

UNIVERSITY OF TEXAS AT AUSTIN

Quiz #12

Discrete distributions.

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Provide your **complete solution** to the following problems. Final answers only, without appropriate justification, will receive zero points even if correct.

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**Problem 12.1.** (5 points) *Source: Sample P exam, Problem #30.*

An actuary has discovered that policyholders are three times as likely to file two claims as to file four claims. The number of claims filed has a Poisson distribution. Calculate the variance of the number of claims filed.

- (a)  $1/\sqrt{3}$
- (b) 1
- (c)  $\sqrt{2}$
- (d) 2
- (e) None of the above.

**Problem 12.2.** (5 points) Let the number of floods in a calendar year be denoted by  $N$  and modeled using the Poisson distribution with mean 5. We say that a flood is “minor” if the damages associated with it do not exceed \$1,000,000. Otherwise, a flood is designated as “major”. The number of floods and the damages caused by individual floods are assumed to be independent.

Assume that the probability that an observed flood is “major” equals  $1/5$ .

Find the probability that the number of “major” floods is 2, given that the **total** number of floods in that year equals 5.

**Problem 12.3.** (5 points) Suppose that the number  $N$  of customers visiting a fast food restaurant in a given morning is Poisson with mean 20. Assume that each customer purchases a drink with probability  $3/4$ , independently from other customers, and independently from the value of  $N$ . Let  $N_1$  be the number of customers who purchase drinks in that time interval and let  $N_2$  be the number of customers that do not purchase drinks.

What is the probability that exactly 3 customers purchase a drink in a given morning, **given** that there is a total of 10 customers on that particular morning?