

The Equity Cost of Capital.

In CAPM: for all investments I:

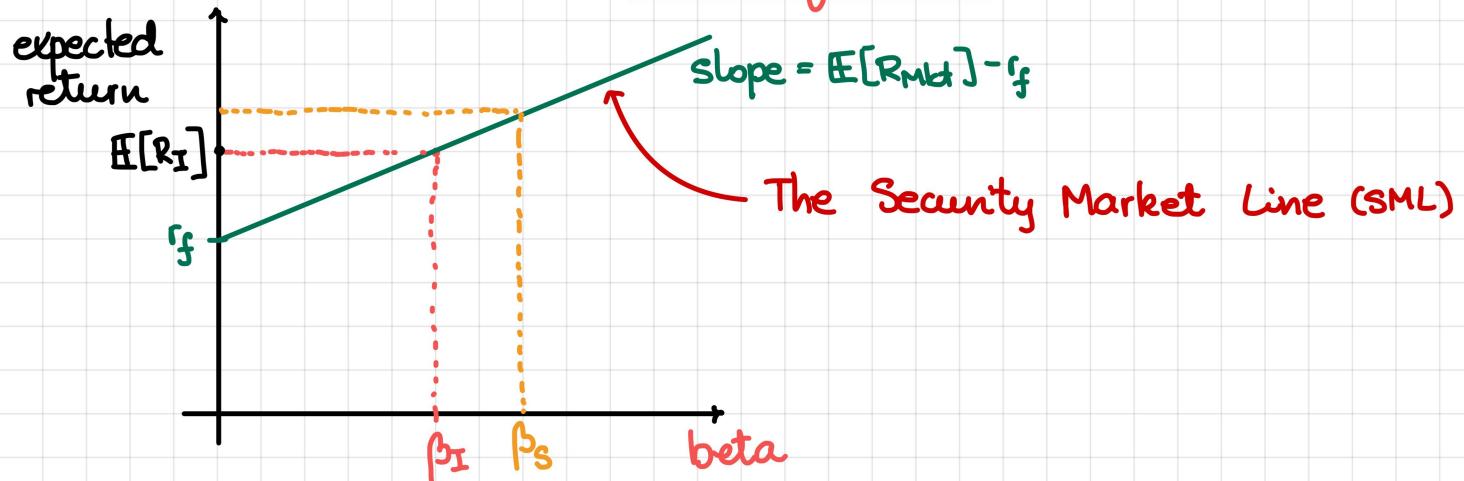
$$\mathbb{E}[R_I] = r_I = r_f + \beta_I (\mathbb{E}[R_{Mkt}] - r_f)$$

↑
"independent argument"

independent of investment I

↑
the slope.

↑
intercept



Beta estimation.

Linear Regression.

Explanatory Random Variable : X

Response Random Variable : Y

Model:

$$Y = \alpha + \beta \cdot X + \varepsilon$$

↑ ↑
intercept slope

w/ $\varepsilon \sim \text{Normal}(0, \text{variance})$
assume to be the same for all values of X

Observed values: (x_i, y_i) , $i=1..n$



$$\hat{\beta} = \frac{SD[Y]}{SD[X]} \cdot \text{corr}[X, Y]$$

$$Y = \alpha + \beta X + \varepsilon \quad (\text{SLR})$$

"Attacking" the SLR w/ the expectation.

$$\mathbb{E}[Y] = \alpha + \beta \mathbb{E}[X] + 0$$

↑ ↓

They can be estimated from the least-squares line.

In our applications:

$$\underbrace{R_I - r_f}_{\text{excess return for investment I}} = \alpha_I + \beta_I \left(\underbrace{R_{Mkt} - r_f}_{\text{excess return of market}} \right) + \varepsilon_I$$

↑ ↗ ↘ ↙

the intercept of the linear regression the slope of the linear regression the error term

Now, we see how we can estimate α_I and β_I from the observed values of excess returns across different time intervals.

Taking the expectation above, we get

$$\mathbb{E}[R_I] - r_f = \alpha_I + \beta_I (\mathbb{E}[R_{Mkt}] - r_f) + \mathbb{E}[\varepsilon_I]$$

$$\mathbb{E}[R_I] = r_f + \beta_I (\mathbb{E}[R_{Mkt}] - r_f) + \alpha_I$$

the Security Market Line

the distance from the SML, i.e., the stock's alpha