

UNIVERSITY OF TEXAS AT AUSTIN, DEPARTMENT OF MATHEMATICS  
M358K - Applied StatisticsPRACTICE PROBLEMS ON  $t$ - PROCEDURES.

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**Free-response problems.****Problem 4.1.** (15 points) *Source: Ramachandran-Tsokos.*

A study of two kinds of machine failures shows that 58 failures of the first kind took on the average 79.7 minutes to repair with a sample standard deviation of 18.4 minutes, whereas 71 failures of the second kind took on average 87.3 minutes to repair with a sample standard deviation of 19.5 minutes. Find a 99% confidence interval for the difference between the true average amounts of time it takes to repair failures of the two kinds of machines.

**Problem 4.2.** (8 points) To write an article about Denver for a tourist magazine you would like to estimate the average nightly cost for a hotel room in the Denver area. You are willing to assume that the nightly cost of a room is normally distributed.

You open up the yellow pages and take a random sample of hotels. The sample of 16 hotels gives an average nightly cost of \$55.98 and a sample standard deviation of \$12. Estimate the mean nightly cost and include a 95% confidence interval.

**Problem 4.3.** (10 points)

It is claimed that the bags of chocolate chips available in Costco contain at least 4 pounds (64 ounces).

A random sample of 50 bag measurements resulted in the sample average of 62 and the sample standard deviation of 8. Please, test the hypothesis that the bags contain at least 64 ounces of delicious chocolate chips at the significance level of 5%.

**Problem 4.4.** *Source: Ramachandran-Tsokos.*

In a salary equity study of faculty at a certain university, sample salaries of 50 male assistant professors and 50 female assistant professors yielded the following basic statistics:

- for male assistant professors, the sample mean was \$46,400 with a sample standard deviation of \$360;
- for female assistant professors, the sample mean was \$46,000 with a sample standard deviation of \$220.

Assume independent samples. Test the hypothesis that the mean salary of male assistant professors exceeds the mean salary of female assistant professors at the significance level of 0.05.

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**Multiple-choice problems.**

**Problem 4.5.** An experiment was designed to test whether people's reaction times to an orange light are different from their reaction times to a blue light. Upon being signaled with a light, the subjects would hit a button and the reaction time (in seconds) would be recorded. The reaction time (in seconds) of 16 subjects was recorded. The average reaction time for the blue light was 0.2025 seconds, and the average reaction time for the orange light was 0.1380 seconds. The sample standard deviation of the differences between reaction times was 0.0565. What is the 80%-confidence interval for the difference in mean reaction times? Assume the normal model for the reaction times.

- (a)  $0.0645 \pm 0.0189$
- (b)  $0.0645 \pm 0.0122$
- (c)  $0.2025 \pm 0.0189$
- (d)  $0.1380 \pm 0.0122$

- (e) None of the above.

**Problem 4.6.** Twenty-five fortunate middle schoolers were put on an intense rope-jumping regimen in the hope of improving their times in the 40-yard dash. Assume that the distribution of the differences in the run times is normal. Let  $\mu_d$  be the mean difference between the "pre-run" (before the regimen) and "post-run" (after the regimen). We want to test

$$H_0 : \mu_d = 0 \quad \text{vs.} \quad H_a : \mu_d > 0.$$

The observed average difference in run times was  $\bar{x}_d = 0.0854$  while the sample standard deviation was  $s_d = 0.2432$ . What can you say about the  $p$ -value for this hypothesis test?

- (a) It's below 0.01.
- (b) It's between 0.01 and 0.02.
- (c) It's between 0.02 and 0.025.
- (d) It's between 0.025 and 0.05.
- (e) None of the above.