

UNIVERSITY OF TEXAS AT AUSTIN

Quiz # 4

Confidence intervals (the normal distribution).

Provide your **final answer only** to the following questions.

Problem 4.1. (2 points) The margin of error for a confidence interval for the population mean μ increases as the sample size increases. *True or false?*

Problem 4.2. (2 points) The margin of error for a confidence interval for the population mean μ , based on a fixed specified sample size n , increases as the confidence level decreases. *True or false?*

Problem 4.3. (2 points) The Midsomer Worthy Middle School has calculated a 95% confidence interval for the population mean height μ of 11-year-old boys at their school. They found it to be 57 ± 2 inches.

This means that there is a 95% probability that the population mean μ is between 55 and 59. *True or false?*

Problem 4.4. (2 points) The Midsomer Worthy Middle School has calculated a 95% confidence interval for the population mean height μ of 11-year-old boys at their school. They found it to be 57 ± 2 inches.

If we took many additional random samples of the same size and from each computed a 95% confidence interval for μ , approximately 95% of these intervals would contain the population mean μ . *True or false?*

Problem 4.5. (2 points)

Resident statistician Margie N. Rivera calculated a confidence interval of $[-0.56, 0.88]$. Her assistant boasts: “We should be 95% confident that the **sample average** falls in the provided interval”. This is a valid statement. *True or false?*

Problem 4.6. (5 points)

To estimate a population mean, our resident statistician Martyn Rivera plans to pick two simple random samples, each of size 100, from the population. He also plans to calculate the confidence interval with level C for each sample. What is the probability that **exactly one** of his confidence intervals will cover the population mean?

- a.: C^2
- b.: $1 - C^2$
- c.: $2C(1 - C)$
- d.: $1 - (1 - C)^2$
- e.: None of the above