C} are defined by

$$\alpha = \gamma = \mathrm{id}, \qquad [\![x = \mathbf{c}]\!] \uparrow_x \doteq \{\mathbf{c}\}, \qquad [\![x \neq \mathbf{c}]\!] \uparrow_x \doteq \Sigma \setminus \{\mathbf{c}\}.$$

6.5 Strings

To abstractly represent infinite sets of strings, we define a domain \hat{S} of regular expressions over abstract characters \hat{C} , consisting of the empty language \emptyset , the empty string ε , abstract character literals $\hat{c} \in \hat{C}$ such that $\hat{c} = \{c_1, c_2, \dots, c_n\} \equiv c_1 + c_2 + \dots + c_n$, concatenation $\square \cdot \square$ (usually elided), alternation $\square + \square$, the Kleene star \square^* , and optionals $\square^? \equiv \varepsilon + \square$. We also allow the abbreviations $\square^+ = \square\square^*$ and $\square^n = \square\square \cdots \square$ where \square is repeated n times, with n < 1 resulting in \emptyset and $\square^0 = \varepsilon$.

The domain $\hat{\mathbf{S}}$ forms a complete complemented lattice $\langle \hat{\mathbf{S}}, \sqsubseteq, \bot, \top, \sqcup, \sqcap, \neg \rangle$ with $\bot = \emptyset$, $\top = \Sigma^*$, and the standard operations on regular sets [Hopcroft and Ullman 1979, chap. 3]. The language $L(\hat{s})$ describes all strings generated/recognized by a regular expression $\hat{s} \in \hat{\mathbf{S}}$, thus $\gamma(\hat{s}) = L(\hat{s})$. We can of course only abstract sets of strings that form a regular language, i.e., $\alpha(S) = \hat{s} \iff S = L(\hat{s})$. While α is not generally realizable [Gold 1967], we can define an abstract semantics over string relations, excerpted in Fig. 8, that allows us to abstract all strings expressed via relations between common string operations.

$$\Box^{\hat{n}} = \bigsqcup_{[a,b] \in \hat{n}} \Box^{[a,b]} \qquad \Box^{[a,b]} = \begin{cases} \Box^a \Box^* & \text{if } b = \infty \\ \Box^a + \Box^{a+1} + \dots + \Box^b & \text{otherwise} \end{cases}$$

$$\begin{bmatrix} |s| \ \emptyset \ \hat{n} \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{n}} \qquad \begin{bmatrix} |s| \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \emptyset$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \hat{c} \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}} \hat{c} \Sigma^* \qquad \begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}}$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \hat{c} \end{bmatrix} \uparrow_s \doteq \Sigma^* \hat{c} \Sigma^{\hat{i}-1} \qquad \begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \emptyset$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \hat{c} \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}} (\Sigma^{\hat{j}-\hat{i}+1} \Box \hat{t}) \Sigma^* \qquad \begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}}$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \hat{c} \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}} (\Sigma^{\hat{i}-\hat{i}+1} \Box \hat{t}) \Sigma^* \qquad \begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}}$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}} (\Sigma^{\hat{i}-\hat{i}+1} \Box \hat{t}) \Sigma^* \qquad \text{if } \hat{t} = \emptyset$$

$$\begin{bmatrix} |s[\hat{i}] \ \emptyset \ \emptyset \end{bmatrix} \uparrow_s \doteq \Sigma^{\hat{i}} ((-(\Sigma^*\hat{t}\Sigma^*)) \Box \Sigma^{\hat{i}-\hat{k}}) \hat{t} \Sigma^* \qquad \text{otherwise}$$

Fig. 8. Abstract relational semantics for strings. Abstract values are denoted $\hat{\Box}$. We assume all concrete values have been lifted to singleton sets, e.g., $s[i] = c \rightarrow s[\hat{i}] \ \emptyset \ \hat{c}$ where $\hat{i} = [i, i]$ and $\hat{c} = \{c\}$.

7 Implementation and Evaluation

We have implemented our approach in the PANINI prototype system, available at

https://github.com/mcschroeder/panini

It includes a basic Python frontend with a small default set of λ_{Σ} axioms mimicking the semantics of common Python string functions. Our implementation is written in Haskell and uses the Z3 theorem solver [De Moura and Bjørner 2008] and is modular with respect to the abstract domains used during grammar inference. Panini can be used as a library, a standalone batch-mode command-line application, or interactively via a read-eval-print loop.

7.1 Efficient Regular Expressions

An important aspect for the practical viability of our approach is an efficient implementation of the underlying abstract domains, in particular abstract strings \$\hat{S}\$ and abstract characters \$\hat{C}\$. The machine representation of Ĉ is based on complemented PATRICIA tries [Kmett 2012; Morrison 1968; Okasaki and Gill 1998], which enable compact representation of complemented sets while allowing all common set operations. For \hat{S} , we implemented an efficient regular expression type whose literals are abstract characters from \hat{C} and whose operations, like regular intersection and complement, are performed purely algebraically, without going through finite automata. Our approach is based on Brzozowski [1964] derivatives [see also V. Antimirov 1996] and uses Arden's lemma and Gaussian elimination to solve systems of regular equations that model these operations [Acay 2018; Arden 1961]. To effectively compute precise derivatives over large alphabets, we use a local mintermization technique [Keil and Thiemann 2014]. To keep regular expressions concise, for readability as well as performance, we aggressively simplify intermediate terms using a set of rewrite rules and heuristics [Kahrs and Runciman 2022]. We also employ a variety of efficient algebraic decision procedures for regular language membership [Nipkow and Traytel 2014], inclusion (which admits a polynomial test in many practical situations) [Hovland 2012], and equivalence (via refutation) [Almeida et al. 2008; V. M. Antimirov and Mosses 1995].

7.2 Experiments

To provide insights into the efficacy and applicability of our approach, we used the Panini prototype to infer regular grammars for a number of ad hoc parser implementations.

Dataset. We created a benchmark dataset comprising 204 regular ad hoc parsers written in Python and then translated to C. The dataset is diverse across two dimensions: complexity of accepted grammar and structure of parser code. We generated the dataset by writing straightforward parsers for increasingly complex combinations of regular language operations and then added variations of each parser, e.g., using loops to iterate over the characters in a string, using high-level Python string functions such as index, parsing the input from back-to-front, and so on. Figures 2 and 9 to 12 show subjects from the benchmark dataset.

To facilitate a structured analysis, we classified the parsers within the dataset into three overarching categories based on their structural features: *Straight-Line Programs* are ad hoc parsers characterized by linear execution flow without branching constructs such as conditionals or loops (e.g., Fig. 9); *Programs with Conditionals* are ad hoc parsers that incorporate conditional statements to make decisions based on input characteristics (e.g., Fig. 2); and *Programs with Loops* are ad hoc parsers containing iterative constructs alongside conditional statements for string manipulation tasks (e.g., Fig. 10).

Methodology. For each ad hoc parser in the dataset, we used Panini to transpile the original Python source to λ_{Σ} and automatically infer a grammar from the parser's λ_{Σ} representation. We compared each inferred grammar G_i against a manually derived ground truth grammar \hat{G}_i . We differentiate between exact matches, where $L(G_i) = L(\hat{G}_i)$; successful under-approximations $L(G_i) \subset L(\hat{G}_i)$, which correctly identify a subset of allowed strings; trivial underapproximations to the empty language $L(G_i) = \emptyset$; and cases where PANINI reports an error due to limitations of the prototype implementation or the underlying abstract domains. We additionally computed the precision and recall of each inferred grammar. Precision measures the percentage of inputs accepted by G_i that are also accepted by \hat{G}_i , whereas recall measures the pecentage of inputs accepted by \hat{G}_i that are also accepted by G_i . We generate up to 1000 random sample inputs from the respective grammars to compute each measure. Low precision indicates over-approximation, i.e., the inferred grammar allows more inputs than would be safely accepted by the

```
def getAddrSpec(email):

b1 = email.index('<',0)+1

b2 = email.index('>',b1)

return email[b1:b2]

getAddrSpec = \lambdaemail: \mathbb{S}.

let v_0 = index email "<" 0 in

let v_1 = ge v_0 0 in

let v_1 = assert v_1 in

let b1 = add v_0 1 in

let b2 = index email ">" b1 in

let v_3 = ge b2 0 in

let v_3 = ge b2 0 in

let v_3 = ge v_0 0 in

let v_0 = assert v_0 in

let v_0 = assert v_0 in

let v_0 = assert v_0 in

slice email v_0 = v_0 in
```

Fig. 9. A straight-line ad hoc parser.

```
def lsb_check(s):
    i = 0
   while i < len(s)-1:
       assert s[i] == '0'
       i += 1
   assert s[i] == '1'
lsb check = \lambda s : \mathbb{S}.
   \operatorname{rec} L_2 : \{i : \mathbb{Z} \mid \star\} \to \mathbb{1} = \lambda i : \mathbb{Z}.
       let v_0 = length s in
       \mathbf{let} \ v_1 = \mathbf{sub} \ v_0 \ 1 \ \mathbf{in}
       let v_2 = \text{lt } i \ v_1 \text{ in}
       if v_2 then
           let v_3 = slice1 s i in
           let v_4 = match v_3 "0" in
           \mathbf{let} = \mathbf{assert} \ v_4 \ \mathbf{in}
           let i = add i 1 in L_2 i
       else
           let v_5 = slice1 s i in
           let v_6 = match v_5 "1" in
           assert v_6
   in L_2 0
```

Fig. 10. An ad hoc parser with loops.

			Inferred Language								
Type	Parser Exam	ple	#	=	\subset	Ø	Error	SR	P	R	Time (s)
Straight	getAddrSpec	[^<>]*<[^>]*>.*	89	84	0	0	5	.94	1.00	1.00	0.16 ±0.27
+ Cond.	Figure 3	a [^a]b.*	51	50	0	0	1	.98	1.00	1.00	0.09 ± 0.05
+ Loops	lsb_check	0*1	64	40	7	7	10	.84	1.00	.76	2.32 ± 4.77
			204	174	7	7	16	.92	1.00	.93	0.82 ±2.85
CD.	. D	n 11									

Table 2. Results of evaluating Panini on a varied dataset of ad hoc parsers.

SR = success rate, P = precision, R = recall

parser program, while low recall indicates under-approximation, i.e., the inferred grammar is unnecessarily stricter than the actual program.

We aggregated precision and recall across each of the three parser categories and additionally report the *success rate*, the percentage of benchmark subjects for which Panini is able to infer a grammar. Finally, we also report average wall-clock execution time. All benchmarks were run on a MacBook Pro with an Apple M4 processor and 24 GB RAM, using Z3 4.8.10 for SMT solving.

Results. Table 2 presents our experimental results. Out of the 204 parser programs in our dataset, Panini is able to successfully infer a grammar for 188, a success rate of 92 %. As expected, the precision of inferred grammars is 100 % across all types of parsers: *Panini never over-approximates*. The average overall recall is 93 %. Panini achieves exact inference for all straight-line and purely conditional programs and for 40 programs containing loops; it safely under-approximates the grammar of 7 loop programs; and it fails to find a meaningful refinement beyond the empty language for another 7 loop programs.

The performance of grammar inference is mostly in the sub-second range, with some loop programs as outliers. Most of the inference time is spent during classical refinement inference, where SMT solving is still the biggest bottleneck.

7.3 Comparison with Other Approaches

Table 3 presents a comparison of Panini and other grammar inference systems. We compare operating requirements (whether the parser's source code needs to be available; whether the parser needs to be executed in some way, perhaps instrumented or modified; and whether the approach requires pre-existing input samples), the type of output (a regular expression, a context-free grammar, an automaton), and the results of running the approach on the Panini benchmark dataset (see § 7.2). The systems and algorithms selected for comparison represent the state-of-the-art in grammar inference:

Exbar [Lang 1999] is the fastest known algorithm for finding minimal DFAs from labeled samples only. This type of grammar inference—known as *passive automata learning*—is notable in that it does not require the existence of a parser program at all, neither to run nor inspect. Other prominent algorithms in this category include RPNI [Oncina and García 1992] and the approximative ED-BEAM [Lang 1999]. Unfortunately, the requirement of a well-labeled set of representative input samples is unrealistic in many settings, including ours.

TTT [Isberner 2015; Isberner et al. 2014] is a leading algorithm in active automata learning, specifically within the minimally adequate teacher (MAT) framework. Established by Angluin [1987] with the introduction of the seminal L^* algorithm, MAT formulates grammar learning as an interactive process, in which a teacher—an oracle or black-box parser program—can answer two types of question: whether a certain input is a member of the target language, and whether a hypothesized language is equivalent to the target language, providing a counterexample if it is not.

	Requirements				Panini benchmark			
Approach	Source	Execution	Samples	Output	SR	P	R	Time (s)
Panini	Python or λ_{Σ}	-	-	Regex	.92	1.00	.93	0.82 ±2.85
STALAGMITE	С	symbolic	-	CFG	.96	.87	.73	80.01 ± 178.84
Mimid	Python or C	traced	positive	CFG	.67	.97	.81	27.39 ± 42.78
TreeVada	-	oracle	positive	CFG	.98	.99	.66	72.63 ± 100.84
TTT	-	oracle	positive	DFA	.99	.13	1.00	2.74 ± 15.17
Exbar	-	-	pos. + neg.	DFA	-	-	-	-

Table 3. Comparison of state-of-the-art grammar inference approaches.

In practice, the requirement of equivalence queries is quite onerous, which is why they are usually approximated by conformance testing [Aichernig et al. 2024] using known positive input samples.

When running TTT on the Panini benchmark, we generated up to 10 000 positive input samples for each parser, simulating a best-case scenario. The results (13 % average precision, 100 % recall) indicate that TTT tends to significantly over-approximate the true input language for these kinds of ad hoc parsers, even with a very large number of input samples.

TREEVADA [Arefin et al. 2024] is the state-of-the-art in black-box inference of context-free grammars. Other approaches in this vein are ARVADA [Kulkarni et al. 2021] and the pioneering GLADE [Bastani et al. 2017]. These systems do not require equivalence queries, which makes them much more practical than traditional MAT algorithms, but they do all require a well-covering set of positive input samples in order to produce accurate grammars [Bendrissou et al. 2022].

When given up to 20 positive input samples per parser in the Panini benchmark, TreeVada achieves near-perfect 99 % precision (on average) but under-approximates the true grammars with only 66 % average recall. We found that doubling the amount of input samples improves recall by less than 10 % while more than doubling the runtime.

Mimid [Gopinath et al. 2020a] generalizes positive sample inputs into a context-free grammar by analyzing execution traces of an instrumented version of the parser, which needs to be available in source form. *Mimid* significantly improves on the previous white-box approach AUTOGRAM [Höschele and Zeller 2016], but it still requires a good set of pre-existing input samples to produce an accurate grammar. A general advantage of white-box approaches is that the inferred grammars tend to be very readable, because they can incorporate identifiers from the source code.

On the Panini benchmark, with up to 1000 positive sample inputs for each parser, Mimid produces grammars of reasonably high precision (97 % on average) but tends to under-approximate (81 % average recall). It also has a low success rate of only 67 %, meaning Mimid failed to infer any grammar for a third of the parsers in the dataset.

STALAGMITE [Bettscheider and Zeller 2024] is a recent white-box approach that obviates the need for input samples by transforming the source program into a version amenable for symbolic execution. In addition to inserting tracing calls, this includes limiting recursion depth and the number of loop iterations, which enables a symbolic test generator like KLEE [Cadar, Dunbar, et al. 2008] to automatically generate input samples that cover all execution paths. After running the modified parser on a large enough number of samples, the collected symbolic input traces are woven together to produce a context-free grammar.

STALAGMITE exhibits mediocre performance on the Panini benchmark, producing grammars that are both imprecise (87 % average precision) and under-approximated (73 % average recall). While it does not require any pre-existing input samples, the symbolic execution of the parser programs is quite resource intensive.

Note that **Panini** is the only approach that requires neither positive input samples nor any interaction with the parser. It is therefore uniquely suited to deal with ad hoc parsers, for which input samples are generally not available and which occur as code fragments that cannot always be expected to run as-is. In its current form, Panini is limited to inference of at-most regular languages, but we conjecture that these make up the highest share of ad hoc parsers in the wild [Schröder, Goritschnig, et al. 2023]. We argue that all other existing approaches have requirements that make them impractical to use in this setting, including prohibitive resource usage.

7.4 Real-World Case Studies

To investigate Panini's suitability for real-world grammar inference, we look at two regular-language ad hoc parsers from the *Mimid* benchmark suite [Gopinath et al. 2020b].

cgidecode.py. This is a Python program to decode CGI-encoded strings, an encoding where spaces are replaced by plus signs and other invalid characters are replaced by a hexadecimal encoding prefixed with a percent sign. If an improperly encoded string is encountered, the program raises an error. The regular expression ([^%]|%[0-9A-Fa-f][0-9A-Fa-f])* encompasses the input language of this ad hoc parser.³ As Table 4 shows, all approaches do fairly well on precision. TreeVADA ex-

Table 4. cgidecode.py benchmark

	P	R	Time (s)
Panini	1.00	1.00	1.49
STALAGMITE	1.00	1.00	58.52
Mimid	.90	.96	139.07
TreeVada	.96	.60	288.40
TTT	1.00	1.00	3.60

hibits the lowest recall, likely due to prioritizing larger-scale inference of context-free properties, to the detriment of regular language accuracy. Panini, Stalagmite, and TtT all achieve perfect precision and recall. TtT does so with the help of 10 000 known positive input samples, while Stalagmite requires a one-off symbolic execution harness specifically tailored to cgidecode.py. Only Panini can infer an exact grammar without having access to any pre-existing knowledge about the parser program or its possible inputs.

urlparse.py. This is the URL parser part of the Python *urllib* library. Even though this parser is quite large and complex (>1000 LoC), it is written very defensively. The only time it actually rejects an input is when the network location part of an otherwise valid URL contains an insufficiently bracketed IPv6 address. The parser's input language is equivalent to the regular expression (([a-zA-Z0-9.+-]+:)?//($[^/?#]*([[^/?#]*[]]][]][^/?#]*[]]][]][^/?#]*[].*[]][][][][^/?#].*]])|(.*([^:]]]$

Table 5. urlparse.py benchmark

	P	R	Time (s)
Panini	-	-	-
STALAGMITE	-	-	-
Mimid	1.00	0.19	157.00
TreeVada	.00	0.96	625.35
TTT	.00	1.00	1.75

|[^a-zA-Z0-9.+-].*)//.*), which looks somewhat baroque but is surprisingly permissive.⁴ This proves to be a difficult case for grammar inference: As shown in Table 5, TreeVada and TTT over-approximate the correct grammar to the extent that they achieve no precision; *Mimid* achieves perfect precision at the cost of severely under-approximating the true grammar; and neither STALAGMITE nor Panini are able to infer any grammar at all. STALAGMITE requires C source code, which does not exist for this program, while Panini's Python frontend is not yet capable of automatically translating this syntactically complex parser into λ_{Σ} .

 $^{^{3}}$ The golden grammar included by the Mimid artifact is insufficient: it does not include all possible two-digit hexadecimals and is limited to a subset of the ASCII alphabet.

⁴This is again significantly different from the golden grammar included by the *Mimid* artifact, which is much more restrictive, yet at the same time does not prevent the parser's actual error case.

7.5 Current Limitations and Future Work

Our Panini prototype is a proof-of-concept that shows the viability of our approach; it is not yet a practical end-user system. Based on the results of our evaluation, including the two case studies, we see the following main areas of improvement as part of future work:

Parser Extraction. Panini is built around λ_{Σ} , a calculus for representing ad hoc parsers. While the present work focuses on synthesizing grammars from λ_{Σ} programs, a significant part of our envisioned grammar inference process is the extraction of λ_{Σ} from general-purpose programming languages (cf. § 2.1). The Panini prototype does include some machinery to automatically extract and transpile ad hoc parser slices from Python to λ_{Σ} , but this is still very limited. We are currently experimenting with different parser slicing techniques and continue to improve our Python front end. We are also hoping to add prototypical support for other languages in the near future.

Language Features. The λ_{Σ} language is by design minimal, in order to provide a common intermediate representation for a wide range of ad hoc parser implementations and to simplify many aspects of refinement and grammar inference. However, its lack of language features makes it difficult to easily capture many real-world parser programs, such as those involving generic data types. We are currently working on extending the λ_{Σ} language to add support for polymorphism and user-defined data types.

Invariant Inference. In our approach, the solving of non-grammar κ variables is delegated to the classical refinement inference machinery (§ 3.3). In particular, this includes the generation of loop/recursion invariants, which our prototype infers using a textbook implementation of purely conjunctive predicate abstraction, a technique that is inherently limited in the shape of invariants that can be produced and is highly dependent on a good set of candidate predicates; it is also a runtime bottleneck. We plan to improve our qualifier extraction heuristics and integrate external state-of-the-art invariant generators.

Abstract Domains. Abstract interpretation is bounded by the limits of the underlying abstract domains (§ 6). For example, our integer domain $\hat{\mathbf{Z}}$ cannot efficiently represent congruence classes, e.g., infinite sets of even or odd numbers. This can lead to under-approximations, as in Fig. 11, where Panini can only infer the subset (ab)? of the true grammar (ab)*. By design, our system is modular in the choice of underlying abstract domains, and we are working on extending them.

Relational Semantics. If Panini lacks the semantics to rewrite, normalize, or abstract a particular relation (see § 5), it will eventually become stuck. We can increase the capabilities of the system by extending the set of semantic rules—i.e., adding more equations to Fig. 8. But take the parser in Fig. 12, which leads to Panini trying to compute the abstraction $[s[0] = s[1]] \uparrow_s$. In isolation, this constraint is not even

```
def f250(s):
    i = 0
    while i < len(s):
        assert s[i] == "a"
        assert s[i+1] == "b"
        i += 2</pre>
```

Fig. 11. A parser for (ab)*

```
def f521(s: str):
    assert s[0] == "a"
    assert s[1] == s[0]
```

Fig. 12. A parser for aa.*

expressible in a regular string domain—even though the final grammar is regular. To handle such tricky cases, a more complex non-local rewriting strategy might be needed.

Context-Free Grammars. If Panini encounters a context-free parser, it will likely yield \emptyset or get stuck, since the underlying string domain is built on regular expressions and cannot represent context-free constructs. Non-trivial recursion exhibited by a parser might impede invariant inference, however we do not see any limitations inherent to our technique that would in principle prevent us from eventually inferring (deterministic) context-free grammars.

8 Related Work

String Constraint Solving. Precise formal reasoning over strings can be accomplished using string constraint solving (SCS), a declarative paradigm of modeling relations between string variables and solving attendant combinatorial problems [Amadini 2023]. It is usually assumed that collecting string constraints requires some kind of (dynamic) symbolic execution [Kausler and Sherman 2014], with practical applications ranging from generating test inputs [Bjørner, Tillmann, et al. 2009; Cadar, Ganesh, et al. 2008; Li et al. 2011] to detecting vulnerabilities (e.g., cross-site scripting, SQL injection) [Bultan et al. 2018; Holík et al. 2018; Loring et al. 2017; Saxena et al. 2010]. The latter type of work is concerned with the inverse of our problem: modeling the possible strings a function can return or express, instead of the strings a function can accept.

In our approach, we use purely static means (viz. refinement type inference) to collect input string constraints (see § 3), which we then simplify/solve in ways not dissimilar but nonetheless different from traditional SCS techniques (see § 4). Our implementation makes some use of the (incomplete) string theories embedded in the Z3 constraint solver [De Moura and Bjørner 2008], whose current version unfolds regular membership relations using symbolic derivatives [Stanford et al. 2021]. Recent advances in SCS for SMT promise stronger procedures that support checking more complex functions over strings and regular expressions [Berzish et al. 2021; Blahoudek et al. 2023; Y.-F. Chen, Havlena, Hečko, et al. 2025; Y.-F. Chen, Havlena, Lengál, et al. 2020; T. Chen et al. 2019; Day, Ehlers, et al. 2019; Day, Kulczynski, et al. 2020; Hague et al. 2025; Kan et al. 2022; Kulczynski et al. 2022; Lotz et al. 2023; Mora et al. 2021; Trinh et al. 2020].

Abstract Domains. Abstract string domains approximate strings to track information precisely enough to analyze particular behaviors while only preserving relevant information. Most of the existing work in string domains differs in what kind of behavior is of interest and how the approximation is achieved efficiently. Costantini et al. [2015] introduce a suite of different abstract semantics for concatenation, character inclusion, and substring extraction (particularly pre- and suffixes). In their work, they explicitly discuss the trade-off between precision and efficiency. Amadini, Gange, et al. [2020] review the dashed string abstraction, an approach that considers strings as blocks of characters and the constraints on these blocks, which exhibits good performance on constraints involving length, equality, concatenation, and regular membership. M-String [Cortesi and Olliaro 2018] considers a parametric abstract domain for strings in the C programming language, extending the array segmentation approach of P. Cousot, R. Cousot, and Logozzo [2011]. Arceri et al. [2022] focus on relational string domains that try to capture the relation between string variables and expressions for which we cannot compute static values, such as user input. TSARIS [Negrini, Arceri, Cortesi, et al. 2024; Negrini, Arceri, Ferrara, et al. 2021] is an automata-based domain that approximates string values through finite automata over an alphabet of whole strings instead of single characters, obtaining more precise results than other approaches.

There have been a multitude of abstract domains that aim at strings in specific target languages, e.g., JavaScript [Amadini, Jordan, et al. 2017; Jensen et al. 2009; Kashyap et al. 2014; Park et al. 2016].

Precondition Inference. Input grammars are essentially preconditions for parsers, thus grammar inference can be viewed as a special case of *precondition inference*. There exist a wide variety of approaches for computing various kinds of preconditions: weakest precondition inference for unstructured programs [Barnett and Leino 2005], inference of necessary preconditions using abstract interpretation [P. Cousot, R. Cousot, Fähndrich, et al. 2013], abductive inference for inductive invariants [Dillig et al. 2013], counterexample-guided inference [Seghir and Kroening 2013], data-driven inference [Padhi et al. 2016], etc. We are not aware of any approaches that focus specifically on string operations, or that would enable the reconstruction of an input grammar in a way suitable for the envisioned applications.

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Data-Availability Statement

The latest version of the Panini system is available at https://github.com/mcschroeder/panini. This repository also includes our full evaluation dataset. We additionally provide a self-contained artifact at https://doi.org/10.5281/zenodo.16928759 to easily reproduce our claims.

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