

## M378K Introduction to Mathematical Statistics Problem Set #19 Hypothesis testing.

Problem 19.1. An instructor of a massive online course claims that students solve at most 20 problems per week (on average). To verify this conviction, the instructor intends to conduct a hypothesis test. What are the null and alternative hypotheses in this case?

Ho: 
$$\mu = \mu_0 = 20$$
  
Ha:  $\mu < \mu_0 = 20$ 

With a sample size of 256 what is the test statistics appropriate the test the above claim? What is its (approximate) distribution under the null?

Say that the sample average equals 19.7 and that the sample variance equals 9 What is the p-value associated with these data?

Probles =  $P[TS < \frac{49.7 - 20}{3}] = P[Z < \frac{0.3}{3}]$   $= \Phi(-1.6) = 0.0548$ 

Assume that the given significance level is 5%. What would the decision be?

Fail to reject the null hypothesis.





