50. Assume the Black-Scholes framework.

You are given the following information for a stock that pays dividends continuously at a rate proportional to its price.

- (i) The current stock price is 0.25.
- (ii) The stock's volatility is 0.35.
- (iii) The continuously compounded expected rate of stock-price appreciation is 15%.

Calculate the upper limit of the 90% lognormal confidence interval for the price of the stock in 6 months.

- (A) 0.393
- (B) 0.425
- (C) 0.451
- (D) 0.486
- (E) 0.529

51-53. DELETED

54. Assume the Black-Scholes framework. Consider two nondividend-paying stocks whose time-t prices are denoted by $S_1(t)$ and $S_2(t)$, respectively.

You are given:

- (i) $S_1(0) = 10$ and $S_2(0) = 20$.
- (ii) Stock 1's volatility is 0.18.
- (iii) Stock 2's volatility is 0.25.
- (iv) The correlation between the continuously compounded returns of the two stocks is -0.40.
- (v) The continuously compounded risk-free interest rate is 5%.
- (vi) A one-year European option with payoff max $\{\min[2S_1(1), S_2(1)] 17, 0\}$ has a current (time-0) price of 1.632.

Consider a European option that gives its holder the right to sell either two shares of Stock 1 or one share of Stock 2 at a price of 17 one year from now.

Calculate the current (time-0) price of this option.

- (A) 0.67
- (B) 1.12
- (C) 1.49
- (D) 5.18
- (E) 7.86
- **55.** Assume the Black-Scholes framework. Consider a 9-month at-the-money European put option on a futures contract. You are given:
 - (i) The continuously compounded risk-free interest rate is 10%.
 - (ii) The strike price of the option is 20.
 - (iii) The price of the put option is 1.625.

If three months later the futures price is 17.7, what is the price of the put option at that time?

- (A) 2.09
- (B) 2.25
- (C) 2.45
- (D) 2.66
- (E) 2.83

56-76. DELETED