M 3397: February 10th, 2023.

A Very Important Equality [Review].

$$\mathbb{E}[Y^{L}] = \mathbb{E}[X] - \mathbb{E}[X \wedge d] = \mathbb{E}[(X - d)_{+}]$$

$$\mathbb{E}[Y^{L}] = \frac{\mathbb{E}[Y^{L}]}{S_{X}(d)} = \frac{\mathbb{E}[X \wedge d]}{S_{X}(d)} = e_{X}(d)$$

160. You are given a random sample of observations:

0.1 0.2 0.5 0.7 1.3

You test the hypothesis that the probability density function is:

$$f(x) = \frac{4}{(1+x)^5}, \quad x > 0$$

Calculate the Kolmogorov-Smirnov test statistic.

- Less than 0.05 (A)
- (B) At least 0.05, but less than 0.15
- At least 0.15, but less than 0.25 (C)
- (D) At least 0.25, but less than 0.35
- (E) At least 0.35

161. DELETED

162. A loss, X, follows a 2-parameter Pareto distribution with $\alpha = 2$ and unspecified parameter θ . You are given:

 $E[X-100 \mid X > 100] = \frac{5}{3}E[X-50 \mid X > 50]$ Calculate E[X - 150 | X > 150]. X~ Pareto (d=2,0)

- (A) 150
- (B) 175
- (C) 200
- 225 (D)
- (E) 250

Exalxal =
$$\mathbb{E}[X] - \mathbb{E}[X \wedge d]$$

$$\mathbb{E}[X - d \mid X > d] = \frac{\mathbb{E}[X] - \mathbb{E}[X \wedge d]}{S_X(d)}$$

$$\frac{\Theta}{d-1} - \frac{\Theta}{d-1} \left(\frac{\Theta}{d+\Theta} \right)^{d-1} \right)$$

$$\frac{\Theta}{d-1} \left(\frac{\Theta}{d+\Theta} \right)^{d-1} = \frac{d+\Theta}{d-1}$$

$$\frac{\Theta}{d+\Theta} = \frac{1}{3}(50+\Theta)$$

In this problem: $(X = 2)$

$$100 + \Theta = \frac{5}{3}(50+\Theta)$$

$$2\Theta = 50$$

$$\Theta = 25$$

$$2\Theta = 50$$

$$\Theta = 25$$

100. The unlimited severity distribution for claim amounts under an auto liability insurance policy is given by the cumulative distribution:

$$F(x) = 1 - 0.8e^{-0.02x} - 0.2e^{-0.001x}, \quad x \ge 0$$

The insurance policy pays amounts up to a limit of 1000 per claim.

Calculate the expected payment under this policy for one claim.

- (A) 57
- (B) 108
- (C) 166
- (D) 205
- (E) 240

101. The random variable for a loss, X, has the following characteristics:

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Calculate the mean excess loss for a deductible of 100. (A) 250 $e_{\chi}(100) = \text{E}[\chi^{P}] = \text{E}[\chi^{-}d] \times \text{A} \times $			x	F(x)	$E(X \wedge x)$		
Calculate the mean excess loss for a deductible of 100. (A) 250 $e_{\chi}(100) = \text{E}[\chi^{\rho}] = \text{E}[\chi - d \chi > d]$			0	0.0	0		
Calculate the mean excess loss for a deductible of 100. (A) 250 $e_{x}(100) = \mathbb{E}[x^{p}] = \mathbb{E}[x - d x > d]$			100	0.2	91	X ~ 4000 = X	
Calculate the mean excess loss for a deductible of 100. (A) 250 $e_{x}(100) = \mathbb{E}[x^{p}] = \mathbb{E}[x - d x > d]$			200	0.6	153	^	
(A) 250 $e_{\chi}(100) = \mathbb{E}[\chi^{p}] = \mathbb{E}[\chi - d \chi > d]$			1000	1.0	331		
	can take is 1000.						
	(A)	250 e	?x(100) = E[x*]=E[X-d	[bex		
(C) 350 $1-F_{\chi}(1\infty)$	(C)	350		L-Fx (100)			
(D) 400	(D)	400		004 04			
(E) $450 = \frac{331 - 91}{1 - 0.2} = 340.5 = 300$	(E)	450	=		—= 240· 5	300	