

UNIVERSITY OF TEXAS AT AUSTIN

Quiz #16

Required returns. CAPM assumptions.

Provide your **complete solutions** to the following problems:**Problem 16.1.** (9 points) State the assumptions of the **Capital Asset Pricing Model**.**Solution:**

- I. The market is *competitive*, i.e., the securities are bought and sold at the same price. There are no taxes or transaction costs. Both borrowing and lending are at the risk-free interest rate.
- II. Investors hold only efficient portfolios.
- III. *Homogeneous expectations*: The investors have the same beliefs about the expected values, volatilities, and correlations of returns of securities.

Problem 16.2. (2 points) You are given the following information about stock X and a portfolio P :

- The annual effective risk-free rate is 4%.
- The portfolio's expected return is 0.08 and its volatility is 0.25.
- The expected return of stock X is 6% and its volatility is 0.4.
- The correlation between the returns of stock X and the portfolio P is -0.2 .

Then, the investor holding portfolio P should invest in stock X . *True or false? Why?***Solution: TRUE**The β for the stock X equals

$$\beta_X = \frac{0.4(-0.2)}{0.25} = -0.32.$$

So, the stock X has a required return equal to

$$r_X = r_f + \beta_X(\mathbb{E}[R_P] - r_f) = 0.04 + (-0.32)(0.08 - 0.04) = 0.0272.$$

Since the expected return exceeds the required return, one should invest in stock X .**Problem 16.3.** (2 points) Portfolio P has expected return 0.08 and volatility equal to 12%. Portfolio Q has expected return 0.10 and volatility equal to 12.5%. Then, we can say with certainty that portfolio P is not efficient. *True or false? Why?***Solution: FALSE**Since both the expected return and the volatility of portfolio Q are bigger than those of portfolio P , there is no way for us to compare the two with just the information provided.**Problem 16.4.** (2 points) You are given the following information about stock X and a portfolio P :

- The annual effective risk-free rate is 3%.
- The portfolio's expected return is 0.10 and its volatility is 0.20.
- The expected return of stock X is 0.06 and its volatility is 0.30.
- The correlation between the returns of stock X and the portfolio P is -0.25 .

Then, the investor holding portfolio P should invest in stock X . *True or false? Why?***Solution:**The β for the stock X (with respect to portfolio P) equals

$$\beta_X = \frac{0.3(-0.25)}{0.2} = -0.375.$$

So, the stock X has a required return equal to

$$r_X = r_f + \beta_X(\mathbb{E}[R_P] - r_f) = 0.03 + (-0.375)(0.10 - 0.03) = 0.00375.$$

Since the expected return $\mathbb{E}[R_X] = 0.06$ exceeds the required return, one should invest in stock X .