## $\underline{M378K\ Introduction\ to\ Mathematical\ Statistics}}\\ \underline{Problem\ Set\ \#6}$

## Cumulative distribution functions.

**Problem 6.1.** Source: Sample P exam, Problem #342.

Consider a Poisson distributed random variable X. As usual, let's denote its cumulative distribution function by  $F_X$ . You are given that

$$\frac{F_X(2)}{F_X(1)} = 2.6$$

Calculate the expected value of the random variable X.

**Problem 6.2.** Consider a random variable Y whose cumulative distribution function is given by

$$F_Y(y) = \begin{cases} 0, & \text{for } y < 0 \\ y^4, & \text{for } 0 \le y < 1 \\ 1, & \text{for } 1 \le y \end{cases}$$

 $\label{lem:calculate} \textit{Calculate the expectation of the random variable } Y.$