

UNIVERSITY OF TEXAS AT AUSTIN

Quiz # 4

The binomial distribution.

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Provide your *final answer only* to the following problem:

**Problem 4.1.** (5 pts) Let  $X$  denote the number of 1's in 100 throws of a fair die. Find  $\mathbb{E}[X^2]$ .

- (a)  $125/9$
- (b)  $50/3$
- (c)  $875/3$
- (d)  $1585/9$
- (e) None of the above

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Provide your **complete solution** to the following problem:

**Problem 4.2.** (10 points) *Source: Problem 2.1.5. from Pitman.*

**Given** that there are 12 heads in 20 independent tosses, find the probability that at least two of the first five tosses landed heads.

*Note: It is OK to leave binomial coefficients in your answer; simplify the remainder of your expression as much as you can.*