

UNIVERSITY OF TEXAS AT AUSTIN

Problem Set #10

Binomial option pricing: Forward trees. Two periods.

Problem 10.1. (5 points) Assume that the a stock price is modeled using a one-period forward binomial tree with the length of a single period equal to three months. According to this model, the stock price can take either the value of \$50, or the value of \$40 in exactly three months. Calculate the volatility of the stock price.

- (a) About 0.22
- (b) About 0.28
- (c) About 0.30
- (d) About 0.32
- (e) None of the above.

Problem 10.2. The current price of a continuous-dividend-paying stock is \$100 per share. Its volatility is given to be 0.30 and its dividend yield is 0.03.

The continuously compounded risk-free interest rate equals 0.06.

Consider a \$95-strike European put option on the above stock with three months to expiration. Using a one-period forward binomial tree, find the price of this put option.

- (a) \$3.97
- (b) \$4.52
- (c) \$4.70
- (d) \$4.97
- (e) None of the above.

Problem 10.3. The current price of a stock is \$100 per share. Its dividend yield is 0.01 and volatility is 0.3. In order to model the stock price at the end of a year, Bertie constructed a forward binomial tree. He then calculated the price of a one-year, 90-strike European put option on this stock and obtained \$8.50. What is the **positive** continuously compounded, risk-free interest rate Bertie used?

Problem 10.4. For a two-period binomial model, you are given that:

- (1) each period is one year;
- (2) the current price of a non-dividend-paying stock S is $S(0) = \$20$;
- (3) $u = 1.2$, with u as in the standard notation for the binomial model;
- (4) $d = 0.8$, with d as in the standard notation for the binomial model;
- (5) the continuously compounded risk-free interest rate is $r = 0.04$.

Consider a **special** call option which pays the excess above the strike price $K = 23$ (if any!) at the end of every binomial period.

Find the price of this option.