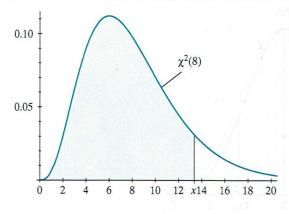
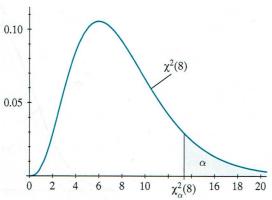
Table IV The Chi-Square Distribution





$$P(X \le x) = \int_0^x \frac{1}{\Gamma(r/2)2^{r/2}} w^{r/2 - 1} e^{-w/2} dw$$

|    | $(S) \Phi = P(X \leq x) \Phi$ |                     |                    |                    |                    |                    |                     |                    |
|----|-------------------------------|---------------------|--------------------|--------------------|--------------------|--------------------|---------------------|--------------------|
|    | 0.010                         | 0.025               | 0.050              | 0.100              | 0.900              | 0.950              | 0.975               | 0.990              |
| r  | $\chi^2_{0.99}(r)$            | $\chi^2_{0.975}(r)$ | $\chi^2_{0.95}(r)$ | $\chi^2_{0.90}(r)$ | $\chi^2_{0.10}(r)$ | $\chi^2_{0.05}(r)$ | $\chi^2_{0.025}(r)$ | $\chi^2_{0.01}(r)$ |
| 1  | 0.000                         | 0.001               | 0.004              | 0.016              | 2.706              | 3.841              | 5.024               | 6.635              |
| 2  | 0.020                         | 0.051               | 0.103              | 0.211              | 4.605              | 5.991              | 7.378               | 9.210              |
| 3  | 0.115                         | 0.216               | 0.352              | 0.584              | 6.251              | 7.815              | 9.348               | 11.34              |
| 4  | 0.297                         | 0.484               | 0.711              | 1.064              | 7.779              | 9.488              | 11.14               | 13.28              |
| 5  | 0.554                         | 0.831               | 1.145              | 1.610              | 9.236              | 11.07              | 12.83               | 15.09              |
| 6  | 0.872                         | 1.237               | 1.635              | 2.204              | 10.64              | 12.59              | 14.45               | 16.81              |
| 7  | 1.239                         | 1.690               | 2.167              | 2.833              | 12.02              | 14.07              | 16.01               | 18.48              |
| 8  | 1.646                         | 2.180               | 2.733              | 3.490              | 13.36              | 15.51              | 17.54               | 20.09              |
| 9  | 2.088                         | 2.700               | 3.325              | 4.168              | 14.68              | 16.92              | 19.02               | 21.67              |
| 10 | 2.558                         | 3.247               | 3.940              | 4.865              | 15.99              | 18.31              | 20.48               | 23.21              |
| 11 | 3.053                         | 3.816               | 4.575              | 5.578              | 17.28              | 19.68              | 21.92               | 24.72              |
| 12 | 3.571                         | 4.404               | 5.226              | 6.304              | 18.55              | 21.03              | 23.34               | 26.22              |
| 13 | 4.107                         | 5.009               | 5.892              | 7.042              | 19.81              | 22.36              | 24.74               | 27.69              |
| 14 | 4.660                         | 5.629               | 6.571              | 7.790              | 21.06              | 23.68              | 26.12               | 29.14              |
| 15 | 5.229                         | 6.262               | 7.261              | 8.547              | 22.31              | 25.00              | 27.49               | 30.58              |
| 16 | 5.812                         | 6.908               | 7.962              | 9.312              | 23.54              | 26.30              | 28.84               | 32.00              |
| 17 | 6.408                         | 7.564               | 8.672              | 10.08              | 24.77              | 27.59              | 30.19               | 33.41              |
| 18 | 7.015                         | 8.231               | 9.390              | 10.86              | 25.99              | 28.87              | 31.53               | 34.80              |
| 19 | 7.633                         | 8.907               | 10.12              | 11.65              | 27.20              | 30.14              | 32.85               | 36.19              |
| 20 | 8.260                         | 9.591               | 10.85              | 12.44              | 28.41              | 31.41              | 34.17               | 37.57              |
| 21 | 8.897                         | 10.28               | 11.59              | 13.24              | 29.62              | 32.67              | 35.48               | 38.93              |
| 22 | 9.542                         | 10.98               | 12.34              | 14.04              | 30.81              | 33.92              | 36.78               | 40.29              |
| 23 | 10.20                         | 11.69               | 13.09              | 14.85              | 32.01              | 35.17              | 38.08               | 41.64              |
| 24 | 10.86                         | 12.40               | 13.85              | 15.66              | 33.20              | 36.42              | 39.36               | 42.98              |
| 25 | 11.52                         | 13.12               | 14.61              | 16.47              | 34.38              | 37.65              | 40.65               | 44.31              |
| 26 | 12.20                         | 13.84               | 15.38              | 17.29              | 35.56              | 38.88              | 41.92               | 45.64              |
| 27 | 12.88                         | 14.57               | 16.15              | 18.11              | 36.74              | 40.11              | 43.19               | 46.96              |
| 28 | 13.56                         | 15.31               | 16.93              | 18.94              | 37.92              | 41.34              | 44.46               | 48.28              |
| 29 | 14.26                         | 16.05               | 17.71              | 19.77              | 39.09              | 42.56              | 45.72               | 49.59              |
| 30 | 14.95                         | 16.79               | 18.49              | 20.60              | 40.26              | 43.77              | 46.98               | 50.89              |
| 40 | 22.16                         | 24.43               | 26.51              | 29.05              | 51.80              | 55.76              | 59.34               | 63.69              |
| 50 | 29.71                         | 32.36               | 34.76              | 37.69              | 63.17              | 67.50              | 71.42               | 76.15              |
| 60 | 37.48                         | 40.48               | 43.19              | 46.46              | 74.40              | 79.08              | 83.30               | 88.38              |
| 70 | 45.44                         | 48.76               | 51.74              | 55.33              | 85.53              | 90.53              | 95.02               | 100.4              |
| 80 | 53.34                         | 57.15               | 60.39              | 64.28              | 96.58              | 101.9              | 106.6               | 112.3              |

This table is abridged and adapted from Table III in Biometrika Tables for Statisticians, edited by E.S.Pearson and H.O.Hartley.