Focus on the Delta.	
value fition: v(s,t, r, v)	
Del'h. The Delta $\Delta(s,t) := \frac{\partial}{\partial s} v(s,t)$	
Example. Outright Purchase of a Non-Dividend Paying Stock	e
v(3t) = 5 stands for the timert stock price	
$= / (\Delta (3, \mathcal{E})^2 \perp)$	
Example. European Coul. Δ $v_c(s,t) = s \cdot N(d_1(s,t)) - Ke^{-r(T-t)} \cdot N(d_2(s,t))$	
$v_c(s,t)=s\cdot N(d_1(s,t))-Ke^{-r(T-t)}\cdot N(d_2(s,t))$	
$d_1 = \frac{1}{\sigma\sqrt{T-t'}} \left[\ln\left(\frac{5}{K}\right) + \left(r + \frac{\sigma^2}{2}\right) \left(T-t\right) \right]$	
and $d_2 = d_1 - o\sqrt{\tau - t}$	
By del'n: $\Delta_c(s,t) = \frac{\partial}{\partial s} v_c(s,t)$	
We need: the product rule & the chain rule	
$\Delta_{c}(s,t) = N(d_{1}(s,t)) > 0$	
The positivity nakes sense since the call is long w.r.t the underlying	
long w.r.t the underlying	

Example. European put.

$$V_p(s,t) = Ke^{-r(T-t)}N(-d_2(s,t)) - sN(-d_1(s,t))$$
 $\Delta_p(s,t) = -N(-d_1(s,t)) < 0$
 $\Delta_p(s,t) = -N(-d_1(s,t)) < 0$

Puts are short w.r.t. the underlying.

 $v_{c}(s,t) - v_{p}(s,t) = s - Ke^{-r(T-t)}$ $\Delta_{c}(s,t) - \Delta_{p}(s,t) = 1$

 $\Delta_{P}(s,t) = \Delta_{C}(s,t) - 1 = N(d_{1}(s,t)) - 1 = -N(-d_{1}(s,t))$

- (A) 7.32 million
- (B) 7.42 million
- (C) 7.52 million
- (D) 7.62 million
- (E) 7.72 million

You are considering the purchase of a 3-month 41.5-strike American call option on 8. a nondividend-paying stock.

You are given:

- The Black-Scholes framework holds. (i)
- (ii) The stock is currently selling for 40.
- (iii) The stock's volatility is 30%.
- (iv) The current call option delta is 0.5.

Determine the current price of the option. (3(6),0)=?

(A)
$$20 - 20.453 \int_{-\infty}^{0.15} e^{-x^2/2} dx$$

(B)
$$20 - 16.138 \int_{-\infty}^{0.15} e^{-x^2/2} dx$$

(C)
$$20 - 40.453 \int_{-\infty}^{0.15} e^{-x^2/2} dx$$

(D)
$$16.138 \int_{-\infty}^{0.15} e^{-x^2/2} dx - 20.453$$

(E)
$$40.453 \int_{-\infty}^{0.15} e^{-x^2/2} dx - 20.453$$

$$\Delta_{c}(s(\omega), 0) = 0.5$$
 $N(d_{4}(s(\omega), 0)) = 0.5$

$$\frac{d_{1}(s(0),0)=0}{d_{1}(s(0),0)=0}$$

$$\frac{1}{\sigma \Gamma} \left[\ln \left(\frac{40}{44.5} \right) + \left(r + \frac{0.09}{2} \right) \cdot \frac{1}{4} \right] = 0$$

$$r + 0.045 = 4 \ln \left(\frac{44.5}{40} \right)$$

$$r = 4 \ln \left(\frac{44.5}{40} \right) - 0.045 = \frac{0.4032}{d_1(S(0),0)} - 6\sqrt{r} = 0.26$$

$$v_c(S(0),0) = S(0) \cdot N(d_1(S(0),0)) - Ke^{-r} N(d_2(S(0),0))$$

$$= 40 \cdot 0.5 - 44.5 e^{-0.4032(\frac{1}{4})} \cdot N(-0.15)$$

$$= 20 - 40.453 (1 - N(0.15))$$

$$= 40.454 \cdot N(0.15) - 20.453$$

$$\int_{0.45}^{1} \int_{1}^{2} \left(\frac{1}{2^{n}} \right) e^{-\frac{2^{n}}{2}} dz$$