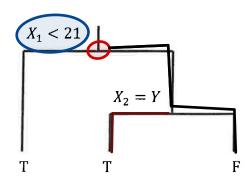
40.

You are given the following classification decision tree and data set:



i	X_I	X_2	Y
1	12	Y	T
2	12 23	N	F
3	4	Y	F
4	<u>32</u>	Y	F
5	<u>22</u>	N	Ţ
6	22 30	Y	T
7	18	N	T

Determine the relationship between the classification error rate, the Gini index, and the cross-entropy, summed across all nodes.

- A. cross-entropy > Gini index > classification error rate
- B. cross-entropy > Gini index = classification error rate
- C. classification error rate > Gini index > cross-entropy
- D. Gini index > cross-entropy > classification error rate
- E. The answer is not given by (A), (B), (C), or (D).

Caveat: They explicitly say: "summed across all nodes" which is different from computing a weighted average.

```
--: For X1 < 21, we have observations i= 1, 3, 7
               and they have Y=T, Y3=F, Y7=T
              => From the tree, we know that the classification @ that node is T
             => The classification error is \left(\frac{1}{3}\right)
         For X1 > 21 and X2 = Y, observations i= 4,6
               are in that terminal node w/ Y4=F, Y6=T
            From the tree, the classification @ that node is T
                   \Rightarrow The classification error is \left(\frac{1}{2}\right),
         For X_1 \ge 21 and X_2 = N, observations i = 2, 5
            are in that terminal node w/ Yz=F, Y5=T
           In the tree, that node is F
                 => The classification error is (\frac{1}{2})
    The overall classification error: \frac{1}{3} + \frac{1}{2} + \frac{1}{2} = \frac{4}{3} = \frac{12}{9}
     At the 1st node, the Gini index: \frac{1}{3}(\frac{2}{3}) + \frac{2}{3}(\frac{1}{3}) = \frac{4}{9}
    At the 2<sup>nd</sup> node, -11 - : 2 \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{2}
At the 3<sup>rd</sup> node, -11 - :  the same \frac{1}{2}
   => The Total Gini index: 4+1+1=13
   The cross entropy @ 1^{37} node: -\frac{1}{3}\ln(\frac{1}{5}) - \frac{2}{3}\ln(\frac{2}{3})
                         @ 2nd and 3rd nodes: -\frac{1}{2} ln(\frac{1}{2}) - \frac{1}{2} ln(\frac{1}{2})
    => The Total Cross : Entropy: 2.022809
```