

# ViF

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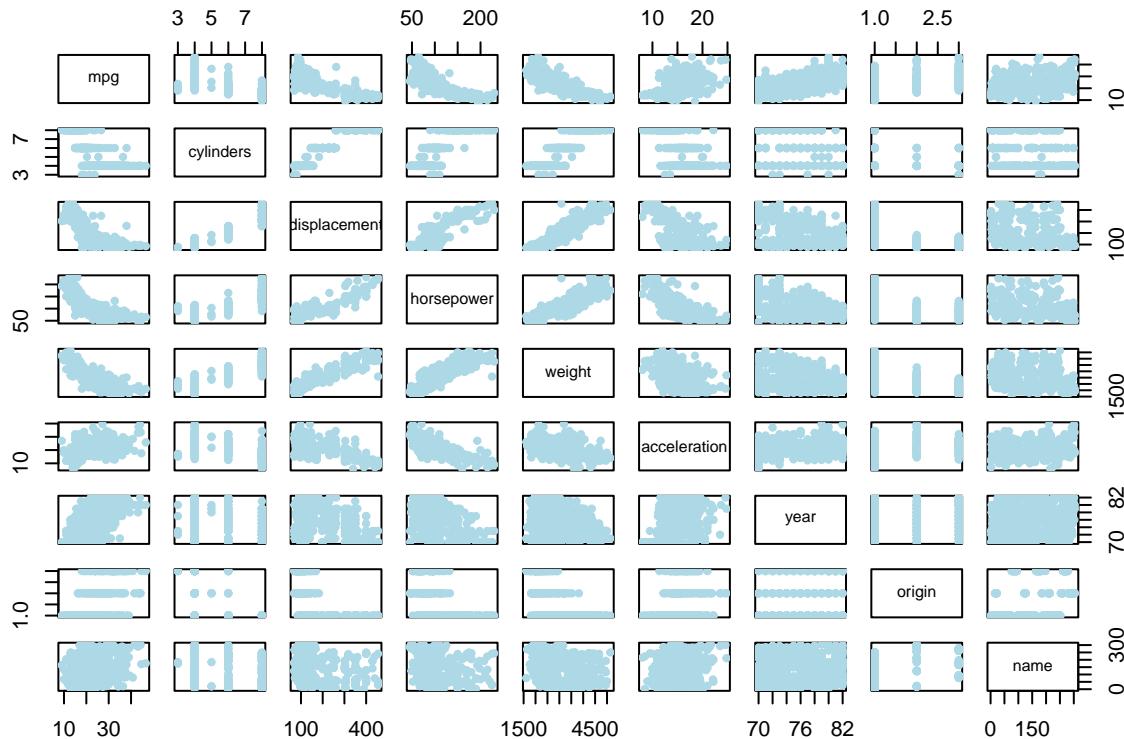
## Car efficiency [revisited]

First, let's import the textbook's library.

```
library(ISLR2)
attach(Auto)
#View(Auto)
```

Let's do some exploratory analysis.

```
pairs(Auto,
      pch=20, col="lightblue")
```



```
round(cor(Auto[,-c(8,9)]),4)
```

```
##          mpg cylinders displacement horsepower weight acceleration
## mpg      1.0000   -0.7776     -0.8051    -0.7784 -0.8322     0.4233
## cylinders -0.7776    1.0000      0.9508     0.8430  0.8975    -0.5047
## displacement -0.8051    0.9508     1.0000     0.8973  0.9330    -0.5438
## horsepower   -0.7784    0.8430     0.8973     1.0000  0.8645    -0.6892
## weight       -0.8322    0.8975     0.9330     0.8645  1.0000    -0.4168
## acceleration  0.4233   -0.5047    -0.5438    -0.6892 -0.4168     1.0000
## year        0.5805   -0.3456     -0.3699    -0.4164 -0.3091     0.2903
```

```

##                  year
## mpg             0.5805
## cylinders     -0.3456
## displacement -0.3699
## horsepower    -0.4164
## weight         -0.3091
## acceleration   0.2903
## year           1.0000

```

We notice some pretty sizable correlations. What about a multiple linear regression?

```

lm.fit=lm(mpg~cylinders+horsepower+weight,data=Auto)
summary(lm.fit)

```

```

##
## Call:
## lm(formula = mpg ~ cylinders + horsepower + weight, data = Auto)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.5260  -2.7955  -0.3559   2.2567  16.3209
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 45.7368172  0.7959566 57.461 < 2e-16 ***
## cylinders   -0.3889745  0.2988302 -1.302 0.193806
## horsepower  -0.0427277  0.0116196 -3.677 0.000269 ***
## weight       -0.0052723  0.0006424 -8.208 3.37e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.236 on 388 degrees of freedom
## Multiple R-squared:  0.7077, Adjusted R-squared:  0.7054
## F-statistic: 313.1 on 3 and 388 DF,  p-value: < 2.2e-16

```

We should import the `car` library (nothing to do with vehicles; it's short for *Companion to Applied Regression*.).

```
library(car)
```

```

## Loading required package: carData
vif(lm.fit)

## cylinders horsepower      weight
##  5.660847   4.358007   6.485732

```

Our textbook says: \*“...a VIF value that exceeds 5 or 10 indicates a problematic amount of collinearity...”

## Seat Position

Let's consider another data set. This one is from the `faraway` library.

```

#install.packages("faraway")
library(faraway)

```

```

##
## Attaching package: 'faraway'
## The following objects are masked from 'package:car':

```

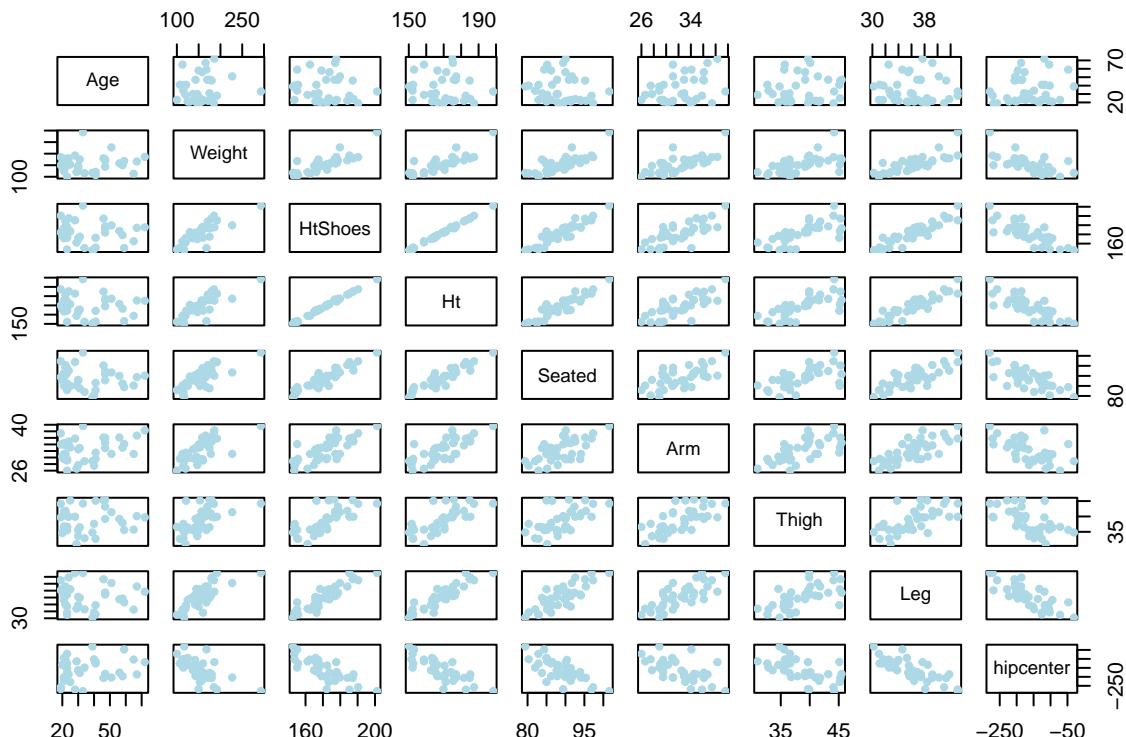
```
##  
##      logit, vif
```

The data set `seatpos` is used to predict the carseat position (`hipcenter`) based on biometric data of the driver.

```
data(seatpos)
```

When we look at the documentation, we see that one of the variables is `HtShoes`, i.e., height in shoes, and another is `Ht`, i.e., height barefoot. These are bound to be incredibly correlated. Similarly, there is the `Seated`, i.e., the seated height, `Weight`, and others that should be heavily positively correlated. Let's do some exploratory data analysis:

```
pairs(seatpos,  
      pch=20, col="lightblue")
```



```
round(cor(seatpos),4)
```

	Age	Weight	HtShoes	Ht	Seated	Arm	Thigh	Leg
## Age	1.0000	0.0807	-0.0793	-0.0901	-0.1702	0.3595	0.0913	-0.0423
## Weight	0.0807	1.0000	0.8282	0.8285	0.7756	0.6976	0.5726	0.7843
## HtShoes	-0.0793	0.8282	1.0000	0.9981	0.9297	0.7520	0.7249	0.9084
## Ht	-0.0901	0.8285	0.9981	1.0000	0.9282	0.7521	0.7350	0.9098
## Seated	-0.1702	0.7756	0.9297	0.9282	1.0000	0.6252	0.6071	0.8119
## Arm	0.3595	0.6976	0.7520	0.7521	0.6252	1.0000	0.6711	0.7538
## Thigh	0.0913	0.5726	0.7249	0.7350	0.6071	0.6711	1.0000	0.6495
## Leg	-0.0423	0.7843	0.9084	0.9098	0.8119	0.7538	0.6495	1.0000
## hipcenter	0.2052	-0.6403	-0.7966	-0.7989	-0.7313	-0.5851	-0.5912	-0.7872
## hipcenter								
## Age		0.2052						
## Weight			-0.6403					
## HtShoes				-0.7966				
## Ht					-0.7989			

```

## Seated      -0.7313
## Arm        -0.5851
## Thigh      -0.5912
## Leg        -0.7872
## hipcenter   1.0000

```

Age appears to be the only predictor not linked with other predictors.

Let's try a multiple linear regression.

```

lm.fit=lm(hipcenter~.,data=seatpos)
summary(lm.fit)

```

```

##
## Call:
## lm(formula = hipcenter ~ ., data = seatpos)
##
## Residuals:
##    Min     1Q Median     3Q    Max 
## -73.827 -22.833 -3.678 25.017 62.337 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 436.43213 166.57162  2.620  0.0138 *  
## Age         0.77572   0.57033  1.360  0.1843    
## Weight      0.02631   0.33097  0.080  0.9372    
## HtShoes    -2.69241   9.75304 -0.276  0.7845    
## Ht          0.60134  10.12987  0.059  0.9531    
## Seated      0.53375   3.76189  0.142  0.8882    
## Arm         -1.32807   3.90020 -0.341  0.7359    
## Thigh       -1.14312   2.66002 -0.430  0.6706    
## Leg         -6.43905   4.71386 -1.366  0.1824    
## ---        
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 
## 
## Residual standard error: 37.72 on 29 degrees of freedom
## Multiple R-squared:  0.6866, Adjusted R-squared:  0.6001 
## F-statistic:  7.94 on 8 and 29 DF,  p-value: 0.00001306

```

As anticipated, we get much nonsense. So, let's check out the variance inflation factors.

```
vif(lm.fit)
```

```

##      Age     Weight    HtShoes        Ht     Seated      Arm     Thigh
## 1.997931 3.647030 307.429378 333.137832 8.951054 4.496368 2.762886
##      Leg
## 6.694291

```

It seems that we really should take a pick between height in shoes and height without.

```

lm.fit.1=lm(hipcenter~. - Ht,data=seatpos)
summary(lm.fit.1)

```

```

##
## Call:
## lm(formula = hipcenter ~ . - Ht, data = seatpos)
##
## Residuals:
## 
```

```

##      Min     1Q   Median     3Q    Max
## -74.107 -22.467 -4.207  25.106 62.225
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 436.84207 163.64104  2.670  0.0121 *
## Age          0.76574  0.53590  1.429  0.1634
## Weight       0.02897  0.32244  0.090  0.9290
## HtShoes     -2.13409  2.53896 -0.841  0.4073
## Seated        0.54959  3.68958  0.149  0.8826
## Arm          -1.30087  3.80833 -0.342  0.7350
## Thigh         -1.09039  2.46534 -0.442  0.6615
## Leg           -6.40612  4.60272 -1.392  0.1742
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 37.09 on 30 degrees of freedom
## Multiple R-squared:  0.6865, Adjusted R-squared:  0.6134
## F-statistic: 9.385 on 7 and 30 DF,  p-value: 0.000004014
vif(lm.fit.1)

##          Age     Weight    HtShoes    Seated      Arm     Thigh      Leg
## 1.824607 3.580351 21.550054 8.906032 4.434329 2.454805 6.601632

```

What if we get rid of height in shoes as well?

```

lm.fit.2=lm(hipcenter~. - Ht-HtShoes,data=seatpos)
summary(lm.fit.2)

```

```

##
## Call:
## lm(formula = hipcenter ~ . - Ht - HtShoes, data = seatpos)
##
## Residuals:
##      Min     1Q   Median     3Q    Max
## -68.296 -23.340 -5.672  24.183  74.065
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 409.00851 159.49517  2.564  0.0154 *
## Age          0.83110  0.52771  1.575  0.1254
## Weight       -0.03251  0.31254 -0.104  0.9178
## Seated        -1.73576  2.48225 -0.699  0.4896
## Arm          -2.00541  3.69731 -0.542  0.5914
## Thigh         -1.91970  2.24858 -0.854  0.3998
## Leg           -8.40876  3.91939 -2.145  0.0399 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 36.91 on 31 degrees of freedom
## Multiple R-squared:  0.6791, Adjusted R-squared:  0.617
## F-statistic: 10.94 on 6 and 31 DF,  p-value: 0.000001571
vif(lm.fit.2)

```

```

##          Age     Weight    Seated      Arm     Thigh      Leg

```

```
## 1.786192 3.396124 4.069626 4.219519 2.061632 4.832701
```

We have not sacrificed anything in terms of  $R^2$  by eliminating the two height variables. Just the `Leg` is still statistically significant with `Age` in the surprising second place.

Just for laughs, how about a simple linear regression on `Leg`?

```
lm.fit.s<-lm(hipcenter ~ Leg, data=seatpos)
summary(lm.fit.s)
```

```
##
## Call:
## lm(formula = hipcenter ~ Leg, data = seatpos)
##
## Residuals:
##    Min     1Q Median     3Q    Max
## -78.10 -26.11 -1.86 18.54 94.42
##
## Coefficients:
##             Estimate Std. Error t value   Pr(>|t|)
## (Intercept) 335.351     65.601   5.112 0.00001066600 ***
## Leg         -13.795      1.801  -7.658 0.00000000459 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 37.29 on 36 degrees of freedom
## Multiple R-squared:  0.6196, Adjusted R-squared:  0.6091
## F-statistic: 58.65 on 1 and 36 DF,  p-value: 0.000000004587
```

So, more predictors are not always better?