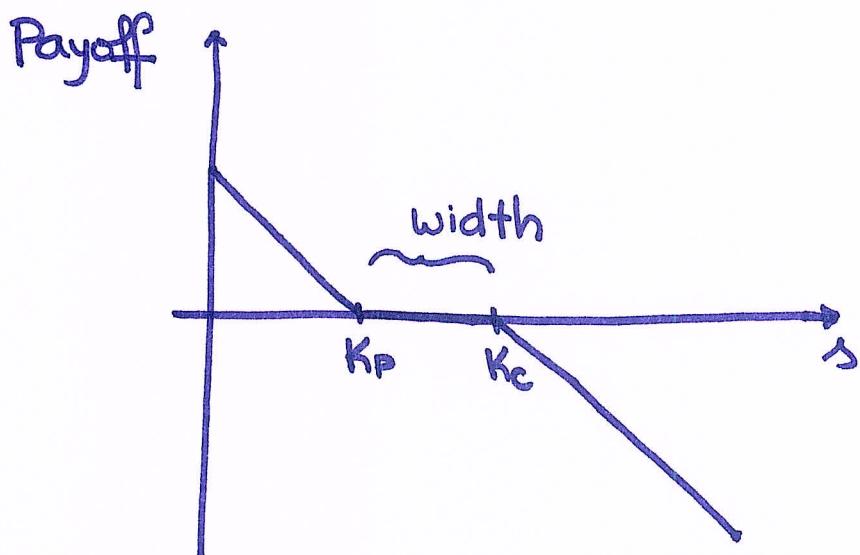


④ : April 5<sup>th</sup>, 2019.

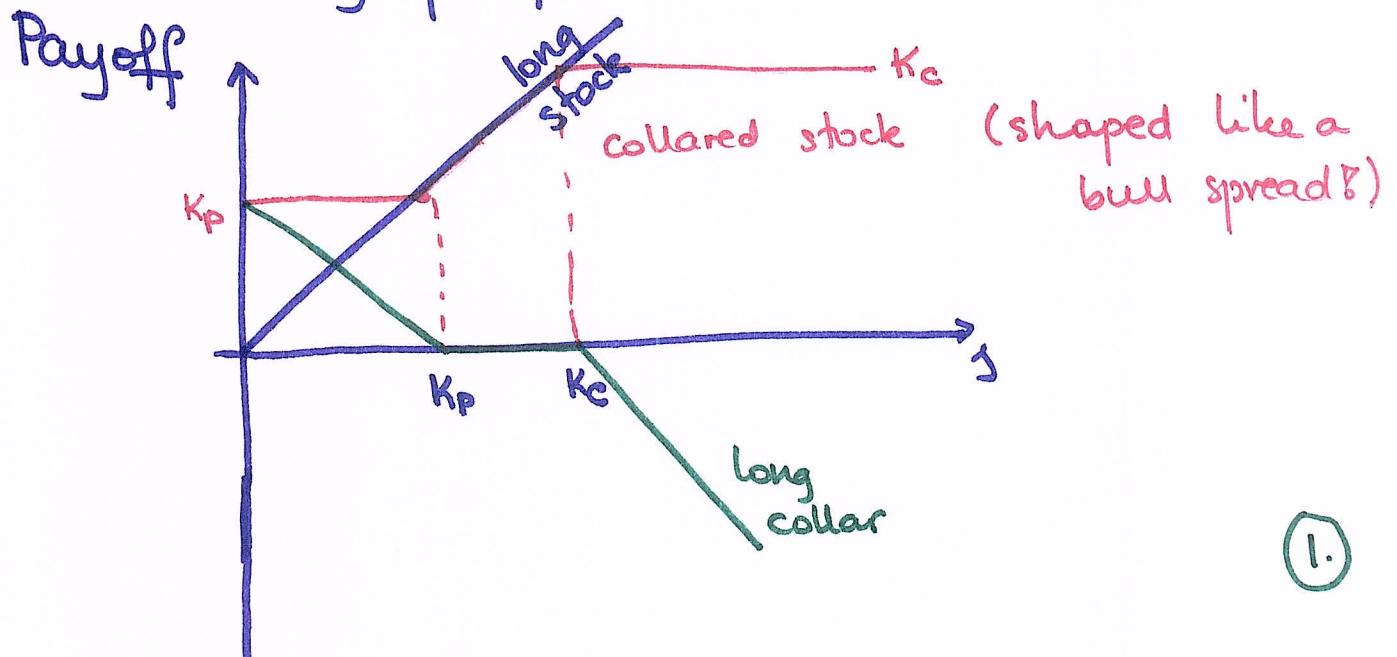
## Collars [review].

Let  $K_p \leq K_c$ .

- { • LONG the  $K_p$ -strike put
  - WRITE/SHORT the  $K_c$ -strike call }
- European ; otherwise identical



We use the long collar to hedge a long stock.  
The resulting portfolio is a collared stock.



1.

59.

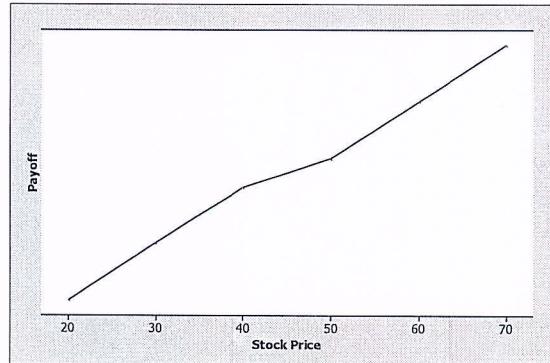
An investor has a long position in a non-dividend-paying stock, and additionally, has a long collar on this stock consisting of a 40-strike put and 50-strike call.

Determine which of these graphs represents the payoff diagram for the overall position at the time of expiration of the options.

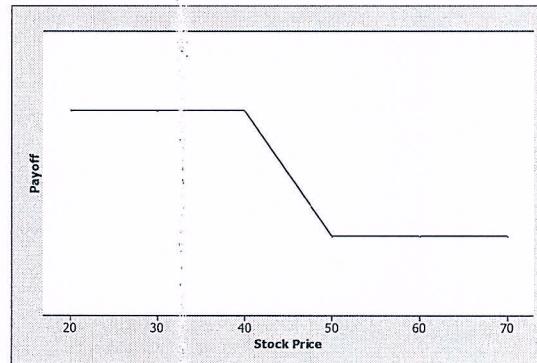
bear spread + bond =

= short collared stock

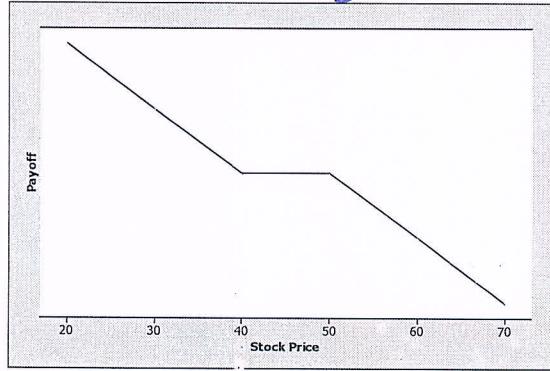
(A)



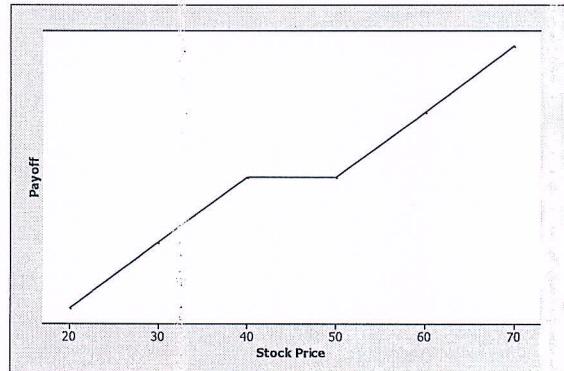
(B)



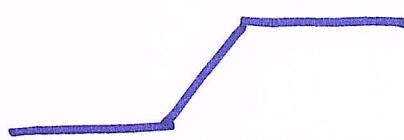
(C) "naked" long collar



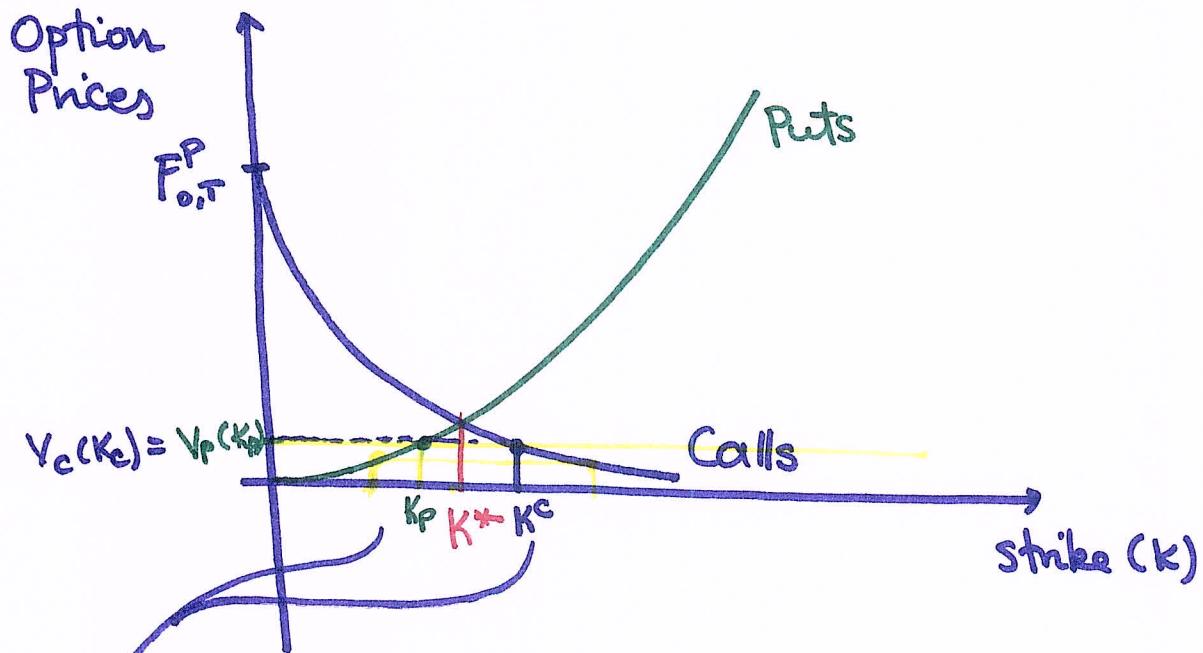
(D) "naked" short collar



(E)



## Zero-Cost Collars



By put-call parity:

$$0 = V_c(K^*) - V_p(K^*) \Leftrightarrow F_{0,T}^P - PV_{0,T}(K^*)$$

$$\Rightarrow F_{0,T}^P = PV_{0,T}(K^*)$$

$$\Rightarrow K^* = F_{0,T}$$

For each pair  $K_p$  &  $K_c$  obtained as above, we end up w/ a  $(K_p, K_c)$ -collar whose cost is ZERO.

We have infinitely many zero-cost collars.

## Ratio Spreads.

Let  $K_1 < K_2$

- LONG  $m$  calls w/ strike  $K_1$
  - SHORT/WRITE  $n$  calls w/ strike  $K_2$
- } European;  
otherwise  
identical

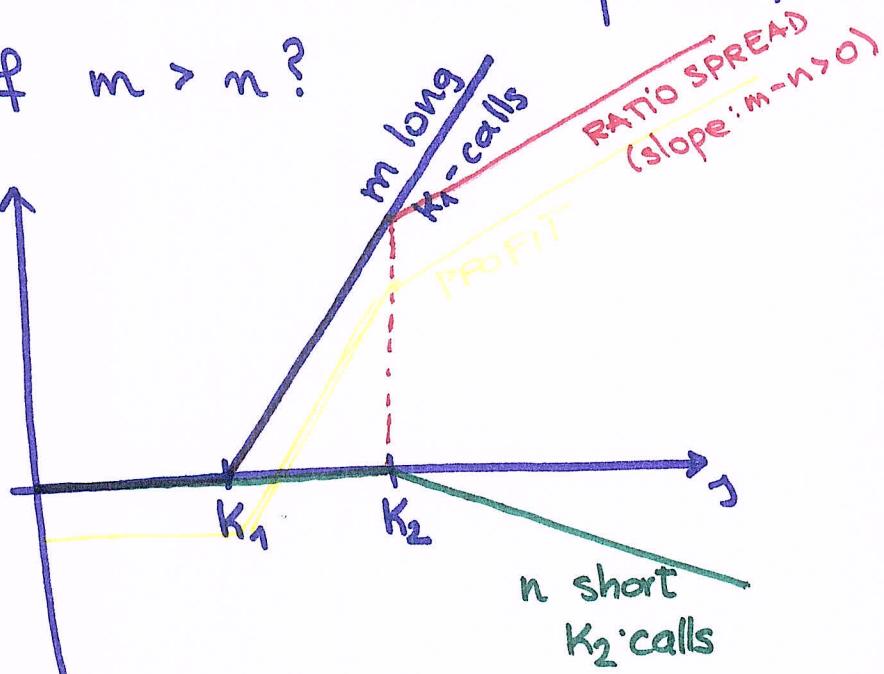
w/  $m$  and  $n$  positive constants; usually integers.

Q: What if  $m = n$ ?

It's like  $m$  call bull spreads.

Q: What if  $m > n$ ?

Payoff



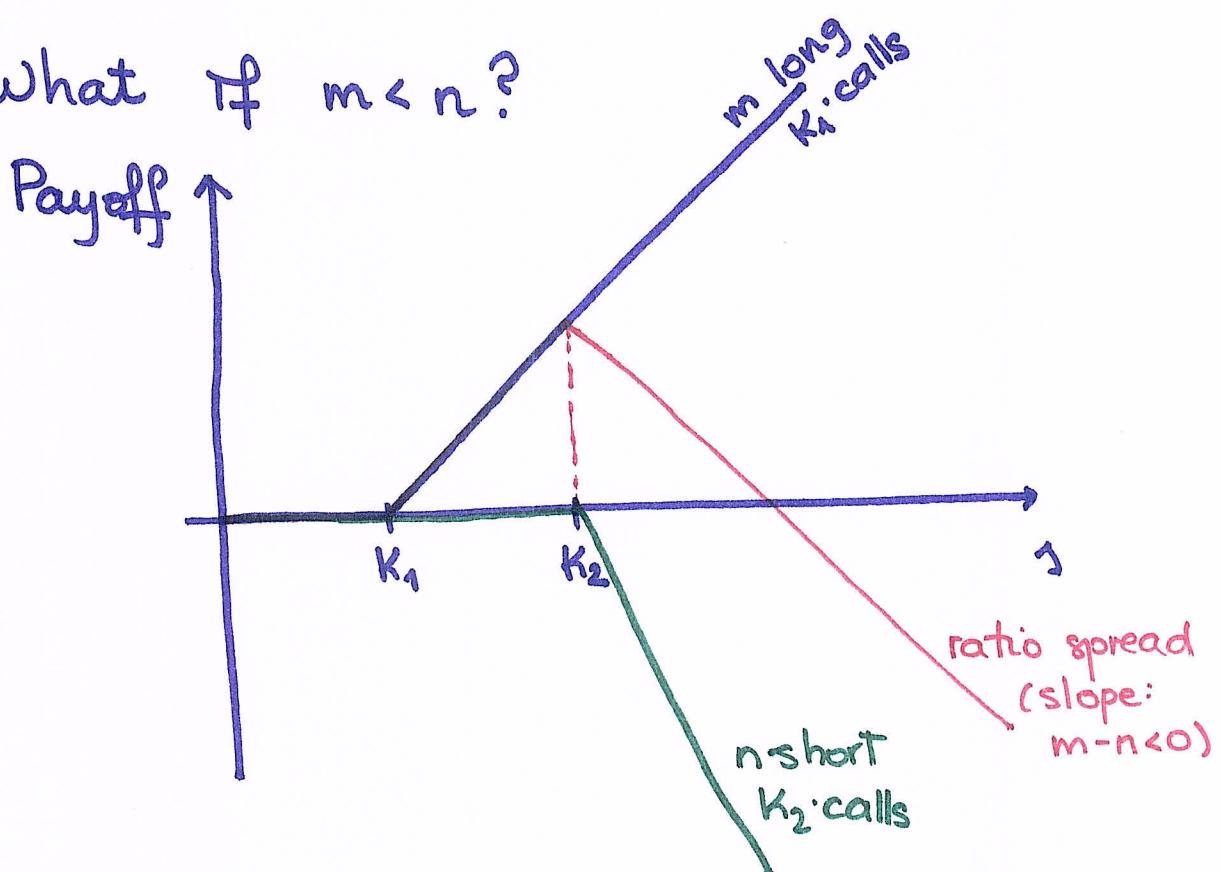
Q: Who would trade in this position?

- Speculators on higher prices.

- Long w.r.t. the underlying

=> Use it to hedge a short position.

Q: What if  $m < n$ ?



Q: Who would invest in this ratio spread?

- Arbitrageur  $\times$  No lower bound!
- Speculator : Low volatility & low likelihood of high prices
- Hedger  $\times$  No directionality!

38.

The current price of a medical company's stock is 75. The expected value of the stock price in three years is 90 per share. The stock pays no dividends.

You are also given

- i) The risk-free interest rate is positive.
- ii) There are no transaction costs.
- iii) Investors require compensation for risk.

The price of a three-year forward on a share of this stock is  $X$ , and at this price an investor is willing to enter into the forward.

Determine what can be concluded about  $X$ .

- (A)  $X < 75$
- (B)  $X = 75$
- (C)  $75 < X < 90$
- (D)  $X = 90$
- (E)  $90 < X$

39.

Determine which of the following strategies creates a ratio spread, assuming all options are European.

### calendar spreads

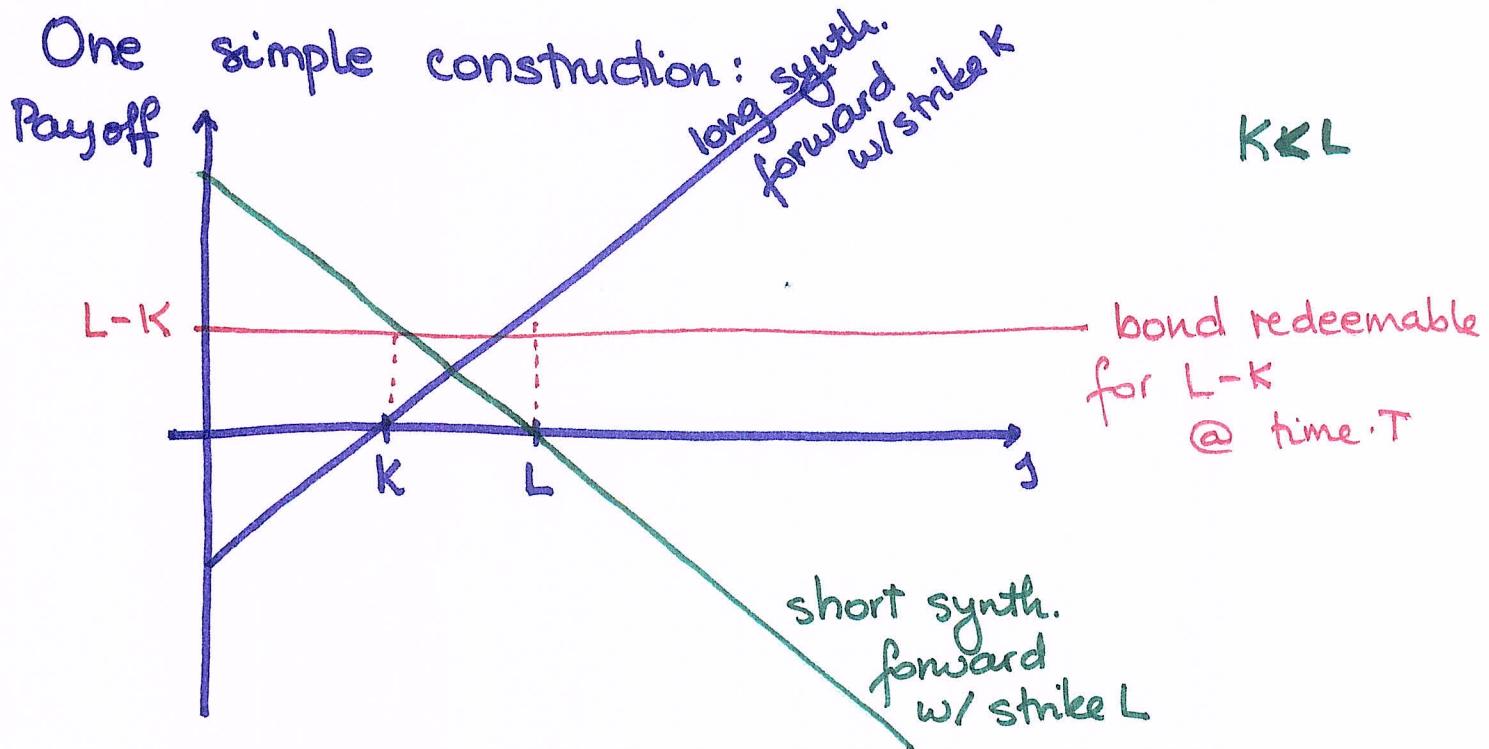
- (A) Buy a one-year call, and sell a three-year call with the same strike price.
- (B) Buy a one-year call, and sell a three-year call with a different strike price.
- (C) Buy a one-year call, and buy three one-year calls with a different strike price.
- (D) Buy a one-year call, and sell three one-year puts with a different strike price.
- (E) Buy a one-year call, and sell three one-year calls with a different strike price. ☺

long call + long bond  
"

long put + long stock

## Box Spreads

... replicate a bond



## Put-call Parity:

- { • long a  $K$ -strike call \* } LONG synthetic forward w/ strike K
- { • short a  $K$ -strike put \* }
- { • short an  $L$ -strike call \* } SHORT synthetic forward w/ strike L
- { • long an  $L$ -strike put \* }

Box Spread : { \* LONG  $(K,L)$ -call bull spread  
\* LONG  $(K,L)$ -put bear spread

53.

For each ton of a certain type of rice commodity, the four-year forward price is 300. A four-year 400-strike European call option costs 110.

The continuously compounded risk-free interest rate is 6.5%.

Calculate the cost of a four-year 400-strike European put option for this rice commodity.

- (A) 10.00
- (B) 32.89
- (C) 118.42
- (D) 187.11
- (E) 210.00

54.

DELETED

55.

Box spreads are used to guarantee a fixed cash flow in the future. Thus, they are purely a means of borrowing or lending money, and have no stock price risk.

Consider a **box spread** based on two distinct strike prices ( $K, L$ ) that is used to lend money, so that there is a positive cost to this transaction up front, but a guaranteed positive payoff at expiration.

Determine which of the following sets of transactions is equivalent to this type of box spread.

- (A) A long position in a  $(K, L)$  bull spread using calls and a long position in a  $(K, L)$  bear spread using puts.
- (B) A long position in a  $(K, L)$  bull spread using calls and a short position in a  $(K, L)$  bear spread using puts. ↑↑ ×
- (C) A long position in a  $(K, L)$  bull spread using calls and a long position in a  $(K, L)$  bull spread using puts. ×
- (D) A short position in a  $(K, L)$  bull spread using calls and a short position in a  $(K, L)$  bear spread using puts. BORROWING!
- (E) A short position in a  $(K, L)$  bull spread using calls and a short position in a  $(K, L)$  bull spread using puts. ↓↓ ×

## Spreads etc.

<i>+ hedge</i> 	call	bull	spreads	↑	$\geq 0$	monot.
	put	bull	-  -	↑	$\leq 0$	cord slope
	call	bear	-  -	↓	$\leq 0$	cord slope
	put	bear	-  -	↓	$\geq 0$	moubt.

butterfly spreads + speculation on low vol. convexity

straddles + strangles  
speculation on high vol

- collars
  - ratio spreads
  - box spreads