## **Advanced Derivatives Questions**

- 1. Consider a European call option and a European put option on a nondividend-paying stock. You are given:
  - (i) The current price of the stock is 60.
  - (ii) The call option currently sells for 0.15 more than the put option.
  - (iii) Both the call option and put option will expire in 4 years.
  - (iv) Both the call option and put option have a strike price of 70.

Calculate the continuously compounded risk-free interest rate.

$$e^{-4r} = \frac{59.85}{70}$$

$$-4r = \ln\left(\frac{59.85}{70}\right)$$

$$r = -\frac{1}{4}\ln\left(\frac{59.85}{70}\right) = 0.03946$$

In general:

$$V_{c}(0) - V_{p}(0) = S(0) - Ke^{-rT}$$

$$Ke^{-rT} = S(0) - V_{c}(0) + V_{p}(0)$$

$$e^{-rT} = \frac{S(0) - V_{c}(0) + V_{p}(0)}{K}$$

$$-rT = ln\left(\frac{S(0) - V_{c}(0) + V_{p}(0)}{K}\right)$$

$$F = -\frac{1}{T} ln\left(\frac{S(0) - V_{c}(0) + V_{p}(0)}{K}\right)$$

implied interest rate

## 77. You are given:

- i) The current price to buy one share of XYZ stock is 500.
- ii) The stock does not pay dividends.
- iii) The continuously compounded risk-free interest rate is 6%
- iv) A European call option on one share of XYZ stock with a strike price of K that expires in one year costs 66.59.
- v) A European put option on one share of XYZ stock with a strike price of K that expires in one year costs 18.64.

Using put-call parity, calculate the strike price, K.

- (A) 449 66.59-18.64 = 500-Ke<sup>-0.06</sup>
- $Ke^{-0.06} = 500 47.95 = 452.05$ 
  - (C) 480
  - (D) 559  $K=452.05e^{0.06}=480.0032$
  - (E) 582
- 78. The current price of a non-dividend paying stock is 40 and the continuously compounded risk-free interest rate is 8% You are given that the price of a 35-strike call option is 3.35 higher than the price of a 40-strike call option, where both options expire in 3 months.

Calculate the amount by which the price of an otherwise equivalen 40 strike put option exceeds the price of an otherwise equivalen 35 strike put option.

- (C) 1.75  $3.35 + (Y_0(0, K_2=40) V_0(0, K_4=35)) = 5e^{-0.02}$
- (D) 3.25 answer =  $5e^{-0.02}$  3.35 = 1.55

П

(E) 3.35

