

M3396: November 11<sup>th</sup>, 2024.

0.632

Say, we are doing bootstrap.

Let our original sample be  $x_1, x_2, \dots, x_n$

With bootstrap, we draw **with replacement** from the original sample.

Focusing on, say  $x_1$ , the probability of it not being chosen in one draw is

$$\underline{1 - \frac{1}{n}}$$

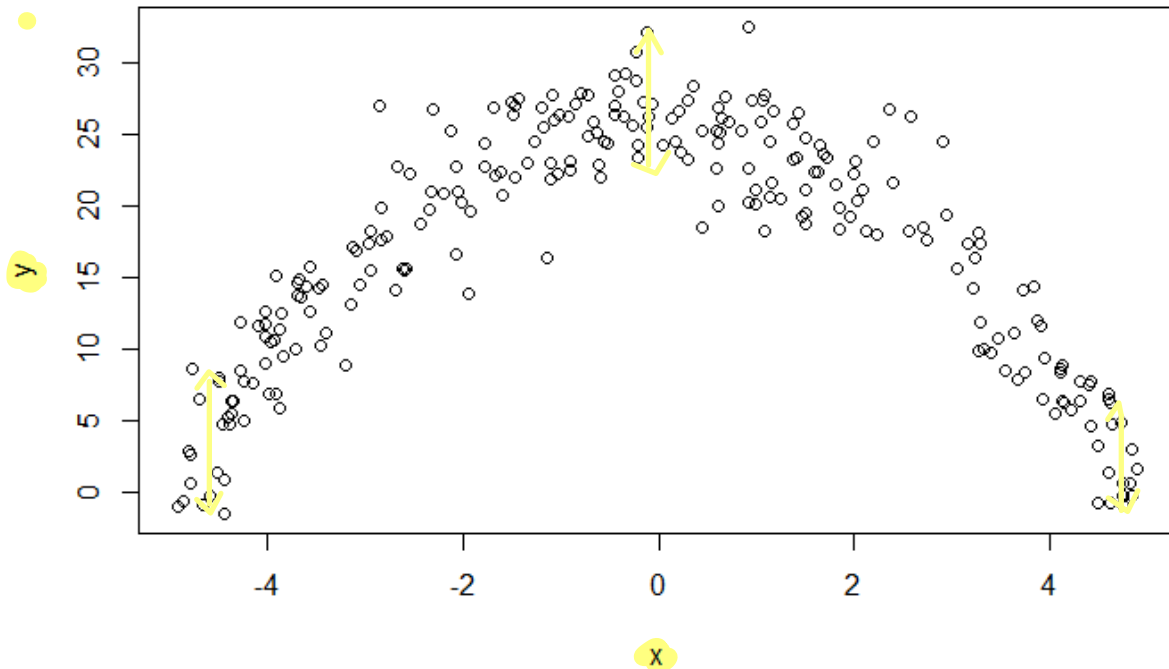
But, there are  $n$  **independent** draws. So, the total probability of never choosing  $x_1$  is

$$\underline{\left(1 - \frac{1}{n}\right)^n} \xrightarrow{n \rightarrow \infty} \frac{1}{e} = e^{-1} \approx 0.368$$

So,  $1 - e^{-1} = 0.632$  is the proportion (on average) of the data points that do end up in the bootstrapped sample.

39. You are given a dataset with two variables, which is graphed below. You want to predict  $y$  using  $x$ .

Determine which statement regarding using a generalized linear model (GLM) or a random forest is true.



- ☒ (A) A random forest is appropriate because the dataset contains only quantitative variables. *Trees in general work well w/ qualitative predictors.*
- ☒ (B) A random forest is appropriate because the data does not follow a straight line. *The opposite is true.*
- ☒ (C) A GLM is not appropriate because the variance of  $y$  given  $x$  is not constant. *The variance looks pretty constant.*
- ☒ (D) A random forest is appropriate because there is a clear relationship between  $y$  and  $x$ . *Could be anything!*
- (E) A GLM is appropriate because it can accommodate polynomial relationships.

