

Due on November 29, 2021
M339W/389W Financial Mathematics for Actuarial Applications
Fall 2021, University of Texas at Austin
Graduate Homework III
Instructor: Milica Čudina

The following problems are meant to be the extra special homework assignment for graduate students. If you are taking this course as an undergraduate course, your score on will count as extra credit. Details are below.

A part of the homework involves simulations while the rest involves calculations (and a bit of simulations). You are required to use **R** to complete this part of the assignment. Please, do not include a list of your simulated values in your final submission.

If you are a graduate student, this HW will be taken into account when your HW average is calculated (see the First-Day Handout). It will have the weight of **two** regular homework assignments. If you are taking this course as an undergraduate course and you decide to attempt this assignment, then your score will serve as extra credit toward your final score in the course. More precisely, a full score in this homework will be worth 2 points in the final score in this course.

Problem 1.1. (30 points) Let the current stock price of a continuous-dividend-paying stock be \$100. Let its dividend yield be 0.02 and let its volatility be 0.25. Under your model, the mean rate of return on this stock is 0.06.

- (i) (10 pts) Simulate 1000 values of the stock price at time $t = 3$. Draw a histogram of the obtained set of values.
- (ii) (2 pts) Find the median of the set of simulated values you obtained in part (i).
- (iii) (2 pts) Find the average of the set of simulated values you obtained in part (i).
- (iv) (4 pts) Draw the graph of the density of a lognormal distribution of S_3 with the appropriate parameters and compare it to the histogram from part (i).
- (v) (12 pts) If you did not do so in the first place, simulate the values from (i) using the step-by-step method, calculating S_1 and S_2 as auxiliary simulated values. What is the proportion of paths that you created in this way that crosses above \$105 at any time? What is the proportion of paths such that $S_1 > \$100$?

[illegible]