```
M378K: October 11+4, 2024.
   The \chi^2(n) distribution.
     If Y~N(0,1), then W=Y2~X2(df=1)
     Its density is
f_{\omega}(\omega) = \frac{1}{\sqrt{2\pi\omega}} e^{-\frac{\omega}{2}} 1_{(0,\infty)}(\omega)
     Its mgf is m_{w}(t) = (1-2t)^{-1/2} = \frac{1}{\sqrt{1-2t'}}
    Example. Y, NN10,1), Y2NN10,1) and independent
                 Set W=(x2+(x22)
                 Let's get is mgf.
             m_{w}(t) = m_{12}(t) \cdot m_{22}(t)
                           = \frac{1}{\sqrt{1-2t'}} \cdot \frac{1}{\sqrt{1-2t'}} = \frac{1}{1-2t} = \frac{\frac{1}{2}}{\frac{1}{2}-t}
                 From the HW, we know that WNE(T=2)
  So, \chi^2(df=2) in the same as E(\tau=2).
Defin. The \chi^2-distin \omega/ n degrees of freedom in the distin
          where Yi NN(0,1) for i=1..n
               and they're independent.
         We write W \sim \chi^2(n) = \chi^2(df=n)
```

Note:
$$m_{\omega}(t) = \left(\frac{1}{\sqrt{1-2t'}}\right)^{n} = (1-2t)^{n/2}$$

Example. Let
$$Y \sim \chi^2(df=5)$$

>: Tables.

The Gamma Distribution.

Defin. A random variable Y is said to have the gamma distribution ω / parameters k>0 and t>0, if its may $m_Y(t)=\left(\frac{1}{1-t\cdot t}\right)$

$$m_{\Upsilon}(t) = \left(\frac{1}{1-T \cdot t}\right)^{k}$$

We unte YNT(k, T)

Q: Say that YN (1, T). Do you know another name for it?

Q: Say that $Y \sim \Gamma(\frac{n}{2}, 2)$.

Q: $Y_1 N \Gamma(k_1, T)$ and $Y_2 N \Gamma(k_2, T)$ $Y_1 + Y_2 N \Gamma(k_1 + k_2, T)$ independent