

## M378K Introduction to Mathematical Statistics

### Problem Set #4

#### Cumulative distribution functions.

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**Problem 4.1.** Source: Sample P exam, Problem #342.

Consider a Poisson distributed random variable  $X$ . As usual, let's denote its cumulative distribution function by  $F_X$ . You are given that

$$\frac{F_X(2)}{F_X(1)} = 2.6$$

Calculate the expected value of the random variable  $X$ .

**Problem 4.2.** Consider a random variable  $Y$  whose cumulative distribution function is given by

$$F_Y(y) = \begin{cases} 0, & \text{for } y < 0 \\ y^4, & \text{for } 0 \leq y < 1 \\ 1, & \text{for } 1 \leq y \end{cases}$$

Calculate the expectation of the random variable  $Y$ .